# Thermodynamic Properties of Multialkane Synthetic and Real Petroleum Mixtures

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Measurements of enthalpy increments from the temperature of the ordered phases of low temperatures at 293.4 K up to the liquid phase above the melting point were carried out by differential scanning calorimetry using discontinuous mode temperature programming on 18 multiparaffinic mixtures, prepared by melting pure alkanes, and 4 commercial petroleum waxes. Temperatures and enthalpies of the solid/ solid transitions and melting were determined, as well as the total enthalpy variations from the order/ disorder transition onset temperature up to the melting end temperature and the heat capacity variations in the ordered solid solution and the liquid phase, as a function of temperature. The comparison of the experimental results with the values, calculated for equivalent ideal mixtures from the thermodynamic data of pure *n*-alkanes, allows us to highlight a deviation in relation to the ideality in the solid state for all of these mixtures: the ordered solid phase reveals a significant gap in relation to ideality, whereas the liquid mixtures show athermal behavior. The composition characteristic parameters of the mixtures (shape of the *n*-alkane mole fraction distribution, number of *n*-alkanes, and percentage of the other nonlinear hydrocarbons in the petroleum mixtures) are closely related to the degree of internal disorder in the solid solutions and thus to the deviation in relation to the ideality in the solid state.

### Introduction

The formation of solid deposits during the exploitation, transportation, and refining process of paraffinic crude oils is a major issue for the petroleum industry: the removal of the undesirable solids increases production costs. A better understanding of the complex *n*-alkane (hereafter denoted by  $C_n$ ) mixtures and the development of thermo-dynamic models enable us to predict their onset crystal-lization point, which will make it possible to adjust process operating parameters and reduce costs. The modeling requires thermodynamic data (phase-transformation temperatures and pseudoconstituents occurring in the solid/liquid equilibria.

A previous paper<sup>1</sup> proposed simple predictive relationships concerning the variations of the pure  $C_n$  thermodynamic properties as functions of the *n* carbon atom number of the  $C_n$  chain by combining new calorimetric experimental results<sup>2</sup> with a general review of literature data.<sup>3,4</sup>

In this article, the thermodynamic properties of complex multi- $C_n$  mixtures are obtained by differential scanning calorimetry to determine their thermodynamic characteristics in relation to the ideality in the solid phase and the liquid phase, also required for their modeling.

## **Further Details**

The term "synthetic mixtures", previously quoted in the literature,<sup>4–17</sup> is applied to the multi- $C_n$  mixtures obtained in the laboratory from 2, 3, 4...*N* pure  $C_n$ 's by the melting process and is used in relation to the term multi- $C_n$  "real mixtures" from industrial or commercial origin.

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Structural analyses carried out recently by X-ray diffraction on synthetic and real multi- $C_n$  complex mixtures highlighted the influence of specific parameters of the sample composition<sup>4–17</sup> on the final crystalline state, as follows:

(i) the width (number of C<sub>n</sub>'s, *N*) of the continuous distribution of  $x_n$  mole fractions of consecutive C<sub>n</sub>'s, determined by comparing 16 synthetic mixtures with  $x_n$  distributions of the exponential decreasing type<sup>4</sup> ( $x_{n+1} = 0.858x_n$ ; Figure 1a) and *N* numbers of consecutive C<sub>n</sub>'s from  $2 \le N \le 21$ ;

(ii) the shape of  $x_n$  distributions determined by comparing two  $C_{22}-C_{36}$  synthetic samples from  $C_{22}$  up to  $C_{36}$  (N=15) with two different<sup>4</sup>  $x_n$  distributions—one of normal logarithmic (or Gaussian) type and the other of exponential decreasing type (Figure 1);

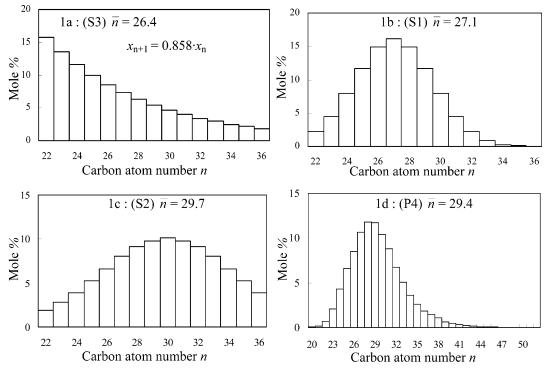
(iii) the standard deviation and the *n* real mean carbon atom number of the  $x_n$  distribution determined by comparing two C<sub>22</sub>-C<sub>36</sub> synthetic mixtures with  $x_n$  distributions of the normal logarithmic type, whose  $x_n$  compositions of C<sub>n</sub>'s are different;

(iv) the percentage of nonlinear hydrocarbons determined by comparing real and synthetic mixtures whose  $x_n$  distributions of the normal logarithmic type are identical.

The aim of our experimental calorimetric studies is to complete the previous structural analyses<sup>4-11</sup> and to determine the influence of the composition parameters on the thermodynamic properties.

## Synthetic Mixtures with C<sub>n</sub> Mole Fraction Distributions of the Exponential Decreasing Type

**Sample Preparation.** The industrial and commercial multi- $C_n$  samples that have been studied in the literature<sup>5–7,9,10</sup> show a continuous  $x_n$  distribution of the normal



**Figure 1.** Shapes of the  $x_n$  distributions of S1, S2, and S3 mixtures containing 15 identical  $C_n$ 's and a P4 real mixture: (a) distribution of exponential decreasing type (S3); (b–d) distribution of the normal logarithmic or Gaussian type (S1, S2, P4).

Table 1. Group 1, 2, and 3 Mixtures with $x_n$ Distributions of the Exponential Decreasing Type	Table 1.	Group 1. 2	2. and 3 Mixture	s with x <sub>n</sub> Distributi	ons of the Expon	ential Decreasing Type
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				first solid solution			second solid solution			third solid solution		
mixtures	N	$\bar{n}$	c/Å	$\bar{n}_{\rm c}$	structure	<i>c</i> /Å	$\bar{n}_{\rm c}$	structure	c/Å	$\bar{n}_{\rm c}$	structure	
C <sub>24</sub> -C <sub>25</sub>	2	24.5	66.2	24.2	$\beta' + \beta''$							
$C_{24} - C_{26}$	3	24.9	66.8	24.8	β"							
$C_{22} - C_{25}$	4	23.3	62.7	23.2	β'							
$C_{21} - C_{25}$	5	22.7	61.4	22.6	$\beta'$							
$C_{22} - C_{27}$	6	24.1	64.4	23.8	β'							
$C_{22} - C_{29}$	8	24.7	66.7	24.7	β'							
$C_{22} - C_{30}$	9	25.0	67.8	25.2	$\beta'$							
$C_{22} - C_{33}$	12	25.8	67.3	25.0	'β'	71.2	26.5	$\beta'$				
$\begin{array}{c} { m C}_{22} - { m C}_{35} \\ { m C}_{22} - { m C}_{36} {}^{b} \end{array}$	14	26.2	67.3	25.0	β'	75.1	28.0	$\beta'$				
$C_{22} - C_{36}^{b}$	15	26.4	67.5	25.0	β'	82.1	30.8	$\beta'$				
$C_{21} - C_{36}$	16	25.5	66.0	24.4	β'	83.6	31.3	$\beta'$				
$C_{20} - C_{36}$	17	24.7	63.3	23.4	$\beta' + \beta - \mathbf{RI}$	84.1	31.6	$\beta'$	65.9	24.4	$egin{smallmatrix} eta' \ eta' \end{pmatrix}$	
$C_{19} - C_{36}$	18	23.8	61.9	22.8	$\beta$ -RI	80.0	30.0	$\beta'$	72.9	27.2	β'	
$C_{18} - C_{36}$	19	23.0	59.8	22.0	$\beta$ -RI	83.7	31.4	$\beta'$	76.7	28.6	$\beta'$	
$C_{17} - C_{36}$	20	22.1	58.9	21.7	$\beta$ -RI	86.1	32.4	$\beta'$	73.8	27.5	$\beta'$	
$C_{16} - C_{36}$	21	21.2	56.8	20.8	$\beta$ -RI + $\alpha$ -RII	82.5	30.9	'β'	74.6	27.8	$\beta'$	

<sup>*a*</sup> Evolution of the crystalline solid phase number, long *c* parameter,  $\bar{n}_c$  (mean carbon atom number), and crystalline structure as a function of the *N* number of  $C_n$ 's in each sample, with  $\bar{n}$  corresponding to the mean carbon atom number of the mixtures. <sup>*b*</sup> Mixture corresponding to the S3 sample.

