# Vapor-Liquid Equilibrium for Benzene + 2-Methylpentane and Allyl Alcohol + 1-Propanol ${ }^{\dagger}$ 

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#### Abstract

The saturation pressures of 1-propanol at (311 to 353) K were measured by the ebulliometric method. The vapor-liquid equilibrium (VLE), simultaneous measurements of pressure, temperature, and composition of liquid and vapor phases ( $x, y, p, T$ ), was measured by an ebulliometric method for the system benzene +2 -methylpentane at ( $313.14,323.14$, and 333.13 ) K and for the system allyl alcohol + 1-propanol at ( $313.15,333.15$, and 353.15 ) K . The experimental vapor pressures were correlated with the Antoine and association + equation of state (AEOS) equations, and VLE was correlated with equations representing the activity coefficient and with the AEOS equation of state.


## Introduction

This work is part of an ongoing investigation of phase equilibria for systems of industrial interest sponsored by Project 805 of the Design Institute for Physical Property Data (DIPPR) of the American Institute of Chemical Engineers. In this paper, we report some of the experimental measurements that have been made under Project 805(E)/00. For the investigated mixtures, total pressure data have been reported in the literature only for the system benzene +2 -methylpentane by Funk et al. ${ }^{1}$ The complete set of $(x, y, p, T)$ vapor-liquid equilibrium (VLE) data have not been reported, and results cannot be predicted with sufficient accuracy either by using purecomponent property data or using a semiempirical method (e.g., a method based on a group contribution concept such as ASOG $^{2}$ or UNIFAC ${ }^{3}$ ).

## Experimental Section

Chemicals. Benzene (CA reg. no. 71-43-2) purchased from Sigma-Aldrich Chemie GmbH (HPLC standard > 99.5 $\mathrm{mol} \%, 99.69$ mass \% by GLC) was distilled at subambient pressure on a 25 theoretical plate column. The final purity was $>99.9$ mass $\%$, and the water content was $<0.04 \%$ (both by GLC). 2-Methylpentane (CA reg. no. 107-83-5) was purchased from Sigma-Aldrich Chemie GmbH (physicochemical standard $>99.5 \mathrm{~mol} \%$, purity $>99.82$ mass $\%$, and water content $<0.07 \%$ by GLC). Allyl alcohol (CA reg. no. 107-18-6) was purchased from Fluka Chemie GmbH (physicochemical standard $>99.5 \mathrm{~mol} \%$, purity $>99.75$ mass $\%$, and water content $<0.01 \%$ were found by GLC). 1-Propanol (CA reg. no. 71-23-8) was purchased from Fluka Chemie GmbH (physicochemical standard >99.8 mol \%, purity $>99.9$ mass $\%$, and water content $<0.01 \%$ by GLC). The last three substances were used without further purification.
Analytical Procedure. For the determination of purity and for the analysis of samples equilibrated in the course of VLE measurements via the GLC method with the HP 5890 series II gas chromatograph equipped with an HP

[^0]3396 integrator, a thermal conductivity detector (TCD) and an HP-FFAP (poly(ethylene glycol)-TPA modified) 30 m $\times 0.53 \mathrm{~mm} \times 0.01 \mu \mathrm{~m}$ film thickness column was used. An internal standard was used in the calibration procedure.

Vapor Pressure. Measurements of the pure-compound vapor pressure were performed in Swiẹtosłwski's ebulliometer modified for the determination of VLE $(x, y, p, T)$, as described earlier (Rogalski and Malanowski ${ }^{4}$ ).

The ebulliometer was connected to the pressure-stabilizing system, which consisted of a $0.6-\mathrm{m}^{3}$ buffer vessel coupled to a vacuum pump and a pressurized argon container. The pressure was manually adjusted using a system of valves and a pressurized rubber balloon until the boiling temperature of the sample in the ebulliometer had achieved the desired constant temperature within $\pm 0.005$ K . The equilibrium temperature was measured with a SYSTEMTEKNIK AB S1228 thermometer with a platinum resistance probe (resolution: 0.001 K ). The temperature fluctuation during runs lasting several hours was within $\pm 0.005 \mathrm{~K}$. No systematic deviations in the temperature measurements were observed. The pressure was determined using a Texas Instruments $144-01$ precision pressure gauge with a quartz Bourdon tube no. 8 type 2 (resolution: 0.3 Pa ), enabling the pressure determination in the range of $(1-137) \mathrm{kPa}$ with a resolution of $\pm 0.5 \mathrm{~Pa}$.

