# Gaseous pvTx Properties of Mixtures of Carbon Dioxide and Propane with the Burnett Isochoric Method 

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#### Abstract

The gaseous pvTx properties of $\mathrm{CO}_{2}$ (1, CAS No. 124-38-9) + propane (2, CAS No. 74-98-6) mixtures were measured using the Burnett-isochoric method with 225 data points obtained for temperatures from (320 to 400 ) K, pressures up to 7784 kPa , and densities up to $141 \mathrm{~kg} \cdot \mathrm{~m}^{-3}$ at $x_{1}=0.5158$ and $x_{1}=0.8017$. Burnett measurements for argon (CAS No. 7440-37-1) were conducted at 319 K and for $\mathrm{CO}_{2}$ at 343 K . The $p v T$ properties and virial coefficients of argon and $\mathrm{CO}_{2}$ agreed well with literature results when the effective cell constant for each fluid instead of that of the helium calibration was used in the density calculations. The temperature, pressure, density, and mole fraction uncertainties were estimated to be $\pm 5 \mathrm{mK}, \pm 300$ $\mathrm{Pa}, \pm 0.05 \%$, and $\pm 0.01 \%$, respectively. A truncated virial equation was used to correlate the experimental $p v T x$ data of $\mathrm{CO}_{2}+$ propane mixtures with root-mean-square deviations of $\pm 0.03 \%$. The second and third virial coefficients for the binary mixtures were also determined.


## Introduction

Environmentally friendly working substances have succeeded in preventing the ozone layer from being destructed by anthropogenic chemicals, and they are also important in decelerating the climate change. Natural refrigerants such as hydrocarbons, carbon dioxide, and ammonia have attracted increasing attention because of their zero ozone-depletion potentials and low global-warming potentials. ${ }^{1}$ However, the disadvantages of each pure natural refrigerant have restricted their wide applications. Mixtures are one option to provide useful refrigerants. Binary mixtures of carbon dioxide and propane are promising alternative refrigerants to replace R13 in low temperature cycles when the evaporator temperature is higher than $201 \mathrm{~K},{ }^{2}$ and these mixtures can also be used as solvents to extract oil from seeds. ${ }^{3,4}$

Various pvTx measurements ${ }^{5-9}$ and cross virial coefficient data ${ }^{10-14}$ have been published for such mixtures for the liquid and/or gaseous phases since 1951. However, the published gaseous $p v T x$ data for this mixture shows a maximum discrepancy larger than $2 \%,{ }^{8}$ which is not precise enough to establish an equation of state. There are only 15 data points for the second cross virial coefficient for the limited temperature range from (273 to 333) K with an uncertainty larger than $\pm 5 \mathrm{~cm}^{3} \cdot \mathrm{~mol}^{-1} .{ }^{15}$ Thus, the Burnett isochoric method was used here to precisely measure the gaseous $p v T x$ properties of $\mathrm{CO}_{2}+$ propane mixtures for temperatures from ( 320 to 400 ) K and pressures up to 7784 kPa to provide more accurate $p v T x$ data and virial coefficients over a larger temperature range. To validate the results for mixtures reliably, the experimental system was tested with pure $\mathrm{CO}_{2}$ and argon.

## Experimental System

Apparatus. The Burnett isochoric coupling method was used for the measurements. A diagram of the apparatus is shown in Figure 1. The system was rebuilt from a previous system with

[^0]improved thermostatic baths, temperature measurement system, pressure measurement system, vacuum system, and data acquisition system as described by Feng et al. ${ }^{16}$ The system has been used to accurately measure vapor pressures of fluorinated propanes. ${ }^{17}$ The system used here was the same as that vapor pressure measurement system except for a new sensitive diaphragm pressure transducer with smaller random errors and zero drift.

The overall temperature uncertainty was estimated to be within $\pm 5 \mathrm{mK}$, including the $\pm 2 \mathrm{mK}$ uncertainty of the platinum resistance thermometer, the $\pm 0.3 \mathrm{mK}$ uncertainty of the thermometer bridge (model: MI 6242T), and the $\pm 3.4 \mathrm{mK}$ stability and uniformity uncertainty of the thermostatic bath. The temperature was determined on the basis of the International Temperature Scale of 1990 (ITS-90). Before the experiments, the platinum resistance thermometers, the thermometer bridge, and the digital manometers were calibrated by the National Institute of Metrology (NIM), China.

