

Position Group Contribution Method for the Prediction of Critical Volume of Organic Compounds

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In this study, a combined approach of group contribution and position distribution function is presented to estimate the critical volume of a variety of pure organic compounds involving a carbon chain from C2 to C18. The results indicate that our model provides very satisfactory results, and the deviation from the most reliable experimental data is not more than 2.1 %. The overall average absolute difference for critical volume V_c predictions of 219 organic compounds is $8.8 \text{ cm}^3 \cdot \text{mol}^{-1}$ and 2.1 % means relative derivation, which is compared to $26.5 \text{ cm}^3 \cdot \text{mol}^{-1}$ and 6.0 % with the method of Joback and $23.5 \text{ cm}^3 \cdot \text{mol}^{-1}$ and 5.6 % with the method of Constantinou and Gani. The higher prediction accuracy of the proposed method shown in our previous works and this work suggests that it is possible to use a similar framework to predict the three critical properties, T_c , P_c , and V_c of organic compounds containing various functionalities.

Introduction

Critical properties are important to predict various thermodynamic properties using the principle of corresponding states. Unfortunately, experimental critical properties data of organic compounds are limited due to the fact that many compounds become unstable during measurements near or even far from the vicinity of the critical point. In such conditions, mathematical models can be used to provide a reasonable estimate of these properties. The method used in estimating critical property data in various applications including chemical process design is the group contribution method. Jensen et al.,¹ Joback and Reid,² Somayajulu,³ and Li et al.⁴ proposed such methods for the prediction of a variety of thermodynamic properties (e.g., vapor pressure, critical temperature, critical pressure, boiling point) of organic compounds.

However, most group contribution methods have a serious problem that they cannot distinguish among structural isomers. To overcome this problem, many researchers have tried to improve group contribution methods. Constantinou and Gani,⁵ Marrero and Gani,⁶ and Olsen and Nielsen⁷ developed methods which perform estimations at different levels. Recently, Nannoolal et al.⁸ developed some new equations for the prediction of critical parameters, and our laboratory proposed a position group contribution method for the prediction of critical parameters of organic compounds that requires only the knowledge of their chemical structure.^{9,10}

As our preliminary work on the critical temperature and the critical pressure showed significant improvements with respect to the published methods, it was decided to also invest further effort into the development of a new group contribution method for critical volume.

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Method Proposed in This Work

Experimental Data. A total of 219 compounds were used for the determination of group contributions, which include linear and branched alkanes (48) and cycloalkanes (11), alkenes (11), aromatics (9), ketones (41), aldehydes (8), alcohols and ether oxides (36), acids (9), esters (20), amines and pyridines (17), and nitriles and alkane thiols (9).

The sources of experimental data were from a series of critical compilation reviews by the critical properties group of the IUPAC I: two on thermodynamics, and the works were published in *J. Chem. Eng. Data* by Ambrose,^{11,12} Tsonopoulos,^{13,16,18} Gude,¹⁴ Daubert,¹⁵ Kudchadker,¹⁷ and Marsh et al.^{19,20} Critical data were also obtained from a compilation of organic property data by Ma.²¹

Position Group Contributions for the Critical Volume. The critical volume function is constructed by all groups' contribution as well as by the position correlation factor. The position correlation factor was used to take into account longer distance interactions, which could distinguish most isomers including *cis*- and *trans*- or *Z*- and *E*-structures of organic compounds for their thermodynamics properties.

Here, the position distribution function for the estimation of critical volume is expressed as

$$V_C/\text{cm}^3 \cdot \text{mol}^{-1} = V_0 + \sum_i A_i N_i + \sum_j A_j \tanh(N_j/N) + \sum_k A_k P_k + a_1 \exp(1/M) + a_2 \exp(1/N) \quad (1)$$

$$N = \sum_i N_i + \sum_j N_j \quad (2)$$

Parameter A_i or A_j stands for i or j group contributions, N_i for the number of each group that the carbon element forms the center of the group in the molecular formula, N_j for the number of each group that the noncarbon element forms the center, N for the total number of groups, P_k for the position correlation factor, and a_1 , a_2 for parameters of the model. The set of