The calibration of the thermometer was made with the ice point of water. The pressure meter was calibrated with vacuum to better than $10^{-2} \mathrm{~Pa}$. In addition, the saturation vapor pressure as a function of temperature was measured for pure hexane and compared with literature data (Willingham et al. ${ }^{5}$ ). The results agree within the claimed $\delta P / \mathrm{Pa}= \pm 8$ and $\delta T / \mathrm{mK}= \pm 3$.
The estimated accuracy of the pressure measurement was $\pm 10 \mathrm{~Pa}$. The estimated accuracy of the temperature measurement was $\pm 0.01 \mathrm{~K}$. In the handling of vaporliquid equilibria, the most crucial data are the saturation vapor pressure data of pure components. The vapor pressure data for benzene have been very widely discussed. ${ }^{6}$ For the purpose of this paper, we have used the data of Forziati et al. ${ }^{7}$ as the closest to our results. For 2-methylpentane, the data of Wilingham et al. ${ }^{5}$ have been found to be the most suitable. The temperatures have been converted to the International Temperature Scale of 1990 ITS90 according to method described by Preston-Thomas. ${ }^{8}$ The data were fit with the Antoine equation, and the compari-

Table 1. Parameters of Vapor Pressure Equations for Hydrocarbons

|  | Antoine equation parameters |  |  | $\frac{\operatorname{rmsd}(p) / \mathrm{Pa}}{\text { literature }}$ | deviation from literature |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | A | $B$ | C |  |  |
| benzene ${ }^{a}$ | 6.027183 | 1208.767 | 52.664 | 0.8 | 3.2 |
| 2-methyl- | 5.966299 | 1136.685 | 46.422 | 1.4 | 3.2 |
| AEOS Equation Parameters |  |  |  |  |  |
|  | $T^{\prime}{ }_{\mathrm{c}} / \mathrm{K}$ | $P_{\text {c }}$ /bar | $\omega^{\prime}$ | $\operatorname{rmsd}(p) / \mathrm{kPa}$ | $T$ range/K |
| benzene ${ }^{\text {c }}$ | 556.1 | 48.61 | 0.2451 | 1.5 | 287-334 |
| 2-methylpentane ${ }^{c}$ | 494.75 | 29.54 | 0.2929 | 1.6 | 285-334 |

${ }^{a}$ Reference 7. ${ }^{b}$ Reference 5. ${ }^{c}$ Reference 22.


Figure 1. Vapor pressure of 1-propanol correlated with the Antoine equation. Deviations from experimental data: $\bullet$, this work; $\Delta$, Ambrose and Sprake; ${ }^{10} \nabla$, Kemme and Kreps; ${ }^{11} \square$, Schmidt; ${ }^{12}$ O, Gierycz et al. ${ }^{13}$

Table 2. Vapor Pressure $p$ as Function of the Temperature $T$ of Alcohols

| allyl alcohol |  |  |  |  | 1-propanol |  |  |  |
| :---: | ---: | ---: | ---: | :--- | :--- | ---: | ---: | ---: |
| $T / \mathrm{K}$ | $p / \mathrm{kPa}$ | $T / \mathrm{K}$ | $p / \mathrm{kPa}$ |  | $T / \mathrm{K}$ | $p / \mathrm{kPa}$ | $T / \mathrm{K}$ | $p / \mathrm{kPa}$ |
| 311.42 | 6.954 | 341.54 | 31.723 |  | 310.17 | 5.876 | 339.01 | 26.907 |
| 315.81 | 8.869 | 344.27 | 35.822 |  | 313.15 | 6.983 | 342.11 | 31.121 |
| 319.97 | 11.079 | 346.97 | 40.304 |  | 314.84 | 7.693 | 345.18 | 35.819 |
| 326.70 | 15.672 | 351.37 | 48.613 |  | 319.89 | 10.176 | 347.71 | 40.123 |
| 331.84 | 20.194 | 353.15 | 52.334 |  | 324.71 | 13.142 | 349.93 | 44.262 |
| 334.20 | 22.603 | 353.59 | 53.299 |  | 328.14 | 15.748 | 352.44 | 49.359 |
| 337.96 | 26.943 | 355.70 | 58.108 |  | 332.18 | 19.313 | 353.17 | 50.949 |
|  |  |  |  |  | 333.15 | 20.268 | 356.70 | 59.130 |
|  |  |  |  |  | 335.34 | 22.559 |  |  |

son is given in Table 1. A discussion of the data for allyl alcohol was given earlier (Lubomska et al. ${ }^{9}$ ). These data were supplemented to cover a wider temperature range. The vapor pressure of 1-propanol has been determined in the course of this work because of discrepancies in the literature data. ${ }^{10-13}$ Examples of the discrepancies are given in Figure 1. The estimated accuracy of the pressure measurement was $\pm 10 \mathrm{~Pa}$, and that of the temperature was $\pm 10 \mathrm{mK}$. The results for both alcohols are given in Table 2. The vapor pressure data were correlated with the Antoine equation:

$$
\begin{equation*}
\log (p / \mathrm{kPa})=A-\frac{B}{T / \mathrm{K}-\mathrm{C}} \tag{1}
\end{equation*}
$$

The details were described earlier (Antosik et al. ${ }^{14}$ ). Both alcohols are associating compounds. To represent such