The pressure measurement system, which could measure pressures from ( 0 to 10 ) MPa , included an absolute digital manometer (model: Yokogawa, MT 210, ( 0 to 130 ) kPa), two gauge pressure digital manometers (model: Yokogawa, MT 210, ( 0 to 3500 ) kPa; Ruska, 7050 i , ( 0 to 10 ) MPa) and a sensitive diaphragm pressure transducer (model: Rosemount 3051S, ( 0 to 20) kPa ). The pressure uncertainty was estimated to be less than $\pm 300 \mathrm{~Pa}$ including the uncertainty of the absolute digital manometer of $\pm 30 \mathrm{~Pa}$ from ( 0 to 130 ) kPa , the uncertainty of the gauge pressure digital manometer (MT210) of $\pm 80 \mathrm{~Pa}$ from ( 0 to 3500 ) kPa , the uncertainties of the Ruska manometer of $\pm 0.005 \%$, and the uncertainty of the differential pressure detector of less than $\pm 20 \mathrm{~Pa}$.

A turbo-molecular pump (model: KYKY, FD 110) with an extreme vacuum of $1 \cdot 10^{-6} \mathrm{~Pa}$ provided the vacuum for the experimental system.

The Burnett apparatus including the two cells was made of 1 Cr 18 Ni 9 Ti stainless steel. The insides of the sample cell, B2, with a volume of 500 mL and the expansion cell, B1, with a volume of 200 mL were polished to reduce the physical


Figure 1. Burnett isochoric experimental apparatus: B, thermostatic bath; B1, expansion cell ( 200 mL ); B2, sample cell ( 500 mL ); CP, cooler; D, stirrer; DPI, differential pressure detector; H , heater; LN , liquid nitrogen; MTa, absolute pressure digital manometer; MTgL/MTgH, gauge pressure digital manometer for low and high pressures; NH, $\mathrm{N}_{2}$ bottle; NL, pressure damper; PC, personal computer; PG1, PG2, pressure gauges; ST, HART 1590 super thermometer; SW, selector switch; T, platinum resistance thermometer; TB, MI 6242 T thermometer bridge; V1 to V12, valves; VM, digital multimeter; VP, vacuum pump.
adsorption effects of experimental fluids onto the cell surfaces. Before the experiments, the two cells were rinsed with acetone and the experimental fluids to remove any residue from previous experiments. The valves in the Burnett system were changed in this work to reduce the microleakage.

A gas chromatograph (model: Shimadzu, GC 2014) with a thermal conductivity detector (TCD) and a $3 \mathrm{~m} \times 3 \mathrm{~mm}$ Porapak-Q column was used to measure the sample purities and the mixture compositions. Ultrapure helium (99.999 \%) was used as the carrier gas at a flow rate of $45 \mathrm{~mL} \cdot \mathrm{~min}^{-1}$. The column temperatures were programmed for each fluid from (308 to 373 ) K. The oven and TCD temperatures were set to 373 K . After injection of the sample into the column, the effluence was analyzed for 20 min . The impurity evaluations were based on the GC area ratios.
Samples. Helium and argon samples with stated mole purities of 99.999 \% were obtained from Air Products Corp. and Qianxi Corp., respectively. The $\mathrm{CO}_{2}$ sample was obtained from Beiwen Gas Corp. with the stated mole purity of $99.995 \%$. The propane sample was obtained from Huayuan Gas Corp. with the stated mole purity of $99.95 \%$. Helium and argon were used without further purification. The $\mathrm{CO}_{2}$ sample was also used without further purification except for being cooled in liquid nitrogen and evacuated by a vacuum pump to remove possible air impurities. The $\mathrm{CO}_{2}$ sample impurities measured by the GC system were less than $0.005 \%$. The propane was purified from $99.93 \%$ to $99.97 \%$ (percentages are in terms of the area ratios of the GC measurements, approximate to mole fraction) based on the different boiling points of propane and the impurities.
Absolute deviations of measured vapor pressures of propane samples are shown in Figure 2. The reference vapor pressures of propane were calculated from Lemmon and Goodwin. ${ }^{18}$ Several sets of representative accurate vapor pressures are also plotted in Figure 2. The vapor pressures of 99.93 \% propane showed small positive deviations below 360 K but were ( 3 to 6) kPa higher than other data near the critical region. Vapor pressures of purified propane ( $99.97 \%$ ) of this work matched well with the measured results of McLinden ${ }^{19}$ and Thomas and Harrison ${ }^{20}$ and the calculated value of Lemmon et al. ${ }^{21}$ Experimental vapor pressures from Kratzke ${ }^{22}$ were lower than


