

# Adsorption Equilibrium, Kinetics, and Enthalpy of N<sub>2</sub>O on Zeolite 4A and 13X

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The adsorption equilibrium, kinetics, and enthalpy of nitrous oxide adsorption on zeolites 4A and 13X were measured volumetrically at temperatures of (194, 237, and 298) K and gas pressure up to 108 kPa. It was found that zeolite 4A adsorbs more N<sub>2</sub>O than 13X in all of the conditions used. The Langmuir, Freundlich, and Toth isotherm models were employed to correlate the adsorption isotherms. N<sub>2</sub>O diffusivity in these adsorbents at 298 K was calculated from the adsorption kinetic uptake curves by using a simple micropore diffusion model. It was found that the average diffusivity values in zeolite 4A and 13X are  $(3.38 \cdot 10^{-14}$  and  $1.05 \cdot 10^{-12}) \text{ m}^2 \cdot \text{s}^{-1}$ , respectively. The heat of adsorption values are between  $(-33$  and  $-21) \text{ kJ} \cdot \text{mol}^{-1}$  for zeolite 4A and  $(-28$  and  $-22) \text{ kJ} \cdot \text{mol}^{-1}$  for 13X for adsorption loadings between  $(0.5$  and  $3.5) \text{ mmol} \cdot \text{g}^{-1}$ .

## 1. Introduction

Nitrous oxide (N<sub>2</sub>O) is one of the major industrial byproduct gases that is generated from industrial synthesis facilities for producing nitric acid, adipic acid, or nylon.<sup>1,2</sup> It is identified as a very acute greenhouse gas that is 150 times stronger than that of carbon dioxide.<sup>3,4</sup> Besides having the greenhouse gas properties, it can also deplete the ozone layer, thereby making it one of the worst polluting gases of the present industrial age. Until today, the key technology for preventing N<sub>2</sub>O from mixing into the main airstream is reduction or decomposition over a suitable catalyst, which is commonly known as an “end-of-pipe” treatment.<sup>5</sup>

The catalysts that have been employed for the reduction of N<sub>2</sub>O include zirconia,<sup>6</sup> platinum,<sup>7,8</sup> or  $\alpha$ -manganese sesquioxide<sup>9</sup> in old times. In modern days, the catalysts that have been introduced successfully for the reduction of N<sub>2</sub>O are the MFI type of zeolites, mainly Fe-ZSM-5, used at about 773 K in the presence of a small amount of NO<sub>x</sub> as a promoter.<sup>10–16</sup> Very recently, it has been claimed that a bimetallic ferrierite (FER) catalyst containing iron and ruthenium increases the catalytic activity.<sup>17</sup> Despite the major progress in the technology of catalytic removal of N<sub>2</sub>O, the main drawback of this method is that the high temperatures required in these processes greatly increase the cost of the system.<sup>18</sup> Moreover, in the catalytic reduction process, N<sub>2</sub>O cannot be recovered, as it could be reutilized as an intermediate for the synthesis of some valuable fine chemicals.<sup>19,20</sup>

The removal of N<sub>2</sub>O by adsorption in porous materials is uncommon as compared to the catalytic reduction strategy. Adsorption of N<sub>2</sub>O in silicalite-1 was performed by Groen et al.<sup>5</sup> over the temperature range of (273 to 398) K and pressure up to 120 kPa, and the adsorption capacity of N<sub>2</sub>O obtained was  $2.5 \text{ mol} \cdot \text{kg}^{-1}$  at 273 K. The Henry's law constant and enthalpy of adsorption were also calculated to characterize the gas–solid interactions. Different varieties of activated carbon were evaluated for N<sub>2</sub>O adsorption by Peng et al.<sup>21</sup> over the temperature range of (195 to 323) K and pressures up to 101 kPa. The N<sub>2</sub>O adsorption capacities were reported to be within  $(12$  to  $18) \text{ mol} \cdot \text{kg}^{-1}$  with a typical type III isotherm for all of

the activated carbon adsorbents. MOF-5, MOF-177, and zeolite 5A were employed for the adsorption of N<sub>2</sub>O by Saha et al.<sup>18</sup> The highest adsorption capacity was obtained on zeolite 5A (mass fraction,  $w = 0.177$ ), followed by MOF-5 ( $w = 0.044$ ) and MOF-177 ( $w = 0.003$ ) at an ambient temperature and N<sub>2</sub>O gas pressure up to 1 bar. They also calculated the intracrystalline diffusivity of N<sub>2</sub>O within the adsorbents, and those were reported as  $(1.9 \cdot 10^{-11}$ ,  $1.1 \cdot 10^{-9}$ , and  $2.2 \cdot 10^{-9}) \text{ m}^2 \cdot \text{s}^{-1}$  for zeolite 5A, MOF-5, and MOF-177, respectively.<sup>18</sup> The adsorption of N<sub>2</sub>O was also reported in certain types of pseudomorphs by Lamb and West.<sup>22</sup>

