(p, ρ, T) Properties and Apparent Molar Volumes V_{ϕ} of ZnCl₂ in CH₃OH

E. C. Ihmels[†] and J. T. Safarov^{*,‡}

Laboratory for Thermophysical Properties LTP GmbH, Institute at the University of Oldenburg, Marie-Curie-Strasse 10, D-26129 Oldenburg, Germany, and Heat and Refrigeration Techniques Department, Azerbaijan Technical University, H. Javid Avenue 25, AZ1073 Baku, Azerbaijan

The (p, ρ, T) properties and apparent molar volumes V_{ϕ} of ZnCl₂ in methanol at T = (298.15 to 398.15) K and pressures up to p = 40 MPa are reported. An empirical correlation for the density of the (ZnCl₂ + CH₃OH) with pressure, temperature, and molality has been derived. For the solutions the experiments were carried out at molalities $m = (0.13476, 0.47677, 0.80178, 1.03861, 1.97685, \text{ and } 5.36750) \text{ mol} \cdot \text{kg}^{-1}$ of zinc chloride.

Introduction

The efficiency of an absorption refrigeration cycle is largely dependent on the physical and chemical properties of the heat transfer fluids. These systems work with the heat transfer fluid, which contains two working pairs, usually water/salt solutions, which are used with evaporator temperatures above 0 °C due to freezing of the refrigerant (water).

The most serious problems by using the conventional aqueous solutions of electrolytes were discussed in our previous publications of the investigation of methanol solutions of electrolytes.^{1,2} Using methanol as a refrigerant in absorption systems reduces these problems and can replace aqueous solutions at temperatures below the freezing point of water.

In the present work, the (p, ρ, T) properties and apparent molar volumes V_{ϕ} of the ZnCl₂ in methanol at T = (298.15 to 398.15) K and pressures up to p = 40 MPa are reported. An empirical correlation for the density of the (ZnCl₂ + CH₃OH) with pressure, temperature, and molality has been derived. The (p, ρ, T) properties and apparent molar volumes of ZnCl₂ in methanol solutions were not available in the literature.

Experimental Section

The (p, ρ, T) properties were investigated using a high pressure—high temperature vibrating-tube densimeter.^{2,3} The observed reproducibility and estimated maximum uncertainty of the density measurements between T = (298.15 to 398.15) K and up to p = 40 MPa is within $\rho = \pm 0.05 \text{ kg} \cdot \text{m}^{-3}$ and $\rho = \pm 0.2 \text{ kg} \cdot \text{m}^{-3}$, respectively. This leads to maximum relative uncertainties of ± 0.03 % for the performed measurements for the solutions. For the pressure measurement, a pressure transducer (model PDCR 922 up to 60 MPa, from Druck, Leicester, England) is used. The accuracy after calibration with a deadweight pressure gauge was estimated to be better than $\pm 6 \text{ kPa}$. The calibrated (ITS-90) Pt100 temperature sensors installed show a resolution of ± 3 mK and an accuracy of ± 30 mK, while the thermostat has a stability of ± 20 mK.

 $ZnCl_2$ (w > 0.998) was supplied from Merck, Germany, and was used without further purification. Before experiment, the



Figure 1. Plot of experimental density ρ of methanol solutions of ZnCl₂ vs pressure *p* at $m = 0.80178 \text{ mol} \cdot \text{kg}^{-1}$: \blacklozenge , 298.27 K; \blacksquare , 323.23 K; \blacktriangle , 348.27 K; \blacklozenge , 373.29 K; \Box , 398.32 K.

salt was dried about 72 h in a special cell by heating at 413.15 K and reduced pressure. To prevent absorption of water, preparation of salt solutions has been performed in a glovebox. The samples were obtained by successive dilutions of the concentrated solutions. Methanol (w > 0.998) was supplied from the Carl Roth Company and was degassed by vacuum distillation using a Vigreux column with a height of 90 cm. The final purity of the methanol was checked by gas chromatography (w > 0.999) and Karl Fischer titration (water content < 50 ppm). The solutions were prepared by mass using an electronic scale with resolution of 0.0001 g.