Table 1. Position Group Contributions for the Prediction of V_c^a

group	A $\text{cm}^3 \cdot \text{mol}^{-1}$	group	A $\text{cm}^3 \cdot \text{mol}^{-1}$
C—(CH ₃)(H)3	28.836	C—(C)(Cl)(H)2	68.973
C—(CH ₂)(H)3	32.124	C—(C)2(Cl)(H)	78.093
C—(CH)(H)3	44.253	C—(C)(Cl)2(H)	68.266
C—(C)(H)3	39.010	C—(S)(H)3	41.775
C—(C)2(H)2	64.715	C—(C)(S)(H)2	62.527
C—(C)3(H)	78.892	C—(C)2(S)(H)	81.299
C—(C)4	102.700	C—(C)3(S)	105.706
Cd—(H)2	118.285	Cb—(N)	-378.326
Cd—(C)(H)	66.042	C—(N)(H)3	12.0841
C—(Cd)(C)(H)2	115.088	C—(C)(N)(H)2	71.040
C—(Cd)(H)3	79.600	C—(C)2(N)(H)	85.499
Cd—(C)2	-22.636	C—(C)3(N)	127.735
C—(Cd)(C)2(H)	137.840	C—(C)(CN)(H)2	141.376
Cd—(Cd)(H)	259.960	N—(CH ₃)(H)2	56.628
C—(O)(H)3	24.628	N—(CH ₂)(H)2	54.114
C—(CO)(H)3	63.932	N—(CH)(H)2	46.908
C—(C)(CO)(H)2	100.338	N—(cyclopentyl)(H)2	-14.360
C—(C)2(CO)(H)	126.274	N—(cyclohexyl)(H)2	-34.516
C—(C)3(CO)	182.117	N—(C)2(H)	367.7
C—(C)(O)(H)2	46.625	N—(C)3	1243.887
C—(C)2(O)(H)	60.101	N—(Cb)(H)2	2807.391
C—(C)3(O)	82.642	N—(C)2 correction	-27.248
CO—(CH ₃)(O)	112.500	N—(C)3 correction	-138.294
CO—(CH ₂)(O)	170.243	NI—(Cb)2	-187.90
CO—(CH)(O)	209.270	S—(C)(H)	207.134
CO—(O)(H)	68.875	Cl—(C)	164.290
CO—(C)(H)	15.324	ortho correction ^b	-2.268
CO—(C)2	-15.991	meta correction ^b	11.567
CO—(O)(Cd)	897.969	cyclopentane correction	-104.566
Cb—(H)	30.627	cyclohexane correction	-92.337
Cb—(C)	15.102	C_{ob}^c	6.466
C—(Cb)(H)3	51.359	C_{mb}^c	6.466
C—(Cb)(C)(H)2	52.579	C_{pb}^c	6.163
C—(Cb)(C)2(H)	93.578	cyclopropane correction ^d	90.607
C—(Cb)(C)3	112.641	—(CH) ₂ position correction ^d	-5.060
Cb—(O)	2803.033	>(C) ₂ position correction ^d	-8.151
O—(Cb)(H)	-3476.48	double bond position correction ^d	-2.441
O—(C)(H)	72.835	hydroxyl position correction ^d	4.369
O—(C)2	372.475	benzene correction ^d	210.031
O—(CO)(CH ₃)	221.203	trans or cis structure correction ^d	-2.068
O—(CO)(CH ₂)	409.728	carbonyl position correction ^d	1.684
O—(CO)(CH)	405.810	phenol position correction ^d	28.993
C—(C)(Br)(H)2	118.396	a_2	46.240
C—(C)2(Br)(H)	161.123	a_1	989.257
V_0	-1011.117		

^a Notice: The first symbol represents the element that forms the center of the group. The symbols between parentheses represent the elements to which it is linked. Usual symbols are used to represent the elements in their normal valence state. Elements in other valence states are distinguished by using additional characters; furthermore, different symbols represent multiple bonded carbons, depending on the element at the other end of the multiple bond: Cd, carbon forming a double bond with another carbon; Cb, carbon involved in a benzene or a pyridine ring; CO, C=O group; CN, C≡N group; Ni, nitrogen of the imide (C=N-) function. Also used for the nitrogen of pyridine derivatives. The pyridine ring is considered as formed of five Cb and one Ni. trans or cis correction: cis-structure correction is 1 and trans structure is -1.

^b Ortho and meta corrections consider interactions between alkyl chains through a benzene ring. ^c Corrections for pyridines: C_{ob} , C_{mb} , and C_{pb} pyridine corrections take into account alkyl ligands in position ortho, meta, and para with respect to the N element, respectively. ^d Position correction.

contributions that allowed us to minimize the residual estimation difference was then computed by regression. V_0 is -1011.117 $\text{cm}^3 \cdot \text{mol}^{-1}$, and M is molecular weight. According to the IUPAC nominating method, we draw the structures and assign the P_k values for the relevant positional correction. Table 1 reports the values computed for the group contributions A_i , and our method developed is applicable only to comparatively low-molar-mass compounds involving the carbon chain from C2 to C18.

Table 2. Comparison of V_c Predicted with Our Method and with the Methods of Joback and Constantinou for Various Class Organic Compounds^a

chemical family	no. of compounds	Joback		Constantinou		this work	
		AAD $\text{cm}^3 \cdot \text{mol}^{-1}$	$100\bar{\delta}$ $\text{cm}^3 \cdot \text{mol}^{-1}$	AAD $\text{cm}^3 \cdot \text{mol}^{-1}$	$100\bar{\delta}$ $\text{cm}^3 \cdot \text{mol}^{-1}$	AAD $\text{cm}^3 \cdot \text{mol}^{-1}$	$100\bar{\delta}$ $\text{cm}^3 \cdot \text{mol}^{-1}$
alkanes	48	21.4	3.2	21.3	3.2	11.0	2.1
cycloalkanes	11	4.2	1.2	18.5	5.9	11.6	4.5
alkenes	11	4.0	1.2	5.7	2.0	3.2	1.1
aromatics	9	4.9	1.3	3.8	1.0	12.2	3.2
ketones	41	29.9	4.1	36.3	5.5	5.3	1.0
aldehydes	8	14.4	4.2	10.2	3.1	8.5	1.9
alcohols & ether oxides	36	57.5	13.8	13.3	3.1	6.8	1.6
acids	9	12.4	2.8	9.0	2.1	14.1	4.0
esters	20	22.4	6.2	22.9	6.5	11.7	3.4
amines and pyridines	17	18.7	6.2	17.7	6.0	3.3	1.2
nitriles & alkane thiols	9	26.8	8.4	23.7	7.1	11.3	3.5
overall	219	26.5	6.0	23.5	5.6	8.8	2.1

^a AAD is the overall average absolute difference and $\bar{\delta}$ is the average mean difference.