The objective of this study is to measure the adsorption equilibrium and kinetics of nitrous oxide on zeolite 4A and 13X. The adsorption equilibrium was measured volumetrically at three different temperatures, (194, 237, and 298) K, and kinetic data were measured at 298 K and N<sub>2</sub>O pressure up to 108 kPa. The heat of adsorption was calculated from the adsorption isotherms at the three temperatures, which allows us to compare the adsorbate–adsorbent interaction. The diffusivity values of N<sub>2</sub>O in the adsorbents were estimated from the kinetic data. These data will provide necessary information for the adsorbent selection and performance comparison; they will also help us to understand the adsorption fundamentals.

## 2. Experimental Section

The two zeolite samples (4A and 13X) were kindly provided by Mr. Li Shenan of Nanjing Refinery, SINOPEC, China.

**2.1. Adsorption Experiments.** The equilibrium and kinetics of nitrous oxide adsorption on both adsorbents were measured volumetrically in a Micromeritics ASAP 2020 surface area and porosity analyzer. Adsorption isotherms were measured at three temperatures, (194, 237, and 298) K, and N<sub>2</sub>O pressures up to 108 kPa. The temperature of the sample bath was constantly monitored with the help of a thermocouple, and it was observed that the temperature variation was no more than  $\pm 1$  K for experiments at 298 K and  $\pm 2$  K for experiments at (237 and 194) K, respectively. These temperatures [(194, 237, and 298) K] were achieved by using dry ice, a solid form of a commercially available engine coolant, and room temperature water, respectively. Kinetic data were recorded during the isotherm measurements at 298 K and four different pressures. The zeolite samples were activated at 623 K under a vacuum

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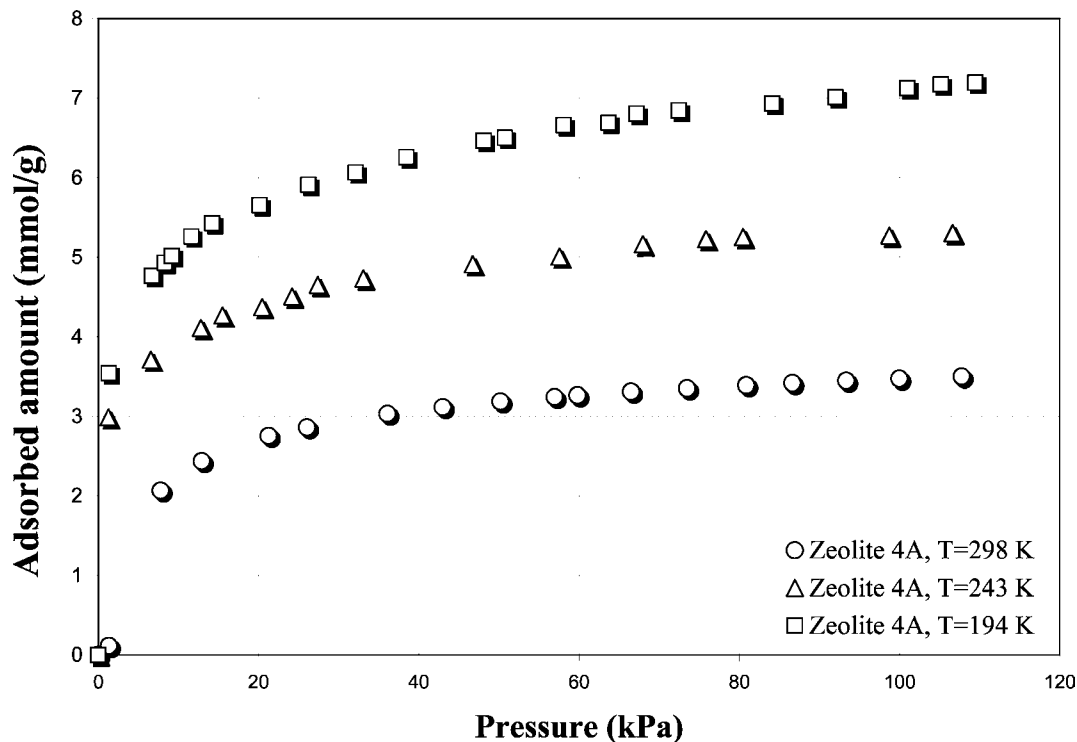


Figure 1.  $N_2O$  adsorption isotherms in zeolite 4A at (298, 237, and 194) K.