Results and Discussion

In this work, the (p, ρ, T) properties and apparent molar volumes V_{ϕ} of ZnCl₂ in methanol at T = (298.15 to 398.15) K, at pressures up to p = 40 MPa are reported. The experiments were carried out at $m = (0.13476, 0.47677, 0.80178, 1.03861, 1.97685, \text{ and } 5.36750) \text{ mol} \cdot \text{kg}^{-1}$ of ZnCl₂. The obtained (p, ρ, T) results are listed in Table 1.

^{*} Corresponding author present address: Lehrstuhl für Thermische Verfahrenstechnik, Friedrich-Alexander-Universität Erlangen-Nürnberg, Egerlandstr. 3, D-91058 Erlangen, Germany. Tel: +49 9131 85 27453. Fax: +49 9131 85 27441. E-mail: javid.safarov@cbi.uni-erlangen.de.

[†] Institute at the University of Oldenburg.

[‡] Azerbaijan Technical University.

Table 1.	Experimental	(p,	ρ,	T)	Results	of	the	$(ZnCl_2 +$	CH ₃ OH)
----------	--------------	-----	----	----	---------	----	-----	-------------	---------------------

p/MPa	$ ho/(kg \cdot m^{-3})$	p/MPa	$ ho/(kg \cdot m^{-3})$	p/MPa	$ ho/(kg \cdot m^{-3})$	p/MPa	$ ho/(kg \cdot m^{-3})$	p/MPa	$\rho/(kg \cdot m^{-3})$
$m = 0.13476 \text{ mol} \cdot \text{kg}^{-1}$									
T =	298.27 K	T = 1	323.24 K	T = 3	348.27 K	T =	373.30 K	T = 1	398.33 K
0.205	801.32	0.209	777.17	0.308	752.15	0.533	725.48	0.893	695.88
5 004	805.97	4 990	782 51	4 989	758.25	4 995	732 41	4 994	703 77
10,000	810.57	10.003	702.31	0.003	764.30	0.085	730.51	0.084	712.30
15.000	010.57	14.000	707.77	7.775	704.30	7.705	739.31	7.704	712.37
15.010	814.96	14.999	/92./1	14.999	/69.95	15.001	746.08	14.988	/20.18
20.007	819.13	20.000	797.39	19.998	775.25	19.986	752.14	19.984	727.30
24.999	823.11	24.994	801.85	24.994	780.25	24.992	757.83	25.003	733.89
30.002	826.95	29.993	806.09	29.998	785.01	29.985	763.18	29.996	740.01
34.993	830.61	35.007	810.14	34.998	789.52	35.008	768.23	34.993	745.75
40.006	834.16	39 997	814.00	39 998	793.81	39 993	773.04	39 989	751 12
40.000	054.10	37.771	014.00	37.770	775.01	37.775	115.04	37.707	751.12
				m = 0.476	677 mol∙kg ^{−1}				
T =	298.28 K	T = 1	323.23 K	T=3	348.26 K	T =	373.29 K	T = 1	398.32 K
0.188	833.84	0.207	808.23	0.320	782.80	0.527	755.90	0.908	726.55
4.994	838.00	4.985	813.47	4.983	788.73	4.990	762.64	4.981	734.09
10.004	841.99	9,994	818.67	9,998	794.70	9.984	769.58	9,983	742.44
1/ 082	845.90	14 982	823.55	1/ 085	800.24	14 985	776.00	1/ 003	750.05
20.019	840.66	10.005	023.33	10.020	805.49	10.087	770.00	10.004	750.05
20.018	049.00	19.993	020.21	19.969	003.40	19.967	701.90	19.994	757.02
25.032	853.57	24.999	832.65	24.996	810.44	24.985	/8/.59	24.992	/63.4/
30.004	857.56	29.987	836.86	29.985	815.14	30.012	792.89	30.005	769.51
34.993	862.15	35.003	840.94	34.987	819.64	34.987	797.89	34.992	775.14
39.997	866.01	39.994	844.83	40.007	823.94	40.000	802.68	40.002	780.53
					179 mol.1.a=1				
<i>T</i> –	200 07 V	T – 1	222.22.12	m = 0.80	1/8 morekg -	T –	272 20 17	T – 1	200 22 17
1 =	298.27 K	I = I	323.23 K	I = s	548.27 K	1 =	3/3.29 K	I = .	598.52 K
0.170	861.37	0.233	835.94	0.328	810.17	0.523	783.25	0.907	/54.11
4.996	865.98	4.983	841.09	4.999	816.01	4.994	789.83	4.988	761.40
