# Isochoric *PVTx* Measurements for the $N_2O + R125$ Binary System

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Isochoric *PVTx* measurements are reported for nitrous oxide (N<sub>2</sub>O, R744A) + pentafluoroethane (CHF<sub>2</sub>CF<sub>3</sub>, R125) for both the two-phase and the superheated vapor regions at temperatures ranging from (217 to 363) K and pressures from (160 to 1853) kPa along six isochores. The data obtained in the two-phase region were used to derive vapor-liquid equilibrium (VLE) parameters using a flash method with the Carnahan–Starling–De Santis equation of state (CSD EOS). The dew point was also found for each isochore from the intersection of the P-T sequences. The dew points were then used to derive VLE parameters from CSD EOS. Results from the superheated region were compared with those predicted from the virial EOS and from the CSD EOS.

## Introduction

In the search for fluids potentially suitable for low-temperature refrigeration applications (i.e., cascade cycles), we have turned our attention to systems consisting of R744A and R125. The cascade cycle is a very interesting application for the food industry, where evaporating temperatures between -30 °C and -40 °C are needed. Where lower temperatures are needed, carbon dioxide (R744) is no longer a feasible solution due to its triple-point temperature (216.58 K), which prevents its use in vapor compression cycles intended for use at lower temperatures. One of the chemicals potentially suitable for use in lowtemperature refrigeration applications is R744A, whose critical parameters and saturated pressures are very similar to those of carbon dioxide (R744). The main advantage of R744A over R744 lies in its very low melting temperature (182.34 K), whereas its global warming potential (GWP, which is 310) is low but not low enough to be considered environmentally friendly.

R125, a hydrofluorocarbon, is an important refrigerant used as a constituent in some binary or ternary mixtures. Its thermophysical properties have been extensively studied during the past decade. Nevertheless, published data on *PVTx* properties of systems containing R744 or R744A as one of the components and a fluorocarbon as the second component are rare. Thus, the combination of R744A and R125 provides important data for future applications. In addition, to our knowledge no experimental results have been published in the open literature on the *PVTx* properties of this specific binary system. The study presented in this paper aims to partially fill this gap.

Isochoric measurements were consequently taken, covering temperatures from (217 to 363) K, to make up for the lack of vapor—liquid equilibrium (VLE) and *PVTx* data. VLE parameters were derived from data in the two-phase region, applying the Carnahan—Starling—De Santis equation of state (CSD EOS),<sup>1</sup> while data obtained from the superheated region were compared with the predictions obtained with the virial EOS and the CSD EOS.

#### **Experimental Section**

*Chemicals.* Nitrous oxide and pentafluoroethane were supplied by Sol SpA. Their purity was checked by gas chromatography, using a thermal conductivity detector, and found to be 99.99 % and 99.96 %, respectively, basing all estimations on an area response.

Apparatus. The setup has already been described elsewhere,<sup>2</sup> so it is only briefly outlined here. The main changes made to the original apparatus<sup>3,4</sup> concerned the twin thermostatic baths (7) filled with different silicone oils (Baysilone M10 and Baysilone M100, Bayer). After charging with the sample mixture, the setup could be operated over two temperature ranges, approximately from (210 to 290) K and from (290 to 360) K, depending on which bath was used. The two silicone oils have different kinematic viscosity values (10<sup>-5</sup> and 10<sup>-4</sup>  $m^{2} \cdot s^{-1}$  at room temperature, respectively). The one with lower kinematic viscosity but of higher volatility and lower thermal stability was applied only for the low-temperature range, while that with a greater viscosity was applied only at the higher temperatures. The thermostatic baths were easy to move thanks to the new system configuration. The spherical cells and pressure transducer are immersed in one of the two thermostatic baths (7). An auxiliary thermostat (14) was used to reach belowambient temperatures. The cell volume was estimated (as explained elsewhere<sup>4</sup>) to be (273.5  $\pm$  0.3) cm<sup>3</sup> at room temperature.