Figure 2. Absolute deviations of vapor pressures for propane: $\boldsymbol{\square}$, purified sample, $99.97 \%$; $\mathbf{\Delta}$, sample before purification, $99.93 \%$; ○, McLinden; ${ }^{19}$ $\square$, Thomas and Harrison; ${ }^{20} \Delta$, Kratzke; ${ }^{22}---$, Lemmon et al. ${ }^{21}$
the other results perhaps due to the systematic errors and/or impurities in the samples. The deviations of vapor pressures of purified and unpurified propane correlated well with the GC analysis results that the propane contained impurities with higher boiling points such as ethane.

Great efforts were made for the mixture measurements to prepare the samples with accurate mole fractions. The masses of $\mathrm{CO}_{2}$ and propane introduced into sample cell B 2 were determined by measuring the weight changes of cylinders containing each component using an accurate electronic balance (model: Mettler Toledo, PR 1203) with a precision of $\pm 0.001$ g . The cylinders were rinsed with the samples more than three times and evacuated to vacuum at a level lower than $5 \cdot 10^{-5}$ Pa . The mass of the cylinders was carefully measured to exclude systematic errors. Possible errors can occur due to (1) adsorption of water on the surface of the cylinders after cooling with liquid nitrogen, (2) microleakage of the cylinder valves and cylinders, one cylinder accidently having sand holes resulting in leakage, and (3) the position and direction of the cylinders on the balance. In this work, the masses were measured more than three times to obtain an accurate initial mole fraction for the mixtures. During each Burnett expansion procedure, the expansion valve V1 was open for more than 45 min with the thermostatic bath
temperature controlled to maintain the constant mole fraction, and after measurement of each density, the samples in the expansion cell B1 were collected in a cooled, evacuated cylinder and then heated to room temperature and introduced into the GC system to measure the mole fraction. The uncertainty of the calculated mixture compositions was estimated to be less than $\pm 0.0001$ mole fraction, and the GC results showed a stable mole fraction during the Burnett expansion procedures.

## Experimental Procedure and Validation

The Burnett isochoric method developed by Burnett in $1963^{23}$ is a traditional method for accurate $p v T(x)$ measurements. First, the temperature and pressure were measured on an isochoric line, and then the samples were expanded from the sample cell to expansion cell at the highest temperature to reduce the density. The isothermal expansion was repeated for several isochors to obtain temperatures and pressures for the whole measured region. The densities were calculated as:

$$
\begin{equation*}
\rho_{i}=\frac{p_{i}}{Z_{i} R T}=\frac{1}{N^{i} A R T} \tag{1}
\end{equation*}
$$

where $\rho_{i}$ denotes the molar density, $p_{i}$ is the pressure, $Z_{i}=p_{i} /$ $\rho_{i} R T$ is the compressibility factor, $R$ is the universal gas constant, $T$ is the temperature, $N$ is the cell constant, and $i$ is the expansion number.

$$
\begin{equation*}
N \equiv \frac{V_{1}+V_{2}}{V_{2}} \tag{2}
\end{equation*}
$$

where $V_{1}$ is the volume of cell B 1 and $V_{2}$ is the volume of cell B2.
$A$ is the gas-filled constant:

$$
\begin{equation*}
\frac{1}{A}=\lim _{p_{i} \rightarrow 0} p_{i} N^{i} \tag{3}
\end{equation*}
$$

