# Molecular Interactions in Glycylglycine $-MnCl_2$ Aqueous Solutions at (288.15, 293.15, 298.15, 303.15, 308.15, 313.15, and 318.15) K

# M. S. Santosh, D. Krishna Bhat,\* and Aarti S. Bhat

Department of Chemistry, National Institute of Technology Karnataka, Surathkal, Mangalore, India

The viscosities, ultrasonic velocities, densities, and refractive indices of glycylglycine and MnCl<sub>2</sub> in water have been studied at different temperatures and concentrations. Excess thermodynamic parameters such as adiabatic compressibility ( $\beta_{ad}$ ), apparent molar volume ( $\Phi_V$ ), apparent molar compressibility ( $\Phi_K$ ), intermolecular free length ( $L_f$ ), specific acoustic impedance (Z), relative association ( $R_A$ ), and solvation number ( $S_n$ ) have been calculated. The variations in apparent molar volume were confirmed by Scaled particle theory, and the changes in apparent molar compressibilities were interpreted using the Kirkwood model. The variations in apparent molar volumes were fitted with Masson's equation. The viscosity data have been fitted using the Jones-Dole empirical equation. The molecular relaxation of MnCl<sub>2</sub> and glycylglycine in water gives an idea about solute—solute interactions. The interactions also suggest the formation of H-bonding in the system. The structure forming tendency of the solute has also been indicated by the solvation number.

### Introduction

Interactions of amino acids with their surrounding environment play an important role in their conformational characteristics. These interactions are mainly those between the amino acid molecules and solvent ions. Most of these interactions such as hydrogen bonding and electrostatic interactions have a noncovalent nature. The study of these interactions provides an important insight into the conformational stability and unfolding behavior of amino acids and proteins.<sup>1</sup> The properties of amino acids and proteins such as their structure, solubility, denaturation, activity of enzymes, etc. are greatly influenced by electrolytes. The effect of electrolytes on structure and function of both proteins and amino acids has been widely studied in terms of structure making and structure breaking properties. Proteins are complex molecules, and their behavior in solutions is governed by a number of specific interactions.<sup>2</sup> Protein hydration plays a crucial role in this matter. Salt solutions are known to produce remarkable effects on the conformation and properties of proteins. Due to the complex structure of proteins, a variety of different interactions with salts may occur, and it is difficult to resolve straightaway the various interactions participating in protein hydration.<sup>3</sup>

Most of the previous studies<sup>4–10</sup> on amino acids have been carried out in different solvents and aqueous solutions at a given temperature, but interesting results have been obtained when they were studied under various temperatures and pressures in water, not only because it is used in chemistry and other related fields to control factors such as solubility, reactivity, and stability of the system but also for the fact that biological molecules are ultimately found in water.<sup>11</sup> Most of the studies on amino acids and biomolecules have been carried out in pure and mixed aqueous solvents. But such investigations in the presence of metal ions, which play a vital role in the functioning of living organisms, are still scanty. Transition metal ions play an important role in plant growth, lipid metabolism, and regulation of physiological systems.

Table 1. Viscosities  $(\eta)$  of Aqueous Glycylglycine (1) + Densities  $(\rho)$  of Aqueous Sodium Chloride Solutions (2) at Various Temperatures and Concentrations<sup>*a*</sup>

	.5				
Μ	Т	obtained values $\eta$	lit. values $\eta$		
mol•dm <sup>-3</sup>	K	m•Pa•s	m•Pa•s		
0.025 (Gly-Gly)	293.15	$1.0190 \pm 0.0004$	$1.0194 \pm 0.0010$		
	298.15	$0.9026 \pm 0.0002$	$0.9028 \pm 0.0007$		
	303.15	$0.8068 \pm 0.0003$	$0.8065 \pm 0.0019$		
		ρ	ρ		
		kg•m <sup>-3</sup>	kg•m <sup>-3</sup>		
0.20910 (NaCl)	298.15	1005.459	1005.571 (0.20918)		
0.50660		1015.258	1017.344 (0.50653)		
1.01276		1034.190	1036.690 (1.01279)		
1.50258		1049.726	1054.672 (1.50262)		
1.97404		1074.453	1071.353 (1.97403)		
2.44956		1088.006	1087.608 (2.44952)		

<sup>*a*</sup> The values given in brackets are the concentrations of aqueous sodium chloride solution.

metal salt solution systems which would fill the gap and may provide new insights and better understanding of this field of science. Through this paper, we make an attempt to present variations occurring under diverse conditions. Accordingly, this paper presents a systematic study of the viscosities, ultrasonic velocities, densities, and refractive indices of the aqueous solutions of glycylglycine and MnCl<sub>2</sub> as a function of concentration and temperature over wide ranges.

#### **Experimental Section**

Glycylglycine of 99 % purity from the Sigma Aldrich Company and MnCl<sub>2</sub>·4H<sub>2</sub>O of 99 % purity analytical grade from the Central Drug House were used. MnCl<sub>2</sub> was used after drying for 72 h in a vacuum desiccator at room temperature. Deionized, doubly distilled, degassed water with a specific conductance less than  $1.29 \cdot 10^{-6} \ \Omega^{-1} \cdot \text{cm}^{-1}$  was used for the preparation of all solutions. The solutions were prepared on a weight basis by using a Mettler balance having a precision of  $\pm 0.01$  mg. In the first case (Tables 2 and 4), the concentration

<sup>\*</sup> Corresponding author. E-mail: denthaje@gmail.com.