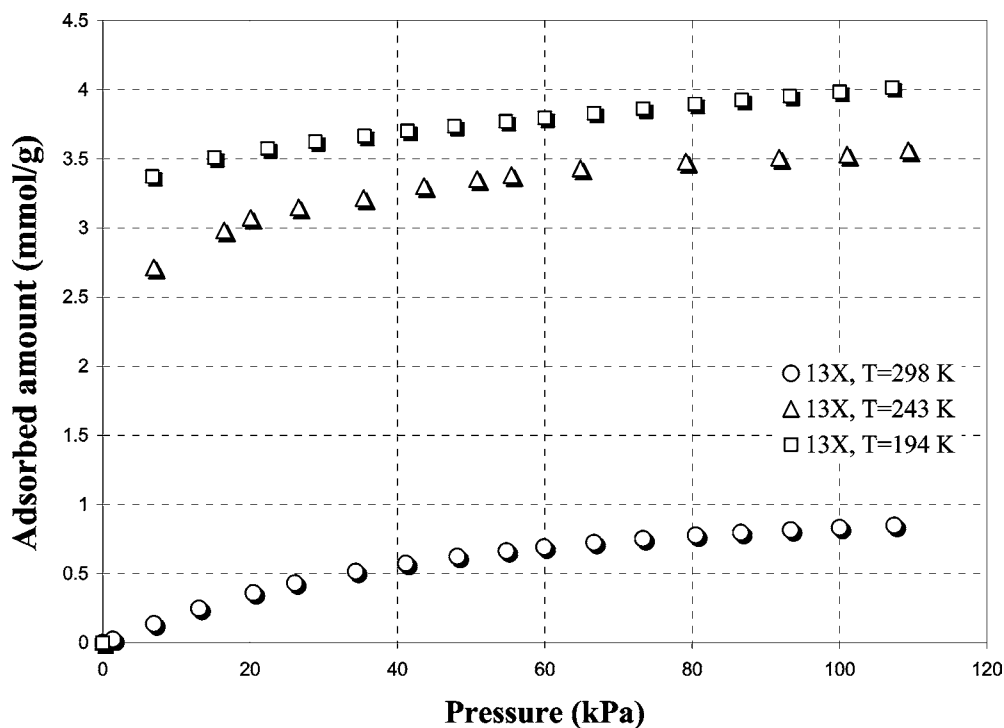


Figure 2.  $N_2O$  adsorption isotherms in 13X at (298, 237, and 194) K.

( $1.33 \cdot 10^{-6}$  kPa) for 12 h before the adsorption measurements. High purity nitrous oxide (99+ %) was introduced into a gas port of the adsorption unit for the adsorption measurements. To ensure that the instrument is measuring each data point accurately, it was calibrated by employing two standards which were provided by the instrument manufacturing company, and it was found that the measured values are within  $\pm 2$  % error with the given values. Each of the isotherms reported in this paper is repeated thrice, and it was noticed that the data points vary no more than  $\pm 1$  %.