Theoretically, the cell constant $N$ is a function of only the experimental volumes of the cells and does not change with the experimental fluid. Since the two cells were made of the same stainless steel, our experience is that the cell constant was independent of temperature but a weak function of pressure:

$$
\begin{equation*}
N\left(p_{i-1}, p_{i}\right)=N_{0} \frac{1+m p_{i}}{1+m p_{i-1}} \tag{4}
\end{equation*}
$$

where $m$ is a constant calculated from the mechanical properties of the material of the cells and $N_{0}=\lim _{p_{i} \rightarrow 0} p_{i-1} / p_{i}$. Accurate cell constants are usually obtained using helium as the standard calibration gas in the Burnett method due to its small third virial coefficient and good linearity of $p_{i-1} / p_{i}$ versus $p_{i}$.
The gas-filled constant $A$ was fit from a least-squares program using experimental data for each experimental run.

The truncated virial equation, eq 5 , is usually used to describe the gaseous $p v T(x)$ properties. The second and third virial coefficients $B$ and $C$ can also been determined from eq 5 by analysis of the $(Z-1) / \rho$ versus $\rho$ plot along an isotherm,

$$
\begin{equation*}
(Z-1) / \rho=B+C \rho \tag{5}
\end{equation*}
$$

The second method to calculate the densities is to use data along an isochore starting with the density at the highest temperature ( 400 K ) determined from eq 1 for each Burnett expansion step combined with the calculated cell expansion characteristics for each temperature and pressure. The densities were calculated with both methods with differences within $\pm$ $0.05 \%$. The present densities from this work were calculated using the first method because the exact thermal expansion

Table 1. Helium Calibration Results

|  | pressure range |  | $B$ | $B^{15}$ | $B^{24}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| K | kPa | $N_{0}$ | $\mathrm{cm}^{3} \cdot \mathrm{~mol}^{-1}$ | $\mathrm{cm}^{3} \cdot \mathrm{~mol}^{-1}$ | $\mathrm{cm}^{3} \cdot \mathrm{~mol}^{-1}$ |
| 318.165 | 138 to 6676 | $1.378010 \pm 0.00002$ | $11.40 \pm 0.1$ | $11.67 \pm 0.3$ | 11.30 |
| 343.127 | 563 to 7534 | $1.378092 \pm 0.00005$ | $11.21 \pm 0.1$ | $11.55 \pm 0.3$ | 11.18 |

coefficient of the cell was unknown, and all of measured fluids were nonpolar with negligible adsorption on the cell surfaces.

The temperature and pressure data were recorded by a data acquisition system. During the high-pressure measurements, the operation should be done extremely carefully because dozens of openings and closings of the expansion valve V1 can cause abrasions of the needle inside the valve that may result in microleakage. As expansion cell B1 was evacuated, the pressures in sample cell B2 were also recorded to detect leakage.

Helium Calibration. Table 1 lists the detailed results of helium calibration before and after measurements of the mixtures at temperatures of (318 and 343) K. The second virial coefficients agreed well with the Dymond ${ }^{15}$ correlation and REFPROP $8.0^{24}$ as shown in Table 1 and Figure 3. The cell constant $N_{0}$ slightly shifted due to random errors or the abrasion of the needle in the expansion valve V1, resulting in small shifts of the cell volumes. In $p v T(x)$ measurements using the Burnett isochoric method, the experimental system uncertainties and the data reduction procedure are both important to obtain accurate data. Especially when $p v T(x)$ data are used to calculate the virial coefficients, the systematic and random errors may accumulate at low pressures resulting in large uncertainties of virial coefficients. The agreement of the virial coefficients for helium validates that temperature and pressure measurements as well as the data reduction procedure are reliable.
$\mathrm{CO}_{2}$. After the measurements for mixtures of $\mathrm{CO}_{2}(1)+$ propane (2) $\left(x_{1}=0.5158\right)$, the gaseous $p v T$ properties of pure $\mathrm{CO}_{2}$ were measured at a supercritical temperature of 343.13 K to validate the experimental system and the data reduction program for other fluids. The $(Z-1) / \rho$ versus $\rho$ plot departed from linear values with an obvious downward trend at the low densities plotted in Figure 4. The systematic errors with $(Z-$ $1) / \rho$ versus $\rho$ plot for $\mathrm{CO}_{2}$ look like the "adsorption effect". ${ }^{25}$ However, nonpolar, supercritical $\mathrm{CO}_{2}$ should have negligible adsorption on the polished stainless steel surfaces. The $\mathrm{CO}_{2}$ samples were tested on the GC system before and after the Burnett expansions with no impurities found by the GC analysis. Since the temperature and pressure measurement systems and the data reduction program to obtain the gas-filled constant $A$ had been tested with helium, the possible reasons for these discrepancies depend on the samples and cell constant $N_{0}$. The


