Excess Enthalpies of Binary Mixtures of 1-Hexene with Some *n*-Alkanes at 298.15 K

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Excess molar enthalpies, measured at 298.15 K in a flow microcalorimeter, are reported for mixtures of 1-hexene with *n*-heptane, *n*-octane, *n*-decane, *n*-dodecane, and *n*-tetradecane. Smooth Redlich–Kister representations of the results are described. It was found that the Liebermann–Fried model also provided good representations of the data.

Introduction

The use of alkenes to improve the octane ratings of blended gasolines has provided an incentive to study the thermodynamic properties of mixtures of an alkene with various hydrocarbons. The present paper reports excess molar enthalpies, measured at 298.15 K, for binary mixtures of 1-hexene (1HX) with the following normal alkanes: *n*-heptane (nC7), *n*-octane (nC8), *n*-decane (nC10), *n*-dodecane (nC12), and *n*-tetradecane (nC14).

Experimental Section

The 1HX, nC7, nC8, nC10, nC12, and nC14 used in the present work were obtained from the Aldrich Chemical Co. In all cases the purities stated by the manufacturer were at least 99 mol %. Apart from partial degassing, the components were used without further purification. Densities, $\rho/\text{kg}\cdot\text{m}^{-3}$ at 298.15 K, measured with a precision of 0.03 kg·m⁻³ in an Anton-Paar digital densimeter (model DMA 02C), were 668.73, 680.17, 698.72, 726.30, 745.32, and 759.36 for 1HX, nC7, nC8, nC10, nC12, and nC14, respectively. These results agree within ±0.1% with the corresponding literature¹ values 668.48, 679.46, 698.62, 726.35, 745.18, and 759.20.

An LKB flow microcalorimeter (model 10700-1), thermostated at (298.150 \pm 0.003) K, was used to measure the excess molar enthalpies $H_{\rm m}^{\rm E}$. Details of the equipment and its operation have been described previously.^{2,3} Over most of the mole fraction range, the errors of the excess molar enthalpies and the mole fractions are estimated to be less than 0.5% and 5 \times 10⁻⁴, respectively.

Results and Discussion

Excess molar enthalpies, $H_{m,12}^E$, measured at 298.15 K, for the five binary mixtures 1HX (1) + nC7 (2), 1HX (1) + nC8 (2), 1HX (1) + nC10 (2), 1HX(1) + nC12 (2), and 1HX (1) + nC14 (2) are listed in Table 1 and plotted in Figure 1.

The Redlich–Kister smoothing function

$$H_{m,12}^{E}/J \cdot \text{mol}^{-1} = x_1(1-x_1)\sum_{k=1}^n h_k(1-2x_1)^{k-1}$$

was fitted to the results in Table 1 by a least-squares method, with all points weighted equally. Values of the coefficients h_k are listed in Table 2, along with the standard



Figure 1. Excess molar enthalpies, $H_{m,12}^{E}$, for 1HX (1) + *n*-alkane (2) at 298.15 K. Experimental results: ∇ , nC7; \bigcirc , nC8; \triangle , nC10; \Box , nC12; \diamond , nC14. Curves: -, calculated from the representation of the results by eq 1 using the coefficients in Table 2; - --, fit of the results by means of the Liebermann–Fried model.

deviation *s* for the representation. Plots of those representations are shown as solid curves in Figure 1. For the five systems, the maximum of $H_{m,12}^{E}$ occurs near $x_1 \approx 0.5$, and the value increases with the alkane chain length.

Recent work^{4,5} indicates that an extension of the model of Liebermann and Fried^{6,7} can be useful in representing the excess enthalpies of binary mixtures and also has the potential for estimating the vapor—liquid equilibria of mixtures and the excess enthalpies of ternary mixtures, from data for the pure components and their binary mixtures. It is therefore of interest to examine how well the Liebermann—Fried model can represent the enthalpies of the present binary systems.