Table 3. Correlation of Alcohols' Vapor Pressures

| compound: | allyl alcohol | 1-propanol |
| :---: | :---: | :---: |
| T/K: | 310-360 | 310-360 |
| Parameters of Antoine Equation (T/K, $p / \mathrm{kPa}$ ) |  |  |
| $A=$ | 6.936209 | 7.219284 |
| $B=$ | 1513.129 | 1629.492 |
| $C=$ | 63.131 | 57.556 |
| errors: $\operatorname{rmsd}(p) / \mathrm{Pa}=$ | 7.4 | 14.7 |
| $T^{\prime}$ Parameters of AEOS Equation |  |  |
| $T^{\prime}{ }_{c} / \mathrm{K}$ | 577.132 | 478.990 |
| $P_{\text {c }}$ /lbar | 63.425 | 48.416 |
| $\omega^{\prime}$ | 0.2948 | 0.2875 |
| $\Delta H^{\circ} /\left(\mathrm{kJ} \cdot \mathrm{mol}^{-1}\right)$ | -10.438 | -22.539 |
| $\Delta S^{\circ} /\left(\mathrm{J} \cdot \mathrm{mol}^{-1}\right)$ | -78.58 | -90.63 |
| $\Delta C_{p}{ }^{0}\left(\left(\mathrm{~J} \cdot \mathrm{~mol}^{-1}\right)\right.$ | -251.7 | -34.01 |
| errors: $\operatorname{rmsd}(p) / \mathrm{Pa}=$ | 15.4 | 12.6 |

Enthalpy of Vaporization ( $\Delta_{\text {vap }} H^{\circ} / \mathrm{kJ} \cdot \mathrm{mol}^{-1}$ ) at $T / \mathrm{K}=298.15$ calculated from our vapor pressure $46.41 \quad 47.75$ calorimetric $\quad 47 \pm 1^{a} \quad 47.3-47 .{ }^{a}$ Daubert and Danner prediction $45.90^{b} \quad 47.75^{b}$
${ }^{a}$ Reference 24. ${ }^{b}$ Reference 18.
Table 4. Experimental Results of Vapor-Liquid Equilibrium

| $x_{1}$ | $y_{1}$ | $P / \mathrm{kPa}$ | $x_{1}$ | $y_{1}$ | $P / \mathrm{kPa}$ | $x_{1}$ | $y_{1}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $T / \mathrm{K}=313.140$ |  | $T / \mathrm{K}=323.137$ | $T / \mathrm{KPa}=333.134$ |  |  |  |  |

$\begin{array}{llllllllll}0.0000 & 0.0000 & 50.650 & 0.0000 & 0.0000 & 72.200 & 0.0000 & 0.0000 & 100.400\end{array}$ $\begin{array}{lllllllllll}0.1143 & 0.0867 & 49.389 & 0.1124 & 0.0911 & 70.448 & 0.1163 & 0.0861 & 98.167\end{array}$ $0.2298 \quad 0.158047 .6760 .2302 \quad 0.1558 \quad 68.1530 .23090 .1578$ 95.014 $\begin{array}{lllllllll}0.3166 & 0.2137 & 46.293 & 0.3179 & 0.2054 & 66.175 & 0.3127 & 0.2046 & 92.276\end{array}$ $\begin{array}{lllllllll}0.4461 & 0.2835 & 44.110 & 0.4427 & 0.2752 & 63.203 & 0.4410 & 0.2703 & 88.330\end{array}$ $\begin{array}{llllllllll}0.5558 & 0.3396 & 41.932 & 0.5533 & 0.3411 & 60.112 & 0.5486 & 0.3398 & 83.984\end{array}$ 0.63310 .392540 .1120 .63220 .395157 .6050 .62920 .392980 .684 $\begin{array}{llllllllll}0.7154 & 0.4627 & 37.907 & 0.7150 & 0.4629 & 54.417 & 0.7152 & 0.4653 & 76.350\end{array}$ $\begin{array}{lllllllll}0.7870 & 0.5401 & 35.318 & 0.7820 & 0.5399 & 51.023 & 0.7916 & 0.5392 & 72.075\end{array}$ $\begin{array}{llllllllll}0.8543 & 0.6133 & 33.025 & 0.8518 & 0.6233 & 47.765 & 0.8546 & 0.6144 & 67.362\end{array}$ $\begin{array}{llllllllllll}0.8941 & 0.6913 & 31.087 & 0.8925 & 0.6938 & 45.216 & 0.8908 & 0.7050 & 63.997\end{array}$ $\begin{array}{llllllllll}0.9313 & 0.7844 & 28.731 & 0.9327 & 0.7899 & 41.952 & 0.9340 & 0.7939 & 59.779\end{array}$ $\begin{array}{lllllllll}0.9574 & 0.8596 & 27.140 & 0.9565 & 0.8597 & 39.907 & 0.9538 & 0.8539 & 57.408\end{array}$ $1.00001 .0000 \quad 24.3501 .00001 .000036 .1501 .00001 .0000$

$$
T / \mathrm{K}=313.15 \quad T / \mathrm{K}=333.15 \quad T / \mathrm{K}=353.15
$$