### 3. Results and Discussion

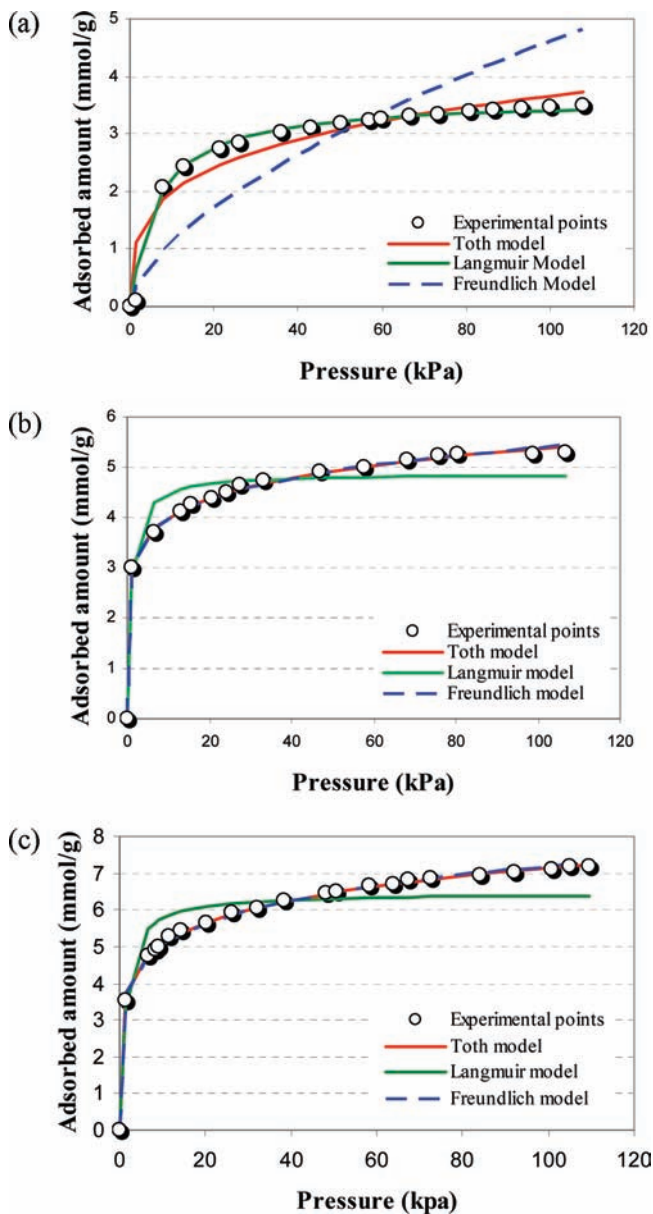
**3.1. Adsorption Equilibrium.** Adsorption isotherms of nitrous oxide on both zeolite 4A and 13X at (298, 237, and 194) K are shown in Figures 1 and 2, respectively. All of the isotherms are of type I according to the IUPAC nomenclatures. It is observed from the isotherms shown in Figures 1 and 2 that zeolite 4A adsorbs more  $N_2O$  than 13X. The adsorption amounts at (298, 237, and 194) K and a  $N_2O$  pressure of 107 kPa are (3.49, 5.3, and 7.29)  $\text{mmol} \cdot \text{g}^{-1}$  for zeolite 4A, as compared to

**Table 1. Isotherm Model Parameters for Zeolite 4A**

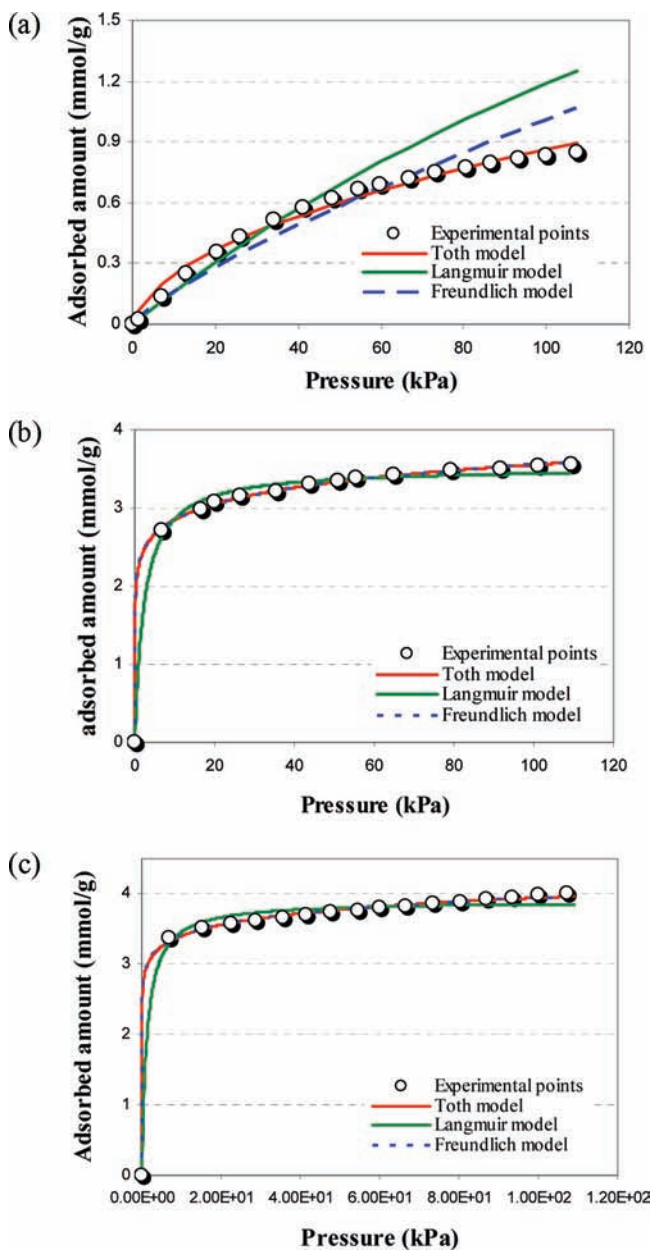
isotherm model	model parameters	temperature (K)	parameter values	ARE %
Langmuir model	$a_m$	298	3.604	6.59
	$b$		0.166	
	$a_m$	237	4.873	28.30
	$b$		1.159	
Freundlich model	$a_m$	194	6.464	44.55
	$b$		0.829	
	$k$	298	0.274	61.83
	$n$		1.630	
$k$	237	2.930		
Toth model	$k_T$	298	0.434	19.08
	$\alpha_T$		399.468	
	$t$		0.060	4.43
	$k_T$	237	0.163	
$\alpha_T$		399.49		
Toth model	$k_T$	194	0.199	3.32
	$\alpha_T$		399.42	
	$t$		0.030	4.43
	$t$		0.038	

