

Thermal Conductivity and Thermal Diffusivity of Twenty-Nine Liquids: Alkenes, Cyclic (Alkanes, Alkenes, Alkadienes, Aromatics), and Deuterated Hydrocarbons

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Experimental values of the thermal conductivity λ and thermal diffusivity a of 29 pure substances are presented in the temperature range of -15°C to 65°C under atmospheric or saturation pressure. The materials measured were as follows: alkenes (1-pentene, 1-hexene, 1-heptene, 1-octene, 2,3-dimethyl-1-butene, 2,3-dimethyl-2-butene), cycloalkenes (cyclopentene, cyclohexene), cycloalkanes (cyclopentane, cyclohexane, methylcyclopentane, cycloheptane, cyclooctane), aromatics and their relatives (benzene, ethylbenzene, *o*, *m*, and *p*-xylenes, propylbenzene, isopropylbenzene, hemimellitene, pseudocumene, mesitylene, 1,3-cyclohexadiene, 1,4-cyclohexadiene, bicyclo[2.2.1]hepta-2,5-diene [norbornadiene]), and deuterated hydrocarbons (benzene-*d*₆, cyclohexane-*d*₁₂, toluene-*d*₈). Measurements were made with the transient hot-wire method in the manner previously presented, and the thermal diffusivity values were corrected by reference to the heat capacity of heptane as a reference material. Heat capacities (volumic, $c_p\rho$; massic, c_p ; molar, $C_{m,p}$) were complementally derived from the relationship $c_p\rho = \lambda/a$, with values for the density and the molar mass. The uncertainty of the data is estimated to be 0.4% for the thermal conductivity (absolutely measured) and about 1.8% for the thermal diffusivity (with a coverage factor of $k_p = 2$; $p = 95\%$), although that of λ (not of a) is possibly inferior for a few substances containing slightly more impurities (i.e., mainly other isomers).

Introduction

The thermophysical transport properties of chain, branched, and cyclic hydrocarbons, with their respectively different structures, including their isomers and deuterated hydrocarbons, are important for investigating the mechanism of the conductive heat transfer on various chemical processes. The authors have previously presented their results on alkanes obtained with the transient hot-wire method.^{1–3} In a continuation of this work, reported here are measurements of 29 hydrocarbons and deuterated compounds. The materials measured were the following: C₅H₈ (cyclopentene), C₅H₁₀ (1-pentene, cyclopentane), C₆H₆ (benzene), C₆H₈ (1,3-cyclohexadiene, 1,4-cyclohexadiene), C₆H₁₀ (cyclohexene), C₆H₁₂ (1-hexene, 2,3-dimethyl-1-butene, 2,3-dimethyl-2-butene, methylcyclopentane, cyclohexane), C₇H₈ (bicyclo[2.2.1]hepta-2,5-diene [norbornadiene]), C₇H₁₄ (1-heptene, cycloheptane), C₈H₁₀ (ethylbenzene, 1,2-dimethylbenzene (*o*-xylene), 1,3-dimethylbenzene (*m*-xylene), 1,4-dimethylbenzene (*p*-xylene)), C₈H₁₆ (1-octene, cyclooctane), C₉H₁₂ (*n*-propylbenzene, (1-methylethyl)-benzene (isopropylbenzene, cumene), 1,2,3-trimethylbenzene (hemimellitene), 1,2,4-trimethylbenzene (pseudocumene), 1,3,5-trimethylbenzene (mesitylene)), and three deuterated hydrocarbons (benzene-*d*₆, toluene-*d*₈, cyclohexane-*d*₁₂). The present paper illustrates the lists of these results in detail.

The thermal conductivity and thermal diffusivity measurements were analyzed using two temperatures, T_i and T_a , which are referred to for the two measured values.^{3,4} A small diameter is required for the wire (platinum, $\sim 15\text{ }\mu\text{m}$) in order to derive the thermal diffusivity in the transient

hot-wire method, but its accurate determination is generally difficult. Uniformity along the axis is also needed. Therefore the calibration factors k_f are introduced for the thermal diffusivity values using the relationship $a_{\text{ref}} = \lambda_m/c_p\rho$ with the volumic heat capacity value $c_p\rho$ (1.5270 MJ·m⁻³·K⁻¹) and the measured thermal conductivity λ_m at 298.15 K of heptane.⁴ The correction or calibration factor is about 0.8–1.7% for the thermal diffusivity values calculated as $2r = 15\text{ }\mu\text{m}$ in diameter, and this corresponds to the adjustments by 0.4–0.9% for the diameter of the wires.

Measurement Procedure

Transient Hot-Wire Method Model. An actual model of the transient hot-wire method can be described by a transfer function having a feedback loop (i.e., the heating rate of the wire, $q(t) = Q_0(1 + A\Delta T(t) + B\Delta T^2(t) + \dots)$, $t \geq 0$), where A and B are fixed by the temperature dependence of the wire resistance and the circuit arrangement including the type of power supply, because the wire acts in two ways: as an electrical heating element and as a resistance thermometer. The temperature rise in the wire $\Delta T(t)$ is fitted to the working equation, and analytically derived, with the parameters thermal conductivity λ and thermal diffusivity a .^{4,5}

Effective Temperature T_i and T_a to be Referred to as λ and a . In techniques such as the transient hot-wire method that involve a temperature gradient, the temperatures associated with the thermal conductivity λ and thermal diffusivity a values ought to be modified from T_0 , which is the bath temperature or the starting temperature. Modified temperatures T_i and T_a are derived from the values of the temperature dependence of the thermal conductivity and thermal diffusivity, the heating parameter

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Table 1. List of Materials: Names (Alternative Names), Chemical Abstracts Service Registry Numbers, Formulas, Claimed Purities, and Suppliers

name (alternative name)	CASRN	formula	purity	supplier ^a /lot
1-pentene	109-67-1	C ₅ H ₁₀	98%	T.C.I./FGG01
1-hexene	592-41-6	C ₆ H ₁₂	98%	W.P.C./ACH6692
2,3-dimethyl-1-butene	563-78-0	C ₆ H ₁₂	98%	W.P.C./KSK5578
2,3-dimethyl-2-butene	563-79-1	C ₆ H ₁₂	98%	A.O.U./A014156801 ^b
1-heptene	592-76-7	C ₇ H ₁₄	98%	T. C. I./FIF01
1-octene	111-66-0	C ₈ H ₁₆	99%	A.O.U./A014156301
cyclopentene	142-29-0	C ₅ H ₈	97%	W.P.C./ACR2120
cyclohexene	110-83-8	C ₆ H ₁₀	97%	W.P.C./ELP6186
cyclopentane	287-92-3	C ₅ H ₁₀	98%	T. C. I./FHJ01
cyclohexane	110-82-7	C ₆ H ₁₂	99.8%	W.P.C./TPF9454
cyclohexane- <i>d</i> ₁₂	1735-17-7	C ₆ D ₁₂	99.5%	Al.C.Co./99.5% deuterium
methylcyclopentane	96-37-7	C ₆ H ₁₂	98%	W.P.C./ACM4380
cycloheptane	291-64-5	C ₇ H ₁₄	97%	W.P.C./ACL5336
cyclooctane	292-64-8	C ₈ H ₁₆	98%	W.P.C./SKE5436
benzene	71-43-2	C ₆ H ₆	99%	Dojin-Do/EL115
benzene- <i>d</i> ₆	1076-43-3	C ₆ D ₆	99.6%	W.P.C./ACR7174
1,3-cyclohexadiene	592-57-4	C ₆ H ₈	97%	Al.C.Co./KU12404KU ^c
1,4-cyclohexadiene	628-41-1	C ₆ H ₈	97%	Al.C.Co./TU11510LU ^d
toluene- <i>d</i> ₈	2037-26-5	C ₇ D ₈	98%	Sig.Al.Jpn./151998 ^e
bicyclo[2.2.1]hepta-2,5-diene (norbornadiene)	121-46-0	C ₇ H ₈	98%	Al.C.Co./04902CU ^f
ethylbenzene	100-41-4	C ₈ H ₁₀	98%	W.P.C./WTE4346
1,2-dimethylbenzene (<i>o</i> -xylene)	95-47-6	C ₈ H ₁₀	98%	W.P.C./PAP4854
1,3-dimethylbenzene (<i>m</i> -xylene)	108-38-3	C ₈ H ₁₀	98%	W.P.C./WTJ5486
1,4-dimethylbenzene (<i>p</i> -xylene)	106-42-3	C ₈ H ₁₀	98%	W.P.C./PAR4422
<i>n</i> -propylbenzene	103-65-1	C ₉ H ₁₂	99%	T.C.I./FGG01
(1-methylethyl)-benzene(cumene)	98-82-8	C ₉ H ₁₂	99%	T.C.I./GK01
1,2,3-trimethylbenzene (hemimellitene)	526-73-8	C ₉ H ₁₂	95+	W.P.C./WTP4537 ^g
1,2,4-trimethylbenzene (pseudocumene)	95-63-6	C ₉ H ₁₂	98%	W.P.C./PAL5310
1,3,5-trimethylbenzene (mesitylene)	108-67-8	C ₉ H ₁₂	97%	W.P.C./PAN5011