Results and Discussion

Prediction of Critical Volume. The results of the reference compounds obtained using the new position group contribution method were presented in detail in Table 3. To illustrate the application of the proposed method, a detailed procedure for the estimation of critical properties is given in Appendix A for the critical volume. Table 2 compares the critical volume predictions obtained using our method and previous methods to experimental data. Also, the overall average absolute difference (AAD) between experimental and predicted values for each group of molecules as well as the overall mean differences $\bar{\delta}$ and the average mean differences $\bar{\delta}$ are summarized in Table 2.

$$\text{AAD} = \frac{\sum |V_{c,\text{exp}} - V_{c,\text{pred}}|}{n} \quad (3)$$

$$\delta = \left| \frac{V_{c,\text{exp}} - V_{c,\text{pred}}}{V_{c,\text{exp}}} \right| \quad (4)$$

$$\bar{\delta} = \frac{1}{N} \sum_n \left| \frac{V_{c,\text{exp}} - V_{c,\text{pred}}}{V_{c,\text{exp}}} \right| \quad (5)$$

The performance of the new model has been compared with two well-known estimation methods from the literature, and the results indicate that the new model is significantly more reliable. Results presented in Table 2 show that the proposed method is more accurate than other methods for the critical volume. The AAD for critical volume V_c predictions of 219 organic compounds is $8.8 \text{ cm}^3 \cdot \text{mol}^{-1}$ and $\bar{\delta}$ is 2.1 %, which is compared to $26.5 \text{ cm}^3 \cdot \text{mol}^{-1}$ and 6.0 % with the method of Joback and $23.5 \text{ cm}^3 \cdot \text{mol}^{-1}$ and 5.6 % with the method of Constantinou and Gami. Results presented in Tables 3 prove that the predicted critical volume agrees well with the experimental results.

Uncertainty of the New Model. According to the F distribution function, the degree of confidence is calculated with the incomplete beta function which could be calculated from the gamma function. The results show that the correlation coefficient is 0.9946, the value of F distribution is 274.51, and the degree of confidence is 0.9990, which confirms the greater precision of our position group contribution method which can be used for the best estimation of the critical volume of organic compounds.