The pressure and temperature data acquisition systems were identical to those of the previous apparatus.<sup>3,4</sup> A PID device was used to control the temperature, which was measured using a calibrated resistance thermometer; the total uncertainty of the temperature measurements was  $\pm$  0.02 K. The uncertainty in the pressure measurements stems from the uncertainty of the transducer and null indicator system and the pressure gauges. The uncertainty of the digital pressure indicator (Ruska, model 7000) is  $\pm$  0.003 % of its full scale (6000 kPa). Temperature fluctuations due to bath instability can also affect the total uncertainty in the pressure measurement, which was nonetheless found to be less than  $\pm$  1 kPa.

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Table 1. Measurements at Bulk Compositions  $z_1$  and Masses  $m_1$  and  $m_2$  for the R744A (1) + R125 (2) System over the Temperature Range,  $\Delta T$ , and Pressure Range,  $\Delta P$ , with Resultant Dew Temperatures,  $T_d$ , and Dew Pressures,  $P_d$ 

	$\Delta T$	$\Delta P$	Ν	$m_1$	$m_2$	$T_{\rm d}$	$P_{\rm d}$
$z_1$	K	kPa	mol	g	g	Κ	kPa
0.082	228-363	160-1853	0.1973	0.789	21.745	293.9	1327
0.147	238-363	250-1125	0.1116	0.721	11.428	273.8	779
0.280	217-363	161-1323	0.1323	1.633	11.428	274.6	915
0.475	218-363	223-1056	0.1028	2.148	6.479	259.2	699
0.649	218-363	310-1361	0.1331	3.800	5.608	258.2	893
0.793	218-363	403-1728	0.1696	5.916	4.225	255.8	1118

Table 2. Experimental Molar Volumes V as a Function of Pressure P and Temperature T at Composition  $z_1$  within the VLE Boundary for the R744A (1) + R125 (2) System

Т	Р	V	Т	Р	V	
K	kPa	$dm^3 \cdot mol^{-1}$	K	kPa	$dm^3 \cdot mol^{-1}$	
$z_1 = 0.082$			258.02	588	2.065	
228.06	160	1.383	263.07	676	2.065	
233.02	194	1.383	268.13	775	2.065	
237.90	234	1.383	273.13	882	2.066	
242.94	282	1.384		$z_1 = 0.475$		
247.92	336	1.384	218.52	223	2.653	
252.94	399	1.384	223.13	259	2.654	
257.98	471	1.385	228.10	302	2.654	
263.03	552	1.385	233.08	349	2.655	
268.11	646	1.385	238.04	401	2.655	
273.10	749	1.386	242.99	460	2.656	
278.03	864	1.386	247.97	528	2.656	
283.01	993	1.386	253.15	602	2.657	
288.00	1137	1.387	258.03	679	2.658	
$z_1 = 0.147$			$z_1 = 0.649$			
238.09	250	2.446	218.27	310	2.049	
243.08	298	2.446	223.12	363	2.050	
248.09	354	2.447	228.10	422	2.050	
253.08	416	2.447	233.07	485	2.051	
258.10	488	2.448	238.02	554	2.051	
263.12	569	2.448	243.00	631	2.052	
268.16	663	2.449	247.99	711	2.052	
273.11	734	2.449	253.01	797	2.052	
$z_1 = 0.280$			$z_1 = 0.793$			
217.76	161	2.061	218.27	403	1.608	
223.13	196	2.061	223.13	473	1.608	
228.10	233	2.062	228.11	556	1.608	
233.07	276	2.062	233.08	644	1.609	
238.03	324	2.063	238.03	736	1.609	
242.99	379	2.063	243.02	835	1.609	
247.97	440	2.064	248.00	942	1.610	
252.99	509	2.064	253.03	1049	1.610	

**Experimental Procedure.** Mixtures were prepared using the gravimetric method. First of all, the pure samples were charged in different bottles, degassed to remove non-condensable gases and air, and then weighed with an analytical balance (uncertainty  $\pm$  0.3 mg). After evacuating the cell, the bottles were then emptied into the cell immersed in the bath. Then the bottles were weighed again, and the mass of the charge was calculated from the difference between the two masses. The dispersion of the mass inside the duct was estimated to be between (0.01 and 0.06) g, depending on the charging temperature, pressure, and molar mass of the sample. The uncertainty in mixture preparation was estimated to be constantly lower than 0.001 in mole fraction.