logarithmic type (Figure 1d). Here, 16 samples were composed of consecutive  $C_n$ 's whose  $x_n$  mole fractions decrease regularly according to the recurrence relationship  $x_{n+1} = \alpha x_n$ . The coefficient  $\alpha$  was fixed at 0.858 because this value corresponded to the average compositions observed in crude oils (Figure 1a). The mixtures were prepared by mass from solid pure  $C_n$ 's, followed by melting and thoroughly mixing. The homogeneous paraffinic liquid solution was allowed to cool to ambient temperature. All of the pure  $C_n$ 's were purchased from Fluka; their purity was  $\geq$ 98%, as determined by our gas chromatography analyses. The multi- $C_n$  mixtures were split into three characteristic groups (Table 1):

(i) group 1: four mixtures composed of a consecutive  $C_n$  number, N, as follows:  $2 \le N \le 5$  ( $C_{24}-C_{25}$ ,  $C_{24}-C_{26}$ ,  $C_{22}-C_{25}$ , and  $C_{21}-C_{25}$ );

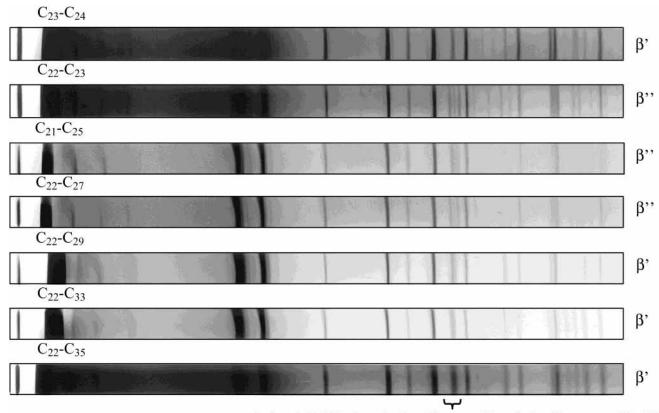
(ii) group 2: six mixtures with a middle width of  $x_n$  distributions (6  $\leq N \leq$  15) going from C<sub>22</sub>-C<sub>27</sub> to C<sub>22</sub>-C<sub>36</sub>;

the lightest  $C_n$  is always  $C_{22}$ , and these distributions differentiate themselves by the successive addition of heavier  $C_n$ 's from  $C_{27}$  to  $C_{36}$ .

(iii) group 3: six mixtures with larger  $x_n$  distributions  $(16 \le N \le 21)$  going from  $C_{21}-C_{36}$  to  $C_{16}-C_{36}$ : the heaviest  $C_n$  is always  $C_{36}$ , and these distributions differentiate themselves by the successive addition of lighter  $C_n$ 's from  $C_{22}$  up to  $C_{16}$ .

*X-ray Diffraction Studies.* All of these solid samples were analyzed by X-ray diffraction at ambient temperature (T = 294.15 K) according to two methods:

(i) A Guinier de Wolff Nonius camera was used to characterize the structure of the solid phases. This method provides a good separation of the Bragg reflections, especially in the  $21-22^{\circ}$  region of Bragg angles, where the symmetry of the structure can be identified. These experiments were carried out on powder samples using  $\lambda K\alpha$  copper radiation (Figure 2). The spacing between two



angular domain 21-22° = determination of the type of the orthorhombic structure :  $\beta$ ' or  $\beta$ ''

**Figure 2.** Structural identifications of multi- $C_n$  mixtures with distributions of the exponential decreasing type by comparison with the powder X-ray diffraction patterns carried out on binary mixtures ( $C_{23} + C_{24}$ ) and ( $C_{22} + C_{23}$ ), whose  $\beta'$  and  $\beta''$  intermediate-phase orthorhombic structures are known.

reflections was measured with an accuracy of 0.25 mm for distances ranging from 10.5 to 125 mm. Corrections were made employing spectroscopic pure gold as a standard. The exposure time of the films was fixed at 24 h for all experiments.

(ii) A counter diffractometer ( $\lambda K\alpha$  copper radiation) was used to bring out the number of solid solutions and their lattice parameters, especially the *c*-axis crystalline parameter along the carbon chains. The Bragg angle values were measured with an accuracy of 0.05°. The samples were prepared by slow cooling on a water surface of the melted  $C_n$  mixtures. This mode of sample preparation does not change the structural state of multi- $C_n$  mixtures and allows us to increase the intensity of the (001) diffraction lines by preferential crystallographic orientations, the carbon chains being perpendicular to the water surface. This experimental method allows to accurately determine

-the number of crystalline solid phases in the sample from the number of series of (001) harmonic diffraction peaks and

-the  $\bar{n}_c$  mean number of carbon atoms per molecule of each phase, determined from the experimental values of their *c* crystalline parameter.

Indeed,  $\bar{n}_c$  is calculated according to the relationship, established by Chevallier et al.<sup>12</sup> from the structural data of literature, concerning (*Pbcm*) orthorhombic pure odd-numbered  $C_n$ 's ( $n \le 41$ ,)<sup>4,13</sup> as follows:

$$c/\text{\AA} = 2.5448\bar{n}_{c} + 3.7504$$
 with  $c/\text{\AA} = 2d_{(002)}$   
 $\bar{n}_{c} = \frac{c - 3.7504}{2.5448}$ 

 $d_{(002)}$ /Å is equal to the thickness of the molecular layer in

the orthorhombic structure of pure odd-numbered  $C_n$ 's and molecular alloys. This thickness is equal to the length of the "average molecule" in the multi- $C_n$  phase.

Note that the real average  $\bar{n}$  of carbon atoms per molecule of mixture is calculated by the following relationship:

$$\bar{n} = \sum_{n_{\min}}^{n_{\max}} x_n n$$

with  $n_{\text{max}}$  and  $n_{\text{min}}$ , respectively, being the number of carbon atoms of the longest and the shortest  $C_n$ 's of the distribution.  $x_n$  is the mole fraction, and n is the number of carbon atoms of each  $C_n$ .

The characteristic structural parameters of these singlephase or polyphase samples, the number of crystallized solid solutions at ambient temperature, the crystalline *c* parameter and the  $\bar{n}_c$  mean number of carbon atoms of the solid phases, the crystallographic structure, and the  $\bar{n}$  real mean number of carbon atoms of the distribution are provided in Table 1. All of these structural data are necessary to understand the differences in the thermodynamic properties from one mixture to another.

(i) The mixtures of groups 1 and 2 with  $N \leq 11$  form a single solid phase whose orthorhombic structure is isostructural to the  $\beta'$  or  $\beta''$  ordered intermediate phase of binary and ternary  $C_n$  alloys.<sup>14–16</sup> A single periodicity of the molecular layer stacking along the long crystallographic c axis is observed; it corresponds to the mean chain length of a hypothetical orthorhombic odd-numbered  $C_n$  with a  $\bar{n}_c$  number of carbon atoms equal to the  $\bar{n}$  real mean number of carbon atoms of multi- $C_n$  mixtures with an

	Table 2.	Experimental	Thermodynamic	Properties of Grou	p 1, 2, and 3 Mixtures <sup>a</sup>
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					melting			order/di	sorder	total	
mixtures	ħ	$ar{M}$ g·mol^{-1}	$N \text{ of } C_n \text{ 's }$	number of solid solutions	$\Delta T_{\rm fus}({\rm exptl})$ /K	$\Delta_{\rm fus} H({\rm exptl}) / k J \cdot {\rm mol}^{-1}$	$\Delta_{\rm fus} h({\rm exptl}) / {\bf J} \cdot {\bf g}^{-1}$	$\Delta T_{o-d}(exptl) /K$	$\Delta H_{o-d}(exptl) / kJ \cdot mol^{-1}$	$\Delta H_{T_{\mathrm{o}-\mathrm{d}}}^{T_{\mathrm{fus}}}$ /kJ·mol <sup>-1</sup>	$\Delta h_{T_{\mathrm{o-d}}}^{T_{\mathrm{fus}}}$ /J·g <sup>-1</sup>
$C_{24} - C_{25}$	24.5	344.7	2	2	323.9-325.0	56.0	162.4	313.6-316.0	) 22.1	89.2	258.9
$C_{24} - C_{26}$	24.9	350.8	3	1	324.9 - 326.0	54.2	154.6	312.6 - 315.1	18.7	86.1	245.4
$C_{22} - C_{25}$	23.3	328.6	4	1	319.4 - 320.9	48.9	149.0	302.2 - 305.0	12.4	84.5	257.3
$C_{21} - C_{25}$	22.7	320.0	5	1	317.5 - 319.0	47.1	147.3	297.2 - 300.6	5 10.3	77.5	242.1
$C_{22} - C_{27}$	24.1	339.1	6	1	321.3 - 323.0	52.2	155.0	302.4 - 306.1	11.1	83.6	246.5
$C_{22} - C_{29}$	24.7	348.3	8	1	322.7 - 325.3	53.7	154.2	302.8-308.0	12.9	85.3	244.8
$C_{22} - C_{30}$	25.0	352.4	9	1	322.4 - 325.8	52.5	148.8	302.4-307.1	12.4	84.4	239.6
$C_{22} - C_{33}$	25.8	363.1	12	2	322.4 - 326.9	52.6	143.8	301.8-306.0	9.7	84.5	232.8
$C_{22} - C_{35}$	26.2	368.9	14	2	322.4 - 328.0	51.6	139.8	301.3-306.7	/ 13.3	85.9	233.0
$C_{22} - C_{36}$	26.4	371.4	15	2	322.5 - 329.8	52.1	140.4	302.2-306.0	8.3	88.1	237.3
$C_{21} - C_{36}$	25.5	359.7	16	2	319.9-328.7	47.8	132.8	297.0 - 300.9	7.6	83.5	232.0
$C_{20} - C_{36}$	24.7	347.8	17	2	317.1-327.6	47.2	135.8	b	b		
$C_{19} - C_{36}$	23.8	335.8	18	3	312.9-326.5	43.7	130.2	b	b		
$C_{18} - C_{36}$	22.9	323.5	19	3	306.7 - 324.6	44.2	136.6	b	b		
$C_{17} - C_{36}$	22.1	303.1	20	3	304.6 - 325.8	42.0	138.6	b	b		
$C_{16} - C_{36}$	21.2	298.5	21	3	301.4 - 325.7	42.4	142.0	b	b		