The equations used in this application have been outlined by Wang et al.⁵ Values of the Liebermann–Fried

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| Table 1. | Experimental Mole | Fractions, x ₁ , | and Excess Molar | Enthalpies, I | H ^E _{m 12} , for | Mixtures of | f 1HX with r | nC7, nC8, | nC10, |
|----------|--------------------------|-----------------------------|------------------|---------------|--------------------------------------|-------------|---------------------|-----------|-------|
| nC12, ar | nd nC14 at 298.15 K | | | - | , | | | | |

| | $H_{\mathrm{m,12}}^{\mathrm{E}}$ | | $H_{\mathrm{m,12}}^{\mathrm{E}}$ | | $H_{\mathrm{m},12}^{\mathrm{E}}$ | | $H_{\mathrm{m,12}}^{\mathrm{E}}$ | | |
|--------------------|----------------------------------|------------|----------------------------------|------------|----------------------------------|------------|----------------------------------|--|--|
| <i>X</i> 1 | $J \cdot mol^{-1}$ | <i>X</i> 1 | $J \cdot mol^{-1}$ | <i>X</i> 1 | $J \cdot mol^{-1}$ | <i>X</i> 1 | J•mol ^{−1} | | |
| 1HX (1) + nC7 (2) | | | | | | | | | |
| 0.0500 | 11.13 | 0.2998 | 50.46 | 0.5498 | 61.38 | 0.8000 | 41.33 | | |
| 0.1000 | 21.21 | 0.3500 | 54.95 | 0.6000 | 59.65 | 0.8499 | 33.05 | | |
| 0.1499 | 30.30 | 0.3984 | 58.88 | 0.6496 | 56.64 | 0.9000 | 23.38 | | |
| 0.1998 | 37.57 | 0.4492 | 61.03 | 0.6992 | 52.81 | 0.9500 | 11.71 | | |
| 0.2496 | 44.68 | 0.5005 | 61.42 | 0.7497 | 47.37 | | | | |
| 1HX (1) + nC8 (2) | | | | | | | | | |
| 0.0500 | 11.36 | 0.3000 | 54.95 | 0.5499 | 67.25 | 0.8002 | 45.33 | | |
| 0.1000 | 22.25 | 0.3497 | 59.97 | 0.5994 | 65.86 | 0.8499 | 36.91 | | |
| 0.1500 | 32.65 | 0.3998 | 63.87 | 0.6500 | 62.90 | 0.9000 | 26.29 | | |
| 0.2036 | 41.61 | 0.4500 | 66.13 | 0.6998 | 58.72 | 0.9500 | 13.89 | | |
| 0.2496 | 48.28 | 0.5000 | 67.70 | 0.7501 | 52.79 | | | | |
| | | | 1HX (1) + | nC10 (2) | | | | | |
| 0.0500 | 16.10 | 0.2997 | 72.95 | 0.5501 | 90.82 | 0.7998 | 62.21 | | |
| 0.1000 | 30.36 | 0.3504 | 79.63 | 0.5996 | 89.04 | 0.8501 | 51.08 | | |
| 0.1503 | 43.01 | 0.3999 | 85.18 | 0.6496 | 85.48 | 0.9000 | 36.08 | | |
| 0.2001 | 54.05 | 0.4508 | 88.39 | 0.7004 | 79.66 | 0.9500 | 19.12 | | |
| 0.2482 | 64.31 | 0.4994 | 90.75 | 0.7495 | 72.05 | | | | |
| | | | 1HX (1) + | nC12 (2) | | | | | |
| 0.0501 | 21.42 | 0.2994 | 98.47 | 0.5505 | 123.20 | 0.8001 | 83.86 | | |
| 0.0999 | 40.79 | 0.3494 | 108.33 | 0.5998 | 121.29 | 0.8503 | 67.77 | | |
| 0.1500 | 56.75 | 0.4001 | 115.80 | 0.6501 | 116.32 | 0.8999 | 48.84 | | |
| 0.1999 | 72.63 | 0.4503 | 120.25 | 0.6999 | 108.77 | 0.9500 | 26.20 | | |
| 0.2521 | 87.06 | 0.5001 | 122.66 | 0.7499 | 98.08 | | | | |
| 1HX (1) + nC14 (2) | | | | | | | | | |
| 0.0500 | 25.84 | 0.2970 | 127.49 | 0.5497 | 161.77 | 0.7996 | 110.41 | | |
| 0.1001 | 51.92 | 0.3497 | 141.99 | 0.5998 | 158.83 | 0.8498 | 88.32 | | |
| 0.1501 | 74.99 | 0.4002 | 151.93 | 0.6495 | 152.44 | 0.8999 | 62.85 | | |
| 0.2003 | 95.19 | 0.4498 | 157.48 | 0.6996 | 141.90 | 0.9500 | 31.24 | | |
| 0.2499 | 113.18 | 0.5000 | 161.71 | 0.7502 | 127.83 | | | | |
| | | | | | | | | | |