**Table 2. Isotherm Model Parameters for 13X**

isotherm model	model parameters	temperature (K)	parameter values	ARE %
Langmuir model	$a_m$	298	4.304	13.03
	$b$		0.003	
	$a_m$	237	3.517	6.19
	$b$		0.433	
Freundlich model	$a_m$	194	3.900	7.56
	$b$		0.782	
	$k$	298	0.026	6.98
	$n$		1.259	
$k$	237	2.275		
Toth model	$k_T$	194	2.945	2.35
	$\alpha_T$		10.298	
	$k_T$	298	1.984	2.55
	$\alpha_T$		136.84	
Toth model	$k_T$	237	0.140	1.63
	$\alpha_T$		134.334	
	$t$		0.0256	2.27
	$t$		0.073	
Toth model	$k_T$	194	0.073	2.27
	$\alpha_T$		134.35	
	$t$		0.018	2.27
	$t$		0.018	



**Figure 3.** Comparison isotherm model parameters for zeolite 4A at 298 K (a), 237 K (b), and 194 K (c).



**Figure 4.** Comparison isotherm model parameters for 13X at 298 K (a), 237 K (b), and 194 K (c).

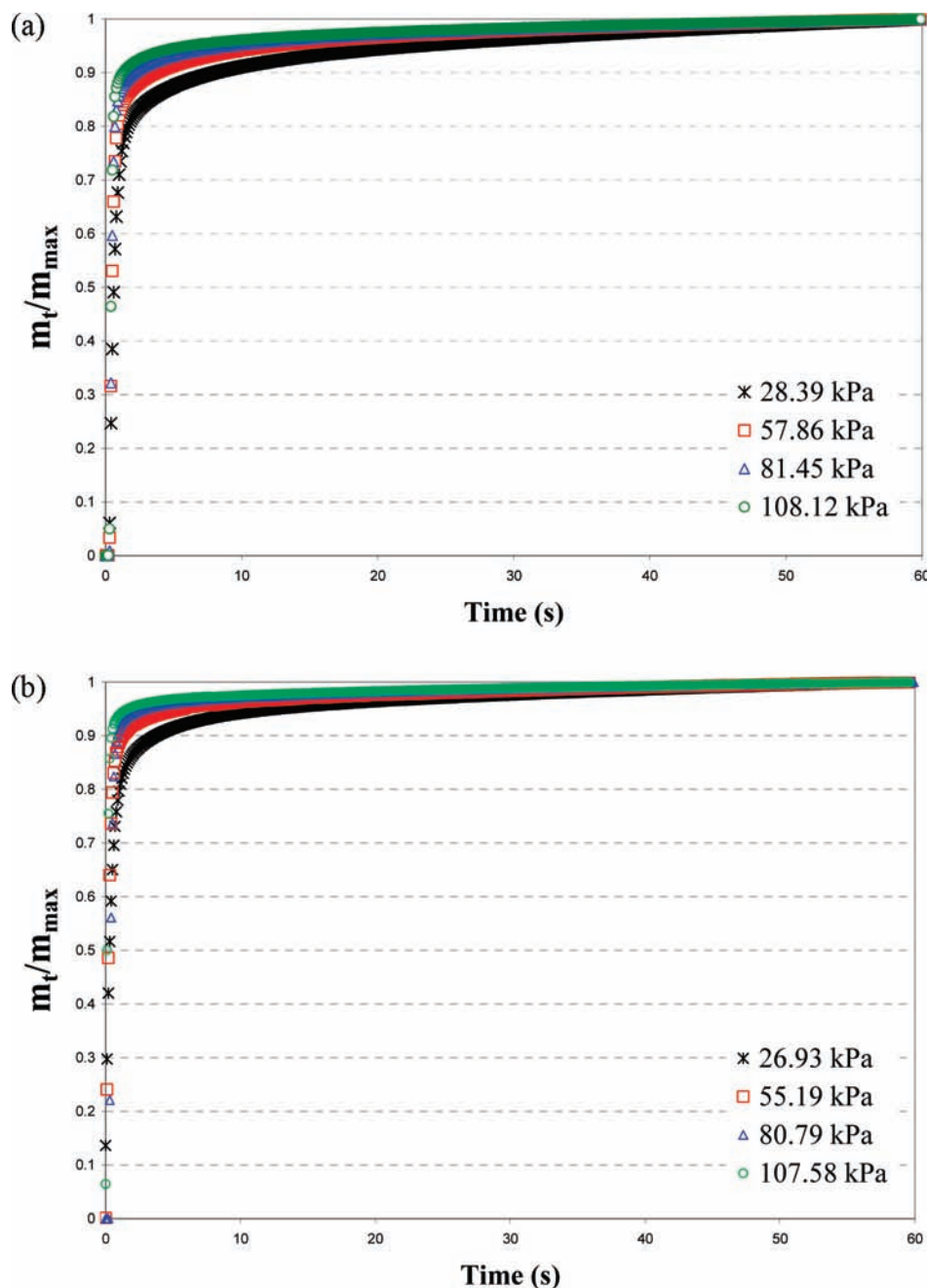


Figure 5. Kinetic plots of  $\text{N}_2\text{O}$  adsorption on to zeolite 4A (a) and 13X (b).

(0.84, 3.58, and 3.96)  $\text{mmol}\cdot\text{g}^{-1}$  for 13X. The  $\text{N}_2\text{O}$  adsorption capacity at 298 K and  $\text{N}_2\text{O}$  pressure about 1 bar on 4A is higher than that of silicalite-1 (around  $1.75 \text{ mmol}\cdot\text{g}^{-1}$ ) reported by Groen et al.<sup>5</sup> but lower than that of zeolite 5A ( $4.03 \text{ mmol}\cdot\text{g}^{-1}$ ) reported by Saha et al.