 $^{a} \Delta T_{\text{fus}}(\pm 0.5)/\text{K}$ , temperature range of melting;  $\Delta_{\text{fus}}H/\text{kJ}\cdot\text{mol}^{-1}$  and  $J\cdot\text{g}^{-1}$  (% diff = 3%), enthalpy of melting;  $\Delta T_{\text{o-d}}(\pm 0.5)/\text{K}$ , temperature range of order/disorder transition;  $\Delta H_{0-d}/\text{kJ}\cdot\text{mol}^{-1}$  and  $J\cdot\text{g}^{-1}$  (% diff = 3%), enthalpy of order/disorder transition;  $\Delta H_{T_{o-d}}^{T_{\text{lus}}}/\text{kJ}\cdot\text{mol}^{-1}$  and  $J\cdot\text{g}^{-1}$  (% diff = 3%), enthalpy variation from  $T_{0-d}$  to  $T_{\text{fus}(\text{end})}$ . <sup>*b*</sup> Not measured.

excess value close to one carbon atom<sup>5,6</sup> ( $\bar{n}_c \approx \bar{n} + 1$ ). Thus, all  $C_n$ 's combine into a single molecular layer: the longer molecules bend to insert themselves between the stacking planes and associate with shorter molecules to obtain a single solid solution with a dense structure.

(ii) The other samples of group 2 ( $12 \le N \le 15$ ) crystallize into two solid solutions with the same orthorhombic structure  $\beta'$  but with different  $\bar{n}_c$  mean numbers of carbon atom. The successive addition of heavier  $C_n$ 's to the distribution induces the instability of the multi- $C_n$  solid solution and the emergence of a second solid phase, richer in heavy  $C_n$ 's; the increase in the chain lengths' disparity requires a second molecular layer to combine all C<sub>n</sub>'s into dense and stable orthorhombic structures. The heavy C<sub>n</sub>'s that are added insert themselves into the structure whose stacking periodicity is compatible with their own chain length in order to minimize the molecular length gaps; they crystallize into the new heavy phase, whose  $\bar{n}_c$  average chain length gradually increases. The lighter phase, with a lower layer thickness, cannot accommodate these new heavy  $C_n$ 's and thus keeps an unchanged  $\bar{n}_c$  average composition.

(iii) For the mixtures of group 3, the broading of the  $C_n$  distribution (16  $\leq N \leq 21$ ) toward lighter  $C_n$ 's involves the emergence of a third solid solution with a middle value of the  $\bar{n}_c$  mean number of carbon atoms. This new solid phase is generated by the miscibility gap in the solid state of the light phase whose structure becomes unstable by the progressive intercalation of new light  $C_n$ 's and an increase in the chain lengths' disparity. The lighter  $C_n$ 's that are added crystallize mainly into the lighter phase; the  $\bar{n}_c$  mean number of carbon atom of this latter phase gradually decreases, whereas the average  $\bar{n}_c$  number of carbon atoms of the two other phases remains invariant.

The main observation is that the number of crystallized solid solutions increases with the *N* number of  $x_n$  distribution  $C_n$ 's of mixtures.

**Principle of Measurement and Operating Condi***tions.* The detailed principle of measurements and the description of the experimental method are defined in the literature,<sup>2,18–20</sup> with further details of the estimations of uncertainties in accuracy and reproductibility. The measurements of the enthalpy increments  $(H_{T_0}^T/\text{kJ}\cdot\text{mol}^{-1}; T_0 =$ 

Table 3. Experimental Specific Enthalpies of PhaseTransformations of Group 3 Mixtures Determined by theDSC Continuous Method

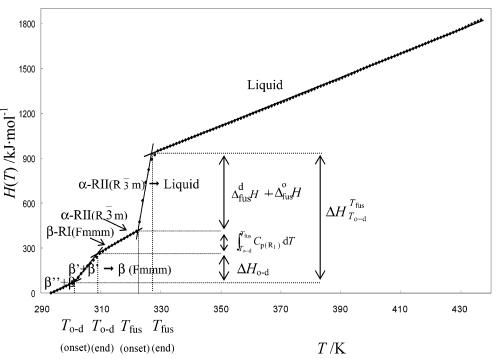
mixtures	$\Delta h_{\mathrm{o-d}}/\mathrm{J}{\cdot}\mathrm{g}^{-1}$	$\Delta h_{\mathrm{d-d}}/\mathrm{J}{\cdot}\mathrm{g}^{-1}$	$\Delta_{\rm fus} h/J \cdot g^{-1}$	$\Delta h_{T_{\mathrm{o-d}}}^{T_{\mathrm{fus}}}/\mathrm{J}{\cdot}\mathrm{g}^{-1}$
C22-C36	22.6	3.1	145.0	241.2
$C_{21} - C_{36}$	22.1	3.3	135.9	237.5
$C_{20} - C_{36}$	17.1	3.3	138.1	235.8
$C_{19} - C_{36}$	18.0	3.2	134.3	231.2
$C_{18} - C_{36}$		2.9	140.1	
$C_{17} - C_{36}$		3.0	142.9	
$C_{16} - C_{36}$		2.6	141.3	

293.4 K) were deduced from differential thermal analyses, performed with a differential scanning calorimeter of the Tian–Calvet type<sup>21</sup> (SETARAM DSC 111) using a discontinuous mode of temperature programming.<sup>2,18–20</sup> The repeatability and the accuracy of enthalpy and temperature measurements have been determined by using pure *n*-alkanes C<sub>18</sub> and C<sub>26</sub>.<sup>2,18–20</sup> The experimental enthalpy values are in good agreement with the literature results,<sup>22,23</sup> and this agreement justifies the experimental method used (percent difference < 1.5%); the accuracy of the temperature measurements is equal to  $\pm 0.5$  K.

The samples richest in light  $C_n$ 's of group 3 (from  $C_{20}$ – $C_{36}$  to  $C_{16}$ – $C_{36}$ ) are in equilibrium (liquid + solids) at 293.15 K, and differential thermal analyses (DTA) were performed with another differential scanning calorimeter of the Tian–Calvet type<sup>21</sup> (SETARAM DSC III) using a continuous mode of temperature programming with cooling or heating by the Peltier effect: the mixtures were heated from 263.15 K to 343.15 K at a rate of 0.5 K·min<sup>-1</sup>. The detailed principle of this device, which is very sensitive, and the description of the experimental method are defined in the literature.<sup>24</sup>

**Results and Discussion.** The experimental order/ disorder transition and melting onset and ending temperatures, the  $(\Delta H/kJ \cdot mol^{-1} \text{ and } \Delta h/J \cdot g^{-1})$  phase transformation enthalpies, and the  $(\Delta H_{T_{\text{trans}}}^{T_{\text{trans}}}/kJ \cdot mol^{-1}$  and  $\Delta h_{T_{\text{o-d}}}^{T_{\text{trans}}}/J \cdot g^{-1})$  enthalpy variations from the  $T_{\text{o-d}}$  order/ disorder transition onset temperature up to the liquid are reported in Tables 2 and 3.