0000 Allyl Alcohol (1) + 1-Propanol (2)
$\begin{array}{llllllllll}0.0000 & 0.0000 & 6.983 & 0.0000 & 0.0000 & 20.268 & 0.0000 & 0.0000 & 50.951\end{array}$ $\begin{array}{llllllllll}0.0781 & 0.0882 & 7.057 & 0.0785 & 0.0851 & 20.393 & 0.0781 & 0.0827 & 51.133\end{array}$ $\begin{array}{lllllllllll}0.1798 & 0.1988 & 7.148 & 0.1800 & 0.1943 & 20.576 & 0.1813 & 0.1885 & 51.361\end{array}$ $\begin{array}{llllllllll}0.2697 & 0.2917 & 7.211 & 0.2698 & 0.2861 & 20.716 & 0.2697 & 0.2790 & 51.516\end{array}$ $\begin{array}{llllllllll}0.3547 & 0.3802 & 7.292 & 0.3563 & 0.3730 & 20.854 & 0.3568 & 0.3666 & 51.739\end{array}$ $\begin{array}{lllllllll}0.4271 & 0.4510 & 7.348 & 0.4276 & 0.4444 & 20.953 & 0.4074 & 0.4360 & 51.845\end{array}$ $\begin{array}{lllllllllll}0.4863 & 0.5090 & 7.401 & 0.4866 & 0.5023 & 21.052 & 0.4661 & 0.4896 & 51.953\end{array}$ $\begin{array}{lllllllllll}0.4982 & 0.5235 & 7.407 & 0.5008 & 0.5164 & 21.063 & 0.4833 & 0.5120 & 51.999\end{array}$ $\begin{array}{lllllllll}0.5800 & 0.6020 & 7.470 & 0.5798 & 0.5940 & 21.181 & 0.5611 & 0.5847 & 52.088\end{array}$ $\begin{array}{lllllllll}0.6794 & 0.6970 & 7.532 & 0.6802 & 0.6902 & 21.276 & 0.6604 & 0.6849 & 52.233\end{array}$ $\begin{array}{llllllllll}0.7450 & 0.7570 & 7.569 & 0.7447 & 0.7538 & 21.327 & 0.7449 & 0.7483 & 52.269\end{array}$ $\begin{array}{llllllllll}0.7949 & 0.8072 & 7.584 & 0.7950 & 0.8019 & 21.365 & 0.7960 & 0.7951 & 52.296\end{array}$ $\begin{array}{lllllllll}0.9045 & 0.9095 & 7.632 & 0.9043 & 0.9073 & 21.454 & 0.9044 & 0.9042 & 52.322\end{array}$ $\begin{array}{llllllllllll}1.0000 & 1.0000 & 7.672 & 1.0000 & 1.0000 & 21.510 & 1.0000 & 1.0000 & 52.336\end{array}$
mixtures properly, a special treatment is necessary. In previous work, ${ }^{15}$ it has been found that the association + equation of state (AEOS) is the most suitable representation of phase equilibria in systems formed by associating or even chemically reacting compounds. In the AEOS model, the thermodynamic properties of an associated mixture are viewed as the result of chemical equilibrium between associated species and physical interactions between all, associated or inert, species in a mixture. Detailed equations have been given (Chylinski et al. ${ }^{16}$ ).
The correlation results are summarized in Table 3. The root-mean-square deviations of pressure $(\operatorname{rmsd}(p) / \mathrm{Pa})$ were calculated by

$$
\begin{equation*}
\operatorname{rmsd}(p / \mathrm{Pa})=\sqrt{\frac{\sum_{i=1}^{n}\left(p_{i}^{\text {exptl }}-p_{i}^{\text {calcd }}\right)^{2}}{n}} \tag{2}
\end{equation*}
$$

Table 5. Correlation of Vapor-Liquid Equilibrium

\begin{tabular}{|c|c|c|c|c|c|c|}
\hline \multirow[b]{2}{*}{equation} \& \multicolumn{4}{|c|}{parameters} \& \multirow[b]{2}{*}{$\underline{\operatorname{rmsd}(y)}$} \& \multirow[t]{2}{*}{$$
\frac{\operatorname{rmsd}(p)}{\mathrm{Pa}}
$$} <br>
\hline \& 1 \& 2 \& 3 \& 4 \& \& <br>
\hline \multicolumn{7}{|c|}{$T / \mathrm{K}=313.14$} <br>
\hline \multirow[t]{4}{*}{Redlich-Kister} \& 0.566097 \& \& \& \& 0.0214 \& 389.6 <br>
\hline \& 0.568363 \& 0.108714 \& \& \& 0.0230 \& 113.7 <br>
\hline \& 0.569499 \& 0.109214 \& -0.010202 \& \& 0.0228 \& 112.2 <br>
\hline \& 0.568310 \& 0.118738 \& -0.006428 \& -0.033797 \& 0.0227 \& 108.1 <br>
\hline WILSON \& -2789.53 \& -4839.19 \& \& \& 0.0234 \& 131.2 <br>
\hline UNIQUAC* \& 3368.48 \& -1488.15 \& \& \& 0.0233 \& 126.0 <br>
\hline \multicolumn{7}{|l|}{} <br>
\hline \multirow[t]{4}{*}{Redlich-Kister} \& \multicolumn{4}{|l|}{0.518517 T/K = 323.137} \& 0.0295 \& 492.4 <br>
\hline \& \multicolumn{4}{|l|}{$0.520741 \quad 0.098894$} \& 0.0312 \& 138.1 <br>
\hline \& \multicolumn{2}{|l|}{$0.521221 \quad 0.099050$} \& -0.004225 \& \& 0.0312 \& 137.7 <br>
\hline \& 0.520801 \& 0.102661 \& -0.002834 \& -0.012685 \& 0.0311 \& 136.8 <br>
\hline \multirow[t]{2}{*}{WILSON UNIQUAC*} \& -2546.52 \& -4675.95 \& \& \& 0.0315 \& 154.0 <br>
\hline \& 3423.44 \& -1653.74 \& \& \& 0.0314 \& 149.5 <br>
\hline \multirow[b]{5}{*}{Redlich-Kister