9.995	870.53	10.002	846.25	9.992	821.86	9.984	796.61	9.984	769.52
15.000	874.88	15.002	851.11	14.985	827.35	15.005	802.94	14.994	776.95
20.001	879.03	19 999	855 74	19 994	832.56	20.005	808 85	19 982	783 77
24 988	883.01	24 989	860.16	24 989	837.48	24 990	814 38	25.006	790.16
20.004	005.01	20.080	964.40	20.087	037. 4 0 042.17	20.007	014.50 910.65	20.004	706.10
24.002	000.07	27.707	004.40	24.000	042.17	27.777	817.05	25.554	201.70
34.992	890.50	34.998	808.48	54.988	840.00	34.985	824.01	35.011	801.72
39.997	894.15	39.995	872.40	39.999	850.97	39.991	829.37	39.992	807.01
				m = 1.038	861 mol·kg ⁻¹				
T =	298.28 K	T = 2	323.23 K	T = 3	348.27 K	T =	373.29 K	T = 2	398.31 K
0.203	881.26	0.220	855.22	0.330	829 39	0.536	802 51	0 904	773 50
4.085	885.56	4 004	860.28	4 004	835.08	4 088	808.88	5.004	780.50
4.985	800.02	4.774	800.28	4.774	833.08	4.900	000.00	0.004	700.37
9.997	889.95	10.005	803.32	10.000	840.82	9.995	815.55	9.995	/88.48
14.987	894.12	14.999	870.09	14.987	846.22	15.009	821.76	14.985	/95./0
19.985	898.15	20.003	874.64	20.003	851.34	20.001	827.53	19.982	802.38
25.003	902.02	24.990	878.98	24.994	856.19	24.989	832.97	24.984	808.61
30.007	905.80	30.007	883.18	30.014	860.81	29.993	838.14	29.996	814.47
34.983	909.40	34,989	887.17	34,990	865.23	34.984	843.03	35.010	819.97
39 991	912 90	39 991	891.04	39 991	869.48	39,990	847 71	39 997	825.19
57.771	12.70	57.771	071.01	57.771	007.10	37.770	017.71	57.771	025.17
				m = 1.976	685 mol∙kg ^{−1}				
T =	298.27 K	T = 1	323.24 K	T=3	348.27 K	T =	373.29 K	T = 1	398.32 K
0.205	959.59	0.230	931.65	0.305	904.26	0.527	876.84	0.905	848.36
5.014	963.97	4.993	936.57	4.984	909.72	5.003	882.85	4.985	854.80
9 996	968 35	9 985	941 48	9 985	915.25	9 986	889.12	9 9 9 9	862 15
1/ 007	072 58	1/ 008	946.20	1/ 002	920.51	15,000	895.06	15 010	868.94
10.020	076.62	10,000	050.72	10.096	025.50	20.012	000.64	10.006	000.74
19.989	970.03	19.999	950.72	19.980	925.50	20.012	900.04	19.996	8/3.28
24.993	980.56	24.989	955.05	24.987	930.28	25.001	905.94	25.009	881.23
29.990	984.35	29.990	959.23	29.990	934.86	29.988	910.98	29.990	886.89
35.014	988.04	35.001	963.27	34.985	939.27	34.997	915.82	35.014	892.27
39.994	991.58	39.997	967.17	39.993	943.53	39.997	920.45	39.988	897.37
					750				
ar.	200 07 V	-	222 24 17	m - 5.50	/ 50 mol•kg		272 20 17	-	200 22 17
1 =	298.2/ K	I = 1	323.24 K	I = 3	948.27 K	1 =	313.29 K	I = I	098.32 K
0.200	1205.67	0.209	1172.87	0.335	1141.63	0.535	1112.11	0.899	1083.75
4.983	1209.53	4.999	1177.21	4.982	1146.29	4.986	1117.02	5.002	1088.78
9.992	1213.48	9.997	1181.61	9.992	1151.14	10.002	1122.33	9.988	1094.64
14.995	1217.30	15.002	1185.89	15.020	1155.81	14.990	1127.43	15.018	1100.25
19 988	1221.03	19 998	1190.03	20.001	1160.36	20,008	1132 37	20.003	1105.62
24 996	1221.03	24 080	119/106	25.001	1164 74	25.001	1137 12	24 080	1110 77
24.770	1224.00	27.707	1107.00	20.001	1160.01	20.001	11/1 70	27.707	1115 75
27.774	1220.21	24.007	119/.99	24,000	1109.01	27.994	1141./2	29.999	1113./3
34.996	1251.68	34.98/	1201.80	34.990	11/3.15	34.986	1146.1/	35.003	1120.56
39.994	1235.10	39.995	1205.55	39.984	11//.19	39.995	1150.53	59.994	1125.22