(a) Enthalpy Increment Curves. The experimental enthalpies  $(H_{T_0}^T/\text{kJ}\cdot\text{mol}^{-1}; T_0 = 293.4 \text{ K})$  variations of 16



**Figure 3.** Enthalpy curve  $(H_{T_o}^T/kJ \cdot mol^{-1}; T_0 = 293.4 \text{ K})$  of the  $C_{22}-C_{35}$  multi- $C_n$  mixture of group 2 from the two-phase  $(\beta' + \beta'')$  ordered solid state up to the liquid phase.

multi- $C_n$  samples with respect to the temperature are listed in Supporting Information. Figure 3 shows the enthalpy increment curve as a function of increasing temperature, obtained for the two-phase sample  $C_{22}-C_{35}$ . With increasing temperature, the solid solution of single-phase systems or only the lighter phase of polyphase mixtures undergoes solid/solid transitions identical to those of the orthorhombic odd-numbered pure  $C_n^{1-7,12,14,16,17}$  (Figure 3):

$$\beta' \text{ or } \beta'' \xrightarrow{T_{o-d}} \beta(Fmmm) \Rightarrow \beta \text{-RI}(Fmmm) \xrightarrow{T_{d-d}} \alpha \text{-RII}(R\bar{3}m) \xrightarrow{T_{\text{fus}}} \text{liquid}$$

where  $\rightarrow$  denotes first-order transitions and  $\rightarrow$  denotes higher-order transitions.

In polyphase systems, the  $\beta'$  middle or heavier phases do not undergo any solid/solid transition up to the liquid phase, and the  $\Delta H_{T_{o-d}}^{T_{fus}}$  enthalpy variations can be decomposed into the following terms:

(i) single-phase sample:

$$\begin{split} \Delta H_{T_{\text{o}-\text{d}}}^{T_{\text{fus}}} &= \Delta H_{\text{o}-\text{d}} + \int_{T_{\text{o}-\text{d}}}^{T_{\text{fus}}} \mathbf{C}_{\rho(\text{R1})} \, \text{d} \, T \\ & (\text{or} + \int_{T_{\text{o}-\text{d}}}^{T_{\text{d}-\text{d}}} \mathbf{C}_{\rho(\text{R1})} \, \text{d} \, T + \Delta H_{\text{d}-\text{d}} + \\ & \int_{T_{\text{d}-\text{d}}}^{T_{\text{fus}}} \mathbf{C}_{\rho(\text{R2})} \, \text{d} \, T)^* + \Delta_{\text{fus}}^{\text{d}} H \end{split}$$

with  $\Delta H_{\text{o-d}}$  and  $\Delta H_{\text{d-d}}$ , enthalpies of order/disorder and disorder/disorder solid/solid transitions;  $T_{\text{o-d}}$  and  $T_{\text{d-d}}$ , onset temperatures of order/disorder and disorder/disorder solid/solid transitions;  $\Delta_{\text{fus}}^{\text{d}} H$ , enthalpy of melting of the disordered rotator phase (R<sub>1</sub> or R<sub>2</sub>), stable below the melting onset temperature;  $T_{\text{fus}}$ , the melting temperature;

$$\int_{T_{\rm o-d}}^{T_{\rm fus}} C_{p({\rm R}1)} \, {\rm d}\, T, \, \int_{T_{\rm o-d}}^{T_{\rm d-d}} C_{p({\rm R}1)} \, {\rm d}\, T, \, {\rm and} \, \int_{T_{\rm d-d}}^{T_{\rm fus}} C_{p({\rm R}2)} \, {\rm d}\, T,$$

the enthalpy consumption in the temperature domains of rotator phases; and  $C_{p(R1)}$  and  $C_{p(R2)}$ , the heat capacities of

the  $\beta$ -RI(*Fmmm*) and  $\alpha$ -RII( $R\bar{3}m$ ) disordered rotator phases<sup>1-7,17</sup>.

(ii) polyphase sample:

$$\begin{split} \Delta H_{T_{\text{o}-d}}^{T_{\text{fus}}} &= \Delta H_{\text{o}-d} + \int_{T_{\text{o}-d}}^{T_{\text{fus}}} \mathbf{C}_{\rho(\text{R1})} \, \mathrm{d}T \\ & (\text{or} + \int_{T_{\text{o}-d}}^{T_{\text{d}-d}} \mathbf{C}_{\rho(\text{R1})} \, \mathrm{d}T + \Delta H_{\text{d}-d} + \\ & \int_{T_{\text{d}-d}}^{T_{\text{fus}}} \mathbf{C}_{\rho(\text{R2})} \, \mathrm{d}T)^* \\ & + \Delta_{\text{fus}}^{\text{d}}H + \mathbf{z} (\Delta_{\text{fus}}^{\text{o}}H + \int_{T_{\text{o}-d}}^{T_{\text{fus}}} \mathbf{C}_{\rho(\beta)} \, \mathrm{d}T) \end{split}$$

with *z*, the number of  $\beta'$  solid solutions, stable up to the melting point;

 $\Delta^{\rm o}_{\rm fus} H$ , the enthalpy of melting of the  $\beta'$  ordered orthorhombic structure;

 $C_{\boldsymbol{p}(\!\beta\!)}\!,$  the heat capacity of the  $\beta'$  ordered orthorhombic structure; and

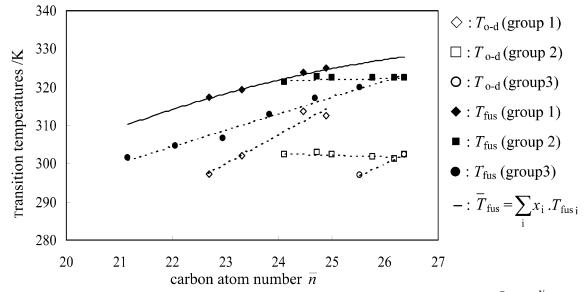
\*
$$(\int_{T_{\rm o-d}}^{T_{\rm d-d}} C_{p({\rm R}1)} \, \mathrm{d}\, T + \Delta H_{\rm d-d} + \int_{T_{\rm d-d}}^{T_{\rm fus}} C_{p({\rm R}2)} \, \mathrm{d}\, T)$$

if the disorder/disorder solid/solid transition is observed in the sample.

**(b)** Phase-Transformation Temperatures. Figure 4 represents the variations in the onset temperatures of the order/disorder transition and melting in relation to the  $\bar{n}$  real average number of carbon atoms of the mixtures and the  $\bar{T}_{fus}$  average melting temperatures, calculated by a linear combination of the  $T_{fus}$  *i* melting temperatures of pure  $C_n$ 's ( $\bar{T}_{fus} = \sum_{i=1}^N x_i T_{fus}$  *i*).

These variations in the experimental transformation temperatures point out three particular behaviors linked to the  $x_n$  distribution of mixtures, particularly to the value of the  $\bar{n}_c$  mean number of carbon atoms of the solid solution that undergoes solid/solid transitions:

(i) For the single-phase mixtures of groups 1 and 2 ( $N \le$  11), the experimental melting points increase with respect



**Figure 4.** Transformation onset temperatures of mixtures of groups 1–3 compared to the variations in the  $(\bar{T}_{fus} = \sum_{i=1}^{N} x_i T_{fus})$  average melting temperatures versus the  $\bar{n}$  real mean number of carbon atoms of the mixtures.

to  $\bar{n}$ , the average number carbon atoms of mixtures, and are brought into alignment with the  $\bar{T}_{\rm fus}$  average values calculated (Figure 4). Below the fusion temperature, these mixtures show a disordered rotator state that is close to ideality according to the literature.<sup>25–28</sup>

(ii) For the two-phase mixtures of group 2, the onset temperatures of the order/disorder transition and melting are lower than those of group 1 samples and remain invariant because the  $\bar{n}_c$ 's, mean numbers of carbon atoms, of the lightest solid solution of two-phase mixtures are almost equal and close to 25 (Table 1). These observations confirm the structural results of the X-ray diffraction studies: the addition of heavy  $C_n$  to the distribution affects only the heaviest phase, the average composition of the light solid solution remaining unchanged.

(iii) For the seven mixtures of group 3, the onset temperatures of the order/disorder transition and the melting decrease (Figure 4). Indeed, according to the structural observations by X-ray diffraction, the  $\bar{n}_c$  mean number of carbon atoms of the lightest phase decreases in relation to the successive addition of lighter  $C_n$ 's (Table 1).

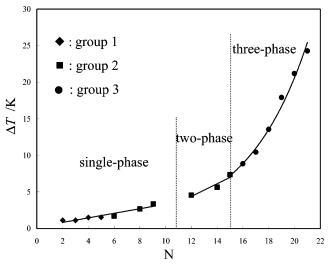
Note that the  $\bar{n}$  real average number of carbon atoms of polyphase mixtures is not the only parameter to take into account in the melting-point estimation. It is necessary to know the  $\bar{n}_c$  average composition of each phase in the polyphase systems.