<sup>18</sup> However, the  $\text{N}_2\text{O}$  uptake by both zeolite 4A and 13X is significantly higher than that of the metal–organic framework MOF-5 ( $1 \text{ mmol}\cdot\text{g}^{-1}$ ) and MOF-177 ( $0.07 \text{ mmol}\cdot\text{g}^{-1}$ ) at similar conditions.<sup>18</sup> The highest adsorption amount at the terminal pressure measured in this work is lower than the values on activated carbon reported by Peng et al.,<sup>21</sup> but because of the typical type-III nature of their isotherms, the adsorption amount seems to be greater on zeolites 4A and 13X at the lower pressure range.

The adsorption isotherms obtained in this work were correlated with the Langmuir, Freundlich, and Toth isotherm equations. The Langmuir equation is given by

$$q = \frac{a_m b p}{1 + b p} \quad (1)$$

where  $a_m$  ( $\text{mmol}\cdot\text{g}^{-1}$ ) is the monolayer adsorption capacity and  $b$  ( $\text{kPa}^{-1}$ ) is the Langmuir adsorption equilibrium constant. Both parameters can be determined from the slope and intercept of a linear plot of  $1/p$  versus  $1/q$ .

The Freundlich model can be written as

$$q = k p^{1/n} \quad (2)$$

where  $k$  and  $n$  are the equation model parameters which can be calculated from a linear plot of  $\ln p$  versus  $\ln q$ .