WILSOn} \& \multicolumn{3}{|l|}{T/K $=333.134$} \& \& \& <br>
\hline \& \multicolumn{2}{|l|}{} \& \& \& 0.0404 \& <br>

\hline \& \multirow[t]{2}{*}{$$
\begin{aligned}
& 0.483482 \\
& 0.482938
\end{aligned}
$$} \& 0.109557 \& \& \& \[

0.0420

\] \& \[

196.1
\] <br>

\hline \& \& $$
0.109373
$$ \& \[

0.004392

\] \& \& \[

0.0421

\] \& \[

195.6
\] <br>

\hline \& $$
\begin{aligned}
& 0.482938 \\
& 0.480175
\end{aligned}
$$ \& \[

0.137503

\] \& \[

0.013180

\] \& $-0.096128$ \& \[

0.0415

\] \& \[

115.5
\] <br>

\hline \& $$
\begin{aligned}
& 0.480175 \\
& -1758.87
\end{aligned}
$$ \& -5518.02 \& \& \& 0.0424 \& 221.0 <br>

\hline UNIQUAC* \& $$
\begin{aligned}
& -1758.87 \\
& 2470.51
\end{aligned}
$$ \& \[

-949.54
\] \& \& \& 0.0423 \& 212.8 <br>

\hline \& \multicolumn{3}{|l|}{$$
T / \mathrm{K}=\text { from } 310 \text { to } 355
$$} \& \& \& <br>

\hline AEOS \& \& eq 5 \& \& \& 0.0104 \& 18.7 <br>
\hline
\end{tabular}

Allyl Alcohol (1) + 1-Propanol (2)

| equation | parameters |  |  |  | $\underline{\operatorname{rmsd}(y)}$ | $\frac{\operatorname{rmsd}(p)}{\mathrm{Pa}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 | 2 | 3 | 4 |  |  |
| $T / \mathrm{K}=313.15$ |  |  |  |  |  |  |
| Redlich-Kister | 0.000000 |  |  |  | 0.0023 | 46.0 |
|  | 0.032382 | 0.015024 |  |  | 0.0012 | 5.2 |
|  | 0.033159 | 0.015456 | -0.006839 |  | 0.0013 | 5.0 |
|  | 0.033065 | 0.029722 | -0.006292 | -0.046049 | 0.0021 | 2.8 |
| WILSON | 4989.52 | -6409.08 |  |  | 0.0012 | 5.5 |
| UNIQUAC ${ }^{a}$ | -3063.02 | 3720.42 |  |  | 0.0012 | 5.5 |
| AEOS | $1.9577 \times 10^{-5}$ | -0.0083 |  |  | 0.0013 | 11.4 |
| $T / \mathrm{K}=333.15$ |  |  |  |  |  |  |
| Redlich-Kister | 0.000000 |  |  |  | 0.0017 | 56.7 |
|  | $0.013889$ | 0.007473 |  |  | $0.0009$ | 9.1 |
|  | $0.015089$ | $0.007985$ | $-0.010404$ |  | $0.0009$ | 6.8 |
|  | $0.015094$ | $0.010884$ | $0.010443$ | -0.009323 | 0.0010 | 6.3 |
|  | $4739.92$ | $-5690.91$ |  |  | 0.0010 | 9.9 |
| UNIQUAC ${ }^{a}$ | $-2727.78$ | $3167.30$ |  |  | 0.0010 | 9.8 |
| AEOS | $1.2306 \times 10^{-5}$ | -0.0104 |  |  | 0.0009 | 36.1 |
| $T / \mathrm{K}=353.15$ |  |  |  |  |  |  |
| Redlich-Kister | 0.000000 |  |  |  | 0.0119 | 46.1 |
|  | $-0.003468$ |  |  |  | 0.0114 | 19.9 |
|  | $-0.002353$ | $0.007811$ | -0.009692 |  | 0.0114 | 14.1 |
|  | -0.002243 | 0.011764 | -0.010080 | -0.012720 | 0.0112 | 11.6 |
|  | $5876.30$ | $-7054.96$ |  |  | $0.0115$ | $22.5$ |
| $\text { UNIQUAC }^{a}$ | $291.13$ | $-291.13$ |  |  | $0.0119$ | $31.6$ |
| AEOS | $0.6286 \times 10^{-5}$ | -0.0273 |  |  | 0.0064 | 454.8 |
| $T / \mathrm{K}=$ from 310 to 355 |  |  |  |  |  |  |
| AEOS | eq 3 | eq 4 |  |  | 0.0038 | 271.8 |

where $n$ is the number of experimental points, $p_{i}^{\text {exptl }}$ is the pressure measured at point number $i$, and $p_{i}^{\text {calcd }}$ is the pressure calculated from eq 2 at point $i$. A comparison of correlation results with literature data for 1-propanol is given in Figure 1.