The  $\Delta T$  gap between the temperatures of the onset and end of fusion also varies in relation to the width of the  $x_n$ distribution. Figure 5 represents the  $\Delta T (\Delta T = T_{\text{fus(onset)}} - T_{\text{fus(end)}})$  variations as a function of the *N* number of *C*<sub>n</sub>'s of the  $x_n$  distribution. Three behaviors can be distinguished:

(i) Single-phase systems:  $\Delta T$  increases linearly with a weak slope (Figure 5).

(ii) Two-phase systems of group 2:  $\Delta T$  also increases linearly with a higher slope (Figure 5);  $T_{\text{fus (onset)}}$ , depending on the lightest solid phase, whose  $\bar{n}_c$  is constant, is invariant (Figure 4), whereas  $T_{\text{fus(end)}}$  increases as a function of the progressive enrichment of a heavier phase in heavy  $C_n$ 's.

(iii) Three-phase systems of group 3:  $\Delta T$  varies exponentially (Figure 5) because  $T_{\text{fus(onset)}}$  strongly decreases with the important enrichment of low-molecular-mass  $C_n$ 's in the lightest phase but  $T_{\text{fus(end)}}$  is constant, the average composition of the heaviest phase remaining unchanged.

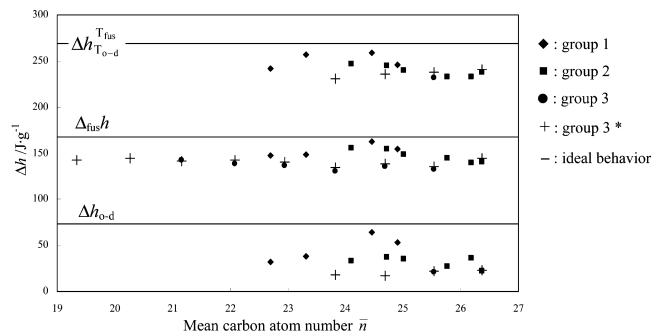


**Figure 5.** Variations of the  $\Delta T$  gap ( $\Delta T = T_{\text{fus(onset)}} - T_{\text{fus(end)}}$ ) as a function of the *N* number of C<sub>*n*</sub>'s in the samples.

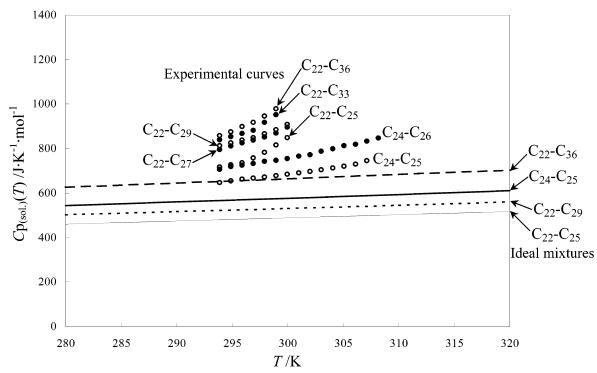
(c) Phase-Transformation Enthalpies. The variations in the  $\Delta h_{0-d}$  order/disorder transition specific enthalpies, the  $\Delta_{fus}h$  melting specific enthalpy, and the  $\Delta h_{T_{0-d}}^{T_{liss}}$  total specific enthalpy are represented in Figure 6 as functions of the  $\bar{n}$  real average number of carbon atom of the mixtures. The experimental phase-transition specific enthalpies are scattered around a mean value, independent of the N number of mixture  $C_n$ 's (Tables 2 and 3):  $\Delta h_{0-d}/$  $J \cdot g^{-1} = 36.3 \pm 1.1$ ;  $\Delta_{fus}h/J \cdot g^{-1} = 144.5 \pm 4.3$ ;  $\Delta h_{T_{0-d}}^{T_{liss}}/J \cdot g^{-1}$  $= 242.3 \pm 7.3$ 

The experimental measurements, determined by DSC and DTA (Tables 2 and 3), are compared with the values calculated from the thermodynamic data<sup>1-4,17</sup> of pure C<sub>n</sub>'s for equivalent ideal mixtures:  $(\Delta \bar{h} = \sum_{i=1}^{N} x_i \Delta h_i; \Delta h_{o-d}/J \cdot g^{-1} = 72; \Delta_{fus}h/J \cdot g^{-1} = 165; \Delta h_{T_{o-d}}^{T_{us}}/J \cdot g^{-1} = 269)$  (Figure 6). The difference between the experimental and calculated values allows us to estimate the deviation in relation to the ideality of mixtures. Figure 6 shows that this difference is always positive.

Indeed,  $C_n$  molecules tend to move away in the paraffinic system to minimize the energies of interaction; the association of molecules of different lengths to form a stable molecular layer in a single solid phase requires a supple-



**Figure 6.** Comparison between the experimental specific enthalpies of phase transformations of the mixtures of groups 1–3 versus the  $\bar{n}$  mean number of carbon atoms in the samples and the values calculated for the equivalent ideal mixtures<sup>1</sup>:  $\Delta h_{T_{o-d}}^{T_{ins}}/J \cdot g^{-1} = 269$ ;  $\Delta_{fus}^{d}/h/J \cdot g^{-1} = 165$ ;  $\Delta h_{o-d}/J \cdot g^{-1} = 72$ ; \* experimental values (+) determined by the DSC continuous method.



**Figure 7.** Comparison between the smoothed curves of experimental heat capacities, in the ordered solid phases near the ordered/ disordered transition temperatures, of group 1 and 2 mixtures versus temperature. Variations in equivalent ideal mixtures (–), situated in the linear part of the function, stemming from Eintein solid's model ( $C_p(T)$ , eq 1).

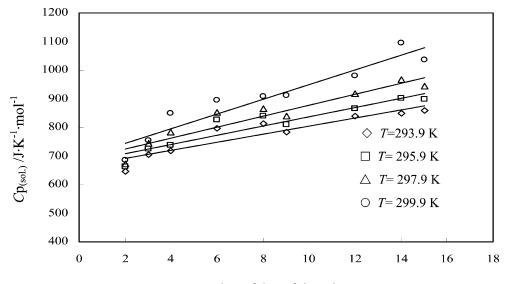
ment of energy, called the "energy of formation of the solid phase". By deduction, the greater the chain lengths' disparity, the higher the energy, the more significant the molecular disorder, and the greater the deviation in relation to ideality. However, this correlation between the amplitude of the deviation in relation to the ideality and the  $C_n$  distribution width is not clearly noticeable, although we note a behavior very close to ideality for the binary mixture  $C_{24}-C_{25}$  ( $\bar{n} = 24.5$ ) (Figure 6).

(d) Heat Capacities in the Ordered Solid Phase. The experimental heat capacity variations of the ordered phase

and those calculated for the equivalent ideal mixtures ( $C_p = \sum_{i=1}^{N} x_i C_{p_i}$ ) are reported in Figure 7 as a function of the temperature. The  $C_{p_i}$  heat capacities of pure  $C_n$ 's are calculated by the predictive equation stemming from the Einstein solid model, established in a previous paper,<sup>1</sup> as follows:

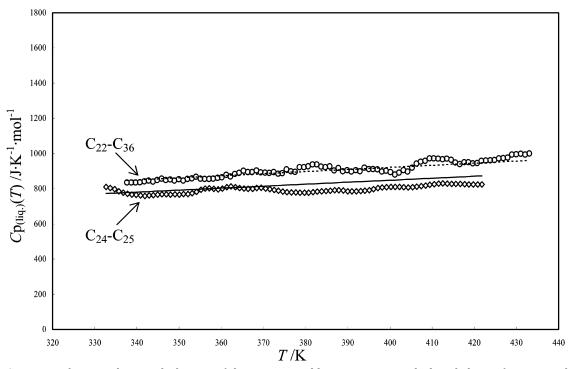
$$C_{p}(T) = 3NR \left(\frac{\theta}{T}\right)^{2} \frac{\exp^{(\theta/T)}}{\left(\exp^{(\theta/T)} - 1\right)^{2}} + cT + dT^{2}$$
(1)

with  $C_p(T)/J\cdot K^{-1}\cdot mol^{-1}$ , the heat capacity of the  $C_n$  in the



N number of  $C_n$ s of the mixtures

**Figure 8.** Isothermal evolutions of the heat capacity in the ordered solid phase as a function of the N number of  $C_n$ 's of the samples.



**Figure 9.** Comparison between the smoothed curves of the experimental heat capacities, in the liquid phase, of group 1 and 2 samples versus temperature and those of equivalent ideal mixtures calculated by  $C_{p(\text{liq})}$  (eq 2).

solid ordered phase at constant pressure ( $P = P_0 = 1$  atm); *T*/K, the considered temperature;  $R/J\cdot K^{-1}\cdot mol^{-1} = 8.314$ , the perfect gas constant; *N*, the number of oscillators per  $C_n$  molecule (each  $C_n$  molecule behaves like a monatomic solid of *N* atoms having 3*N* independent harmonic vibrations);  $\theta$ , the Einstein temperature characteristic of the oscillation frequency of the harmonic vibrations of the atoms; and  $c/K^{-2}$  and  $d/K^{-3}$ , the coefficients of the quadratic part introduced to take into account the skeletal vibrational contribution.