Table 2. Viscosity ( $\eta$ ), Ultrasonic Velocity (U), Density ( $\rho$ ), Refractive Index ( $n_D$ ), and Adiabatic Compressibility ( $\beta_{ad}$ ) for (1) Glygylglycine + MnCl<sub>2</sub> (2) in Water (3) at T = (288.15 to 318.15) KKeeping Glycylglycine Constant at 0.020 M

Table 3. Viscosity $(\eta)$ , Ultrasonic Velocity $(U)$ , Density $(\rho)$ ,						
Refractive Index $(n_D)$ , and Adiabatic Compressibility $(\beta_{ad})$ for (1)						
Glygylglycine + MnCl <sub>2</sub> (2) in Water (3) at $T = (288.15 \text{ to } 318.15) \text{ K}$						
Keeping MnCl <sub>2</sub> Constant at 0.25 M						

М	η	U	$\rho \cdot 10^{-3}$		$\beta_{\rm ad}$ • $10^{10}$	М	η	U	$\rho \cdot 10^{-3}$		$\beta_{\rm ad}$ • $10^{10}$
mol·dm <sup>-3</sup>	m•Pa•s	$m \cdot s^{-1}$	$kg \cdot m^{-3}$	$n_{\rm D}$	$\overline{m^2 \cdot N^{-1}}$	$mol \cdot dm^{-3}$	m•Pa•s	$m \cdot s^{-1}$	$kg \cdot m^{-3}$	$n_{\rm D}$	$\overline{m^2 \cdot N^{-1}}$
		T/K = 2	88.15			-		T/K = 2	88.15		
0.005	1.10	1035.20	0.9990	1.3331	9.340	0.005	1.16	1042.01	0.9998	1.3340	9.2117
0.010	1.20	1040.36	0.9993	1.3332	9.245	0.007	1.33	1050.12	1.0033	1.3349	9.0410
0.030	1.32	1045.15	0.9999	1.3336	9.155	0.010	1.50	1057.16	1.0068	1.3356	8.8970
0.050	1.43	1050.28	1.0030	1.3342	9.038	0.020	1.68	1065.33	1.0104	1.3364	8,7220
0.100	1.15	1057.01	1.0076	1 3351	8 882	0.030	1.85	1072 99	1 0140	1 3373	8 5658
0.250	1.50	1065 33	1.0102	1 3363	8 722	0.050	2.00	1080.28	1.0173	1 3380	8 4232
0.500	1.83	1071.00	1.0102	1 3378	8 613	0.100	2.00	1087 57	1.0201	1 3386	8 2878
0.500	1.05		1.0121	1.5570	0.015	0.100	2.17		1.0201	1.5500	0.2070
		T/K = 2	93.15					T/K = 2	93.15		
0.005	0.99	1105.10	0.9982	1.3328	8.2031	0.005	1.05	1103.15	0.9989	1.3327	8.2263
0.010	1.05	1110.22	0.9987	1.3332	8.1235	0.007	1.14	1111.85	0.9998	1.3336	8.0801
0.030	1.12	1115.18	0.9993	1.3338	8.0466	0.010	1.25	1121.56	1.0007	1.3348	7.9339
0.050	1.20	1120.31	0.9999	1.3345	7.9683	0.020	1.37	1132.27	1.0016	1.3359	7.7876
0.100	1.27	1125.15	1.0007	1.3351	7.8936	0.030	1.44	1140.23	1.0026	1.3367	7.6415
0.250	1.36	1132.27	1.0016	1.3359	7.7876	0.050	1.55	1148.73	1.0035	1.3378	7.4953
0.500	1.47	1137.38	1.0025	1.3368	7.7108	0.100	1.66	1159.66	1.0045	1.3389	7.3491
		T/K = 2	98.15					T/K = 2	98.15		
0.005	0.90	1180.15	0.9970	1.3324	7.2016	0.005	0.94	1184.32	0.9976	1.3320	7.1466
0.010	0.95	1184.23	0.9975	1.3327	7.1485	0.007	1.02	1193.35	0.9984	1.3329	7.0462
0.030	0.99	1189.10	0.9981	1.3331	7.0821	0.010	1.10	1200.65	0.9995	1.3339	6.9458
0.050	1.04	1197.36	0.9988	1.3336	6.9834	0.020	1.17	1208.41	1.0004	1.3348	6.8453
0.100	1.12	1203.29	0.9996	1.3343	6.9092	0.030	1.26	1215.10	1.0013	1.3356	6.7449
0.250	1.17	1208.41	1.0004	1.3348	6.8453	0.050	1.35	1223.53	1.0023	1.3364	6.6445
0.500	1.23	1213.32	1.0008	1.3354	6.7866	0.100	1.47	1234.66	1.0035	1.3378	6.5441
		T/V = 2	02 15					T/V = 2	02.15		
0.005	0.91	1/K = 5	0.0057	1 2217	6 1266	0.005	0.82	1/K = 3	0.0061	1 2212	6 2520
0.003	0.81	1250.10	0.9937	1.3317	6.4200	0.003	0.85	1257.10	0.9901	1.3313	6.3520
0.010	0.84	1250.21	0.9903	1.3324	6.3004	0.007	0.91	1200.40	0.9970	1.3326	6 1 4 9 6
0.050	0.88	1205.29	0.9908	1.3332	6 2020	0.010	0.99	12/4.52	0.9977	1.3343	6.0727
0.030	0.95	12/1.54	0.9974	1.3340	6.1220	0.020	1.04	1204.20	0.9985	1.3330	5.0706
0.100	0.99	12/6.10	0.9979	1.3349	0.1559	0.050	1.11	1295.61	0.9994	1.3370	5.9790
0.230	1.04	1204.20	0.9983	1.3337	6.0727	0.030	1.19	1302.30	0.9999	1.3364	5.0003
0.500	1.09	1290.06	0.9991	1.3304	0.0141	0.100	1.28	1315.27	1.0009	1.5599	5.7954
		T/K = 3	08.15					T/K = 3	08.15		
0.005	0.71	1316.00	0.9940	1.3310	5.8090	0.005	0.74	1321.07	0.9946	1.3303	5.7610
0.010	0.73	1320.15	0.9946	1.3313	5.7690	0.007	0.80	1329.16	0.9954	1.3312	5.7021
0.030	0.77	1325.07	0.9952	1.3318	5.7228	0.010	0.87	1335.43	0.9961	1.3324	5.6432
0.050	0.82	1329.23	0.9958	1.3322	5.6836	0.020	0.93	1340.27	0.9969	1.3334	5.5842
0.100	0.88	1335.18	0.9964	1.3328	5.6297	0.030	1.00	1346.15	0.9977	1.3342	5.5266
0.250	0.93	1340.27	0.9969	1.3333	5.5842	0.050	1.08	1354.83	0.9984	1.3354	5.4646
0.500	0.97	1347.36	0.9975	1.3339	5.5222	0.100	1.20	1363.06	0.9992	1.3366	5.4075
		T/K = 3	13.15					T/K = 3	13.15		
0.005	0.66	1400.05	0.9922	1.3302	5.1417	0.005	0.62	1406.31	0.9924	1.3296	5.0950
0.010	0.69	1407.17	0.9925	1.3304	5.0883	0.007	0.65	1414.56	0.9931	1.3304	5.0225
0.030	0.73	1413.23	0.9931	1.3308	5.0422	0.010	0.69	1425.92	0.9938	1.3313	4 9505
0.050	0.76	1420.28	0.9934	1.3312	4.9903	0.020	0.73	1435.81	0.9945	1.3321	4.8775
0.100	0.79	1428.16	0.9940	1.3317	4.9324	0.030	0.77	1444 43	0.9951	1.3330	4.8050
0.250	0.83	1435.81	0.9945	1.3321	4.8775	0.050	0.82	1455.18	0.9958	1.3338	4.7325
0.500	0.88	1442.08	0.9951	1.3327	4.8318	0.100	0.86	1468.39	0.9969	1.3350	4.6605
		T/V = 2	18 15					T/V = 2	18 15		
0.005	0.47	1/182 21	0.000/	1 3205	1 5800	0.005	0.50	1/10/156	0 0007	1 3200	1 5/21
0.005	0.47	1403.31	0.2204	1 3295	4.5626	0.005	0.50	1490.30	0.9907	1.3290	4.3431
0.010	0.50	1407.14	0.9900	1.3299	4.5050	0.007	0.50	1470.31	0.9913	1 3211	4.49/0
0.050	0.55	1492.10	0.9913	1.3304	4.3310	0.010	0.00	1510.05	0.9920	1.3311	4.4309
0.050	0.57	1490.22	0.991/	1.3309	4.3043	0.020	0.03	1520.27	0.9928	1.3321	4.4040
0.100	0.02	1510.29	0.9924	1.331/	4.4411	0.050	0.71	1520.27	0.9933	1 3220	4.338/
0.230	0.04	1510.27	0.9928	1.3321	4.4040	0.050	0.77	1520 11	0.9943	1.3339	4.3132
0.500	0.09	1317.37	0.7733	1.3347	4.3010	0.100	0.00	1330.11	0.7733	1.3332	4.2000