Vapor-Liquid Equilibrium. Vapor-liquid equilibrium measurements were carried out for both systems under isothermal conditions by means of the ebulliometric method described elsewhere. ${ }^{4}$ The pure compound was introduced into the ebulliometer and heated until the boiling point was
reached at the adjusted pressure. The readouts of pressure and temperature were taken at the equilibrium stage. The specified temperature was measured with an accuracy of $\pm 0.01 \mathrm{~K}$. The pressure was measured with an accuracy of $\pm 10 \mathrm{~Pa}$. Samples of boiling liquid and vapor condensate were collected for analysis. Next, a precise amount of the second component was added, and the steady state was reached at the desired temperature. The measure of the steady state was the stability of temperature within $\pm 0.003$ K for about 5 min . In general, the time between introducing


Figure 2. VLE for propylene benzene (1)+ 2-methylpentane (2): - this work; ■, Funk et al. ${ }^{1}$ Lines represent the correlation with the AEOS. Solid symbols represent experimental bubble points, and hollow symbols represent experimental dew points.
the samples was about 30 min . The whole procedure was repeated until the concentration of the second component exceeded $50 \%$. The sample composition was determined by using gas chromatography. For each system, the calibration procedure was used.

Vapor-liquid measurements were carried out under isothermal conditions. The estimated accuracy of the pressure measurement was $\pm 10 \mathrm{~Pa}$, and that of temperature was $\pm 10 \mathrm{mK}$. The sample composition was determined by the GLC method, with an uncertainty of $0.1 \mathrm{~mol} \%$ for the liquid phase and $0.5 \mathrm{~mol} \%$ for the vapor phase. The results obtained are given in Table 4. The consistency check was made for each isotherm with the method proposed by Eubank et al. ${ }^{17}$ (test 1). The auxiliary data were taken from Daubert and Danner. ${ }^{18}$ The obtained differences between calculated and experimental liquid-phase compositions do not exceed 0.016, which is still reasonable taking into account the fact that $P^{*}(y)$ in this process is a higher-order polynomial.

The $P, T, x, y$ data were reduced to activity coefficients. The equations of Redlich-Kister, with one to four adjustable parameters, Wilson, and UNIQUAC were used as activity coefficients models. The exact form of these equations is given in Malanowski and Anderko. ${ }^{19}$

The necessary fugacity coefficients $\left(\phi_{i}\right)$ of component $i$ in the vapor phase were calculated from

$$
\begin{equation*}
\phi_{i}=\exp \left[\frac{\left(v_{i}^{\mathrm{L}}-\beta_{i}\right)\left(P-P_{i}^{0}\right)-P_{i}^{0}\left(1-y_{i}\right)^{2}\left(\beta_{i}+\beta_{2}\right) / 2}{R T}\right] \tag{3}
\end{equation*}
$$

where virial coefficients $\beta_{i}$ as functions of $T$ were calculated from DIPPR data and equation ${ }^{18}$

$$
\begin{equation*}
p / \mathrm{Pa}=\exp \left(A+\frac{B}{T}+C \ln T+D T^{\mathrm{E}}\right) \tag{4}
\end{equation*}
$$

$A, B, C, D$, and $E$ are recommended parameters.
Second virial coefficients $\beta_{i}$ as functions of $T$ were calculated from the Daubert and Danner ${ }^{18}$ data.


Figure 3. VLE for allyl alcohol (1) + 1-propanol (2): ©, 313.15 K ; $\quad 333.15 \mathrm{~K} ; \mathbf{\Delta}, 353.15 \mathrm{~K}$. Lines represent a prediction with the AEOS. Solid symbols represent experimental bubble points, and hollow symbols represent experimental dew points.

The results obtained are summarized in Table 5.
The mixture benzene +2 -methylpentane consists of two inert compounds, but allyl alcohol + 1-propanol consists of two associating compounds. It was concluded that the association with the equation of state (AEOS) is suitable for both systems. The use of the AEOS equation leads to the split of the compressibility factor into two parts

$$
\begin{equation*}
z=\frac{p V}{R T}=z^{(\mathrm{ph})}+z^{(\mathrm{ch})}-1 \tag{5}
\end{equation*}
$$

where $z^{(\mathrm{ph})}$ and $z^{(\mathrm{ch})}$ are the physical and chemical contributions to the compressibility factor, respectively.

The $z^{(\mathrm{ph})}$ contribution is equivalent to the equation of state for nonreacting monomeric species. In this work, it was calculated from the cubic equation of state of Yu et al. ${ }^{20}$

$$
\begin{equation*}
z^{(\mathrm{ph})}=\frac{v}{v-b}-\frac{a(T) v}{R T[v(v+c)+b(3 v+c)]} \tag{6}
\end{equation*}
$$

where $a(T), b$, and $c$ are generalized functions of the critical temperature $T_{\mathrm{c}}$, critical pressure $P_{\mathrm{c}}$, and acentric factor $\omega$ of a pure component, respectively.