Figure 3. $(Z-1) / \rho$ vs $\rho$ for helium at 318.165 K : $\square$, experimental results; ----, REFPROP 8.0, ${ }^{24}-$, correlation results from Dymond et al. ${ }^{15}$


Figure 4. $(Z-1) / \rho$ vs $\rho$ for $\mathrm{CO}_{2}$ at $343.132 \mathrm{~K}: \square, U_{0}=1.378854 ; \bigcirc, N_{0}$ $=1.378092$.

Table 2. Experimental $p v T$ Data for $\mathrm{CO}_{2}$

| $T$ | $p$ | $\rho / \mathrm{kg} \cdot \mathrm{m}^{-3}$ | $\rho / \mathrm{kg} \cdot \mathrm{m}^{-3}$ |
| :---: | :---: | :---: | :---: |
| K | kPa | $U_{0}=1.378854$ | $N_{0}=1.378092$ |
| 343.133 | 7469.20 | 157.178 | 156.310 |
| 343.132 | 5888.24 | 114.017 | 113.448 |
| 343.131 | 4543.03 | 82.704 | 82.336 |
| 343.134 | 3447.34 | 59.988 | 59.754 |
| 343.131 | 2584.25 | 43.511 | 43.365 |
| 343.133 | 1919.84 | 31.558 | 31.469 |
| 343.133 | 1416.95 | 22.889 | 22.837 |
| 343.133 | 1040.75 | 16.600 | 16.572 |
| 343.128 | 761.77 | 12.040 | 12.026 |
| 343.133 | 556.21 | 8.732 | 8.727 |
| 343.130 | 405.34 | 6.333 | 6.333 |
| 343.134 | 295.01 | 4.593 | 4.595 |
| 343.131 | 214.49 | 3.331 | 3.335 |

calculated cell constant for $\mathrm{CO}_{2}$ should be the same as the apparatus constant $N_{0}$. However, the cell constant for $\mathrm{CO}_{2}$ ( $1.378854 \pm 0.00006$ ) was $0.06 \%$ larger than the helium calibration results (first run: $1.378010 \pm 0.00002$; second run: $1.378092 \pm 0.00005$ ).

Gupta and Eubank ${ }^{26}$ faced similar problems and concluded that the cell constant changed for different fluids because "the valve packing were made of Teflon impregnated with graphite and its pores could swell in the presence of a solvent". The valve packing in this work was also made of Teflon impregnated with graphite, so the effective cell volume changed with different fluids.

Thus, the isotherm cell constant, $U_{0}$, for each fluid was used instead of the helium calibration results, $N_{0}$,

$$
\begin{equation*}
U_{0}=\lim _{p_{i} \rightarrow 0} \frac{p_{i-1}}{p_{i}} \tag{6}
\end{equation*}
$$