of glycylglycine was kept constant at 0.020 M, and that of  $MnCl_2$  was varied as 0.005 M, 0.010 M, 0.030 M, 0.050 M, 0.10 M, 0.25 M, and 0.50 M. In the second case (Tables 3 and 5), the concentration of glycylglycine was varied as 0.005 M, 0.007 M, 0.010 M, 0.020 M, 0.030 M, 0.050 M, and 0.10 M, and that of  $MnCl_2$  was kept constant at 0.25 M. The temperature of water was controlled within  $\pm$  0.01 K using a thermostat.

Viscosities were measured using a Brookfield DV-III Ultra Programmable Rheometer (Brookfield Engineering Laboratories, Inc., USA) which was calibrated using double distilled water, ethanol, DMSO, and THF, and the uncertainty was found to be  $\pm$  0.0001 % for all solutions. Ultrasonic velocities were measured using a variable path ultrasonic interferometer, M-83 (Mittal Enterprises, India), at 3 MHz. Densities of the solutions were calculated using a (Mettler Toledo) Density 30PX digital densitometer having a precision of  $\pm 1 \cdot 10^{-3}$  kg·m<sup>-3</sup> and an accuracy of  $\pm 3 \cdot 10^{-3}$  kg·m<sup>-3</sup>. Refractive indices were calculated using a (Mettler Toledo) Refracto 30PX and 30Gs digital

Table 4. Apparent Molar Volume ( $\Phi_V$ ), Apparent Molar Compressibility ( $\Phi_K$ ), Intermolecular Free Length ( $L_t$ ), Specific Acoustic Impedance (Z), Relative Association ( $R_A$ ), and Solvation Number ( $S_n$ ) of (1) Glycylglycine + MnCl<sub>2</sub> (2) in Water (3) at T =(288.15 to 318.15) K Keeping Glycylglycine Constant at 0.020 M