The $z^{(\mathrm{ch})}$ contribution is equal to the reciprocal mean association number ( $K$ ) and depends on the association model applied. The continuous linear association Mecke-

Kempter model is most suitable for representing the allyl alcohol + 1-propanol mixture at subambient pressure. ${ }^{21}$ The following equation for the chemical term (eq 5) shows that the self- as well as cross-association was used,

$$
\begin{equation*}
z^{(\mathrm{ch})}=\sum_{i=1}\left(\frac{2 x_{A_{i}}}{\left.\left(1+\sqrt{1+4 R T\left(\sum_{j=1}^{2} K_{\mathrm{ij}} \mathrm{x}_{\mathrm{A}}\right.}\right) / V\right)}\right) \tag{7}
\end{equation*}
$$

where $K_{i j}$ is either the self-association constant (for $i=j$ ) or the cross-association constant (for $i \neq j$ ).

The parameters of the AEOS obtained for pure-component data were used without modification for mixture calculations. For allyl alcohol and 1-propanol, data from Table 3 were used, and for benzene and 2-methylpentane, previously published parameters ${ }^{22}$ were used. The detailed procedure was given by Antosik et al. ${ }^{23}$

The temperature dependence of the association constant $K_{i j}$ can be expressed by assuming that $H^{\circ}$ and $S^{\circ}$ of association are linearly dependent on temperature (with appropriate values of $C_{p}$ given in Table 4):

$$
\begin{align*}
& \ln K_{i j}=\frac{-\Delta H^{\mathrm{o}}\left(T_{\mathrm{o}}\right)+\Delta C_{p}^{\mathrm{o}} T_{\mathrm{o}}}{R T}+ \frac{1}{R}\left[\Delta S^{\mathrm{o}}\left(T_{\mathrm{o}}\right)-\Delta C_{p}^{\mathrm{o}}-\right. \\
&\left.\Delta C_{p}^{\mathrm{o}} \ln T_{\mathrm{o}}\right]+\frac{\Delta C_{p}^{\mathrm{o}}}{R} \ln T \tag{8}
\end{align*}
$$

The binary parameters $a, b$, and $c$ of the Yu et al. ${ }^{19}$ equation ( $z^{(\mathrm{ph})}$ term) were calculated using classical mixing rules:

$$
\begin{align*}
a & =\sum_{i=1}^{2} \sum_{i=1}^{2} x_{i} x_{j}\left(1-\theta_{i j}\right) \sqrt{a_{i} a_{j}}  \tag{9}\\
b & =\sum_{i=1}^{2} x_{i} b_{i}  \tag{10}\\
c & =\sum_{i=1}^{2} x_{i} c_{i} \tag{11}
\end{align*}
$$

These mixing rules contain only one binary adjustable parameter $\theta_{12}$. The mixture consists of two polar compounds, and better results were obtained with the crossassociation constant $K_{12}$ calculated from binary data. These mixing rules contain only one binary adjustable parameter $\theta_{12}$. The allyl alcohol +1 -propanol system consists of two polar compounds. The cross-association constant $K_{12}$ of eq 8 was calculated for this system from binary VLE data. The correlation results are summarized in Table 4. The temperature dependence of parameters $K_{12}$ and $\theta_{12}$ has been calculated for the temperature range ( 310 to 355 ) K by linear regression from isothermal VLE data reported in this paper:

$$
\begin{gather*}
K_{12}=1.23 \times 10^{-4}-3.32 \times 10^{-7} T  \tag{12}\\
\theta_{12}=0.1429-4.75 \times 10^{-4} T \tag{13}
\end{gather*}
$$

For the benzene +2 -methylpentane mixture, the following relation for $\theta_{12}$ has been found by the reduction of data reported in Table 4.

$$
\begin{equation*}
\theta_{12}=0.02025-3.546 \times 10^{-5} T \tag{14}
\end{equation*}
$$

The rmsd values for $p$ and $y_{1}$ obtained with these equations are given in Table 5.

The results of calculations by AEOS with eqs 12-14 used for $K_{12}$ and $\theta_{12}$ are given in Table 5 and in Figures 2 and 3 and are satisfactory. A comparison of the correlation results for single isotherms with those predicted for the same isotherms using eqs $12-14$ leads to the conclusion that the correlated results are similar to those predicted with the temperature-dependent $K_{12}$ and $\theta_{12}$ parameters. A reasonable prediction of Funk et al. ${ }^{1}$ data has been obtained (Figure 2).

The $\theta_{12}$ and $K_{12}$ parameters are of similar or better accuracy than those correlated with equations for activity coefficients at one temperature only.