Using a program for standard thermodynamic analysis to describe the (p, ρ, T) properties of methanol solutions of ZnCl₂, the equation of state (eq 1) from ref 1 was used:

$$p = A\rho^2 + B\rho^8 + C\rho^{12} \tag{1}$$

The coefficients of eq 1 (A, B, and C) are functions of temperature and molalities m:

$$A = \sum_{i=1}^{4} T^{i} \sum_{j=0}^{6} a_{ij} m^{j}$$
(2)

$$B = \sum_{i=0}^{3} T^{i} \sum_{j=0}^{6} b_{ij} m^{j}$$
(3)

$$C = \sum_{i=0}^{3} T^{i} \sum_{j=0}^{6} c_{ij} m^{j}$$
(4)

The a_{ij} , b_{ij} , and c_{ij} are the coefficients of the polynomials, and they are given in Table 2. Equations 1 to 4 are described our experimental results with \pm 0.006 % average deviation. During the molality *m* dependence of experimental results, the (*p*, ρ , *T*) properties of methanol from ref 2 were used. The statistical,

Table 2. Values of the Coefficients a_{ij} , b_{ij} , and c_{ij} in Equations 1 to 4

a_{ij}	b_{ij}	C _{ij}
$a_{10} = -3.2320574273$	$b_{00} = -1477.925642552$	$c_{00} = -1380.64064$
$a_{11} = 31.1317287076$	$b_{01} = 286352.1656083$	$c_{01} = -494179.9917153526$
$a_{12} = -421.992228948$	$b_{02} = -2651482.16388571$	$c_{02} = 4679325.534965326$
$a_{13} = 1042.4065547565$	$b_{03} = 6135248.272333951$	$c_{03} = -10845143.9673409$
$a_{14} = -952.592801854$	$b_{04} = -5528630.590143065$	$c_{04} = 9756652.812321812$
$a_{15} = 339.898612167$	$b_{05} = 1969416.312510314$	$c_{05} = -3469682.188901562$
$a_{16} = -36.500223852878$	$b_{06} = -211560.332348847$	$c_{06} = 372375.69140993$
$a_{20} = 1.40111335262 \cdot 10^{-2}$	$b_{10} = 12.130167272$	$c_{10} = 19.552432301$
$a_{21} = -8.10758 \cdot 10^{-2}$	$b_{11} = -2765.71218910273$	$c_{11} = 4517.45214244155$
$a_{22} = 1.6862214$	$b_{12} = 26010.72725075362$	$c_{12} = -43212.4546402518$
$a_{23} = -4.35497186$	$b_{13} = -60377.39067149046$	$c_{13} = 100344.112888808$
$a_{24} = 4.009522573$	$b_{14} = 54444.49307483342$	$c_{14} = -90316.41207528222$
$a_{25} = -1.43034389078$	$b_{15} = -19395.45094714807$	$c_{15} = 32121.92666262618$
$a_{26} = 0.1534603705$	$b_{16} = 2083.45052993937$	$c_{16} = -3447.480837585364$
$a_{30} = -2.30426 \cdot 10^{-5}$	$b_{20} = -1.812152 \cdot 10^{-2}$	$c_{20} = -7.443132332 \cdot 10^{-2}$
$a_{31} = -2.0394195 \cdot 10^{-4}$	$b_{21} = 8.508135242$	$c_{21} = -13.361786362$
$a_{32} = -2.527559864 \cdot 10^{-4}$	$b_{22} = -80.96712412515407$	$c_{22} = 128.73553972$
$a_{33} = 1.602673 \cdot 10^{-3}$	$b_{23} = 188.3622675198797$	$c_{23} = -299.3369197708$
$a_{34} = -1.6178404 \cdot 10^{-3}$	$b_{24} = -169.9367631086781$	$c_{24} = 269.51208602198$
$a_{35} = 5.75543597306 \cdot 10^{-4}$	$b_{25} = 60.54255859374153$	$c_{25} = -95.8612056870612$
$a_{36} = -6.10858737 \cdot 10^{-5}$	$b_{26} = -6.503394322434008$	$c_{26} = 10.28840125167783$
$a_{40} = 1.6126218 \cdot 10^{-8}$	$b_{30} = 1.0961 \cdot 10^{-5}$	$c_{30} = 8.544351 \cdot 10^{-5}$
$a_{41} = 5.276624 \cdot 10^{-7}$	$b_{31} = -8.467978661416 \cdot 10^{-3}$	$c_{31} = 1.288067662334561 \cdot 10^{-2}$
$a_{42} = -3.289147786 \cdot 10^{-6}$	$b_{32} = 8.11769955405 \cdot 10^{-2}$	$c_{32} = -0.1246624482824$
$a_{43} = 6.867150914471 \cdot 10^{-6}$	$b_{33} = -0.1891254685$	$c_{33} = 0.2900941008840552$
$a_{44} = -6.078608884437 \cdot 10^{-6}$	$b_{34} = 0.17067851958934$	$c_{34} = -0.2612296506270426$
$a_{45} = 2.171218215735 \cdot 10^{-6}$	$b_{35} = -6.0808567190033 \cdot 10^{-2}$	$c_{35} = 9.291544596564023 \cdot 10^{-2}$
$a_{46} = -2.34086431973426 \cdot 10^{-7}$	$b_{36} = 6.531880767726 \cdot 10^{-3}$	$c_{36} = -9.972100295663517 \cdot 10^{-3}$