^a T.C.I., Toyo Chemical Industries, Ltd.; W.P.C., Wako Pure Chemical Industries, Ltd.; A.O.U., Acros Organic USA; Al.C.Co., Aldrich Chemical Co.; Dojin-Do, Dojin-Do Laboratories Jpn.; Sig.Al.Jpn., Sigma Aldrich Japan. ^b Stabilized with 0.05% 2,6-bis(1,1-dimethylethyl)-4-methyl-phenol (BHT, butylated hydroxytoluene). ^c Stabilized with 0.05% BHT. ^d Stabilized with ~0.1% 1,4-hydroquinone, containing ~3% benzene. ^e 99% deuterium atom. ^f Stabilized with 0.02–0.1% BHT. ^g (Better than 95%) tested by W.P.C. for our demand.

$Q_0/4\pi\lambda$ (Q_0 is the heating rate of the wire), and the elapsed times t_i and t_f assigned to the initial and final acquisition data for each experiment.^{3,4}

Practical Measurement System. The experimental system and procedure are the same as those reported previously^{3,4} using two hot-wire sensors (4-terminal resistance, ie., AC and BD cells). The frame of the cells was identical to the previous ones, but partly new wires (nominally, $2r = 15 \mu\text{m}$) were introduced. The data sampling was carried out in the same way as previously reported. The sampling interval was 50 ms, the integrating time was always 20 ms, and the data was usually obtained in sets of 20. The elapsed times, t_i and t_f were nominally $t_i \approx 0.03 \text{ s}$ and $t_f \approx 1 \text{ s}$ in the present case. The set of data $\{\Delta T(t_f), t_f\}$ was fitted into the nonlinear working equation using Deming's least-squares method.^{3,4}

Calibration Factors k_f for Thermal Diffusivity. The data for regular configurations were designated set A for cell AC and those for an inverted position, set C; similarly, the regular position for cell BD is associated with set B and the inverted position for set D. To eliminate the systematic differences resulting from the cells and the configuration of the experiment, the data for the thermal diffusivity were adjusted by the correction factor k_f , which was based on the values of heptane, $c_p = 2.2429 \text{ kJ}\cdot\text{kg}^{-1}\cdot\text{K}^{-1}$ and $\rho = 679.46 \text{ kg}\cdot\text{m}^{-3}$ at 298.15 K ,^{6,7} and the relationship $a = \lambda/c_p\rho$ (where $\lambda_{298.15 \text{ K}}$ was determined from the results of an experiment carried out separately for calibration). The calibration factors k_f for thermal diffusivity were then introduced. Measured thermal diffusivity data were multiplied by k_f for the respective groups. These adjustments are about +1.7% for cell AC and -0.8% for cell BD. This is equivalent to an adjustment for the diameter (nominal value of $15 \mu\text{m}$) of the wire by approximately +0.9% for cell AC and -0.4% for cell BD.

Results

Materials. The liquid samples employed in the present measurements were obtained from various chemical product suppliers. We used them without any further purification or removal of dissolved water or air. Since some of the materials used were expensive and some are unstable, and they were stabilized with appropriate materials. The transfer of samples to the hot-wire glass tube was carried out by a syringe and a siphon after pumping to give a rough vacuum inside the sample containers so as to reduce long exposure to the atmosphere.

The list of test materials is presented in Table 1 along with Chemical Abstracts Registry Numbers (CAS RN) and formulas, together with claimed purities and their lot numbers as designated by the suppliers. The additional comments on substances are as follows: 2,3-dimethyl-2-butene is stabilized with 0.05% 2,6-bis(1,1-dimethylethyl)-4-methyl-phenol (BHT, butylated hydroxytoluene); 1,3-cyclohexadiene is stabilized with 0.05% BHT; 1,4-cyclohexadiene is stabilized with ~0.1% 1,4-hydroquinone and containing ~3% benzene; toluene-*d*₈ is 98% pure (99% of deuterium); bicyclo[2.2.1]hepta-2,5-diene is stabilized with 0.02–0.1%; 1,2,3-trimethylbenzene is more than 95% pure, as tested by Wako Pure Chemicals.

Specifying something mixed in the sample is important in order to accurately determine the property of a material, and also the purities claimed by manufacturers may often be over estimated. In addition, the substances of the unsaturated alkenes and dienes among the test materials seem to have been transitional to the other state due to inappropriate handling and preservation. Nevertheless, we referred to the purities indicated or claimed on the labels or catalog by the manufacturers. In fact, most of the impurities are assumed to be isomers that are difficult to separate from the sample material, because their boiling temperatures approach each other. The thermal properties

Table 3. Coefficients of Equations 1 and 2

material	formula	cell	N (data)	$\lambda_0^a / \text{W} \cdot \text{m}^{-1} \cdot \text{K}^{-1}$	$A^a / 10^{-4}$	$a_0^a / 10^{-8} \text{ m}^2 \cdot \text{s}^{-1}$	$B^a / 10^{-2}$
1-pentene	C ₅ H ₁₀	AC	24	0.12227(5)	-3.936(25)	8.865(08)	-2.934(39)
1-hexene	C ₆ H ₁₂	AC	36	0.12582(6)	-3.399(18)	8.829(11)	-2.492(33)
2,3-dimethyl-1-butene	C ₆ H ₁₂	BD	36	0.11241(5)	-3.052(14)	7.861(13)	-2.346(34)
2,3-dimethyl-2-butene	C ₆ H ₁₂	AC	36	0.13035(5)	-3.563(13)	9.067(14)	-2.734(39)
1-heptene	C ₇ H ₁₄	AC	24	0.12913(5)	-3.131(19)	8.890(09)	-2.302(30)
1-octene	C ₈ H ₁₆	AC	30	0.13129(5)	-2.966(15)	8.695(18)	-2.584(55)
cyclopentene	C ₅ H ₈	AC	24	0.14260(6)	-4.324(24)	10.706(09)	-4.003(35)
cyclohexene	C ₆ H ₁₀	AC	36	0.13539(5)	-3.208(15)	9.637(14)	-3.066(42)
cyclopentane	C ₅ H ₁₀	BD	30	0.13623(4)	-3.945(15)	10.502(13)	-4.176(52)
cyclohexane	C ₆ H ₁₂	BD	24	0.12531(7)	-2.858(23)	8.989(15)	-3.077(51)
cyclohexane- <i>d</i> ₁₂	C ₆ D ₁₂	BD	30	0.11809(5)	-2.654(14)	6.994(14)	-2.399(39)
methylcyclopentane	C ₆ H ₁₂	BD	24	0.12250(3)	-3.183(14)	8.971(09)	-3.050(38)
cycloheptane	C ₇ H ₁₄	BD	24	0.12449(3)	-2.431(10)	8.613(10)	-2.454(38)
cyclooctane	C ₈ H ₁₆	AC	26	0.12377(6)	-2.136(16)	7.799(11)	-1.866(29)
benzene	C ₆ H ₆	AC	24	0.14895(3)	-3.255(11)	9.956(14)	-2.098(45)
benzene- <i>d</i> ₆	C ₆ D ₆	AC	30	0.14223(5)	-3.192(15)	8.332(11)	-1.949(30)
1,3-cyclohexadiene	C ₆ H ₈	AC	36	0.14016(6)	-3.057(19)	9.567 ^b	-2.445 ^b
1,4-cyclohexadiene	C ₆ H ₈	BD	36	0.15344(3)	-3.481(09)	10.164(06)	-2.802(20)
toluene- <i>d</i> ₈	C ₇ D ₈	BD	30	0.13135(3)	-2.656(09)	8.069(08)	-2.126(24)
bicyclo[2.2.1]hepta-2,5-diene	C ₇ H ₈	AC	30	0.14401(7)	-3.132(22)	10.321(13)	-3.554(36)
ethylbenzene	C ₈ H ₁₀	AC	30	0.13375(4)	-2.491(12)	9.167(05)	-2.072(15)
1,2-dimethylbenzene	C ₈ H ₁₀	BD	30	0.13396(7)	-2.091(20)	8.900(14)	-1.883(42)
1,3-dimethylbenzene	C ₈ H ₁₀	AC	36	0.13567(4)	-2.497(12)	9.517(06)	-2.199(20)
1,4-dimethylbenzene	C ₈ H ₁₀	BD	24	0.13314(4)	-2.540(10)	9.277(16)	-2.210(43)
<i>n</i> -propylbenzene	C ₉ H ₁₂	AC	30	0.13320(3)	-2.188(10)	8.895(09)	-1.845(27)
(1-methylethyl)-benzene	C ₉ H ₁₂	BD	30	0.12408(4)	-1.985(13)	8.259(07)	-1.810(20)
1,2,3-trimethylbenzene	C ₉ H ₁₂	AC	36	0.13172(6)	-1.681(18)	8.334(10)	-1.380(31)
1,2,4-trimethylbenzene	C ₉ H ₁₂	BD	36	0.13181(5)	-1.923(17)	8.670(07)	-1.686(22)
1,3,5-trimethylbenzene	C ₉ H ₁₂	BD	36	0.14054(5)	-2.197(21)	9.535(10)	-2.148(29)