Table 3. Fully Predictive Estimations of Critical Volume V_c^a

comps	$V_c(\text{exp})$			this work			comps	$V_c(\text{exp})$			this work		
	$\text{cm}^3 \cdot \text{mol}^{-1}$	ref	predict	D	100δ			$\text{cm}^3 \cdot \text{mol}^{-1}$	ref	predict	D	100δ	
ethane	145.5	12	146	0.0	0.0	3-methyloctane					533		
propane	200	12	194	5.7	2.8	4-methyloctane					528		
n-butane	255	12	248	6.6	2.6	2-ethylheptane					538		
2-methylpropane	259	15	256	2.8	1.1	3-ethylheptane					521		
n-pentane	311	12	307	4.2	1.3	4-ethylheptane					516		
2-methylbutane	306	15	303	3.5	1.1	2,2-dimethylheptane					532		
2,2-dimethylpropane	307	15	291	16.1	5.3	2,3-dimethylheptane					529		
n-hexane	368	12	367	0.6	0.2	2,4-dimethylheptane					524		
2-methylpentane	368	15	363	4.9	1.3	2,5-dimethylheptane					519		
3-methylpentane	368	15	346	22.0	6.0	2,6-dimethylheptane					526		
2,2-dimethylbutane	358	15	345	13.4	3.7	3,3-dimethylheptane					517		
2,3-dimethylbutane	361	15	354	7.2	2.0	3,4-dimethylheptane					507		
n-heptane	428	12	429	1.2	0.3	3,5-dimethylheptane					502		
2-methylhexane	421	15	425	3.9	0.9	4,4-dimethylheptane					509		
3-methylhexane	404	15	408	3.8	0.9	3-ethyl-2-methylhexane					517		
3-ethylpentane	416	15	396	20.4	4.9	3-ethyl-3-methylhexane					510		
2,2-dimethylpentane	416	15	406	9.6	2.3	3-ethyl-4-methylhexane					495		
2,3-dimethylpentane	393	15	403	10.5	2.7	4-ethyl-2-methylhexane					512		
2,4-dimethylpentane	418	15	411	7.4	1.8	2,2,3-trimethylhexane					511		
3,3-dimethylpentane	414	15	391	22.7	5.5	2,2,4-trimethylhexane					505		
2,2,3-trimethylbutane	398	15	397	1.0	0.2	2,2,5-trimethylhexane					513		
n-octane	492	12	492	0.2	0.0	2,3,3-trimethylhexane					513		
2-methylheptane	488	15	487	0.5	0.1	2,3,4-trimethylhexane					503		
3-methylheptane	464	15	470	6.3	1.4	2,3,5-trimethylhexane					510		
4-methylheptane	476	15	465	10.8	2.3	2,4,4-trimethylhexane					505		
3-ethylhexane	455	15	458	3.2	0.7	3,3,4-trimethylhexane					490		
2,2-dimethylhexane	478	15	469	9.1	1.9	3,3-diethylpentane					552		
2,3-dimethylhexane	468	15	466	2.0	0.4	3-ethyl-2,2-dimethylpentane					498		
2,4-dimethylhexane	472	15	461	11.0	2.3	3-ethyl-2,3-dimethylpentane					506		
2,5-dimethylhexane	482	15	468	14.0	2.9	3-ethyl-2,4-dimethylpentane					503		
3,3-dimethylhexane	443	15	454	10.9	2.5	2,2,3,3-tetramethylpentane					494		
3,4-dimethylhexane	466	15	444	22.2	4.8	2,2,3,4-tetramethylpentane					496		
2-methyl-3-ethylpentane	442	15	454	11.9	2.7	2,2,4,4-tetramethylpentane					493		
3-methyl-3-ethylpentane	455	15	447	8.0	1.8	2,3,3,4-tetramethylpentane					498		
2,2,3-trimethylpentane	436	15	447	11.5	2.6	<i>n</i> -decane			624	12	618	5.8	0.9
2,2,4-trimethylpentane	468	15	455	13.5	2.9	2-methylnonane					614		
2,3,3-trimethylpentane	455	15	450	5.4	1.2	3-methylnonane					597		
2,3,4-trimethylpentane	460	15	452	8.4	1.8	4-methylnonane					592		
n-nonane	555	12	555	0.2	0.0	5-methylnonane					587		
2-methyloctane			551			3-ethyloctane					585		
4-ethyloctane			580			3-ethyl-2,2-dimethylhexane					577		
2,2-dimethyloctane			607			3-ethyl-2,3-dimethylhexane					557		
2,3-dimethyloctane			592			3-ethyl-2,4-dimethylhexane					554		
2,4-dimethyloctane			587			3-ethyl-2,5-dimethylhexane					561		
2,5-dimethyloctane			582			3-ethyl-3,4-dimethylhexane					547		
2,6-dimethyloctane			577			4-ethyl-2,2-dimethylhexane					557		
2,7-dimethyloctane			584			4-ethyl-2,3-dimethylhexane					560		
3,3-dimethyloctane			580			4-ethyl-2,4-dimethylhexane					561		
3,4-dimethyloctane			570			4-ethyl-3,3-dimethylhexane					542		
3,5-dimethyloctane			565			2,2,3,3-tetramethylhexane					557		
3,6-dimethyloctane			560			2,2,3,4-tetramethylhexane					547		
4,4-dimethyloctane			572			2,2,3,5-tetramethylhexane					554		
4,5-dimethyloctane			560			2,2,4,4-tetramethylhexane					549		
4-propylheptane			580			2,2,5,5-tetramethylhexane					548		
3-ethyl-2-methylheptane			580			2,2,4,5-tetramethylhexane					549		
3-ethyl-3-methylheptane			573			2,3,3,4-tetramethylhexane					550		
3-ethyl-4-methylheptane			558			2,3,3,5-tetramethylhexane					557		
3-ethyl-5-methylheptane			553			2,3,4,4-tetramethylhexane					546		
4-ethyl-2-methylheptane			575			2,3,4,5-tetramethylhexane					546		
4-ethyl-3-methylheptane			558			3,3,4,4-tetramethylhexane					534		
4-ethyl-4-methylheptane			571			3,3-deethyl-2-methylpentane					505		
5-ethyl-2-methylheptane			570			3-ethyl-2,2,3-trimethylpentane					556		
2,2,3-trimethylheptane			574			3-ethyl-2,2,4-trimethylpentane					547		
2,2,4-trimethylheptane			569			3-ethyl-2,3,4-trimethylpentane					555		
2,2,5-trimethylheptane			564			2,2,3,3,4-pentamethylpentane					531		
2,2,6-trimethylheptane			571			2,2,3,4,4-pentamethylpentane					535		
2,3,3-trimethylheptane			576			<i>n</i> -undecane			689	12	682	7.2	1.0
2,3,4-trimethylheptane			566			<i>n</i> -dodecane			754	12	746	8.4	1.1
2,3,5-trimethylheptane			561			<i>n</i> -tridecane			823	12	810	13.4	1.6
2,3,6-trimethylheptane			568			<i>n</i> -tetradecane			894	12	874	20.4	2.3
2,4,4-trimethylheptane			568			<i>n</i> -pentadecane			966	12	938	28.2	2.9
2,4,5-trimethylheptane			556			<i>n</i> -hexadecane			1034	12	1002	32.0	3.1
2,4,6-trimethylheptane			563			<i>n</i> -heptadecane			1103	12	1066	36.7	3.3
2,5,5-trimethylheptane			560			<i>n</i> -octadecane			1189	12	1131	58.4	4.9
3,3,4-trimethylheptane			554			<i>n</i> -nonadecane			1195				