Table 3. Statistical, Absolute, and Average Deviations of Equations1 to 4

molality, <i>m</i> /(mol•kg ⁻¹)	standard deviation ^a	absolute deviation ^b	maximum absolute deviation	average percent deviation ^c
0.13476	0.002	0.008	0.03	0.0011
0.47677	0.033	0.180	0.60	0.0222
0.80178	0.001	0.007	0.02	0.0009
1.03861	0.003	0.015	0.06	0.0018
1.97685	0.002	0.008	0.03	0.0008
5.36750	0.006	0.036	0.09	0.0032

a-c The equations of deviations are available in ref 2.



Figure 2. Plot of experimental density ρ of methanol solutions of ZnCl₂ vs pressure p at T = 298.15 K: \Box , m = 0 (from ref 3); \blacklozenge , m = 0.13476 mol·kg⁻¹; \blacksquare , m = 0.47677 mol·kg⁻¹; \blacktriangle , m = 0.80178 mol·kg⁻¹; \diamondsuit , m = 1.03861 mol·kg⁻¹; \diamondsuit , m = 1.97685 mol·kg⁻¹; \bigtriangleup , m = 5.36750 mol·kg⁻¹; -, calculated by eqs 1 to 4.

absolute, and average deviations of fitting by eqs 1 to 4 are presented in Table 3. Figures 1 to 3 show the plot of pressure of the (ZnCl₂ + CH₃OH) versus density at m = 0.80178



Figure 3. Plot of deviations of experimental density ρ_{exp} from the calculated by eqs 1 to 4 density ρ_{cal} vs pressure $p: \triangle, m = 0.13476 \text{ mol·kg}^{-1}; \square, m$ = 0.47677 mol·kg⁻¹; $\bullet, m = 0.80178 \text{ mol·kg}^{-1}; \triangle, m = 1.03861 \text{ mol·kg}^{-1};$ $<math>\bullet, m = 1.97685 \text{ mol·kg}^{-1}; \blacksquare, m = 5.36750 \text{ mol·kg}^{-1}.$

mol·kg⁻¹, pressure versus density at T = 298.15 K, and deviations of experimental density from calculated density versus pressure.