^a The numbers in parentheses following the coefficients are the numerical values of the standard uncertainties referred to in the corresponding last digits. Results were derived from data obtained with the cell AC and BD. ^b Fitted using the measured values at the three higher temperatures.

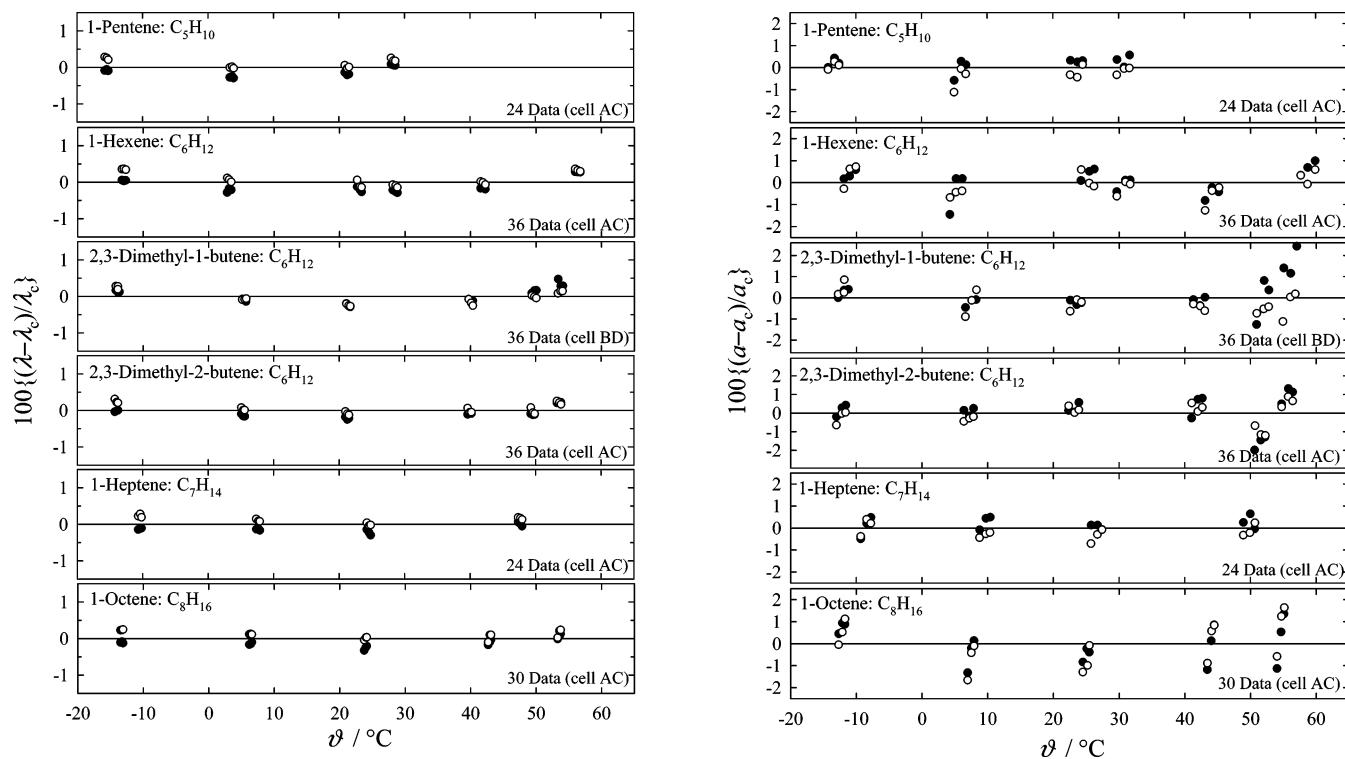


Figure 1. Deviations of measured values from the formulas respectively fitted for six alkenes C_nH_{2n} (*n* = 5–8) (a) thermal conductivity and (b) thermal diffusivity. Values were adjusted by a factor of k_f .

of 1,3- and 1,4-cyclohexadienes, where the data were obtained in due sequence of $\vartheta_0 = 22.53^\circ\text{C}$, 40.20°C , 54.75°C , 5.73°C , -8.78°C , and -15.16°C , respectively, under nearly the same times and conditions. The thermal diffusivities of 1,3-cyclohexadiene at the three higher temperatures indicate ordinary behavior as in those of 1,4-cyclohexadiene but showed a clear peculiarity at the three lower temperatures. On the other hand, the thermal conductivities do not seem to clearly indicate the anomaly

in Figure 7, though the difference between the temperature dependences at the lower and higher temperatures is observed, if examining minutely, as far as seen in Figure 3a. The heat capacity at 298.15 K of 1,3-cyclohexadiene derived from λ and a at the three higher temperatures is consistent with the value in the literature (see Table 5). The density values of samples (1,3- and 1,4-cyclohexadiene), which were taken out from cells after the experiments, were measured as mentioned later. Subsequently,

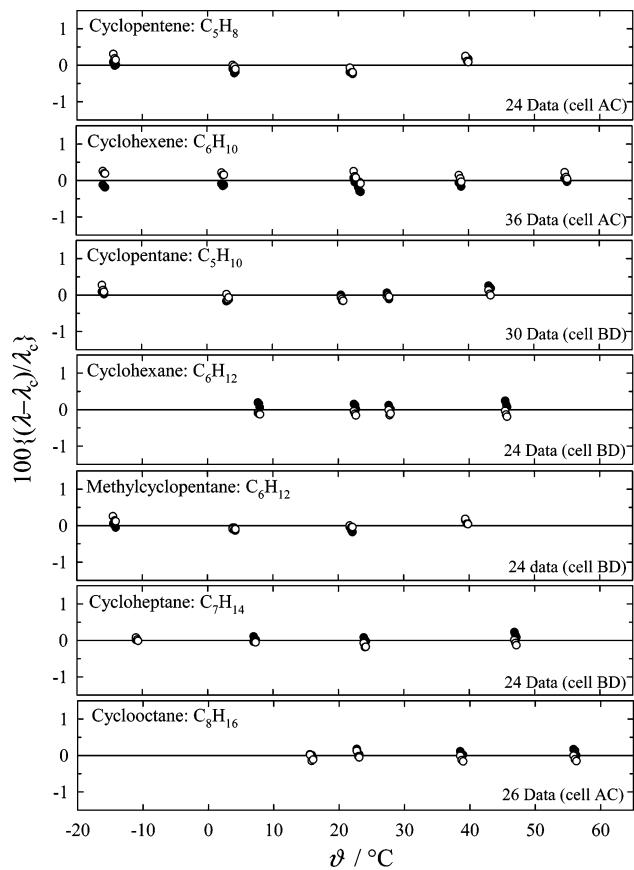


Figure 2. Deviations of measured values from the formulas respectively fitted for cyclopentene and -hexene and five cycloalkanes of C_nH_{2n} ($n = 5-8$) including methylcyclopentane (a) thermal conductivity and (b) thermal diffusivity. Values were adjusted by a factor of k_f . ●, Set A data with cell AC or set B data with BD cell; ○, set C data with cell AC or set D data with cell BD, respectively.