Table 3. Continued

compds	$V_c(\text{exp})$ $\text{cm}^3 \cdot \text{mol}^{-1}$	ref	this work			compds	$V_c(\text{exp})$ $\text{cm}^3 \cdot \text{mol}^{-1}$	ref	this work		
			predict	D	100δ				predict	D	100δ
3,3,5-trimethylheptane			549			cyclopropane	162	15	162	0.0	0.0
3,4,4-trimethylheptane			551			cyclobutane			314		
3,4,5-trimethylheptane			563			cyclopentane	259	15	268	8.8	3.4
3,4-diethylhexane			546			cyclohexane	308	15	341	32.5	10.6
3,3-diethylhexane			567			methylcyclopentane	318	15	317	1.0	0.3
methylcyclohexane	369	15	391	21.9	5.9	1-heptene	409	16	407	2.3	0.6
ethylcyclopentane	375	15	367	8.4	2.2	cis-2-heptene			409		
cis-1,2-dimethylcyclopentane			360			trans-2-heptene			413		
trans-1,2-dimethylcyclopentane			364			cis-3-heptene			410		
cis-1,3-dimethylcyclopentane			355			trans-3-heptene			414		
trans-1,3-dimethylcyclopentane			359			1-octene	468	16	466	2.1	0.4
1,1-dimethylcyclopentane			368			cis-2-octene			470		
1,1-dimethylcyclohexane			443			trans-2-octene			474		
cis-1,2-dimethylcyclohexane	21	435	25.0	5.4		cis-3-octene			470		
trans-1,2-dimethylcyclohexane	21	439	20.9	4.5		trans-3-octene			474		
cis-1,3-dimethylcyclohexane	21	430	13.9	3.3		cis-4-octene			468		
trans-1,3-dimethylcyclohexane	21	434	26.0	5.6		trans-4-octene			472		
cis-1,4-dimethylcyclohexane	21	425	35.2	7.6		1-nonene	526	16	526	0.4	0.1
trans-1,4-dimethylcyclohexane			429			1-decene	584	16	588	3.8	0.6
ethylcyclohexane			441			1-undecene			650		
n-propylcyclopentane			441			1-dodecene			712		
n-propylcyclohexane			504			1,3-butadiene	221	16	221	0.0	0.0
n-butylcyclopentane			492			benzene	256	13	279	22.9	8.9
n-butylcyclohexane			568			methylbenzene	316	13	325	8.6	2.7
n-pentylcyclopentane			555			1,4-dimethylbenzene	378	13	370	7.5	2.0
n-pentylcyclohexane			631			1,2-dimethylbenzene	370	13	368	1.8	0.5
n-hexylcyclopentane			619			1,3-dimethylbenzene	375	13	382	7.1	1.9
n-heptylcyclohexane			683			ethylbenzene	374	13	353	20.5	5.5
1-butene	240.8	16	245	4.4	1.8	1,2,3-trimethylbenzene			424		
cis-2-butene	233.8	16	238	4.3	1.8	1,2,4-trimethylbenzene			426		
trans-2-butene	237.7	16	242	4.5	1.9	1,3,5-trimethylbenzene			452		
1-pentene	298.4	16	295	3.7	1.2	1,2,3,4-tetramethylbenzene			480		
cis-2-pentene			294			1,2,3,5-tetramethylbenzene			494		
trans-2-pentene			298			1,2,4,5-tetramethylbenzene			482		
2-methyl-1-butene			292			1-methyl-2-ethylbenzene			398		
2-methyl-2-butene			291			1-methyl-3-ethylbenzene			412		
3-methyl-1-butene	304.9	16	309	4.2	1.4	1-methyl-4-ethylbenzene			400		
1-hexene	355.1	16	349	5.9	1.7	n-propylbenzene	440	13	415	25.3	5.8
cis-2-hexene			350			isopropylbenzene			447		
trans-2-hexene			355			1-methyl-2-isopropylbenzene			492		
cis-3-hexene			351			1-methyl-3-isopropylbenzene			506		
trans-3-hexene			355			1-methyl-4-isopropylbenzene			495		
2-methyl-1-hexene			399			n-butylbenzene	497	13	476	20.5	4.1
3-methyl-1-hexene			394			sec-butylbenzene			497		
4-methyl-1-hexene			380			tert-butylbenzene	492	21	492	0.0	0.0
n-pentylbenzene	550	21	539	11.2	2.0	5-dodecanone	759	17	759	0.2	0.0
n-hexylbenzene	593	21	601	8.4	1.4	6-dodecanone	762	17	760	1.5	0.2
n-heptylbenzene			664			2-tridecanone	820	17	814	6.0	0.7
butanone	267	17	247	19.8	7.4	3-tridecanone	823	17	820	3.5	0.4
2-pentanone	321	17	307	13.5	4.2	4-tridecanone	823	17	821	1.8	0.2
3-pentanone	331	17	313	18.0	5.4	5-tridecanone	826	17	823	3.1	0.4
3-methyl-2-butanone	308	17	310	1.9	0.6	6-tridecanone	826	17	825	1.4	0.2
2-hexanone	377	17	369	7.8	2.1	7-tridecanone	830	17	826	3.7	0.4
3-hexanone	378	17	375	3.3	0.9	2-tetradecanone	896	17	878	17.8	2.0
3,3-dimethyl-2-butanone	382	17	382	0.0	0.0	3-tetradecanone	896	17	884	12.3	1.4
4-methyl-2-pentanone			471			4-tetradecanone	900	17	885	14.6	1.6
2-heptanone	436	17	432	4.2	1.0	7-tetradecanone	904	17	890	13.5	1.5
3-heptanone	433	17	437	4.3	1.0	propanal	204	17	199	5.1	2.5
4-heptanone	434	17	439	5.0	1.2	butanal	258	17	254	4.1	1.6
2-octanone	497	17	495	2.1	0.4	1-pentanal	313	17	313	0.2	0.1
3-octanone	497	17	500	3.4	0.7	1-hexanal	378	17	374	4.5	1.2
4-octanone	497	17	502	5.1	1.0	1-heptanal	434	17	435	1.4	0.3
2-methyl-3-hexanone			445			1-octanal	488	17	498	9.9	2.0
5-methyl-2-hexanone			412			1-nonanal	543	17	561	17.9	3.3
2,4-dimethyl-3-pentanone			442			1-decanal	599	17	624	25.3	4.2
2-methyl-3-heptanone			485			2-methylpropanal			261		
5-methyl-3-heptanone			470			2-methylhexanal			431		
2,5-dimethyl-3-hexanone			488			3-methylhexanal			414		
5-nonanone	560	17	567	7.2	1.3	ethanol	168	14	171	2.9	1.7
4-nonanone	560	17	566	5.5	1.0	1-propanol	218	14	220	1.8	0.8
3-nonanone	560	17	564	3.9	0.7	2-propanol	222	14	229	7.3	3.3
2-nonanone	560	17	558	1.6	0.3	1-butanol	274	14	275	1.0	0.4
2,6-dimethyl-4-heptanone			537			2-butanol	269	14	272	3.4	1.2
2-decanone	625	17	622	2.9	0.5	2-methyl-1-propanol	274	14	271	3.3	1.2
3-decanone	628	17	628	0.5	0.1	2-methyl-2-propanol	275	14	276	1.4	0.5