The four parameters *N*,  $\theta$ , *c*, and *d* are all functions of the *n* number<sup>1</sup> of carbon atoms of the C<sub>n</sub> chain.

The comparison of the experimental and ideal  $C_p$  values (Figure 7) and the experimental  $C_p$  variations as a function of N, represented by the isotherm curves of Figure 8, involve the following comments:

(i) Because of the mixture effect, the experimental heat capacity values are always higher than the equivalent ideal mixture values: the arrangement of molecules of different lengths in a single multi- $C_n$  solid phase is more disordered than the equivalent assemblage of the "almost perfect" crystals of pure  $C_n$ 's. Greater disorder generates weaker molecular interactions and, thus, a higher amplitude of oscillatory movements, which leads to higher heat capacity values,

(ii) The gap between experimental and ideal values (Figures 7) and the  $C_p$  experimental values (Figures 8) increase in relation to the following: The *N* number of  $C_n$ 's of the  $x_n$  distribution because increasing the *N* number of different molecules induces greater disorder in the molecular layers. The temperature that exponentially increases the conformational defects<sup>4</sup> in the carbon chains in the

course of heating (not taken into account by the Einstein model<sup>1</sup>), particularly near the solid-solid transition temperature.

(e) Heat Capacities in the Liquid Phase. The experimental  $C_{p(\text{liq})}$  heat capacity variations in the liquid phase, as a function of the temperature, are reported in Figure 9 for two samples and are compared with the variations calculated for their ideal mixture, equivalent to a pure  $C_n$  with the number of carbon atoms equal to the  $\bar{n}$  real average number of carbon atoms of the mixture distribution. The ideal heat capacity values were calculated by the relation derived from the group contribution method and established for pure  $C_n$ 's in a previous paper<sup>1</sup>:

$$C_{p(\text{liq})}/\text{J}\cdot\text{K}^{-1}\cdot\text{mol}^{-1} = (0.0343\bar{n} + 0.2855)T + 24.587\bar{n} - 203.370 \quad (2)$$

$$\bar{n} = \sum_{n_{\min}}^{n_{\max}} x_n n$$

*n*: real mean number of carbon atoms of mixtures

All of the liquid mixtures studied present the same behavior, whatever the distribution width and the mean composition. As for the two cases of Figure 9, the heat capacities increase linearly with respect to the temperature, and good agreement is observed between experimental and ideal values. The multiparaffinic liquid mixtures do not show any excess heat capacity,<sup>17,29–33</sup> related to two possibilities: a nil excess enthalpy or an excess enthalpy independent of the temperature.

Measurements of the mixing enthalpy of two multi- $C_n$  liquid phases, carried out by mixing calorimetry,<sup>17</sup> and previous calorimetric experiments of paraffinic mixture dissolving in hydrocarbon liquid phases<sup>29–33</sup> confirm the athermal behavior of multi- $C_n$  synthetic mixtures in the liquid state: the experimental specific enthalpy of mixing of two paraffinic complex liquids<sup>17,29–33</sup> is lower than 1 J·g<sup>-1</sup>.

This behavior can be generalized to all the multi- $C_n$  liquid mixtures, whatever their composition and the N number of  $C_n$ 's: their heat capacity can estimated by the  $Cp_{(liq)}$  previous eq 2.

# Synthetic and Commercial Multi-C<sub>n</sub> Mixtures with C<sub>n</sub> Mole Fraction Distributions of the Normal Logarithmic Type

**Sample Characterization.** The industrial and commercial multi- $C_n$  samples show  $x_n$  mole fraction continuous distributions of consecutive  $C_n$ 's of the normal logarithmic type<sup>5–7,9,10</sup> (Figure 1d). According to Pauly et al.<sup>34</sup> and Dauphin et al.,<sup>35</sup> the complex liquid mixtures, whose  $x_n$  distributions are the exponential decreasing type (Figure 1a) as observed in petroleum cuts, form solid deposits with  $x_n$  distributions of the normal logarithmic type. Calorimetric analyses are also required to determine the thermodynamic properties of these complex mixtures, which are defined as follows:

(i) Four commercial mixtures purchased from Prolabo, called in its commercial catalog paraffins 52-54 °C, 54-56 °C, 58-60 °C ,and 60-62 °C; they are respectively denoted P1, P2, P3, and P4. They are mainly composed of consecutive  $C_n$ 's, from  $C_{20}$ , with  $23 \le N \le 33$ . The other nonlinear hydrocarbons are branched alkanes or naphtens (Table 4). Their structural and thermodynamic states were described in the literature.<sup>4-8</sup>

Table 4. Compositions in $C_n$ 's of the Mixtures with $x_n$	
Distributions of the Normal Logarithmic Type <sup>a</sup>	

Distrib	utions of	the No	rmal Log	arithmic	Type <sup>a</sup>	
	S1	S2	P1	P2	P3	P4
C <sub>20</sub>			0.07	0.05	0.02	0.04
C <sub>21</sub>			0.77	0.45	0.06	0.18
C <sub>22</sub>	2.2	1.9	4.63	2.89	0.44	0.68
C <sub>23</sub>	4.5	2.8	12.82	8.00	1.81	2.08
$C_{24}$	7.9	3.9	20.09	13.10	5.08	4.25
$C_{25}$	11.7	5.2	18.32	14.35	9.19	6.59
$C_{26}$	14.9	6.6	14.64	15.46	14.46	8.48
$C_{27}$	16.2	8	9.40	13.26	15.63	10.62
C <sub>28</sub>	14.9	9.1	6.76	11.44	15.81	11.76
C <sub>29</sub>	11.7	9.8	4.85	8.85	14.00	11.72
C <sub>30</sub>	7.9	10.1	3.51	6.24	11.37	10.38
C <sub>31</sub>	4.5	9.8	2.28	3.45	7.14	8.81
C <sub>32</sub>	2.2	9.1	1.02	1.56	3.28	6.70
C <sub>33</sub>	0.9	8	0.39	0.56	1.10	5.07
C <sub>34</sub>	0.3	6.6	0.18	0.21	0.38	3.57
C <sub>35</sub>	0.1	5.2	0.09	0.08	0.13	2.59
C <sub>36</sub>	0.02	3.9	0.06	0.03	0.05	1.83
C <sub>37</sub>			0.04	0.02	0.02	1.42
C <sub>38</sub>			0.03	0.01	0.01	1.04
C <sub>39</sub>			0.02	0.01	0.01	0.64
$C_{40}$			0.01	0.01	0.00	0.49
C <sub>41</sub>			0.01			0.32
$C_{42}$			0.01			0.25
$C_{43}$						0.16
C44						0.11
$C_{45}$						0.07
$C_{46}$						0.06
C47						0.03
C <sub>48</sub>						0.02
C <sub>49</sub>						0.02
C <sub>50</sub>						0.02
C <sub>51</sub>						0.01
$C_{52}$						0.01
$\bar{n}_{\rm c}$	27.1	29.7	25.6	26.4	27.8	29.4
$\overline{M}$	381.5	417.5	328.6	372.0	390.6	413.2
%C <sub>n</sub> 's	100	100	93.69	86.92	86.43	76.72

 $^a$  S1 and S2 multiparaffinic synthetic and P1, P2, P3, and P4 commercial mixtures.

(ii) Two synthetic mixtures (denoted S1 and S2), obtained by melting 15 pure  $C_n$ 's ranging from  $C_{22}$  to  $C_{36}$  (Table 4, Figure 1b and c):

-S1: variance of 2.50 and shifting of the center of the Gaussian law of 1.5 carbon atoms toward light  $C_n$ 's;

-S2: variance of 4.35 and shifting of 1.5 carbon atoms toward heavy  $C_n$ 's.