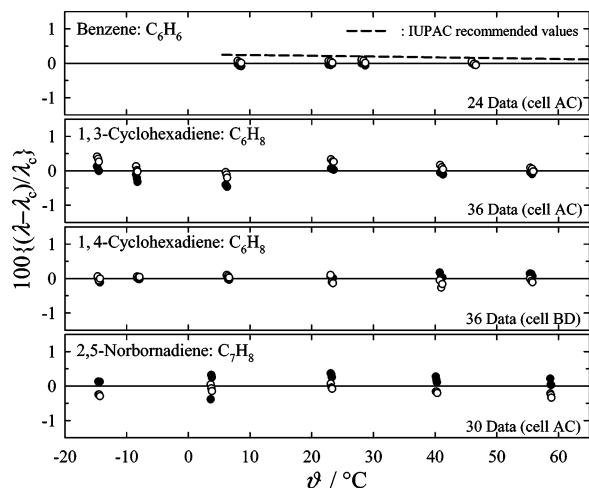
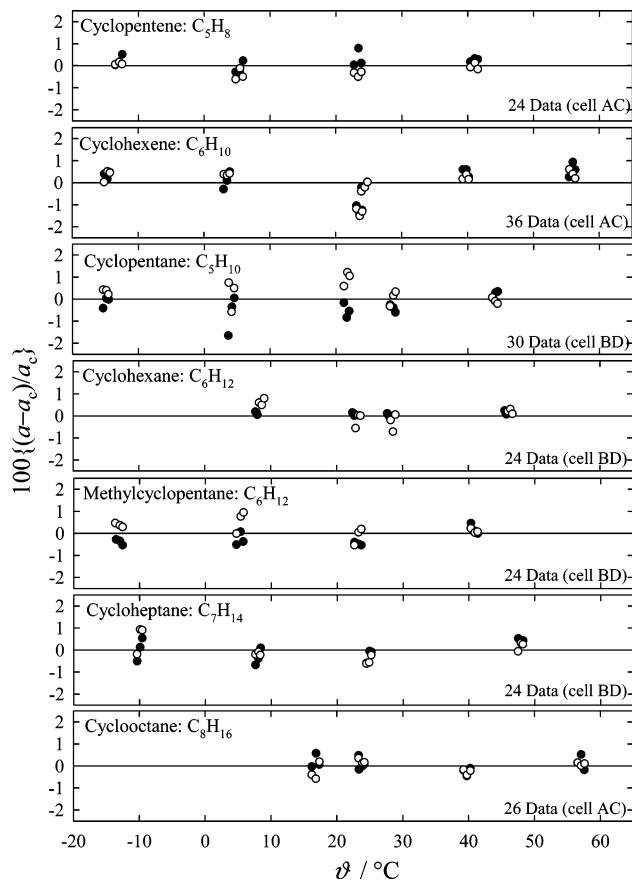
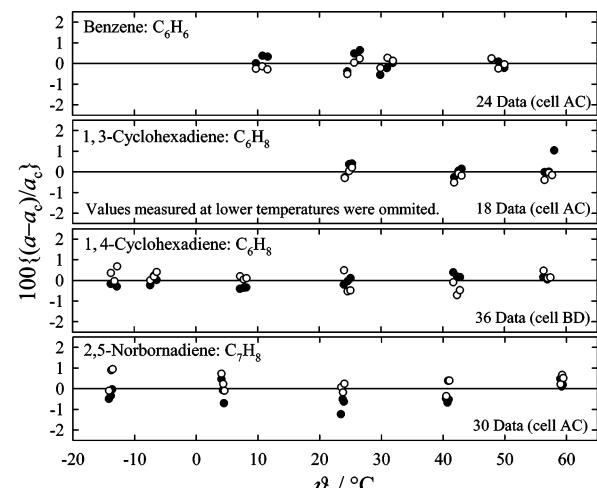


Figure 3. Deviations of measured values from the formulas respectively fitted for benzene, 1,3- and 1,4-cyclohexadienes, and norbornadiene: (a) thermal conductivity and (b) thermal diffusivity. Values were adjusted by a factor of k_f . Fitting values of 1,3-hexadiene were obtained from three higher temperatures. ●, Set A data with cell AC or set B data with the cell BD; ○, set C data with cell AC or set D data with cell BD, respectively.

benzene- d_6 with cell AC and cyclohexane- d_{12} with cell BD were measured, and the results were properly conducted. The mode between the cells AC and BD was changed manually with a mercury contact switch, and the abnormal working in the only measurement with the cell AC was not taken into consideration. Therefore the measurement of 1,3-cyclohexadiene is regarded to have been successfully carried out.

Comparison between Reported and Present Values of Thermal Conductivity. A comparison between the



previously reported data in the literature⁹⁻⁴⁸ and the present results is shown chronologically in Table 4 except for the cases of some materials for which the thermal conductivity was not found. These were not intentionally selected, and their uncertainty is mostly unclear. Therefore, we did not examine each difference between the referred and present data. Additionally, the differences do not arise from the purity of the sample but most naturally from the variance among the individual data obtained by various researchers with their respective techniques.

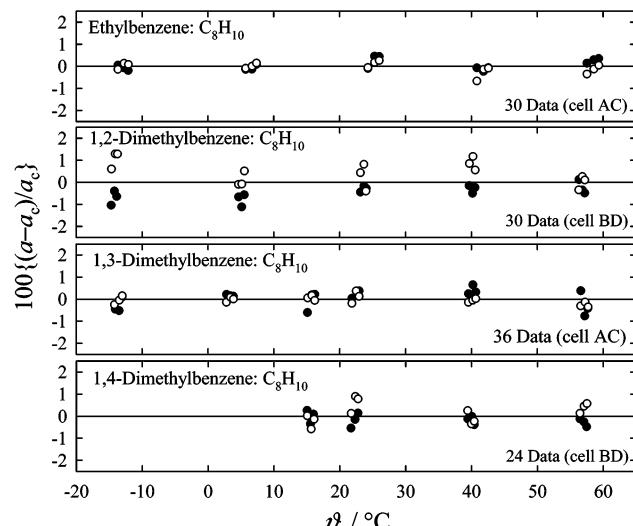
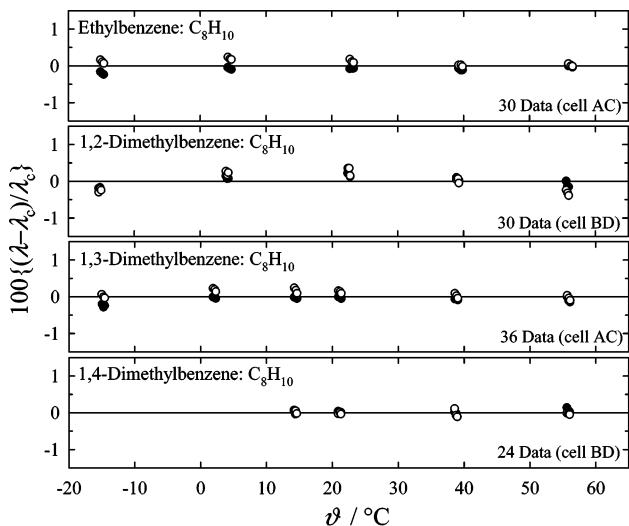


Figure 4. Deviations of measured values from the formulas respectively fitted for ethylbenzene and relatives: (a) thermal conductivity and (b) thermal diffusivity. Values were adjusted by a factor of k_f . ●, Set A data with cell AC or set B data with the cell BD; ○, set C data with cell AC or set D data with cell BD, respectively.