Table 3. Continued

compds	$V_c(\text{exp})$			this work			compds	$V_c(\text{exp})$			this work		
	$\text{cm}^3 \cdot \text{mol}^{-1}$	ref	predict	D	100 δ	compds		$\text{cm}^3 \cdot \text{mol}^{-1}$	ref	predict	D	100 δ	
4-decanone	628	17	629	1.2	0.2	1-pentanol	326	14	333	7.3	2.3		
5-decanone	628	17	631	2.9	0.5	2-pentanol	329	14	331	1.7	0.5		
2-undecanone	692	17	686	6.1	0.9	3-pentanol	325	14	323	2.0	0.6		
3-undecanone	692	17	691	0.6	0.1	2-methyl-1-butanol			317				
4-undecanone	692	17	693	1.1	0.2	3-methyl-1-butanol			324				
5-undecanone	692	17	695	2.8	0.4	2-methyl-2-butanol			323				
6-undecanone	692	17	696	4.5	0.6	3-methyl-2-butanol			321				
2-dodecanone	752	17	750	2.1	0.3	1,2-butanediol			284				
3-dodecanone	752	17	755	3.4	0.5	1,3-butanediol			300				
4-dodecanone	759	17	757	1.9	0.2	1-hexanol	387	14	394	6.5	1.7		
2-hexanol	384	14	391	6.9	1.8	4-ethylphenol			389				
3-hexanol	383	14	383	0.1	0.0	diethyl ether	281	17	279	1.9	0.7		
2-methyl-1-pentanol			377			isopropyl methyl ether			295				
4-methyl-1-pentanol			379			ethyl <i>n</i> -propyl ether	339	17	328	11.2	3.3		
2-methyl-2-pentanol			383			butyl methyl ether	329	17	338	9.4	2.8		
2-methyl-3-pentanol			365			methyl pentyl ether	391	17	392	0.6	0.1		
4-methyl-2-pentanol			377			butyl ethyl ether			381				
3-methyl-3-pentanol			437			dipropyl ether			381				
1-heptanol	435	14	455	19.8	4.6	diisopropyl ether	386	17	391	5.3	1.4		
2-heptanol	442	14	452	10.2	2.3	methyl formiate	172	17	179	6.9	4.0		
3-heptanol	434	14	444	10.5	2.4	methyl acetate	228	17	225	3.4	1.5		
4-heptanol	432	14	449	16.8	3.9	ethyl formiate	229	17	249	19.6	8.6		
1-octanol	497	14	517	19.9	4.0	propyl formiate	285	17	286	0.5	0.2		
2-octanol	519	14	514	4.7	0.9	<i>n</i> -pentyl methanoate	412	17	383	29.5	7.2		
3-octanol	515	14	507	8.5	1.6	ethyl acetate	286	17	295	9.0	3.2		
4-octanol	515	14	511	4.1	0.8	methyl propionate	282	17	285	3.3	1.2		
2-ethyl-1-hexanol			488			propyl acetate	345	17	340	5.5	1.6		
1-nonanol	572	14	580	7.5	1.3	isopropyl acetate	344	17	344	0.0	0.0		
2-nonanol	575	14	577	1.9	0.3	methyl butanoate	340	17	336	4.3	1.3		
3-nonanol	577	14	569	7.9	1.4	methyl isobutanoate	339	17	358	19.0	5.6		
4-nonanol	575	14	586	10.6	1.8	2-propenyl acetate			219				
1-decanol	649	14	642	6.5	1.0	2-ethenyl acetate			154				
2-decanol	646	14	640	6.1	0.9	ethyl propionate	342	17	355	12.5	3.7		
3-decanol	643	14	632	10.9	1.7	butyl acetate			390				
4-decanol	643	14	636	6.5	1.0	pentyl ethanoate	470	17	443	26.7	5.7		
5-decanol	646	14	641	5.1	0.8	propyl propionate			403				
1-undecanol	718	14	706	12.2	1.7	ethyl butanoate	415	17	405	10.0	2.4		
1-dodecanol			769			<i>n</i> -propyl butyrate			458				
phenol			175			ethyl isobutanoate	415	17	421	5.9	1.4		
<i>o</i> -cresol			291			methyl pentanoate	422	17	391	31.5	7.5		
<i>m</i> -cresol			320			ethyl pentanoate			459				
<i>p</i> -cresol			349			propyl pentanoate			515				
2,3-xylenol			432			isobutyl acetate	401	17	395	5.5	1.4		
2,4-xylenol			475			1-methylpropyl ethanoate			382				
2,5-xylenol			492			isobutyl acrylate			433				
2,6-xylenol			533			isobutyl butyrate			519				
3,4-xylenol			490			isobutyl formate	355	17	337	17.8	5.0		
3,5-xylenol			533			diphenyl ether			503				
3-ethylphenol			360			methylamine			125				
2-ethylphenol			331			dimethylamine			180				
ethy lamine	180	19	185	5.4	3.0	3,5-dimethylpyridine	357	19	357	0.2	0.1		
propylamine			236			propanenitrile	246	19	246	0.0	0.0		
isopropylamine	219	19	240	20.9	9.5	butanenitrile			295				