М	$\Phi_V{\scriptstyle \bullet}10^{-6}$	$\Phi_{\rm K}$	$L_{\rm f}$ · 10 <sup>5</sup>	$Z \cdot 10^{-3}$		
$mol \cdot dm^{-3}$	$\overline{m^3 \! \cdot \! mol^{-1}}$	$\overline{\mathrm{mol}^{-1}} \cdot \mathrm{Pa}^{-1}$	$A^0$	$\overline{kg \cdot m^{-2} \cdot s^{-1}}$	$R_{\rm A}$	$S_{n}$
		<i>T</i> /K =	= 288.15			
0.005	112.214	0.0651	1.8673	1034.164	0.9883	0.0250
0.010	112.179	0.0251	1.8577	1039.631	0.9885	0.0942
0.030	105.439	0.0150	1.8487	1045.045	0.9886	0.4875
0.050	100.357	0.0087	1.8368	1053.430	0.9888	1.1314
0.100	91.689	0.0056	1.8209	1065.043	0.9890	2.8560
0.250	83.785	0.0023	1.8044	1076.196	0.9891	7.9961
0.500	77.828	0.0002	1.7931	1083.959	0.9892	18.227
		<i>T</i> /K =	= 293.15			
0.005	130.340	0.0212	1.7700	1103.110	0.9842	0.0101
0.010	127.135	0.0175	1.7614	1108.776	0.9843	0.0310
0.030	122.430	0.0129	1.7530	1114.399	0.9845	0.1794
0.050	118.038	0.0089	1.7445	1120.197	0.9847	0.4583
0.100	112,993	0.0043	1.7363	1125,937	0.9848	1.1740
0.250	108.431	0.0018	1.7246	1134.081	0.9850	3.4402
0.500	103.694	0.0007	1.7160	1140.223	0.9851	8.3333
		<i>T</i> /K =	= 298.15			
0.005	130.498	0.0162	1.6772	1176.609	0.9679	0.0277
0.010	127 174	0.0132	1 6710	1181 269	0.9689	0.0322
0.030	122.524	0.0103	1 6632	1186 840	0.9697	0.1515
0.050	119 126	0.0081	1 6516	1195 923	1 0004	0 3706
0.100	116 084	0.0056	1.6428	1202.808	1.0001	1.0786
0.250	112 148	0.0035	1.6352	1202.000	1.0018	2 9938
0.200	107.632	0.00033	1.6281	1214 411	1.0018	6 9962
0.500	107.052	0.000 T	- 202 15	1211.111	1.0020	0.7702
0.005	112 514	1/K -	1 5006	1244 724	0.0011	0.0600
0.005	112.314	0.0238	1.5990	1244.724	0.9811	0.0009
0.010	103.040	0.0101	1.5915	1251.302	0.9810	0.0842
0.050	98.233	0.0084	1.5820	1239.247	0.9820	0.1505
0.050	91.008	0.0037	1.5/15	1208.034	0.9823	0.5592
0.100	83.340	0.0012	1.5027	12/3.4/3	0.9851	1.0075
0.250	70.456	0.00096	1.5549	1282.273	0.9843	2.8809
0.300	70.430	0.00038	1.3474	1200.090	0.9855	0.7558
		<i>T</i> /K =	= 308.15			
0.005	130.885	0.0212	1.5352	1308.104	0.9658	0.0352
0.010	126.141	0.0160	1.5299	1313.021	0.9663	0.0902
0.030	122.038	0.0115	1.5238	1318.709	0.9672	0.1363
0.050	117.961	0.0089	1.5186	1323.647	0.9676	0.3760
0.100	112.534	0.0048	1.5114	1330.373	0.9687	1.0738
0.250	108.385	0.0013	1.5052	1336.115	0.9692	3.0938
0.500	104.874	0.00081	1.4969	1343.991	0.9699	7.0450
		T/K =	= 313.15			
0.005	127.055	0.0246	1.4557	1389.129	0.9781	0.0189
0.010	119.654	0.0212	1.4481	1396.616	0.9788	0.0591
0.030	110.864	0.0178	1.4416	1403.478	0.9796	0.2465
0.050	102.365	0.0144	1.4341	1410.906	0.9806	0.5072
0.100	94.686	0.0110	1.4258	1419.591	0.9816	1.1962
0.250	86.289	0.0076	1.4178	1427.913	0.9820	3.3159
0.500	78.532	0.0042	1.4112	1435.158	0.9829	7.7655
		T/K =	= 318.15			
0.005	131.361	0.0253	1.3838	1469.070	0.9727	0.0531
0.010	128.584	0.0213	1.3790	1473.458	0.9734	0.0708
0.030	124.723	0.0178	1.3750	1479.118	0.9743	0.1981
0.050	119.432	0.0135	1.3710	1483.801	0.9750	0.4959
0.100	115.218	0.0094	1.3613	1494.842	0.9756	1.3548
0.250	109.834	0.0052	1.3557	1501.292	0.9764	3.5184
0.500	104.726	0.0008	1.3490	1509.190	0.9771	8.4366

refractometer, and its uncertainty was found to be  $\pm$  0.0001 %. The densitometer and refractometer were calibrated using double distilled water. The physical parameters for solutions of glycylglycine–MnCl<sub>2</sub> were measured at temperatures 288.15 K, 293.15 K, 298.15 K, 303.15 K, 308.15 K, 313.15 K, and 318.15 K. The measured viscosity values and their uncertainties of 0.025 M aqueous solutions of glycylglycine agree well with literature values.<sup>12</sup> The densities of aqueous sodium chloride solutions which were found to agree well with literature values<sup>13</sup> at 298.15 K (Table 1). On the basis of the above-mentioned

physical parameters, the excess thermodynamic properties such as adiabatic compressibility ( $\beta_{ad}$ ), apparent molar volume ( $\Phi_V$ ), apparent molar compressibility ( $\Phi_K$ ), intermolecular free length ( $L_f$ ), specific acoustic impedance (Z), relative association ( $R_A$ ), and solvation number ( $S_n$ ) were calculated for the substrates at different concentrations and temperatures. Each measurement was repeated thrice, and the reported values are the average values of all three trials.