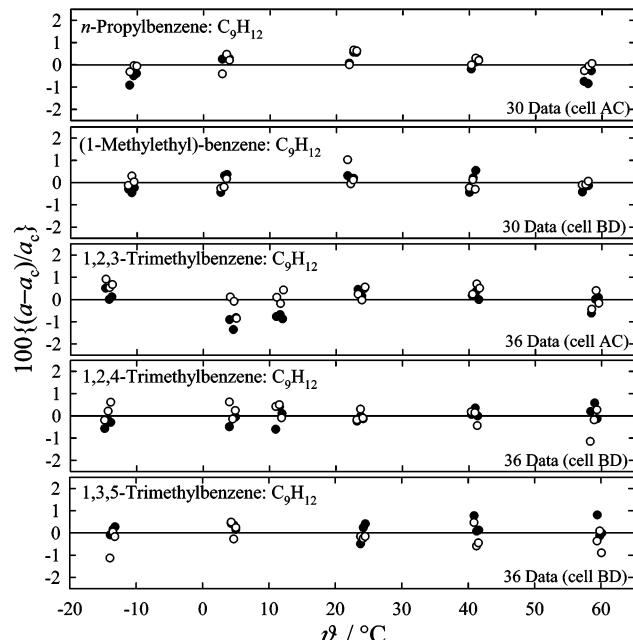
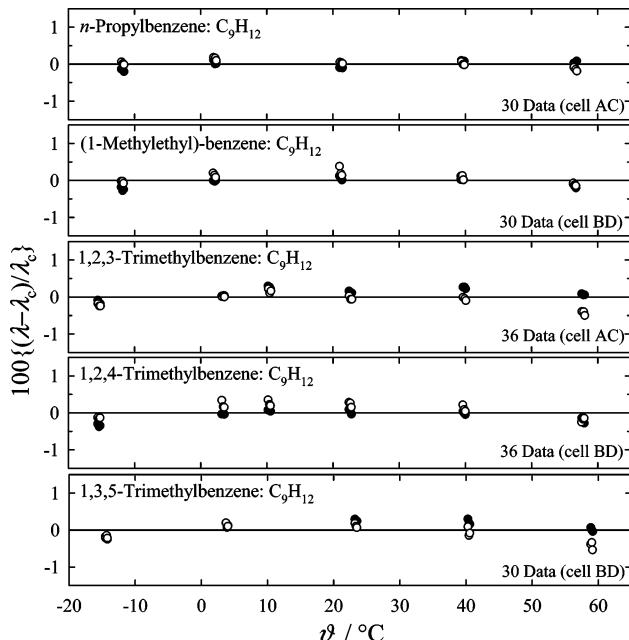


Figure 5. Deviations of measured values from the formulas respectively fitted for propylbenzene and relatives: (a) thermal conductivity and (b) thermal diffusivity. Values were adjusted by a factor of k_f . ●, Set A data with cell AC or set B data with the cell BD; ○, set C data with cell AC or set D data with cell BD, respectively.

Some of the values are calculated from the formula as smoothed values, and the present results (in parentheses) are calculated at the same temperatures reported using eq 1 with the coefficients listed in Table 3.

Summarized Results at 298.15 K. Table 5 lists the values determined for the properties at a nominal temperature of 298.15 K together with the values of the molar heat capacity (with a previously obtained result of toluene).² The massic heat capacity at constant pressure c_p can be derived from the thermal conductivity λ , the thermal diffusivity a , and the density ρ using the equation $a = \lambda/c_p\rho$. The densities of the sample were conventionally obtained from the literature,⁷ together with molar mass, but since those of six materials (cyclohexane- d_{12} , benzene- d_6 , 1,3- and 1,4-cyclohexadienes, toluene- d_8 and norbornadiene) are unavailable, they were measured using a vibrating tube densimeter (Anton Parr DMA5000 SH3). The density values in the literature are believed to be sufficient by

experience for the purpose of deriving the heat capacity. The various (volumic, $c_p\rho$; massic, c_p ; molar, $C_{m,p}$) heat capacities are in agreement with most of the values $C_{m,p}$ found in the literatures, although the reliability of the values were not perfectly examined.^{6,7,49–58} As exceptions, the values of some materials (for example, norbornadiene, 1,3-dimethylbenzene, 1-heptene, and an especially large value for norbornadiene) differed by more than 1.8% (i.e., estimated uncertainty) from those referred to from the literature. The $c_p\rho$ of norbornadiene (an isomer of toluene), however, is very close to that of toluene, although their thermal conductivity, thermal diffusivity, and density are quite different from each other.

The thermal properties are considered to naturally have relevance to the boiling point, density, and/or molar density. Prediction of thermal properties of pure organic liquids has been specially investigated, relating to the molar density.^{59,60} Therefore the consistency of the mea-

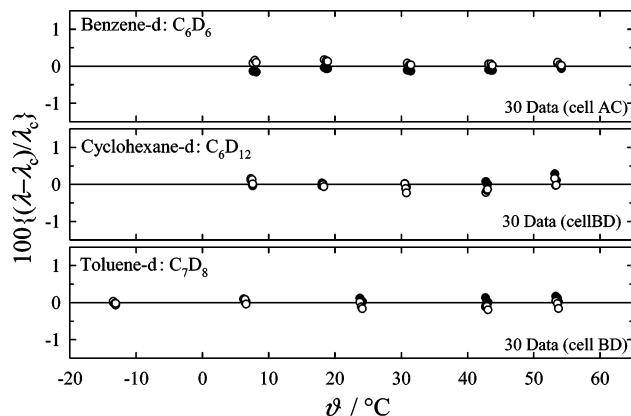


Figure 6. Deviations of measured values from the formulas respectively fitted for three deuterated hydrocarbons: (a) thermal conductivity and (b) thermal diffusivity. Values were adjusted by a factor of k_f . ●, Set A data with cell AC or set B data with the cell BD; ○, set C data with cell AC or set D data with cell BD, respectively.

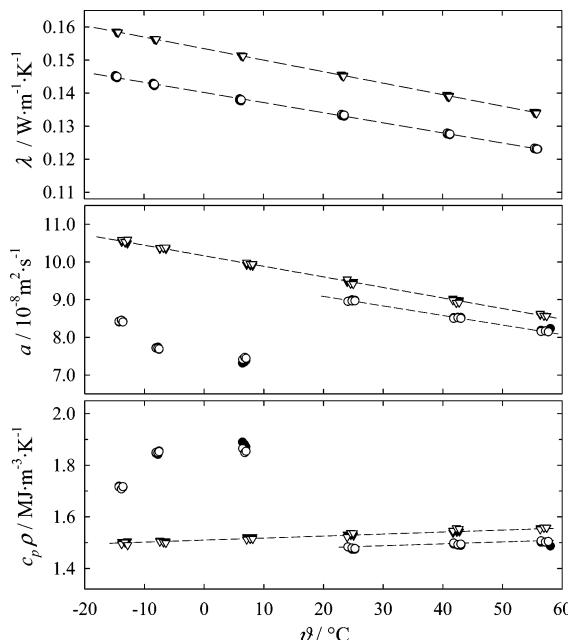
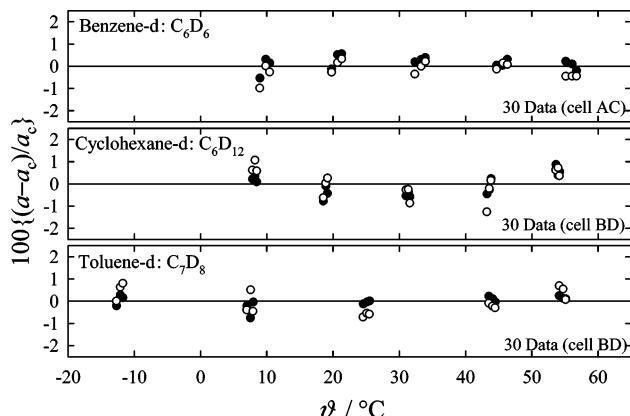


Figure 7. Values of 1,3-cyclohexadiene measured with cell AC and 1,4-cyclohexadienes with cell BD. The volumic heat capacity $c_p\rho$ is calculated by λ/a_m (λ_c , calculated from the fitting equation; a_m , measured value) referred to the temperature ϑ_a . Measurements were made in due sequence of $\vartheta_0 = 22.53^\circ\text{C}$, 40.20°C , 54.75°C , 5.73°C , -8.78°C , and -15.16°C at the same time and under the same condition for both materials. ●, Set A data of 1,3-cyclohexadiene; ○, set C data of 1,3-cyclohexadiene; ▼ set B data of 1,4-cyclohexadiene; ▽ set D data of 1,4-cyclohexadiene.

surement of thermal conductivity and thermal diffusivity was examined by comparing the molar heat capacities representatively. Figure 8 shows the molar heat capacities, $C_{m,p} = (\lambda/a)(M/\rho)$, of 29 materials together with some of the alkanes and the toluene previously obtained.^{2,3} As mentioned above, the heat capacity $C_{m,p}$ of norbornadiene differs greatly (9.2%) from the referred value, but that value was only found in the literature.⁵⁷ Figure 8 shows that the values of $C_{m,p}$ of both toluene (g1) and norbornadiene (g2, C_7H_8) are arranged according to the values ρ/M with a proper tendency, excluding the deuterated materials. Judging from this situation, the present molar heat capacity of norbornadiene might be more reliable than the referred one.