trimethylamine	257	19	257	0.0	0.0	2-methylpropanenitrile			146				
butylamine			292			pentanenitrile			352				
isobutylamine			282			3-methylbutanenitrile			331				
<i>sec</i> -butylamine			284			2,2-dimethylpropanenitrile			167				
<i>tert</i> -butylamine	293	19	293	0.0	0.0	hexanenitrile			412				
diethylamine	304	19	300	4.1	1.4	octanenitrile			536				
pentylamine			350			decanenitrile			663				
cyclopentylamine			290			chloroethane			212				
hexylamine			411			1-chloropropane	264	20	256	7.8	2.9		
1-octanamine	517	19	535	17.9	3.5	2-chloropropane	242	20	257	15.0	6.2		
butyl ethylamine			453			1-chlorobutane			308				
isopropyl propylamine			431			2-chlorobutane			297				
triethylamine	389	19	389	0.0	0.0	2-chloro-2-methylpropane			195				
dipropylamine			402			1-chloropentane			364				
diisopropylamine			421			2-chloropentane			353				
cyclohexylamine			360			1-chlorohexane			423				
dibutylamine			516			1-chloroheptane			483				
1,2-ethanediamine			221			1-chloro-3-methylbutane			372				
1,3-propanediamine			275			1,1-dichloroethane			236				
1,4-butanediamine			333			bromoethane	214	20	214	0.0	0.0		
1,6-hexanediamine			453			1-bromopropane			266				
1,8-octanediamine			577			2-bromopropane			266				

Table 3. Continued

compds	$V_c(\text{exp})$		this work			compds	$V_c(\text{exp})$		this work		
	$\text{cm}^3 \cdot \text{mol}^{-1}$	ref	predict	D	100δ		$\text{cm}^3 \cdot \text{mol}^{-1}$	ref	predict	D	100δ
1,9-nananediamine			640			1-bromobutane			325		
1,10-decanediamine			703			1-bromo-2-methylpropane			320		
1,12-dodecanediamine			830			2-bromo-2-methylpropane			145		
benzamine	291	19	291	0.0	0.0	1-bromopentane			386		
2-methylbenzamine	346	19	346	0.0	0.0	methylthio ethane			187		
3-nethylbenzamine			375			1-methylthio propane			247		
pyridine	247	19	245	1.8	0.7	2-methylthio propane			257		
2-methylpyridine	300	19	301	1.3	0.4	1-methylthio butane			308		
3-methylpyridine	300	19	301	1.3	0.4	2-methyl-2-methylthio propane			307		
4-methylpyridine	300	19	301	1.0	0.3	1-ethylthio propane			296		
2,3-dimethylpyridine	357	19	357	0.2	0.1	2-ethylthio propane			307		
2,4-dimethylpyridine	357	19	356	0.5	0.1	1-ethylthio butane			383		
2,5-dimethylpyridine	357	19	357	0.2	0.1	2-ethylthio butane			376		
2,6-dimethylpyridine	357	19	357	0.2	0.1	2-ethylthio-2-methyl propane			357		
3,4-dimethylpyridine	357	19	356	0.5	0.1	methylthio cyclopentane			317		
1,2-dibromopropane			371			2-methyl-2-pentanethiol			415		
1,1,2-trichloroethane			199			2,3-dimethyl-2-butanol			405		
methylthio methane	147	18	147	0.0	0.0	cyclohexanethiol	401	18	382	19.0	4.7
ethanethiol	207	18	220	13.0	6.3	1-heptanethiol			482		
1-propanethiol	286	18	261	25.3	8.9	1-octanethiol	504		542	38.5	7.6
2-propanethiol			271			acetic acid	171	17	159	11.6	6.8
1-butane	324	18	311	13.4	4.1	n-propanoic acid	233	17	225	7.9	3.4
2-butane			309			acrylic acid			312		
2-methyl-1-propanethiol	307	21	306	0.7	0.2	n-butyric acid	292	17	277	15.3	5.2
2-methyl-2-propanethiol	307	21	309	2.3	0.6	n-pentanoic acid	346	17	333	13.5	3.9
1-pentanethiol			365			2-ethyl butyric acid			380		
2-methyl-1-butane			349			2-ethyl hexanoic acid	528	17	499	28.9	5.5
3-methyl-1-butane			345			n-hexanoic acid	413	17	391	22.2	5.4
2-methyl-2-butane			357			n-heptanoic acid	468	17	451	17.3	3.7
3-methyl-2-butane			354			n-octanoic acid	519	17	512	7.4	1.4
2,2-dimethyl-1-propanethiol			342			n-nonanoic acid			573		
cyclopentanethiol			312			n-decanoic acid	638	17	635	2.6	0.4
1-hexanethiol			423								