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## Literature Cited

(1) Funk, E. W.; Foo-Cheang, C.; Prausnitz, J. M. Thermodynamic Properties of Binary Liquid Mixtures Containing Aromatic and Saturated Hydrocarbons. J. Chem. Eng. Data 1972, 17, 24-27.
(2) Kojima, K.; Tochigi, T. Prediction of Vapor-Liquid Equilibria by the ASOG Method; Elsevier: Amsterdam, 1979.
(3) Fredenslund, A.; Gmehling, J.; Rasmussen, P. Vapor-Liquid Equilibria Using UNIFAC; Elsevier: Amsterdam, 1977.
(4) Rogalski, M.; Malanowski, S. Ebulliometers Modified for the Accurate Determination of Vapor-Liquid Equilibrium. Fluid Phase Equilib. 1980, 5, 97-112.
(5) Williamham, C. B.; Taylor, W. J.; Pignocco, J. M.; Rossini, F. D. Vapor Pressures and Boiling Points of Some Paraffin, Alkylcyclopentane, Alkylcyclohexane, and Alkylbenzene Hydrocarbons. J. Res. Natl. Bur. Stand. (U.S.) 1945, 35, 219-244.
(6) Ambrose, D. Reference Values of Vapor Pressure. The Vapor Pressure of Benzene and Hexafluorobenzene. J. Chem. Thermodyn. 1981, 13, 1161-1167.
(7) Forziati, A. F.; Norris, W. R.; Rossini, F. D. Vapor Pressures and Boiling Points of Sixty API-NBS Hydrocarbons. J. Res. Natl. Bur. Stand. (U.S.) 1949, 43, 555-563.
(8) Preston-Thomas, H. The International Temperature Scale of 1990. Metrologia, 1990, 27, 3-10. Preston-Thomas, H. errata in Metrologia 1990, 27, 107.
(9) Lubomska, M.; Banaś, A.; Malanowski, S. K. Vapor-Liquid Equilibrium in Binary Systems Formed by Allyl Alcohol with Benzene and with Cyclohexane. J. Chem. Eng. Data 2002, 47, 1466-1471.
(10) Ambrose, D.; Sprake, C. H. S. Thermodynamic Properties of Organic Oxygen Compounds. XXV. Vapor Pressures and Normal Boiling Temperatures of Aliphatic Alcohols. J. Chem. Thermodyn. 1970, 2, 631-645.
(11) Kemme, H. R.; Kreps, S. I. Vapor Pressure of Primary n-Alkyl Chlorides and Alcohols. J. Chem. Eng. Data 1969, 14, 98-102.
(12) Schmidt, G. C. Untersuchungen über die Dampfdrucke Homologer Verbindungen. II. Die Dampftensionen der Homologen Reihe der Fettalkohole. Z. Phys. Chem. 1891, 8, 628-646.
(13) Gierycz, P.; Rogalski, M.; Malanowski, S. Vapor-Liquid Equilibria in Binary Systems Formed by $N$-Methylpyrrolidone with Hydrocarbons and Hydroxyl Derivatives. Fluid Phase Equilib. 1985, 22, 107-122.
(14) Antosik, M.; Fraś, Z.; Malanowski, S. K. Vapor-Liquid Equilibrium in 2-Ethoxyethanol + Methanol at 313.15 to 333.15 K. J. Chem. Eng. Data 1999, 44, 368-372.
(15) Anderko, A.; Malanowski, S. K. Calculation of Solid-Liquid, Liquid-Liquid and Vapor-IIquid Equilibria by Means of an Equation of State Incorporating Association. Fluid Phase Equilib. 1989, 48, 223-241.
(16) Chyliński, K.; Fraś, Z.; Malanowski, S. K. Vapor-Liquid Equilibrium for Propylene Glycol + 2-(2-Hexyloxyethoxy)ethanol and 1-Methyl-2- Pyrrolidone + 1-Methoxy-Propan-2-ol. J. Chem. Eng. Data 2004, 49, 18-23.
(17) Eubank, P. T.; Lamonte, B. G.; Alvarado, J. F. J. Consistency Tests for Binary VLE Data. J. Chem. Eng. Data 2000, 45, 10401048.
(18) Daubert, T. E.; Danner, R. P. Physical and Thermodynamic Properties of Pure Chemicals; Taylor \& Francis: London, 1998; Core Edition and Supplements 1-8.
(19) Malanowski, S; Anderko, A. Modeling Phase Equilibria. Thermodynamical Background and Practical Tools; Wiley \& Sons: New York, 1992.
(20) Yu, J. M.; Lu, B. C.-Y.; Iwai, Y. Simultaneous Calculation of VLE and Saturated Liquid and Vapor Volumes by Means of a 3P1T Cubic EOS. Fluid Phase Equilib. 1987, 37, 207-222.
(21) Anderko, A. Cubic and Generalized van der Waals Equations. In Equations of State for Fluids and Fluid Mixtures; Sengers, J. V., Ed.; Elsevier: Amsterdam, 2000.
(22) Wisniewska, B.; Malanowski, S. K. Prediction of Phase Equilibria for Hydrocarbon Systems in a Wide Range of Pressure and Temperature by AEOS Equation of State. Fluid Phase Equilib. 1990, 56, 89-95.
(23) Antosik, M.; Gałka, M.; Malanowski, S. K. Vapor-Liquid Equilibrium for Acetonitrile + Propanenitrile and 1-Pentanamine + 1-Methoxy-2-propanol. J. Chem. Eng. Data 2004, 49, 11-17.
(24) Chemistry WebBook; NIST Standard Reference Database Number 69; March 2003 release (http://webbook.nist.gov/chemistry/).

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