The Toth model can be given by

$$q = \frac{\alpha_T p}{(k_T + p^t)^{1/t}} \quad (3)$$

where  $\alpha_T$ ,  $k_T$ , and  $t$  are equation constants which can be

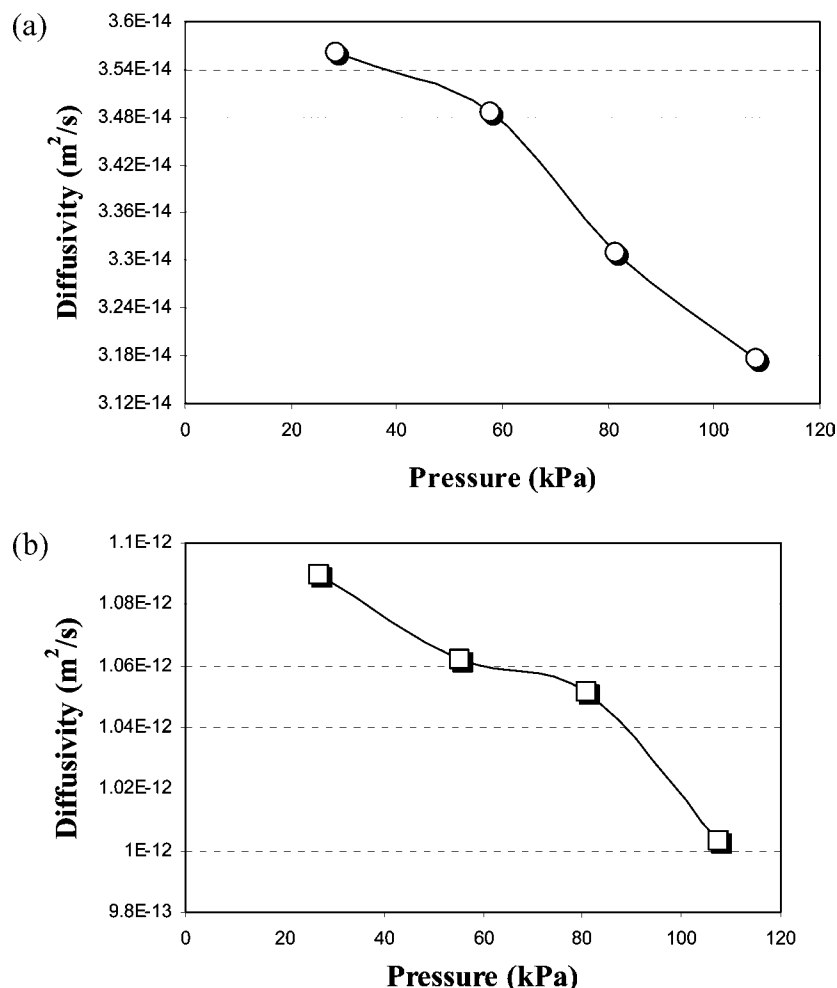


Figure 6. Variation of N<sub>2</sub>O diffusivity with pressure for zeolite 4A (a) and 13X (b).

determined by nonlinear regressions. The degree of model fitting was compared by the absolute relative error (ARE) percent, calculated as

$$\text{ARE \%} = \frac{\sum_{n=1}^N |x_{\text{exp}} - x_{\text{mod}}|}{N} \cdot 100 \% \quad (4)$$

where  $x_{\text{exp}}$  is the experimental point,  $x_{\text{mod}}$  is the modeling point, and  $N$  is the number of points in the isotherm.

Tables 1 and 2 summarize the isotherm model parameters and ARE values for zeolite 4A and 13X, respectively. Figures 3a–c and 4a–c compare the model fitting with the experimental values for zeolite 4A and 13X at (298, 237, and 194) K, respectively. From the tables, it is found that the Langmuir model fits better at 298 K for zeolite 4A; however, the Toth model seems to be better for the remaining isotherms on zeolite 4A. For 13X, the Toth model fits the best for all three isotherms.

**3.2. Adsorption Kinetics.** Adsorption kinetic data of nitrous oxide were collected at the same time, when the isotherms were generated at 298 K and pressure up to 108 kPa. Figure 5a,b shows the kinetic plots at four different pressure ranges for zeolite 4A and 13X, respectively. It is observed that zeolite 4A and 13X reached the adsorption saturation level within (50 to 60) s and (40 to 50) s, respectively. A classical micropore diffusion model was applied to analyze the kinetic data and to estimate the diffusivity of nitrous oxide in the zeolites. For fractional uptakes ( $m_t/m_\infty$ ) higher than 70 %, the diffusion model equation can be written as,<sup>23</sup>

$$1 - \frac{m_t}{m_\infty} = \frac{6}{\pi^2} \exp\left(\frac{-\pi^2 D_c t}{r_c^2}\right) \quad (5)$$

where  $D_c$  is the intracrystalline diffusivity,  $r_c$  is the equivalent crystal radius, and  $t$  is time. The diffusion time constants ( $D_c/r_c^2$ ) and  $s^{-1}$  were calculated from the slope of a linear plot of  $\ln(1 - (m_t/m_\infty))$  versus  $t$  at a given N<sub>2</sub>O pressure. It has been found from the scanning electron microscopy images that the zeolite 4A and 13X samples possess the equivalent crystalline radius of ( $2.5 \cdot 10^{-6}$  and  $2.54 \cdot 10^{-5}$ ) m, respectively. From these crystal radius size values, the average diffusivity of N<sub>2</sub>O in zeolite 4A and 13X is calculated to be ( $3.38 \cdot 10^{-14}$  and  $1.05 \cdot 10^{-12}$ ) m<sup>2</sup>·s<sup>-1</sup>, respectively. Both of these values are lower than that of zeolite 5A, MOF-5, and MOF-177, reported by Saha et al.<sup>18</sup> It is quite challenging to explain the difference between the diffusivity values within these zeolite samples, but most probably, the smaller pore opening of zeolite 4A is responsible for the slower kinetics as compared with 13X. The variations of diffusivity with pressure as shown in Figure 6a,b for zeolite 4A and 13X. It is observed that the diffusivity values decrease with the increase in pressure. This trend is probably attributed to the fact that the pores of the zeolites materials were partially saturated and blocked at the higher adsorption loading at higher pressures.