^a D is the absolute difference. $D = |V_{c,\text{exp}} - V_{c,\text{pred}}|$.

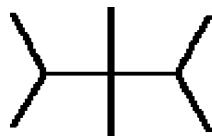
Conclusion

On the basis of the position group contribution method, a new method recently proposed for the estimation of the critical temperature and pressure is extended to the prediction of critical volume. Contributions for compounds containing carbon, hydrogen, oxygen, nitrogen, chlorine, and sulfur were reported, and that position distribution function has been developed which could distinguish between the thermodynamic properties of most isomers of organic compounds including *cis*- and *trans*- or Z- and E-structures. The results indicate that our model provides very satisfactory results, and the deviation from the most reliable experimental data is not more than 2.1 %. The overall average absolute difference for critical volume V_c predictions of 219 organic compounds is $8.8 \text{ cm}^3 \cdot \text{mol}^{-1}$, and 2.1 % is the relative derivation. The higher prediction accuracy of the proposed method shown in our previous works and this work suggests that it is possible to use a similar framework to predict the three critical properties, T_c , P_c , and V_c of organic compounds containing various functionalities.

Appendix

Example 1.

Estimation of the critical volume of 2,3,3,4-tetramethylpentane



This compound is decomposed in position groups as follows: $4\text{C}-(\text{CH})(\text{H})_3$; $2\text{C}-(\text{C})(\text{H})_3$; $2\text{C}-(\text{C})_3(\text{H})$; $1\text{C}-(\text{C})_4$. Total number of groups: $N = 9$.

The position factor: position of (CH) group 2, 4; the position correlation factor is $P = 2 + 4 = 6$.

Position of (C) group 3; the position correlation factor is $P = 3$.

Molecular weight: $M = 128.2551$.

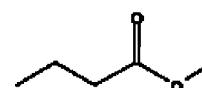
From the contributions in Table 1, the critical volume is estimated by eq 1

$$V_c/\text{cm}^3 \cdot \text{mol}^{-1} = 44.253 \cdot 4 + 39.01 \cdot 2 + 78.892 \cdot 2 + 102.7 \cdot 1 - 5.06 \cdot 6 - 8.151 \cdot 3 + 46.24 \cdot \exp(1/9) + 989.257 \cdot \exp(1/128.2551) - 1011.117 = 498.3$$

The calculated result is $498.3 \text{ cm}^3 \cdot \text{mol}^{-1}$, while the experimental critical volume is $498 \text{ cm}^3 \cdot \text{mol}^{-1}$.

Example 2.

Estimation of the critical volume of Methyl butanoate



This compound is decomposed in position groups as follows:

$1\text{C}-(\text{CH}_2)(\text{H})_3$; $1\text{C}-(\text{C})_2(\text{H})_2$; $1\text{C}-(\text{C})(\text{CO})(\text{H})_2$.

$1\text{CO}-(\text{CH}_2)(\text{O})$; $1\text{O}-(\text{CO})(\text{CH}_3)$; $1\text{C}-(\text{O})(\text{H})_3$.

Total number of groups: $N = 6$.

The position of the (CO) group: the position correlation factor is $P = 4$.

Molecular weight: $M = 102.1317$.

From the contributions in Table 1, the critical volume is estimated by eq 1

$$V_c/\text{cm}^3 \cdot \text{mol}^{-1} = 32.124 \cdot 1 + 64.715 \cdot 1 + 100.338 \cdot 1 + 24.628 + 170.243 \cdot \tanh(1/6) + 221.203 \cdot \tanh(1/6) + 1.684 \cdot 4 + 46.24 \cdot \exp(1/6) + 989.257 \cdot \exp(1/102.1317) - 1011.117 = 335.6$$

Therefore, the calculated result is $335.6 \text{ cm}^3 \cdot \text{mol}^{-1}$, while the experimental critical volume is $336 \text{ cm}^3 \cdot \text{mol}^{-1}$.

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