## **Results and Discussion**

The experimental data of viscosity, ultrasonic velocity, density, refractive index, and the acoustical parameter adiabatic compressibility of glycylglycine and  $MnCl_2$  in water at temperatures of 288.15 K, 293.15 K, 298.15 K, 303.15 K, 308.15 K, 313.15 K, and 318.15 K for the first and second cases are given in Table 2 and Table 3, respectively.

Various acoustical parameters such as apparent molar volume, apparent molar compressibility, intermolecular free length, acoustic impedance, relative association, and solvation number for the first and second cases are given in Table 4 and Table 5, respectively, and were calculated using the following equations

$$\beta_{\rm ad} = 1/U^2 d \tag{1}$$

$$\Phi_{\rm v} = (M_1/d) + \{1000(d_0 - d)/Mdd_0\}$$
(2)

$$\Phi_{\rm K} = \{ (d_0 \beta_{\rm ad} - d\beta_{\rm ad}^0) \cdot 1000 \} / M d_0 + (\beta_{\rm ad}^0 M_1) / d_0$$
(3)

$$L_{\rm f} = k \sqrt{\beta}_{\rm ad} \tag{4}$$

$$Z = U \cdot d \tag{5}$$

$$R_{\rm A} = (d/d_0) \cdot (U_0/U)^{1/3} \tag{6}$$

$$S_{\rm n} = (1 - \eta_0/\eta) \cdot (1 - N_2/N_2) \tag{7}$$

where d and  $d_0$  are the densities of the solute and solvent;  $\eta$  and  $\eta_0$  are the viscosities of the solute and solvent; M is the molarity of the solute; k is the Jacobson constant<sup>14</sup> which is different for different temperatures;  $N_2$  is the mole fraction of the dissolved material;  $M_1$  is the molecular weight of the solute; and  $\beta_{ad}$  and  $\beta_{ad}^0$  are the adiabatic compressibilities of solvent and solute. The variations in apparent molar volumes were least-squares fitted using Masson's equation given below (eq 12).<sup>15</sup>

The present investigation is concerned with the study of the substrate glycylglycine and transition metal salt of  $MnCl_2$  in water. The variation of viscosity with concentration in case one and in case two has been observed to increase (Table 2 and Table 3). A regular change in the viscosity data for different concentrations in water confirms the interactions of solvent—solute. This phenomenon may appear due to H-bond formation, and it may be attributed to the formation of strong intermolecular forces in the solute. The viscosity data have been fitted using the Jones-Dole empirical equation<sup>16</sup> which describes the relative viscosities of electrolyte solutions as a function of concentration (eq 8).

$$\eta/\eta_{\rm o} = 1 + AC^{1/2} + BC \tag{8}$$

where C is the molarity; A is the constant arising from the interactions between the ions; and B is the viscosity B-coefficient. The above equation upon rearrangement becomes

$$(\eta/\eta_{o} - 1)/C^{1/2} = A + BC^{1/2}$$
(9)

The values have been found to be in accordance with the Jones-Dole equation. The values of the *A*- and *B*-coefficients obtained

Table 5. Apparent Molar Volume ( $\Phi_V$ ), Apparent Molar Compressibility ( $\Phi_K$ ), Intermolecular Free Length ( $L_f$ ), Specific Acoustic Impedance (Z), Relative Association ( $R_A$ ), and Solvation Number ( $S_n$ ) of (1) Glycylglycine + MnCl<sub>2</sub> (2) in Water (3) at T =(288.15 to 318.15) K Keeping MnCl<sub>2</sub> Constant at 0.25 M