The graphical analysis of the temperature dependence of the coefficients of eq 1 revealed that, at $T \rightarrow T_c$, $A \rightarrow 0$. Such a behavior of A = f(T) may be explained by the fact that, according to Putilov,⁵ the first term on the right-hand side of eq 1, $A\rho^2$, is the attractive force (attractor pressure), and the second and third terms are the repulsive force (repulsive pressure). As the temperature rises, the spacing between molecules increases, which contributes to a decrease in the attractive force. As the attractive force tends to zero $(A \rightarrow 0)$,

Table 4. Apparent Molar Volumes $V_{\phi}/(\mathrm{cm^{3}\text{-}mol^{-1}})$ of the ZnCl_2 in CH_3OH

	$m/(\mathrm{mol}\cdot\mathrm{kg}^{-1})$								
p/MPa	0.13476	0.47677	0.80178	1.03861	1.97685	5.36750			
		7	r = 298.15	К					
0.101	-11.171	10.806	19.137	22.167	25.530	30.493			
5	-8.834	13.870	20.230	23.401	26.376	31.074			
10	-6.588	16.336	21.201	24.502	27.143	31.603			
15	-4.673	18.149	22.060	25.465	27.812	32.074			
20	-2.959	19.426	22.816	26.296	28.402	32.493			
25	-1.317	20.283	23.479	27.062	28.927	32.874			
30	0.034	20.672	24.069	27.723	29.396	33.214			
35	1.330	20.668	24.592	28.313	29.814	33.520			
40	2.575	20.346	25.069	28.850	30.196	33.799			
		7	= 323.15	K					
0.101	-14.393	9.255	18.392	21.641	25.436	30.539			
5	-11.314	12.434	19.863	23.135	26.554	31.283			
10	-8.623	14,917	21.140	24.436	27.526	31,945			
15	-6.197	16.790	22.260	25.543	28.378	32.526			
20	-4.012	18,148	23.217	26.514	29.115	33.037			
25	-2.167	19.015	24.040	27.358	29.756	33.488			
30	-0.411	19.573	24.796	28.085	30.325	33.893			
35	1.270	19.773	25.455	28.745	30.834	34.254			
40	2.883	19.755	26.040	29.329	31.294	34.578			
		7	- 3/8 15	K					
0.37	-18728	7 /15	15 037	10 106	23 982	29 870			
5	-14.963	10.483	17 878	21.008	25.762	30.822			
10	-11700	13 141	19.617	22.818	26.802	31 704			
15	-8 517	15 258	21 154	22.010	20.002	32 /67			
20	-6.010	16.037	21.134	25 551	28.038	32.407			
25	-3.663	18 278	22.420	25.551	20.750	33 707			
30	-1552	10.270	24 504	27.604	30.540	34 217			
35	0.334	20 164	25 371	27.004	31 192	34 671			
40	2.251	20.839	26.15	29.212	31.784	35.074			
T = 272.15 V									
0.54	-27 403	4 320	-5/5.15	L 1/ 503	20.414	27 873			
5	-22 301	7.041	13 775	17 105	20.414	27.875			
10	-17525	0.540	16 317	10.603	24.460	29.191			
15	-13501	11 720	18/01	21.612	24.400	31 / 87			
20	-10.018	13 624	20.178	23 311	20.000	32 386			
25	-7.015	15.024	21 704	23.311	27.437	33 163			
30	-4 322	16 800	23.001	24.762	20.012	33 830			
35	-2.034	18 125	23.001	20.000	29.013	34 431			
33 40	0.132	10.123	24.131	27.100	31.264	34.451			
40	0.152	17.555	2000.15	20.170	51.204	54.755			
T = 398.15 K									
0.94	-40.270 -22.124	-3.442 -1.506	6 804	10.642	14.011	24.031			
10	-35.134	-1.500	10 661	14.211	20.002	23.002			
10	-20.008	2.301	10.001	14.511	20.002	21.134			
20	-15 626	0.027	15.745	17.243	22.303	29.238			
20	-13.020 -11.642	9.070	10.204	17.000	24.340	21 612			
20	-11.045	11./3/	20 150	21.733	23.990 77 277	31.012			
35	-0.212	14.173	20.159	25.460	21.311	32.333			
35 40	-3.213	10.330	21.077	25.004	20.374	33.337			
40	-2.312	10.300	23.020	20.347	29.010	34.038			

molecules under the effect of the repulsive force are capable of displacement. The extent of their displacement is defined only by the density of the substance (i.e., external pressure). As a result, the aggregate state changes. Note that the form of eq 1 was derived from Putilov's molecular kinetic theory.⁵

The apparent molar volumes V_{ϕ} of ZnCl₂ in methanol were defined⁶ by eq 5 and are listed in Table 4:

$$V_{\phi} = (\rho_{\rm m} - \rho_{\rm s})/(m\rho_{\rm s}\rho_{\rm m}) + M/\rho_{\rm s}$$
(5)

where ρ_m and ρ_s are densities of methanol and solutions, *m* is the molality of solution, and *M* is the molar mass of the dissolved ZnCl₂. The calculations were carried out using the density results of methanol and solution at the same temperatures and pressures.