The structural analyses carried out by X-ray diffraction at ambient temperature (T = 294.15 K)<sup>4–8</sup> reveal that all of these commercial and synthetic mixtures form a single solid solution, isostructural to the  $\beta'$  ordered intermediate phase of binary and ternary C<sub>n</sub> alloys.<sup>14–16</sup>

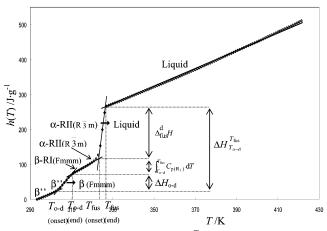
Results and Discussion. The experimental order/ disorder transition and melting onset and end temperatures, the transition enthalpies, and the  $(\Delta H/kJ \cdot mol^{-1}$  and  $\Delta h/J \cdot g^{-1}$ ) total enthalpy variations are given in Table 5 with the compositional characteristics of each mixture. The experimental enthalpy  $(H_T^T/kJ \cdot mol^{-1} \text{ or } h/J \cdot g^{-1}; T_0 =$ 293.4 K) increments with respect to the temperature are listed for each sample in Supporting Information. Figure 10 shows the specific enthalpy increment curve as a function of the increasing temperature obtained for P4. With increasing temperature, all of the mixtures undergo order/disorder and disorder/disorder solid/solid transitions identical to those of the odd-numbered  $C_n$ 's, with the successive appearance of the high-temperature disordered rotator orthorhombic  $\beta$ -RI(*Fmmm*) and rhomboedric  $\alpha$ -RII- $(R\bar{3}m)$  structures.<sup>4,7</sup>

**Phase-Transformation Temperatures and Enthal pies.** The variations in the experimental transition tem-

Table 5. Experimental Thermodynamic Properties of S1 and S2 Synthetic Mixtures and of P1, P2, P3, and P4
Commercial Waxes <sup>a</sup>

					n	melting			order/disorder			total	
mixtures	ħ	$ar{M}$ /g·mol^{-1}	%C <sub>n</sub> 's	$N$ of $C_n$ 's	$\Delta T_{\rm fus} / { m K}$	$\Delta^{\mathrm{d}}_{\mathrm{fus}}H$ /kJ·mol <sup>-1</sup>	$\Delta^{\rm d}_{\rm fus}h/{ m J}\cdot { m g}^{-1}$	$\Delta T_{ m o-d} /  m K$	$\Delta H_{ m o-d}$ /kJ·mol <sup>-1</sup>	$\Delta h_{\mathrm{o-d}}$ /J·g <sup>-1</sup>	$\Delta H_{T_{\mathrm{o}-\mathrm{d}}}^{T_{\mathrm{fus}}}$ /kJ·mol <sup>-1</sup>	$\Delta h_{T_{\mathrm{o-d}}}^{T_{\mathrm{fus}}}$ /J·g <sup>-1</sup>	
S1	27.1	381.5	100	15	327.7 - 331.4	62.6	164.0	312.5-315.8	19.8	52.0	93.7	245.7	
S2	29.7	417.5	100	15	? - 339.7			324.9-?			102.1	244.4	
P1	25.6	328.6	93.7	23	323.2 - 326.3		146.1	304.0-308.7		46.4		233.0	
P2	26.4	372.0	86.9	21	324.8 - 328.7		144.3	307.2 - 313.5		37.9		221.8	
P3	27.8	390.6	86.4	21	328.2 - 332.1		150.3	311.1-318.6		44.1		227.0	
P4	29.4	413.2	76.7	33	327.7 - 334.6		147.4	311.2 - 319.4		39.7		229.1	

<sup>*a*</sup>  $\Delta T_{\text{fus}}(\pm 0.5)/\text{K}$ , temperature range of melting;  $\Delta_{\text{fus}}^{\text{d}} H/\text{k} J \cdot \text{mol}^{-1}$  and  $J \cdot g^{-1}$  (% diff = 3%), enthalpy of melting;  $\Delta T_{o-d}(\pm 0.5)/\text{K}$ , temperature range of order/disorder transition;  $\Delta H_{o-d}/J \cdot \text{mol}^{-1}$  and  $J \cdot g^{-1}$  (% diff = 3%), enthalpy of order/disorder transition;  $\Delta H_{T_{n-d}}^{T_{\text{fus}}}/\text{k} J \cdot \text{mol}^{-1}$  and  $J \cdot g^{-1}$  (% diff = 3%), enthalpy of order/disorder transition;



**Figure 10.** Specific enthalpy curve  $(h_{T_o}^T/k\mathbf{J}\cdot\mathbf{g}^{-1}; T_o = 293.4 \text{ K})$  for the P1 real wax from the  $\beta''$  ordered phase up to the liquid phase above the melting point.

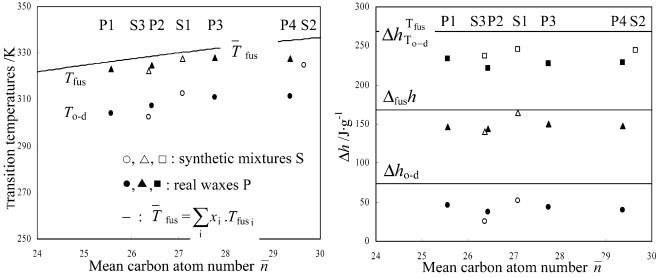
peratures and specific enthalpies are reported in Figure 11 as functions of the  $\bar{n}$  real average number of carbon atoms of the single solid phase of mixtures, and they are compared with the  $\bar{T}$  average melting temperatures ( $\bar{T}_{\text{fus}} = \sum_{i=1}^{N} x_i T_{\text{fus}}$ ) and transformation specific enthalpies<sup>1</sup> of equivalent ideal solid solutions ( $\Delta \bar{h} = \sum_{i=1}^{N} x_i \Delta h_{i}$ ;  $\Delta h_{T_{\text{tor}}}^{T_{\text{tor}}}$ , J·g<sup>-1</sup> = 269;  $\Delta_{\text{fus}}^{\text{d}}h$ /J·g<sup>-1</sup> = 165;  $\Delta h_{\text{o-d}}$  /J·g<sup>-1</sup> = 72)<sup>1</sup>. To highlight the influence of the shape of the  $x_n$  distribution on the thermodynamic behavior of the synthetic paraffinic

mixtures, the phase-transformation temperatures and enthalpies of the two-phase sample  $C_{22}-C_{36}$  of group 2, composed of same consecutive pure  $C_n$ 's ranging from  $C_{22}$ to  $C_{36}$  (Figure 1a) and denoted S3, are reported in Figure 11:

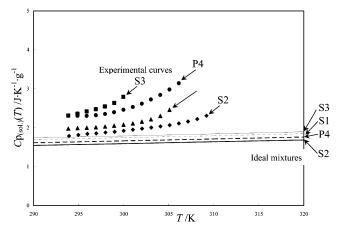
(i) The transformation temperatures of S1 are closer to the calculated average temperatures than those of S3. For sample S2, the order/disorder transition and melting temperatures are very close, and an accurate separation of the two transformations is not possible. Only the value of the  $\Delta h_{T_{a-d}}^{T_{lus}}$  total enthalpy appears in Table 5. The order/disorder transition onset temperature of S2 is higher than those of the S1 and S3 because its composition is richer in heavy C<sub>n</sub>'s.

(ii) The gap between measured and calculated temperatures is constant for P1, P2, and P3, but it considerably increases for P4 (Figure 11), which presents a higher percentage of nonlinear hydrocarbons and an *N* higher  $C_n$ number (Table 4). However, these gaps are slightly greater than those of S1 and S2 but slightly lower than that of S3.

The phase-transformation specific enthalpies of singlephase samples S1 and S2 show behavior closer to ideality than those of two-phase sample S3 (Figure 11). P1, P2, P3, P4, and S3 reveal similar deviations between the experimental enthalpy values and those of equivalent ideal mixtures (Figure 11). The presence of other hydrocarbons involves in P1, P2, P3, and P4 deviations in relation to the ideality identical to that observed in two-phase sample S3.



**Figure 11.** Evolutions of the experimental temperatures and specific enthalpies of phase transformations of S1, S2, S3, P1, P2, P3, and P4 samples versus their  $\bar{n}$  real mean number of carbon atoms compared to the corresponding values of equivalent ideal mixtures<sup>1</sup> (–):  $\Delta h_{T_{u-d}}^{T_{ins}}$  **J**·**g**<sup>-1</sup> = 269;  $\Delta_{f_{us}}^{d}h$ /**J**·**g**<sup>-1</sup> = 165;  $\Delta h_{0-d}$ /**J**·**g**<sup>-1</sup> = 72.



**Figure 12.** Comparison between the smoothed curves of the experimental heat capacities, in the ordered solid phases, of S1, S2, S3, and P4 versus temperature and the values of equivalent ideal mixtures (–), situated in the linear part of the function, stemming from thte Eintein solid model ( $C_p(T)$ , eq 1).