**3.3. Isotheric Heat of Adsorption.** The isotheric heat of adsorption values are a quite important parameter revealing the adsorbate–adsorbent interactions. Isotheric heat of adsorption can be calculated from the van't Hoff equation:

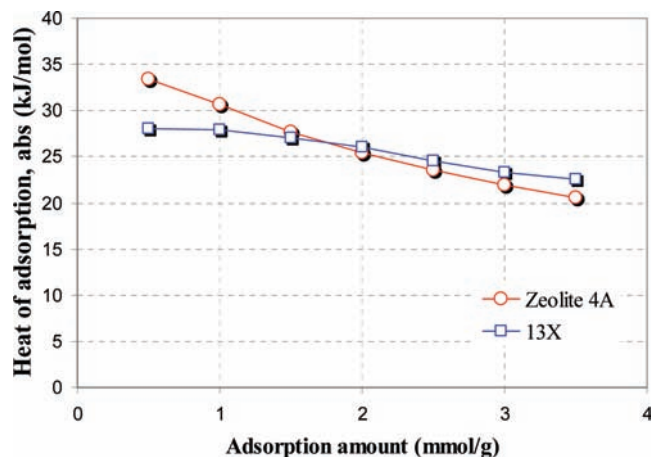


Figure 7. Heat of  $N_2O$  adsorption for zeolite 4A and 13X.

$$\frac{\Delta H}{RT^2} = -\left(\frac{\partial \ln P}{\partial T}\right)_a \quad (6)$$

where  $\Delta H$  is the isosteric heat of adsorption ( $\text{kJ}\cdot\text{mol}^{-1}$ ),  $P$  is gas pressure (kPa),  $T$  is temperature, and  $a$  is the adsorption amount ( $\text{mmol}\cdot\text{g}^{-1}$ ). The integration of eq 6 yields:

$$\ln P = \frac{\Delta H}{RT} + C \quad (7)$$

where  $C$  is an integration constant. In this work, the isotherms at (194, 237, and 298) K were employed to calculate the heat of adsorption values. The isotherm data points were first converted to a set of isosters (linear plot of  $\ln P$  versus  $1/T$ ) and then correlated with eq 7, and the heat of adsorption was then calculated from the slope of the isosters according to eq 7. The variation of heat of adsorption with adsorption loadings is then plotted in Figure 7. It is observed that these values were almost in the same range for both kinds of materials, ( $-33$  to  $-21$ )  $\text{kJ}\cdot\text{mol}^{-1}$  for zeolite 4A and ( $-28$  to  $-22$ )  $\text{kJ}\cdot\text{mol}^{-1}$  for 13X within the adsorption loading of (0.5 to 3.5)  $\text{mmol}\cdot\text{g}^{-1}$ , suggesting that  $N_2O$  interacts with the two zeolites similarly.

#### 4. Conclusions

It is observed that zeolite 4A adsorbs  $N_2O$  more than the 13X sample at (194, 237, and 298) K and  $N_2O$  pressures up to 108 kPa. The highest  $N_2O$  uptake on 4A,  $7.2 \text{ mmol}\cdot\text{g}^{-1}$ , as compared with  $4 \text{ mmol}\cdot\text{g}^{-1}$  on 13X was obtained at 194 K and 108 kPa. All of the isotherms were modeled by Langmuir, Freundlich, and Toth models, and it was found that the Toth model fits the best for most of the isotherms. A kinetic study reveals that the average diffusivity of  $N_2O$  in zeolite 4A and 13X was ( $3.38\cdot 10^{-14}$  and  $1.05\cdot 10^{-12}$ )  $\text{m}^2\cdot\text{s}^{-1}$ , respectively. The slower kinetics in zeolite 4A is probably caused by its narrower pore opening. The diffusivity values decrease with  $N_2O$  pressure for both zeolites, which is probably caused by the partial pore blocking at the greater adsorption amount at higher pressures. The heat of adsorption values were calculated to be ( $-33$  to  $-21$ )  $\text{kJ}\cdot\text{mol}^{-1}$  for zeolite 4A and ( $-28$  to  $-22$ )

$\text{kJ}\cdot\text{mol}^{-1}$  for 13X within the adsorption loading of (0.5 to 3.5)  $\text{mmol}\cdot\text{g}^{-1}$ . The similar heat of adsorption values suggest that  $N_2O$  interacts with both zeolites similarly.

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Received for review January 29, 2010. Accepted April 03, 2010.

JE100105Z