The maximum relative uncertainty⁴ δV_{ϕ} in the V_{ϕ} determination by the investigated concentrations are as follows: δV_{ϕ}



Figure 4. Plot of V_{ϕ} of ZnCl₂ in methanol vs *m* at T = 323.15 K: $\blacklozenge, p = 0.1$ MPa; $\blacksquare, p = 5$ MPa; $\blacklozenge, p = 10$ MPa; $\diamondsuit, p = 15$ MPa; $\diamondsuit, p = 20$ MPa; $\Box, p = 25$ MPa; $\bigtriangleup, p = 30$ MPa; $\bigcirc, p = 35$ MPa; *, p = 40 MPa.



Figure 5. Plot of apparent molar volumes V_{ϕ} of ZnCl₂ in methanol vs temperature *T* at $m = 0.13476 \text{ mol}\cdot\text{kg}^{-1}$: \blacklozenge , p = (0.1, 0.34, 0.54, and 0.94) MPa; \blacksquare , p = 5 MPa; \blacktriangle , p = 10 MPa; \blacklozenge , p = 15 MPa; \diamondsuit , p = 20 MPa; \Box , p = 25 MPa; \bigtriangleup , p = 30 MPa; \bigcirc , p = 35 MPa; *, p = 40 MPa.

= (3.12, 1.01, 0.62, 0.49, 0.27, and 0.10) %, respectively. Figure 4 show the plot of the apparent molar volumes V_{ϕ} of ZnCl₂ in methanol versus *m* at *T* = 323.15 K and various pressures. Figure 5 shows the plot of the apparent molar volumes V_{ϕ} of ZnCl₂ in methanol versus *T* at *m* = 0.13476 mol·kg⁻¹ and various pressures.

Conclusion

For the first time, the (p, ρ, T) properties and apparent molar volumes V_{ϕ} of ZnCl₂ in methanol at T = (298.15 to 398.15) K and pressures up to p = 40 MPa are reported. An empirical correlation for the density of investigated solutions with composition, pressure, and temperature has been derived. The measured volumetric results are useful for the absorption refrigeration machines and heat pumps.

Literature Cited

(1) Safarov, J. T. The investigation of the (p, ρ, T) and (p_s, ρ_s, T_s) properties of $\{(1 - x)CH_3OH + xLiBr\}$ for the application in absorption refrigeration machines and heat pumps. *J. Chem. Thermodyn.* **2003**, *35*, 1929–1937.

- (2) Ihmels, E. C.; Safarov, J.; Hassel, E.; Gmehling, J. (p, ρ, T) properties, and apparent molar volumes V_{ϕ} of ZnBr₂ in methanol at T = (298.15) to 398.15) K and pressures up to p = 40 MPa. *J. Chem. Thermodyn.* **2005**, *37*, 1318–1326.
- (3) Ihmels, E. C.; Gmehling, J. Densities of toluene, carbon dioxide, carbonyl sulfide, and hydrogen sulfide over a wide temperature and pressure range in the sub- and supercritical state. *Ind. Eng. Chem. Res.* 2001, 40, 4470–4477.
- (4) Safarov, J. T.; Najafov, G. N.; Shahverdiyev, A. N.; Hassel, E. (p, ρ, T) and (p_s, ρ_s, T_s) properties, and apparent molar volumes V_{ϕ} of LiNO₃-(aq) in the 298.15–398.15 K temperature range and pressures to p = 60 MPa. *J. Mol. Liq.* **2005**, *116*, 157–163.
- (5) Putilov, K. A. Thermodynamics of simplest liquids. *Issledovaniya po Termodinamike* (Thermodynamic Studies); Nauka: Moscow, 1973; p 105.
- (6) Millero, F. J. The molal volumes of electrolytes. *Chem. Rev.* 1971, 71, 147–176.

Received for review December 3, 2005. Accepted January 26, 2006. J.T.S. thanks the Alexander von Humboldt Foundation of Germany for the support of his research work at the Rostock and Oldenburg Universities of Germany.

JE050509F