After reaching the experimental temperature, the mixing pump was activated for about 15 min. Next, the mixture was allowed to stabilize for about 20 min before the data recording.

#### **Results and Discussion**

The temperature and pressure ranges are shown in Table 1, along with the mixture's composition and the number of moles

Table 3. Experimental Molar Volumes V as a Function of Pressure P and Temperature T at Composition  $z_1$  in the Superheated Vapor Region for the R744A (1) + R125 (2) System

0		. ,			
Т	Р	V	Т	Р	V
K	kPa	$dm^3 \cdot mol^{-1}$	K	kPa	$dm^3 \cdot mol^{-1}$
	$z_1 = 0.0$	82	317.99	1120	2.070
293.08	1298	1.387	322.99	1144	2.070
298.07	1360	1 387	328.11	1167	2.071
202.05	1401	1.307	222.10	1107	2.071
200.03	1401	1.307	228.00	1212	2.071
308.04	1440	1.388	338.09	1212	2.072
313.03	1480	1.388	343.08	1235	2.072
318.02	1518	1.388	348.07	1257	2.073
323.00	1557	1.389	353.05	1279	2.073
328.11	1595	1.389	358.03	1301	2.074
333.10	1632	1 389	363.02	1323	2 074
338.00	1670	1 300	505.02	74 = 0.4	75
242.09	1707	1.300	262.07	702	2659
249.00	1707	1.390	203.07	703	2.038
348.06	1/44	1.390	268.12	121	2.659
353.05	1780	1.391	273.11	752	2.659
358.03	1818	1.391	278.02	769	2.660
363.02	1853	1.391	283.00	787	2.661
	$z_1 = 0.1$	47	288.00	804	2.661
278.03	793	2,450	293.08	821	2.662
283.02	818	2.450	298.07	839	2.662
205.02	010	2.451	202.05	057	2.002
200.01	855	2.451	303.03	830	2.005
293.09	856	2.451	308.04	8/3	2.663
298.07	876	2.452	313.02	890	2.664
303.05	896	2.452	318.01	907	2.665
308.04	915	2.453	322.99	924	2.665
313.02	935	2.454	328.11	941	2.666
318.01	954	2 454	333.10	958	2.666
323.00	073	2.454	338.00	074	2.667
323.00	973	2.455	336.09	974	2.007
327.99	993	2.455	343.08	991	2.008
333.10	1012	2.456	348.07	1007	2.668
338.09	1031	2.456	353.03	1023	2.669
343.08	1050	2.457	358.02	1040	2.669
348.07	1069	2.457	363.01	1056	2.670
353.04	1088	2.458		$z_1 = 0.6$	49
358.02	1106	2 458	258.04	876	2 053
363.02	1125	2.150	263.09	907	2.053
505.02	0.2	2.433	203.08	907	2.055
	$z_1 = 0.2$	80	208.13	930	2.054
278.02	919	2.066	273.12	965	2.054
283.01	955	2.067	278.05	987	2.055
288.00	979	2.067	283.01	1010	2.055
293.08	1004	2.068	287.98	1032	2.056
298.07	1028	2.068	293.08	1056	2.056
303.06	1051	2.069	298.07	1079	2.057
308.04	1075	2.069	303.06	1101	2.057
212.02	1075	2.00)	208.04	1101	2.057
313.02	1098	2.070	308.04	1125	2.037
313.03	1145	2.058	283.01	1278	1.612
318.01	1167	2.058	287.99	1307	1.613
322.99	1188	2.059	293.08	1337	1.613
328.11	1211	2.059	298.07	1365	1.613
333.11	1232	2.060	303.04	1394	1.614
338.09	1254	2.060	308.02	1422	1 614
242.09	1275	2.060	212.01	1450	1.614
249.00	1273	2.001	217.00	1430	1.014
348.06	1297	2.061	317.99	14/8	1.615
353.04	1318	2.062	322.98	1506	1.615
358.03	1340	2.062	328.10	1535	1.615
363.02	1361	2.062	333.09	1563	1.616
	$z_1 = 0.7$	93	338.08	1590	1.616
258.05	1118	1.610	343.07	1618	1.616
263 11	1160	1 611	348.05	1646	1 617
269.11	1100	1.611	352 04	1672	1.617
200.14	1220	1.011	259.04	10/3	1.01/
2/3.13	1220	1.012	358.01	1700	1.018
77×05	1250	1.612	363 ()]	1728	1618