Table 2. Coefficients, h_k , and Standard Deviations, s, for the Representation of

 $H_{m,12}^{E}$ by Eq 1 for the Binary Mixtures at 298.15 K

| component | | | | | | S |
|-----------|------|--------|--------|--------|-------|--|
| 1 | 2 | h_1 | h_2 | h_3 | h_4 | $\overline{\mathbf{J}\boldsymbol{\cdot}\mathbf{mol}^{-1}}$ |
| 1HX | nC7 | 246.37 | -14.39 | | | 0.33 |
| 1HX | nC8 | 270.08 | -20.36 | 0.63 | -9.71 | 0.19 |
| 1HX | nC10 | 362.13 | -41.43 | 9.33 | | 0.28 |
| 1HX | nC12 | 492.55 | -59.45 | | | 0.43 |
| 1HX | nC14 | 647.34 | -76.75 | -20.30 | | 0.66 |

Table 3. Values of the Interaction Parameters, A_{ii} and A_{ii}, Standard Deviations, s, and Isobaric Thermal Expansivities, α_p , at 298.15 K for the Liebermann–Fried **Model Calculations**

| component | | | | S | α _p (k | K ⁻¹) | |
|-----------|------|----------|----------|--|--------------------|---------------------------|--|
| i | j | A_{ij} | A_{ji} | $\overline{\mathbf{J}\boldsymbol{\cdot}\mathbf{mol}^{-1}}$ | i | j | |
| 1HX | nC7 | 1.0344 | 0.9178 | 0.33 | 1.411 ^a | 1.256^{b} | |
| 1HX | nC8 | 1.0646 | 0.8826 | 0.23 | 1.411 ^a | 1.164^{b} | |
| 1HX | nC10 | 1.0986 | 0.8296 | 0.36 | 1.411 ^a | 1.051^{b} | |
| 1HX | nC12 | 1.1107 | 0.7899 | 0.43 | 1.411 ^a | 0.960 ^b | |
| 1HX | nC14 | 1.1104 | 0.7582 | 0.78 | 1.411 ^a | 0.886 ^c | |

^a Riddick et al.⁸ ^b Benson et al.⁹ ^c Estimated from density data.¹

interaction parameters, A_{ij} and A_{ji} , for each of the binary mixtures are given in Table 3. These were obtained by fitting the Liebermann–Fried formula for $H^{\!\mathrm{E}}_{\mathrm{m},ij}$ to the primary experimental results in Table 1. Also included in Table 3 are values of the standard deviations s achieved in the fitting process and values^{8,9} of the isobaric thermal expansivities, α_p , of the components, used in evaluating the contributions due to different molecular sizes. It is evident from a comparison of the standard deviations in Tables 2 and 3 that the Liebermann-Fried model provides fits of the experimental data which are very similar to those obtained with the Redlich-Kister forms. This is illustrated in Figure 1, where the Liebermann–Fried values of $H_{m,12}^{E}$ are shown as broken curves and are hardly distinguishable from the solid Redlich-Kister fits.

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