Furthermore it is interesting that norbornadiene and 1,4-cyclohexadiene show almost the same a value (although λ , c_p , $c_p\rho$, and $C_{m,p}$ differ from each other), because both their

structures are C_6 cyclic rings, their boiling points are almost the same, and they have double bonds on each opposite side of ring.

Thermal Properties of Deuterated Liquids. The thermal properties of three deuterated liquids (benzene- d_6 , toluene- d_8 , and cyclohexane- d_{12}) were compared with those of their ordinary hydrocarbons (λ of toluene).² Horrocks et al. presented a relationship of the ratio λ_H/λ_D of both deuterated and ordinary hydrocarbons to the ratio M_D/M_H as follows²⁰

$$\lambda_H/\lambda_D \approx (M_D/M_H)^{1/2} \quad (3)$$

where M_D and M_H are the molar masses of the deuterated and ordinary materials. Table 6 shows the relative values, λ_H/λ_D , a_H/a_D , and $(C_{m,p})_H/(C_{m,p})_D$, which are calculated from Table 5, together with λ_H/λ_D for C_6H_6/C_6D_6 ($\lambda_H = 0.1426$ at 295.85 K and $\lambda_D = 0.1373$ at 295.95 K) and C_6H_{12}/C_6D_{12} ($\lambda_H = 0.1201$ at 294.55 K and $\lambda_D = 0.1133$ at 295.35 K) reported by Horrocks et al.²⁰ The present results of λ_H/λ_D are consistent by around 1% with the relationship (eq 3) and with those of Horrocks et al. Furthermore, it is very interesting that values a_H/a_D and $(C_{m,p})_H/(C_{m,p})_D$ of the two aromatics (benzene and toluene) are very close to those of the other material, although those of cyclohexane are observed to be clearly different from benzene and toluene.

Evaluations of Uncertainty. The evaluation of the uncertainty components in the measurement was made using the simplified working formula

$$\Delta T = (Q_0/4\pi\lambda) \ln(t/s) + (Q_0/4\pi\lambda) \ln(4as/r^2C) \quad (4)$$

The uncertainty in the thermal conductivity can be evaluated as^{3,4}

$$\frac{\delta\lambda}{\lambda} = \frac{\delta Q_0}{Q_0} + \frac{\delta(dR_W/dT)}{dR_W/dT} + \frac{\delta(\Delta T_f - \Delta T_i)}{\Delta T_f - \Delta T_i} + \frac{\delta\tau(t_f - t_i)}{t_f t_i \ln(t_f/t_i)} + \left(\frac{\delta\lambda}{\lambda}\right)_{\text{sample}} + \left(\frac{\delta\lambda}{\lambda}\right)_{\text{pressure}} + \left(\frac{\delta\lambda}{\lambda}\right)_{\text{others}} \quad (5)$$

where $\delta(*)$ is the uncertainty of the (*) terms, R_W the resistance of the hot-wire sensor, and $\delta\tau$ the ambiguity of the time lag of both trigger signals to the bridge and the digital voltmeter. The magnitude of the respective components, contributing as a random or systematic part, is the same as that in the previous study.⁴ The first component is 0.17%, in terms of the standard uncertainty (as a random part, type A), the second is ~0.05% (as a systematic part, type A), the third is ~0.05% (as a random part, type A),

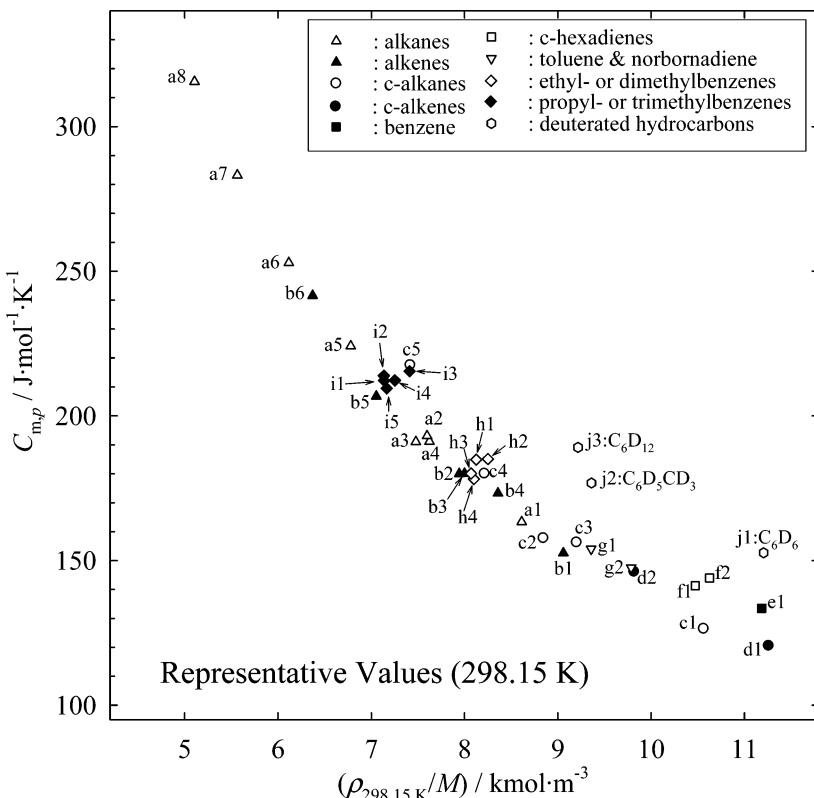


Figure 8. Molar heat capacities calculated at 298.15 K vs molar density together with those of some alkanes.^{2,3} Materials and symbols are designated as follows: a1, pentane; a2, hexane; a3, 2,2-dimethylbutane; a4, 2,3-dimethylbutane; a5, heptane; a6, octane; a7, nonane; a8, decane; b1, 1-pentene; b2, 1-hexene; b3, 2,3-dimethyl-1-butene; b4, 2,3-dimethyl-2-butene; b5, 1-heptene; b6, 1-octene; c1, cyclopentane; c2, methylcyclopentane; c3, cyclohexane; c4, cycloheptane; c5, cyclooctane; d1, cyclopentene; d2, cyclohexene; e1, benzene; f1, 1,3-cyclohexadiene; f2, 1,4-cyclohexadiene; g1, toluene; g2, bicyclo[2.2.1]hepta-2,5-diene (norbornadiene); h1, ethylbenzene; h2, 1,2-dimethylbenzene (*o*-xylene); h3, 1,3-dimethylbenzene (*m*-xylene); h4, 1,4-dimethylbenzene (*p*-xylene); i1, *n*-propylbenzene; i2, (1-methyethyl)-benzene (isopropylbenzene); i3, 1,2,3-trimethylbenzene (hemimellitene); i4, 1,2,4-trimethylbenzene (pseudocumene); i5, 1,3,5-trimethylbenzene (mesitylene); j1, benzene-*d*₆; j2, toluene-*d*₈; j3, cyclohexane-*d*₁₂.

and the fourth is negligible. The fifth (the sample material) is rather difficult to estimate because of the lack of exact information concerning purity. However, most of the impurities are thought to be isomers (as mentioned before) and are expected to be less than 2% (although hemimellitene certainly contains extra impurities (this means other isomers)). Since the sample of 1,4-cyclohexadiene contains ~3% benzene, the corrections were made to values of 100% substances of 1,4-cyclohexadiene using the results of benzene and the magnitudes were 0.08% for λ , 0.01% for a , and 0.07% for $c_p\rho$, respectively. Therefore, this fifth term is assumed to be ~0.10% (as a random part, type B) and the other components, including the potential lead, and the sampling time-step distribution, etc., ~0.04% (a random part, mixed types A and B). Overall, the combined standard uncertainty is about 0.24%, evaluated as the root-sum square of the various components.