charged. On the basis of the analysis of the slope of each T-P sequence, the experimental points were each attributed either to the superheated or to the two-phase region. Table 2 shows the experimental data within the VLE boundary, while Table 3 contains the *PVTx* data. The number of data belonging to each region is also included in Table 1. The data for the two-phase region were fitted using the Antoine equation, while those relating to the superheated region were fitted by a second-degree polynomial, taking temperature as the independent variable.



**Figure 1.** Experimental *P*-*T* data and calculated dew points ( $\blacktriangle$ ).  $\bigcirc$ ,  $z_1 = 0.0816$ ;  $\bigtriangledown$ ,  $z_1 = 0.4748$ ;  $\square$ ,  $z_1 = 0.1469$ ;  $\diamondsuit$ ,  $z_1 = 0.6489$ ;  $\triangle$ ,  $z_1 = 0.2804$ ;  $\bigcirc$ ,  $z_1 = 0.7925$ .

Then the solution of the two equations representing the system's behavior in the two-phase and superheated regions was used to find the dew point temperature and pressure algebraically for each isochore. The uncertainty of temperature and pressure of the dew points arising from the error distribution of the data correlated with the Antoine and polynomial equations were estimated to be of the order of  $\pm$  0.3 K and  $\pm$  2 kPa, respectively. An example of the dew point estimation method based on the slope discontinuity is reported in Figure 1. The solutions are given in Table 1.

*VLE Derivation.* The method used to derive VLE data from the isochoric measurements using the CSD EOS was described elsewhere.<sup>5</sup> This EOS was chosen among two-parameter EOSs because its parameters are fitted to pressures and molar volumes along saturation. For this reason. it is able to accurately represent saturation pressures, volumetric properties along saturation, and vapor phase at superheated region.

One method involves deriving the VLE parameters by means of the "dew point" method with the CSD EOS. The method involves deriving the VLE parameters for each data point in the two-phase region using the "flash method" with the CSD EOS. For this method to be applied to isochoric data, we also need the volumetric properties of both phases, which were calculated from the CSD EOS. T,  $z_i$ , and n (number of moles charged) were kept constant during the correlation having the isochoric cell volume from the gravimetric calibration, the objective function

$$Q = \sum_{i} \left(\frac{\mathrm{d}P}{P}\right)^2$$

was minimized tuning the  $K_{12}$  value. The correlation gives also the parameters of VLE (pressure and composition of both phases) at the bubble and dew point (not reported in tables), which were considered, obviously, as dependent variables. Figure 2 shows the scatter diagram of the relative pressure deviations, which are almost temperature-independent. The pressure deviations amounted to around  $\pm 1$  % for all series except for series 1 where higher deviations (up to 4 %) were evident. This might be caused by incidental greater (but systematic) uncertainty in temperature.