The densities calculated using $U_{0}=1.378854$ and $N_{0}=$ 1.378092 are listed in Table 2. The densities with $U_{0}=1.378854$ matched well with Span and Wagner's ${ }^{27}$ calculated results with an average relative deviation of $\pm 0.005 \%$, while these using $N_{0}$ had large systematic deviations of $-0.6 \%$ at high pressures and $0.1 \%$ at low pressures as shown in Figure 5. The second and third virial coefficients also agreed well with those of Dymond et al. ${ }^{15}$ and Span and Wagner ${ }^{27}$ listed in Table 3. The $(Z-1) / \rho$ versus $\rho$ plot was much straighter at low densities when the cell constant $U_{0}$ for $\mathrm{CO}_{2}$ was used as shown in Figure 4 since the systematic density errors with $N_{0}=1.378092$ at low pressures are magnified when calculating $(Z-1) / \rho$ and the virial coefficients.
When the "effective" cell constant $U_{0}$ was used in the data reduction procedure, the densities and virial coefficients matched


Figure 5. Relative density deviations for $\mathrm{CO}_{2}$ compared to results from Span and Wagner: ${ }^{27} \square, U_{0}=1.378854 ; \bigcirc, N_{0}=1.378092$.

Table 3. Second and Third Virial Coefficients for $\mathrm{CO}_{2}$ at 343.132 K

|  | $B$ |  |  |
| :--- | :---: | :--- | :--- |
|  |  | $C$ |  |
| $\mathrm{~cm}^{3} \cdot \mathrm{~mol}^{-1} \cdot \mathrm{~mol}^{-2}$ |  |  |  |
| $U_{0}=1.378854$ |  | $-88.55 \pm 0.1$ |  |
| $N_{0}=1.378092 \pm 50$ |  |  |  |
| Dymond et al. (correlation results) ${ }^{15}$ | $-84.55 \pm 0.1$ | $2861 \pm 50$ |  |
| Span and Wagner ${ }^{27}$ | $-88.8 \pm 0.3$ | $3821 \pm 120$ |  |
|  | -88.5 | 3997 |  |

Table 4. Experimental $p v T$ Data for Argon

| $T$ | $p$ | $\rho / \mathrm{kg} \cdot \mathrm{m}^{-3}$ | $\rho / \mathrm{kg} \cdot \mathrm{m}^{-3}$ |
| :---: | :---: | :---: | :---: |
| K | kPa | $U_{0}=1.378205$ | $N_{0}=1.378092$ |
| 318.755 | 7231.46 | 111.747 | 111.681 |
| 318.755 | 5275.06 | 81.092 | 81.051 |
| 318.751 | 3845.47 | 58.845 | 58.820 |
| 318.751 | 2800.67 | 42.700 | 42.685 |
| 318.759 | 2038.22 | 30.983 | 30.975 |
| 318.758 | 1482.26 | 22.482 | 22.477 |
| 318.755 | 1077.30 | 16.313 | 16.311 |
| 318.755 | 782.65 | 11.836 | 11.836 |
| 318.751 | 568.39 | 8.589 | 8.589 |
| 318.750 | 412.69 | 6.232 | 6.233 |
| 318.752 | 299.59 | 4.522 | 4.523 |
| 318.752 | 217.45 | 3.281 | 3.282 |
| 318.756 | 157.82 | 2.381 | 2.382 |

better with published data. This conclusion was then validated using the Burnett measurement for argon after the experiments for mixture $2\left(x_{1}=0.8017\right)$.

Argon. The Burnett $p v T$ properties of argon were measured at 318.75 K from ( 158 to 7231 ) kPa . The cell constant $U_{0}$ for argon was estimated to be $1.378205 \pm 0.00004$. The densities calculated with the cell constants $U_{0}$ and $N_{0}$ with results are shown in Table 4 and Figure 6. The densities with $U_{0}=$ 1.378205 matched well with results from Tegeler et al. ${ }^{28}$ with an average relative deviation of $\pm 0.002 \%$. The second and third virial coefficients listed in Table 5 also show that when the cell constant $U_{0}$ is used, it provides reliable results. The plot of $(Z-1) / \rho$ versus $\rho$ in Figure 7 shows a similar trend as with the $\mathrm{CO}_{2}$ which validates that the effective cell constant $U_{0}$ should be used for each fluid instead of the helium calibration results.