For measurement of the thermal diffusivity, the original uncertainty ($2\delta r/l$) is replaced by the term $(\delta a/a)_{cal} = (\delta k/k_f)$ since the adjustment of the diameter of the wire has been made for respective configurations, and the uncertainty is evaluated as follows^{3,4}

$$\begin{aligned}\delta a/a = & (\delta a/a)_{cal} + \delta(\Delta T)_0/(Q_0/4\pi\lambda) + (\delta\lambda/\lambda)^* \\ & \ln(4as/r^2C) + (\delta a/a)_{sample} \quad (6)\end{aligned}$$

In this formula, the first term cannot be evaluated precisely but can tentatively be said to be 0.3% (a systematic part, type B), and the second term $(\delta(\Delta T)_0$, the initially remaining deflection in terms of temperature, originating from an

inadequate balance in the bridge at temperature T_0) is about 0.5% (a random part, type B). According to the third term, subcomponents $\delta Q_0/Q_0$ and $(\delta\lambda/\lambda)_{material}$ in eq 6 do not practically affect $\delta a/a$, and therefore, $(\delta\lambda/\lambda)^*$ is 0.084%. This term is estimated to be 0.67% ($\ln(4as/r^2C) \approx 8$) (a random part, type A). The last term $(\delta a/a)_{sample}$ is actually the same as $(\delta\lambda/\lambda)_{material}$ and is 0.10% (a random part, type B). Finally, the overall uncertainty is estimated to be 0.90%, computed as the root-sum-square of the subcomponents.

Discussion and Conclusions

The original data on the thermal conductivity and thermal diffusivity for the 29 materials of alkenes, cycloalkenes, cycloalkanes, benzene and its relatives, and deuterated hydrocarbons are reported. The various heat capacities were derived at the nominal temperature of 298.15 K from the ratio of the thermal conductivity to the thermal diffusivity λ/κ , the density ρ , and the molar mass M ,⁷ where a part of the density values were measured using a vibrating tube densimeter. The derived c_p (or $C_{m,p}$) seems consistent enough with the values from the literature within the estimated uncertainty of the experimental system (excluding some materials: 1-heptene, norbornadiene, and 1,3-dimethylbenzene), although all of referred values may be not reliable with a high level. The volumic heat capacity of norbornadiene $c_p\rho = \lambda/a$ is very close to that of toluene, which is an isomer, although λ , a , and ρ differ from each other. The consistency of the measurement of thermal conductivity and thermal diffusivity was examined and confirmed by comparing the molar heat capacities representatively. The deuterated hydrocarbons behave

$k_p = 2, p = 95\%$), although that of the thermal conductivity (not for thermal diffusivity) may be inferior for hemimelitene containing comparatively more impurities (i.e., other isomers). A curious phenomenon was observed in the measurement of 1,3-cyclohexadiene in the temperature range of -16°C to 20°C , but it is necessary to accurately determine the cause of this phenomenon. The present result is expected to be of use for estimating or predicting the unknown thermal properties of other materials.

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Note Added after ASAP Posting. This article was released ASAP on 5/21/2004. In the caption to Figure 7, J_0 was changed to ϑ_0 . The paper was reposted 6/2/2004.