The average of the obtained binary interaction parameters values is  $K_{12} = -0.027$  with a statistical uncertainty of  $\pm 0.007$ . Using the averaged  $K_{12}$  value from our measurements in the two-phase region data, we calculated the VLE at three different



**Figure 2.** Pressure deviations between experimental values and those calculated with the  $K_{12}$  coefficients for the N<sub>2</sub>O (1) + R125 (2) system. Symbols denoted as in Figure 1.



**Figure 3.** VLE representation from the CSD EOS for the N<sub>2</sub>O (1) + R125 (2) system at three temperatures: T = 233.15 K (solid lines), T = 253.15 K (dotted lines), and T = 273.15 K (dash-dotted lines).

temperatures (T = 233.15 K, T = 253.15 K, and T = 273.15 K). The results are given in Figure 3. The R744A + R125 system reveals almost ideal behavior in terms of Raoult's law.

**PVTx.** Since there are no published data on the superheated vapor region for the binary systems considered, we compared our experimental *PVTx* findings with data calculated using the virial EOS in the Leiden form. A temperature dependence of the third-degree polynomial was found for the second and third virial coefficients. Then the pressure values were calculated from the virial EOS in the Leiden form, using the isochoric experimental temperatures and molar volumes. The second and third virial coefficients for the two pure fluids ( $B_{ii}$ ,  $B_{jj}$ ,  $C_{iii}$ , and  $C_{jjj}$ ) were drawn from our previous Burnett experiments for R744A<sup>6</sup> and for R125.<sup>7</sup> The following expressions were adopted for the cross virial coefficients ( $B_{ij}$ ,  $C_{iij}$ , and  $C_{ijj}$ ) because the binary system revealed an almost ideal behavior of VLE at lower temperatures:

$$B_{ij} = (B_{ii} + B_{jj})/2$$
 (2)

$$C_{iij} = (2C_{iii} + C_{jjj})/3$$
(3)

$$C_{ijj} = (C_{iii} + 2C_{jjj})/3$$
(4)

The results are given in Figure 4, showing the relative pressure deviations in the superheated region. The first point



Figure 4. Relative pressure deviations for the  $N_2O(1) + R125(2)$  system between experimental values from isochoric and data calculated with the virial EOS. Symbols denoted as in Figure 1.



Figure 5. Relative molar volume deviations for the  $N_2O(1) + R125(2)$  system between experimental values from isochoric and data calculated with the CSD EOS. Symbols denoted as in Figure 1.

measured after the change of phase produced always much higher deviations and was not considered in the elaboration. The deviations for all series were within  $\pm 1$  %. It is worth nothing that the higher deviation that appeared in the two-phase region for series 1 was not evident in the superheated vapor region, confirming the validity of the measurements. Density at superheated region were also compared with the CSD EOS prediction. In this case, the coefficients of the CSD EOS fitted to data along saturation were extrapolated out of range. Also, the  $K_{12}$  value, tuned to the low-temperature two-phase data, was assumed to be temperature-independent. Deviations between experiments and CSD EOS are presented in Figure 5. Overall deviations in pressures from the CSD EOS prediction showed an AAD = 1.3 %. Deviations in Figure 5 showed a systematic shift of about -1 % if compared with Figure 4, being the deviations scattered between 0 and -2 %, again not considering the first point measured after the change of phase. Again, the higher deviation that appeared in the two-phase region for series 1 was not evident in the superheated vapor region. Both these models, which are based on different theoretical approaches, showed a similar trend of deviations in terms of temperature.

### Conclusions

An isochoric apparatus has been used to obtain PVTx measurements on N<sub>2</sub>O + R125. The binary interaction parameters were derived from experimental data in the two-phase region, applying the flash method and the CSD EOS. The dew point parameters were found by interpolating the P-T isochoric sequences. The calculated binary interaction parameters were used to derive the VLE, which revealed an almost ideal behavior in terms of Raoult's law. The PVTx data were predicted by the virial EOS and the CSD EOS, using its coefficients for the system constituents derived from independent measurements. In general, the PVTx are slightly better represented by the virial EOS.

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