M	$\Phi_{V} \cdot 10^{-6}$	$\Phi_{\rm K}$	$L_{\rm f} \cdot 10^5$	$Z \cdot 10^{-3}$		
$mol \cdot dm^{-3}$	$m^3 \cdot mol^{-1}$	$mol^{-1} \cdot Pa^{-1}$	A <sup>0</sup>	$kg \cdot m^{-2} \cdot s^{-1}$	$R_{\rm A}$	Sn
		<i>T</i> /K =	288.15			
0.005	157.785	0.0221	1.8544	1041.801	0.9562	0.0293
0.007	135.753	0.0155	1.8377	1053.266	0.9668	0.0736
0.010	114.721	0.0091	1.8218	1064.731	0.9763	0.1361
0.020	83.785	0.0023	1.8044	1076.196	0.9885	0.3281
0.030	69.657	0.00016	1.7884	1088.652	0.9986	0.5580
0.050	46.625	0.00009	1.7717	1100.108	1.0084	1.0102
0.100	25.593	0.00002	1.7552	1112.564	1.0183	2.1925
		T/K =	293 15			
0.005	183 711	0.0228	1 7725	1101 936	0.9692	0.0133
0.007	158 618	0.0186	1 7566	1112.650	0 9744	0.0404
0.010	132 525	0.0144	1 7407	1123 364	0.9792	0.0864
0.020	108 431	0.0104	1 7246	1134 081	0.9843	0 2277
0.030	85 338	0.0062	1 7089	1144 795	0.9908	0.3833
0.050	59 422	0.0025	1 6930	1155 509	0 9945	0 7354
0.100	32.156	0.00018	1.6771	1167.223	0.9983	1.6389
		T/K =	298 15			
0.005	177 726	0.0250	1 6708	1181 477	0 9642	0.0127
0.007	155 866	0.0185	1.6590	1190.615	0.9767	0.0395
0.010	134 013	0.0120	1.6472	1198 753	0.9892	0.0800
0.020	112 148	0.0056	1.6352	1208 893	1.0018	0.1982
0.030	92.065	0.0049	1.6234	1217 136	1.0010	0.3619
0.050	68 289	0.0043	1.6116	1228 619	1.0269	0.6962
0.100	47 989	0.0035	1 5926	1236 307	1.0392	1 6058
0.100	17.505	0.0035 T/V -	202.15	1230.307	1.0372	1.0050
0.005	107 020	1/K -	1 5002	1252 257	0.0755	0.0072
0.003	161.039	0.0285	1.5905	1252.257	0.9733	0.0072
0.007	124 722	0.0231	1.5705	1205.202	0.9764	0.0348
0.010	134.733	0.0219	1.5078	12/2.207	0.9617	0.0707
0.020	90.179 73.276	0.0190	1.5549	1202.273	0.9645	0.1640
0.050	15.270	0.0133	1.5415	1295.278	0.9873	0.5551
0.050	8 5210	0.0120	1.5545	1312 288	0.9901	1 5003
0.100	0.0210	0.0009	200.15	1512.200	0.7727	1.5005
0.005	196 505	1/K =	1 5290	1212.026	0.0(50	0.0010
0.005	186.595	0.0239	1.5289	1313.930	0.9650	0.0010
0.007	100.525	0.0208	1.5210	1321.329	0.9000	0.0036
0.010	134.433	0.0177	1.5155	1328.722	0.90/9	0.0078
0.020	108.383	0.0130	1.3032	1330.113	0.9692	0.0197
0.030	82.313	0.0119	1.4972	1345.308	0.9709	0.0300
0.030	30.243	0.0088	1.4690	1351.901	0.9724	1.6670
0.100	50.175	0.0039	1.4015	1337.294	0.9739	1.0070
0.005	101 500	T/K =	313.15	1005 (00	0.0700	0.0000
0.005	184.792	0.0204	1.4491	1395.622	0.9790	0.0032
0.007	163.168	0.0176	1.4386	1406.385	0.9800	0.01//
0.010	131.544	0.0150	1.4282	1417.148	0.9809	0.0463
0.020	86.289	0.0118	1.41/8	1427.913	0.9820	0.1315
0.030	64.665	0.0091	1.4075	1438.674	0.9831	0.2493
0.050	33.041	0.0064	1.3980	1449.437	0.9841	0.5121
0.100	1.417	0.0036	1.3866	1460.200	0.9850	1.1630
0.0		T/K =	318.15		0.0=	
0.005	183.607	0.0188	1.3769	1476.697	0.9745	0.0016
0.007	159.076	0.0163	1.3699	1484.895	0.9751	0.0051
0.010	134.545	0.0140	1.3629	1493.093	0.9758	0.0093
0.020	109.834	0.0112	1.3557	1501.292	0.9764	0.0233
0.030	85.483	0.0088	1.3489	1509.489	0.9771	0.0422
0.050	60.952	0.0064	1.3419	1518.687	0.9778	0.0805
0.100	36 421	0.0038	1 3340	1524 885	0.9784	0.1860

along with their standard deviations are summarized in Table 6. The value of the viscosity *A*-coefficient of the Jones-Dole equation is a measure of long-range ion—ion interactions, while the *B*-coefficient is a manifestation of ion—solvent interactions. It is observed that the ultrasonic velocity values in aqueous dipeptide—electrolyte solutions increase with an increase in concentration in both cases, and this may be attributed to the overall increase of cohesion brought about by the solute—solute and solute—solvent interactions in the solutions.<sup>17–19</sup> The decrease in intermolecular free length causes an increase in ultrasonic velocity and vice versa.<sup>20</sup>

Table 6. Viscosity *A*-Coefficient and *B*-Coefficient of Aqueous Glycylglycine and MnCl<sub>2</sub> Solutions at T = (288.15 to 318.15) K

Т	$A \cdot 10^{3/2}$	$B \cdot 10^{3}$		
K	$m^{3/2} \cdot mol^{-1/2}$	$\overline{m^3 \cdot mol^{-1}}$	<sup>a</sup> SD	${}^{b}R^{2}$
	(	Glycylglycine		
288.15	-0.093	0.2156	0.0045	0.8743
293.15	-0.0132	0.1925	0.0036	0.8752
298.15	-0.0185	0.1746	0.0028	0.8759
303.15	-0.0020	0.1571	0.0022	0.8765
308.15	-0.0008	0.1384	0.0014	0.8772
313.15	0.0114	0.1093	0.0009	0.8753
318.15	0.0138	0.0868	0.0003	0.8758
		MnCl <sub>2</sub>		
288.15	0.0051	0.8543	0.0047	0.8723
293.15	-0.0072	0.8321	0.0046	0.8726
298.15	-0.0086	0.8112	0.0044	0.8730
303.15	-0.0037	0.7943	0.0041	0.8734
308.15	-0.0045	0.7702	0.0038	0.8732
313.15	0.0138	0.7543	0.0037	0.8729
318.15	0.0152	0.7298	0.0034	0.8727

<sup>*a*</sup> SD = standard deviation for the fitting of eq 9. <sup>*b*</sup>  $R^2$  = coefficients of determination.