Literature Cited

- (1) Watanabe, H. Accurate Measurement of the Thermal Conductivity and Thermal Diffusivity of Toluene and *n*-Heptane. *Int. J. Thermophys.* **1997**, *18*, 313–325.
- (2) Watanabe, H.; Seong, D. J. The Thermal Conductivity and Thermal Diffusivity of Liquid *n*-Alkanes: C_nH_{2n+2} ($n=5$ to 10) and Toluene. *Int. J. Thermophys.* **2002**, *23*, 337–356.
- (3) Watanabe, H. Thermal Conductivity and Thermal Diffusivity of Sixteen Isomers of Alkanes: C_nH_{2n+2} ($n = 6$ to 8). *J. Chem. Eng. Data* **2003**, *48*, 124–136.
- (4) Watanabe, H. Further Examination of the Transient Hot-Wire Method for the Simultaneous Measurement of Thermal Conductivity and Thermal Diffusivity. *Metrologia* **2002**, *39*, 65–81.
- (5) Watanabe, H. Accurate and Simultaneous Measurement of the Thermal Conductivity and Thermal Diffusivity of Liquids Using the Transient Hot-Wire Method. *Metrologia* **1996**, *33*, 101–115.
- (6) *Kagaku Binran II*; Maruzen, Tokyo: 1993; II-229–232.
- (7) *T. R. C. Thermodynamic Tables, Hydrocarbons*; Thermodynamic Research Center, The Texas A&M University System: College Station, TX, 1999; Vols. I and XI.
- (8) Assael, M. J.; Ramires, M. L. V.; Nieto de Castro, C. A.; Wakeham, W. A. Benzene: A Further Liquid Thermal Conductivity Standard. *J. Phys. Chem. Ref. Data* **1990**, *19*, 113–117.
- (9) Mukhamedzyanov, G. K.; Usmanov, A. G. The Thermal Conductivity of Some Classes of Organic Liquids. *Trudy Kazanskogo Khim. Teknol. sm.-ta*, **1968**, *37*, 52–63.
- (10) Tarzimanov, A. A.; Sharafutdinov, R. A.; Gabitov, F. R. Thermal Conductivity of *n*-Alkanes and 1-Alkenes Not Distorted by Radiative Energy Transfer. I. Experimental Results. *Inz.-Fiz. Zh.* **1990**, *59* (4), 662–667.
- (11) Bogatov, G. F.; Kravtsov, V. A. Thermal Conductivity of Unsaturated Hydrocarbons in the Liquid State. *Izv. Vyssh. Uchebn. Zaved., Neft Gaz.* **1988**, *31* (10), 43–48.
- (12) Gross, U.; Song, Y. W.; Hahne, E. Measurements of Liquid Thermal Conductivity and Diffusivity by the Transient Hot-Strip Method. *Fluid Phase Equilib.* **1992**, *76*, 273–282.
- (13) Sakiadis, B. C.; Coates, J. Studies of Thermal Conductivity of Liquids. *AIChE J.* **1955**, *1* (3), 275–288.
- (14) Li, S. F. Y.; Wakeham, W. A.; Zalaf, M. Thermal Conductivity of Oct-1-ene in the Temperature Range 307 to 360 K at Pressures up to 0.5 GPa. *Int. J. Thermophys.* **1987**, *8* (4), 407–414.
- (15) Jamieson, D. T.; Cartwright, G. Thermal Conductivity of Cycloaliphatic Liquids. *Therm. Conduct.* **1983** (vol. date **1979**), *16*, 435–438.
- (16) Sakiadis, B. C.; Coates, J. Studies of Thermal Conductivity of Liquids. Part III. *AIChE J.* **1957**, *3* (1), 121–126.
- (17) Grigor'ev, B. A.; Ishkhanov, A. M. Thermal Conductivity of Naphthalene Hydrocarbons under High Pressures. *Inz.-Fiz. Zhurnal* **1981**, *41* (3), 491–499.
- (18) Assael, M. J.; Dalaouti, N. K. Thermal Conductivity of Toluene + Cyclopentane Mixtures: Measurements and Prediction. *Int. J. Thermophys.* **2001**, *22* (3), 659–678.
- (19) Briggs, D. K. H. Thermal Conductivity of Liquids. *Ind. Eng. Chem.* **1957**, *49* (3), 418–421.
- (20) Horrocks, J. K.; McLaughlin, E.; Ubbelohde, A. R. Liquid-Phase Thermal Conductivities of Isotopically Substituted Molecules. *Trans. Faraday Soc.* **1963**, *59*, 1110–1113.
- (21) Filippov, L. P.; Nefedov, S. N. Apparatus for Studying a Complex of Thermophysical Properties of Liquids. *Zavodskaiia Laboratoria*, **1979**, *45* (2), 1126–1128.
- (22) Kashiwagi, H.; Oishi, M.; Tanaka, Y.; Kubota, H.; Makita, T. Thermal Conductivity of Fourteen Liquids in the Temperature Range 298–373 K. *Int. J. Thermophys.* **1982**, *3* (2), 101–116.
- (23) Baroncini, C.; Latini, G.; Pierpaoli, P. Thermal Conductivity of Organic Liquid Binary Mixtures: Measurements and Prediction Method. *Int. J. Thermophys.* **1984**, *5* (4), 387–401.
- (24) Li, S. F. Y.; Maitland, G. C.; Wakeham, W. A. Thermal Conductivity of Benzene and Cyclohexane in the Temperature Range 36–90°C at Pressures up to 0.33 GPa. *Int. J. Thermophys.* **1984**, *5* (4), 351–365.
- (25) Rowley, R. L.; Gubler, V. Thermal Conductivities in Seven Ternary Liquid Mixtures at 40 °C and 1 atm. *J. Chem. Eng. Data* **1988**, *33*, 5–8.
- (26) Tanaka, Y.; Hase, T.; Kubota, H.; Makita, T. Thermal Conductivity of Benzene and Cyclohexane under High Pressures. *Ber. Bunsen-Ges. Phys. Chem.* **1988**, *92* (7), 770–776.
- (27) Voss, S. F.; Sloan, E. D. Thermal Conductivity and Heat Capacity of Synthetic Fuel Components. *Int. J. Thermophys.* **1989**, *10* (5), 1029–1040.
- (28) Tufeu, R.; LeNeindre, B.; Johannin, P. Conductibilité Thermique de Quelques Liquides. *C. R. Hebd. Séances Acad. Sci.* **1966**, *262*, 229.
- (29) Pöltz, H.; Jugel, R. The Thermal Conductivity of Liquids-IV, Temperature Dependence of Thermal Conductivity. *Int. J. Heat Mass Transfer* **1967**, *10*, 1075–1088.
- (30) Spirin, G. G. Measurement of the Thermal Conductivity of Superheated Liquids. *Inz.-Fiz. Zh.* **1978**, *35* (3), 445–459.
- (31) Ogiwara, K.; Arai, Y.; Saito, S. Thermal Conductivities of Liquid Hydrocarbons and Their Binary Mixtures. *Ind. Eng. Chem. Fundam.* **1980**, *19* (3), 295–300.
- (32) Atalla, S. R.; El-Sharkawy, A. A.; Gasser, F. A. Measurement of Thermal Properties of Liquids with an AC Heated-Wire Technique. *Int. J. Thermophys.* **1981**, *2* (2), 155–162.
- (33) Ogiwara, K.; Arai, Y.; Saito, S. Thermal Conductivities of Liquids and Their Mixtures for Hydrocarbons and Alcohols. *J. Chem. Eng. Jpn.* **1985**, *18* (3), 273–277.
- (34) Charitidou, E.; Molidou, C.; Assael, M. J. The Thermal Conductivity and Viscosity of Benzene. *Int. J. Thermophys.* **1988**, *9* (1), 37–45.
- (35) Ramires, M. L. V.; Vieira dos Santos, F. J.; Mardolcar, U. V.; Nieto de Castro, C. A. The Thermal Conductivity of Benzene and Toluene. *Int. J. Thermophys.* **1989**, *10* (5), 1005–1011.
- (36) Tarzimanov, A. A.; Yuzmukhametov, F. D.; Gavitov, F. R.; Sharafutdinov, R. A.; Shakirov, N. Z. Thermal Conductivity and Thermal Diffusivity of Liquid Aromatic Hydrocarbons Undistorted by Radiation. *High Temp.* **2002**, *40* (4), 524–530.
- (37) Filippov, L. P. Thermal Conductivity of Organic Liquids. *Vestn. Mosk. Univ. Univ. Ser. III* **1960**, *15* (3), 61–69.
- (38) Mustafaev, R. A.; Gabulov, D. M. Experimental Study of the Thermal Conductivity of Aromatic Hydrocarbons at High Temperatures and Pressures. *Inzh.-Fiz. Zh.* **1977**, *33* (5), 857–863.
- (39) Palavra, A. M. F.; Wakeham, W. A.; Zalaf, M. Thermal Conductivity of Ethylbenzene in the Temperature Range 31–84 °C at Pressure up to 0.5 GPa. *High Temp. - High Pressures* **1986**, *18* (4), 405–410.
- (40) Riedel, L. New Measurement of Thermal Conductivity of Organic Liquids. *Chem. Ingr. Technol.* **1951**, *23* (13), 321–324.
- (41) Naziev, Ya. M.; Gumbatov, A. M.; Gasanov, A. S.; Abasov, A. A. Experimental Study of the Thermal Conductivity of Liquid Binary Mixtures of Hexane with *o*-Xylene. *Zh. Fiz. Khim.* **1987**, *61* (1), 36–39.
- (42) Assael, M. J.; Charitidou, E.; Avgoustiniatos, S. The Thermal Conductivity of Xylene Isomers in the Temperature Range 290–360 K. *Int. J. Thermophys.* **1988**, *9* (4), 501–510.
- (43) Riedel, L. Thermal Conductivity of Liquids. *Mitt. Kaltetechn. Inst. Reichsforsch. Lebensmitt.* **1948**, *22*, 1–47.
- (44) Perkins, R. A.; Sloan, E. D.; Graboski, M. S. Experimental Study of the Thermal Conductivity of Coal Liquefaction Products and Some Constituent Pure Compounds, *Ind. Eng. Chem. Process Des. Dev.* **1986**, *25*, 1016–1022.
- (45) Guseinov, K. D.; Mirzoev, B. M.; Gylmanov, A. A. Experimental Study of Thermal Conductivity of Propylbenzene and Isopropylbenzene. *Zh. Fiz. Khim.* **1976**, *50*, 1995–1998.
- (46) Mason, H. L. Thermal Conductivity of Some Industrial Liquids from 0 to 100 °C. *Trans. ASME* **1954**, *76*, 817–821.
- (47) Rastorguev, Yu. L.; Pugach, V. V. Thermal Conductivity of Organic Hydrocarbons under High Pressure. *Izv. Vyssh. Uchebn. Zaved., Neft Gaz.* **1971**, *14* (2), 81–83.
- (48) Bachmann, R. Liquid Thermal Conductivities of Derivatives of Benzene Measured by An Unsteady-State Hot-Wire Method. *Wärme-u. Stoffubert* **1969**, *2* (3), 129–134.
- (49) Domalski, E. S.; Hearring, E. D. Heat Capacities and Entropies of Organic Compounds in the Condensed Phase. Volume III. *J. Phys. Chem. Ref. Data* **1996**, *25*, 1–295.
- (50) Héberger, K. Empirical Correlation Equations Describing Retention Data of Hydrocarbons on Dinonylphthalate and Polyethylenglycol 4000. *Chromatographia* **1998**, *25*, 725–930.

- (51) Scott, P. W.; Finke, H. L.; McCullough, J. P.; Gross M. E.; Messerly, J. F.; Pennington, R. E. Thermodynamic Properties in the Solid, Liquid and Vapor States. *J. Am. Chem. Soc.* **1955**, *77*, 4993–4998.
- (52) Haida, O.; Suga, H.; Seki, S. Calorimetric Study of the Glassy State. XI. Plural Glass Transition Phenomena of Cyclohexen. *Bull. Chem. Soc. Jpn.* **1977**, *50*, 802–809.
- (53) Douslin, D. R.; Huffman, H. M. The Heat Capacities, Heats of Transition, Heat of Fusion and Entropies of Cyclopentane, Methylcyclopentane, and Methylcyclohexane. *J. Am. Chem. Soc.* **1946**, *68*, 173–176.
- (54) Mraw, S. C.; Naas-O'Rourke, D. F. Thermodynamic Properties of Cyclohexane-*d*₁₂: Low-Temperature Heat Capacity and Enthalpies of Transition and Fusion from Accurate Differential Scanning Calorimetry, and the Entropy from Spectroscopic Results. *J. Chem. Thermodyn.* **1980**, *12*, 691–704.
- (55) Rabinovich, I. B.; Nikolaev, P. N. Isotopic Effect in the Specific Heat of Some Deutero Compounds. *Dokl. Akad. Nauk. SSSR* **1962**, *142*, 1335–1338.
- (56) Steele, W. V.; Chirico, A.; Nguyen, A.; Hossenlopp, I. A.; Smith, N. K. Determination of Some Pure Compound Ideal-Gas Enthalpies of Formation. *AIChE Symp. Series* **1989**, *85*, 140–162.
- (57) Steele, W. V. The Standard Enthalpies of Formation of a Series of C₇ Bridged-Ring Hydrocarbons: Norbornane, Norbornene, Nortricyclene, Norbornadiene, and Quadricyclane. *J. Chem. Thermodyn.* **1978**, *10*, 919–927.
- (58) Kishimoto, K.; Suga, H.; Seki, S. Calorimetric Study of the Glassy State. VIII. Heat Capacity and Relaxational Phenomena of Isopropylbenzene. *Bull. Chem. Soc. Jpn.* **1973**, *46*, 3020–3031.
- (59) Weber, H. F. *Wiedemann's Ann., Phys. Chem.* **1880**, *10*, 103 (original not seen).
- (60) Kuong, J. F. Thermal Conductivity of Liquids. *Br. Chem. Eng.* **1963**, *8*, 356.

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