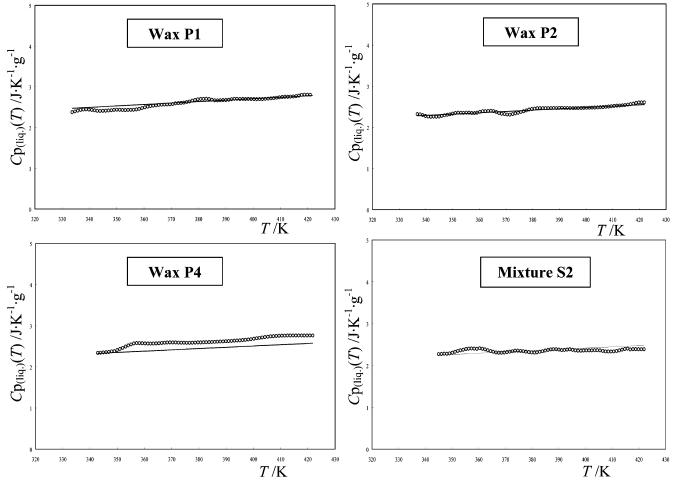
These results highlight the fact that the disorder is higher in synthetic mixtures with a  $x_n$  distribution of the exponential decreasing type (Figure 1a) than in samples with a  $x_n$  distribution of the normal logarithmic type composed of the same  $C_n$ 's (Figure 1b and c). In the mixtures with  $x_n$  distributions of the normal logarithmic type, the value of the  $\bar{n}$  average number of carbon atoms of the single solid phase is situated at the center of gravity of the Gaussian curve (Figure 1b–d) near the majority of  $C_n$ 's, which impose single-crystalline organization and a single *c* parameter corresponding to a molecular layer thickness close to the mean length of their chain, on the lighter and heavier minority  $C_n$ 's. In the case of  $x_n$  distributions of the exponential decreasing type, the value of  $\bar{n}$ , the average number of carbon atoms of the mixtures, is situated near  $C_n$ 's that are not the majority (Figure 1a). For  $C_n$  numbers of  $N \ge 12$ , single-crystalline organization can be imposed neither by these minority  $C_n$ 's nor by the  $C_n$ 's, the lightest of which here are the majority but are too short; this state leads to a higher conformational disorder in these single- or polyphase mixtures.

For the commercial mixtures, the higher internal disorder in relation to that of S1 and S2 is generated by a higher N number of  $C_n$ 's and the ratio of the other hydrocarbons (Table 4).

Whatever the characteristics of the distribution, the synthetic and real mixtures in the solid state present a difference between the thermodynamic experimental results and the ideal values. This gap indicates the enthalpy of formation of the solid solution, which always positive.

# Heat Capacity Variations as a Function of the Temperature

*Heat Capacities in the Ordered Solid Phase.* Figure 12 depictes the experimental specific heat capacity variations of P4, S1, S2, and S3 and those of ideal mixture values  $\overline{(C_p = \sum_{i=1}^{N} x_i C_{p_i})}$  as a function of temperature in the low-temperature ordered phases:  $C_{p_i}$  of pure  $C_n$ 's calculated according to eq 1.



**Figure 13.** Comparison between the smoothed variations of the experimental heat capacities, in the liquid phase, of P1, P2, P4, and S2 versus temperature and those of equivalent ideal mixtures (–), calculated by  $C_{p(liq)}$  (eq 2).

The analysis of the results leads to the following observations:

(i) The experimental heat capacity values are always higher than those calculated for an ideal mixture (because of the mixture effect) and increase gradually at the approach of the order/disorder transition temperatures.

(ii) The heat capacities of S1 and S2 are much lower than those of S3. In S1 and S2 the Gaussian law of  $x_n$  distributions leads to a single ordered phase with stronger intermolecular interactions,

(iii) P1, P2, P3, and P4, whose heat capacity values are similar, show significant gaps between ideal and experimental results; they can be imposed by the ratio of other hydrocarbons and/or the width of the distribution. These deviations in relation to the ideality in the ordered solid phase are close to those observed for S3.

*Heat Capacities in the Liquid Phase.* Figure 13 compares the variations in the S2, P1, P2, and P4 experimental specific heat capacities to the values (eq 2) of  $C_n$  equivalent ideal mixtures,<sup>1</sup> in relation to temperature in the liquid phase.

The experimental heat capacities in the liquid phase of all of the mixtures vary linearly as a function of the temperature, and they are in good agreement with ideal liquid mixture values (Figure 13). This result is valid for all of the samples, except for the wax P4 that reveals higher heat capacities than those of the equivalent ideal liquid. This gap could be explained by a higher ratio of the other hydrocarbons and of heavier  $C_n$ 's from  $C_{40}$  to  $C_{60}$ : these heavy  $C_n$ 's bring about a more significant internal disorder associated with mechanisms of folding, deformation, and tangling of carbon chains, which increase the heat capacity values.<sup>2</sup> According to Van Miltenburg<sup>36</sup> and Atkinson,<sup>37</sup> in a liquid-phase temperature range from the melting point up to 30-40 K, the heat capacities of heavy C<sub>n</sub> do not follow a linear variation law in relation to the temperature. This peculiar behavior corresponds to the supplementary enthalpy consumption needed to break the residual order in the liquid phase and to obtain molecules completely desoriented above the melting point.

### Conclusions

Thermodynamic studies were carried out on 18 multi-C<sub>n</sub> synthetic and 4 real mixtures by differential scanning calorimetry with discontinuous or continuous temperature programming. The  $(H_{T_0}^T/\text{kJ}\cdot\text{mol}^{-1}; h_T^T/\text{J}\cdot\text{g}^{-1}; T_0 = 293.4 \text{ K})$ enthalpy increment measurements of all of the samples are described as a function of the temperature in Supporting Information.

From the structural  $^{4-16}$  and thermodynamic  $^{1-3,17,19,20}$  literature results, these studies highlight the following observations:

(i) S1 and S2 synthetic and P1, P2, P3, and P4 real mixtures with normal logarithmic type  $x_n$  distributions of an N number of consecutive  $C_n$ 's (15  $\leq N \leq$  33) are in a crystalline single-phase solid state.

(ii) The synthetic mixtures with exponential decreasing type  $x_n$  distributions are in a single-phase state if  $N \le 11$  or in a two-phase ( $12 \le N \le 16$ ) or three-phase ( $17 \le N \le 21$ ) state.

The melting onset temperatures, which depend on solid themodynamic state,

(i) vary linearly as a function of  $\bar{n}$ , the average number of carbon atoms ( $22 \le \bar{n} \le 25$ ), of the multi- $C_n$  solid solution in single-phase systems, with the  $\bar{T}_{fus}$  average melting temperatures ( $\bar{T}_{fus} = \sum_{i=1}^{N} x_i T_{fus}$ ), calculated from the pure  $C_n$  values. The influence of nonlinear hydrocarbons, which,

according to the literature,<sup>5,6,10</sup> form an amorphous solid in the real petroleum mixtures, is weak with regard to the behavior of transformation temperatures of P1, P2, and P3, except for P4 where their ratio is higher;

(ii) depend on  $\bar{n}_c$  the mean number of carbon atoms of the lightest phase for the transformation onset temperatures and of the heaviest phase for the transformation end temperatures in the polyphase systems.

The comparison between experimental thermodynamic properties and corresponding values calculated for  $C_n$  equivalent ideal mixtures shows a deviation in relation to the ideality in the ordered solid state of all the mixtures:

(i) For the enthalpies (Figures 6 and 11), this deviation is higher for the single-phase synthetic mixtures with exponential decreasing type  $x_n$  distributions and is much greater for the polyphase synthetic mixtures and in the (multi- $C_n$  crystalline single-phase + amorphous solid) real mixtures than for the single-phase synthetic systems with normal logarithmic type  $x_n$  distributions.

(ii) For the heat capacities, this deviation increases in relation to the increase in the N number of  $C_n$ 's and the complexity in the mixtures and of the temperature (Figures 7 and 12); in all cases, this induces an increase in disorder. For the mixtures with the same  $C_n$ 's, the deviation in relation to ideality is higher for the synthetic mixtures, with exponential decreasing type  $x_n$  distributions, and for the real mixtures than for the single-phase synthetic mixtures, whose  $x_n$  distributions are of the normal logarithmic type. For these latter mixtures, the crystalline organization, imposed by the majority  $C_n$ 's, is more coherent, and the molecular interactions are greater.

In the liquid state, whatever the *N* number of C<sub>n</sub>'s and their molecular length differences, the enthalpy of C<sub>n</sub> mixing is athermal<sup>17,29–33</sup> ( $\Delta H_{liq}^{exc} = 0$ ), and the behavior of all of the liquid multi-C<sub>n</sub> mixtures is ideal, except for P4 whose nonlinear hydrocarbon ratio is higher.

In the solid state, these results highlight a gap in relation to the ideality due to a formation energy of one or several multi- $C_n$  ordered solid solutions that always is positive. The modeling of the mixtures' thermodynamic behavior needs the determination of the excess properties of the mixtures, calculated from the experimental thermodynamic values in this article, from their mixing enthalpies<sup>17</sup> and from the pure  $C_n$  thermodynamic data.<sup>1–3,38</sup> This research is the subject of another study.<sup>17</sup>

### **Supporting Information Available:**

Enthalpy increment versus temperature for  $C_n$  mixtures, S1 and S2 mixtures, and P1–P4 waxes. This material is available free of charge via the Internet at http://pubs.acs.org.

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