The Mn<sup>2+</sup> and Cl<sup>-</sup> ions furnished by electrolytes interact electrostatically with  $NH_3^+$  and  $COO^-$  groups of dipeptide zwitterions.<sup>1,2</sup> In addition, the water dipoles are strongly aligned to the cations/anions as well as to the dipeptide zwitterions by electrostatic forces. The added amount of dipeptide zwitterions may also occupy the cavities of water clusters which may lead to the formation of denser structure of the aqueous electrolyte solution. The rise in temperature and concentration causes the thermal rupture of the icelike structure of water, which in turn enhances cohesion in the solutions. The density values reported show that there is an increase in the density with an increase in the concentration of MnCl<sub>2</sub> and glycylglycine in both the cases. This may be due to the molecular relaxation of MnCl<sub>2</sub> and glycylglycine in water. The refractive index also shows an increase in its values with an increase in concentration. It may be noted that such changes are due to the electronic perturbation of the individual molecules during mixing and therefore depends very much on the nature of the mixing molecules. The adiabatic compressibility values decrease with an increase in concentration. This trend of variation of  $\beta_{ad}$  is in consonance with the variation of ultrasonic velocity with concentration. This is somewhat similar to those observed for other inorganic salt solutions.<sup>20,21</sup> The smaller values of  $\beta_{ad}$  for aqueous electrolyte solutions may be attributed to cation-water dipole and anion-water dipole interactions in water, which ultimately may lead to an overall increase in cohesive forces in water.

The apparent molar volume decreases with an increase in concentration and for a solution of  $MnCl_2$  and glycylglycine indicates predominance of a structure breaking or hydrophilic type of interaction with water<sup>15,22</sup> (Table 4 and Table 5). The decrease in the values of apparent molar volume indicates weak dipeptide–electrolyte interactions since the concentration change is very significant.<sup>23</sup> This was further confirmed by the Scaled particle theory model.<sup>1</sup> The best description for *a*, *b*, and *c* is obtained using the equation

$$\Phi_{y}^{0} = a + b(T - 298) + c(T - 298)^{2}$$
(10)

and it is evident from the above equation that the coefficients can be considered as the value of the limiting molar volume from (288.15 to 318.15) K. Further discussion on the influence of temperature on the limiting molar volumes is

Table 7. Parameters of Equation 10 and the Volume Expansibility of (1) MnCl<sub>2</sub> and Glycylglycine (2) in Water (3) at T = (288.15 to 318.15) K

	•	· · ·			· · · · · · · · · · · · · · · · · · ·
	а	b	С	σ	$\alpha_V^{o} \cdot 10^3$
salt/dipeptide	$cm^3 \cdot mol^{-1}$	$\overline{\text{cm}^3 \cdot \text{mol}^1 \cdot \text{deg}^{-1}}$	$\overline{\text{cm}^3 \cdot \text{mol}^1 \cdot \text{deg}^{-2}}$	$\overline{\text{cm}^3 \cdot \text{mol}^{-1}}$	deg <sup>-1</sup>
		T/K =	288.15		
MnCl <sub>2</sub> •4H <sub>2</sub> O	$22.60\pm0.3$	$-0.383 \pm 0.005$	-0.0022	0.055	$-14.30\pm0.2$
glycylglycine	$24.51\pm0.4$	$-0.678 \pm 0.002$	-0.0030	0.076	$-22.15\pm0.3$
		T/K =	293.15		
MnCl <sub>2</sub> •4H <sub>2</sub> O	$21.73 \pm 0.2$	$-0.374 \pm 0.005$	-0.0021	0.052	$-15.50 \pm 0.3$
glycylglycine	$24.07\pm0.4$	$-0.583 \pm 0.003$	-0.0029	0.064	$-24.26\pm0.4$
		T/K =	298.15		
MnCl <sub>2</sub> •4H <sub>2</sub> O	$21.42 \pm 0.4$	$-0.368 \pm 0.003$	-0.0020	0.047	$-16.16 \pm 0.4$
glycylglycine	$23.67\pm0.2$	$-0.492 \pm 0.004$	-0.0028	0.052	$-25.49\pm0.2$
		T/K =	303.15		
MnCl <sub>2</sub> •4H <sub>2</sub> O	$22.36\pm0.3$	$-0.415 \pm 0.002$	-0.0022	0.052	$-14.43 \pm 0.3$
glycylglycine	$24.38\pm0.2$	$-0.541 \pm 0.005$	-0.0030	0.070	$-23.06\pm0.4$
		T/K =	308.15		
MnCl <sub>2</sub> •4H <sub>2</sub> O	$23.16 \pm 0.3$	$-0.547 \pm 0.002$	-0.0024	0.057	$-13.08 \pm 0.3$
glycylglycine	$25.24\pm0.2$	$-0.596 \pm 0.003$	-0.0031	0.085	$-20.38\pm0.5$
		T/K =	313.15		
MnCl <sub>2</sub> •4H <sub>2</sub> O	$23.92 \pm 0.2$	$-0.589 \pm 0.004$	-0.0025	0.058	$-12.76 \pm 0.4$
glycylglycine	$25.87\pm0.4$	$-0.610 \pm 0.003$	0.0032	0.087	$-19.52\pm0.3$
		T/K =	318.15		
MnCl <sub>2</sub> •4H <sub>2</sub> O	$24.41 \pm 0.4$	$-0.634 \pm 0.005$	-0.0026	0.059	$-11.26 \pm 0.4$
glycylglycine	$26.65\pm0.5$	$-0.623 \pm 0.004$	-0.0034	0.089	$-18.37\pm0.2$

possible using the volume expansibility defined for the limiting apparent molar volumes, by eq 11.

$$\alpha_v^0 = (d\Phi_v^0/dT)_p/\Phi_v^0 \tag{11}$$

It is evident that the values of the temperature coefficient depend on temperature. Moreover, their absolute values increase slightly with increasing temperature. The respective values derived for 288.15 K, 293.15 K, 298.15 K, 303.15 K, 308.15 K, 313.15 K, and 318.15 K are listed in Table 7. This relation is generally well described for solutions of electrolytes by the empirical relationship

$$\Phi_{\rm v} = \Phi_{\rm v}^{\rm o} + S_{\rm v} c^{1/2} \tag{12}$$

known as the Masson equation,<sup>24</sup> where  $\Phi_V^o$  is the apparent molar volume of the salt at infinite dilution which is equal to the respective limiting partial molar volume; *c* is the molar concentration; and  $S_V$  is the slope of the linear plot. Moreover, the data obtained from eq 12 are from a temperature range of (288.15 to 318.15) K.

Figure 1 demonstrates the variation of apparent molar volume  $\Phi_V$ , slope  $S_V$ ,  $a_V$ , and  $b_V$  against temperature of an ionic solute



**Figure 1.** Variation of Masson's parameters with temperature for  $\blacksquare$ ,  $\Phi_V$ ;  $\bullet$ ,  $S_V$ ;  $\bullet$ ,  $a_V$ ; and  $\lor$ ,  $b_V$  at a concentration of 0.25 M MnCl<sub>2</sub>.



**Figure 2.** Variation of Masson's parameters with temperature for  $\blacksquare$ ,  $\Phi_V$ ;  $\bullet$ ,  $S_V$ ;  $\bullet$ ,  $a_V$ ; and  $\lor$ ,  $b_V$  at a concentration of 0.020 M glycylglycine.

MnCl<sub>2</sub> which depends strongly on the concentration. The plots for MnCl<sub>2</sub> are linear in the cases of  $a_V$  and  $b_V$  over the whole temperature range of (288.15 to 318.15) K and the linear relationship

$$\Phi_{\rm V}^{\rm o} = a_{\rm V} + b_{\rm V} c^{1/2} \tag{13}$$

similar in its algebraic nature to the Masson equation (eq 12) is valid. Figure 2 explains the variations of  $\Phi_V$ ,  $S_V$ ,  $a_V$ , and  $b_V$  of glycylglycine which may be due to the presence of amino groups in it. The coefficients of eq 13 are plotted in Figure 1 and Figure 2, respectively. The intercepts of the plots have no physical meaning; i.e., they cannot be considered as the limiting values of the apparent molar volumes of MnCl<sub>2</sub> and glycylglycine because they both consist of independent charge contributions.

The decrease in the apparent molar compressibility indicates strong interaction with the solvent to give a less compressible environment for the solute.<sup>1,2</sup> This may also be produced by electrostriction and structure breaking. The Kirkwood model<sup>19</sup> provides an interpretation for the apparent molar compressibility

values. The electrostricted water has a less open structure as compared to bulk water and is therefore less compressible. The bulk water becomes like electrostricted water upon addition of MnCl<sub>2</sub>, and this accounts for the apparent molar compressibilities of glycylglycine in water varying with the corresponding ones in mixed solvents. The decrease in intermolecular free length and adiabatic compressibility is due to the solvent-solute interaction, and there also exists a dipole-dipole interaction.<sup>24-26</sup> This indicates that the molecules are nearer in the system. Specific acoustic impedance is a quantity depending on the molecular packing of the system. The increase in the specific acoustic impedance suggests the presence of a strong interaction through hydrogen bonding.<sup>25,26</sup> This can also be attributed in the light of Eucken's theory<sup>26</sup> which states that there is a decrease in the number of aggregates of solvent molecules as the concentration and temperature increase. Consequently, water starts behaving like an unassociated liquid as the temperature rises. Further, the addition of a salt to a solvent enhances the process of breaking of aggregates of solvent molecules. Relative association is found to increase with an increase in concentration of MnCl<sub>2</sub> and glycylglycine in both cases while showing a regular trend in the breaking up of the solvent aggregates.<sup>25</sup> As the temperature of solution rises, the aggregates of solvent molecules break up themselves, resulting in increased solvent molecules. For all concentrations, the values of  $R_A$  increase with an increase in the temperature.<sup>26-28</sup> This indicates the decrease in degree of dissociation of aggregates of solvent molecules with an increase in temperature. The structure forming tendency of a solute can be determined by its solvation number. The solvation number increases with an increase in the concentration and temperature in cases one and two, and it is positive for all the concentrations. The positive solvation number indicates structure making tendency of the solute.

## Conclusions

The study of the viscosities, ultrasonic velocities, densities, and refractive indices of glycylglycine and  $MnCl_2$  in various concentrations and temperatures reveals the characteristics and structural properties prevalent in water. It also indicates the presence of interactions between solute, solvent, and substrate. These interactions also suggest the formation of hydrogen bonding in some cases and the extent to which the bonding accelerates the physical property. It is evident from the above study that the interactions of dipeptide and transition metal salt in water show tendencies of structure making of solute and solvent molecules together with solute–solute and solute– solvent interactions.

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