In summary, helium was used as the calibration gas to determine the cell constant $N_{0}$ before and after the mixture measurements. The reliability of the experimental system and data reduction procedure was then validated using gaseous $p v T$ measurements for pure $\mathrm{CO}_{2}$ carefully after the measurements with mixture 1 . Measurements with gaseous argon were used to further verify the conclusions after the measurements with mixture 2. The results indicate that the valve packing swelled


Figure 6. Relative density deviations for argon compared to results from Tegeler et al.: ${ }^{28} \square, U_{0}=1.378205 ; \bigcirc, N_{0}=1.378092$.

Table 5. Second and Third Virial Coefficients for Argon at 318.754 K

|  | $B$ |  |
| :--- | :---: | :---: |
|  | $C$ |  |
| $\mathrm{~cm}^{3} \cdot \mathrm{~mol}^{-1} \cdot \mathrm{~mol}^{-2}$ |  |  |
| $U_{0}=1.378205$ | $-11.63 \pm 0.1$ |  |
| $N_{0}=1.378092(7$ data points) | $-11.30 \pm 0.1$ | $965 \pm 40$ |
| Dymond et al. (correlation results) $^{15}$ | $-11.91 \pm 0.3$ | $1088 \pm 80$ |
| Tegeler et al. ${ }^{28}$ | -11.51 | 1008 |

different amounts for different fluids and released in the vacuum resulting in reversible changes of the cell volume.

## Results and Discussion for $\mathbf{C O}_{\mathbf{2}}+$ Propane

A total of $225 p v T x$ data points for the binary $\mathrm{CO}_{2}(1)+$ propane (2) mixture were obtained in the gaseous phase with temperatures from ( 320 to 400 ) K, pressures up to 7784 kPa , and two mixture compositions of $x_{1}=0.5158\left(w_{1}=0.5153\right)$ and $x_{1}=0.8017\left(w_{1}=0.8014\right)$. The temperature $(T / K)$, pressure $(p / \mathrm{kPa})$, density $\left(\rho / \mathrm{kg} \cdot \mathrm{m}^{-3}\right)$, compressibility factor $(Z)$, and $\mathrm{CO}_{2}$ mole fraction $\left(x_{1}\right)$ data are listed in Table 6. The effective cell constant $U_{0}$ for mixture $1\left(x_{1}=0.5158\right)$ was estimated to be 1.379601 and for mixture $2\left(x_{1}=0.8017\right)$ was 1.379070 for calculating the densities and compressibility factor. The 0.04 $\%$ difference between the two effective cell constants comes from the different solubility of propane and $\mathrm{CO}_{2}$ in the valve packing.
The relative uncertainties for the density and compressibility factor are $\pm 0.05 \%$ and $\pm 0.06 \%$ at a $95 \%$ confidence level. Figure 8 show the $p v T x$ data with the propane vapor pressures calculated from Lemmon et al. ${ }^{21}$ Figure 9 shows the $(Z-1) / \rho$


Figure 7. $(Z-1) / \rho$ vs $\rho$ for argon at $318.754 \mathrm{~K}: \square, U_{0}=1.378205 ; \bigcirc, N_{0}$ $=1.378092$.


Figure 8. Distribution of experimental $\mathrm{CO}_{2}(1)+$ propane (2) data: $\square, x_{1}$ $=0.5158 ; \Delta, x_{1}=0.8017 ; \bullet$, critical point of propane; - , vapor pressures for propane.


Figure 9. $(Z-1) / \rho$ vs $\rho$ for $\mathrm{CO}_{2}(1)+$ propane (2) $\left(x_{1}=0.8017\right)$ : (a) $N_{0}$ $=1.378092$; (b) $U_{0}=1.379070$.
versus $\rho$ plot for mixture 2 ( $x_{1}=0.8017$ ) when different cell constants were used to calculate the results which also show that the effective cell constant $U_{0}$ should be used. The ( $Z-$ $1) / \rho$ versus $\rho$ plot for the mixture also proved that this trend was not caused by the adsorption effect between gases and surfaces of experimental cells because the $(Z-1) / \rho$ versus $\rho$ plot showed similar trends at different temperatures, while the adsorption effect was a strong function of the temperature.

A truncated virial equation of state for the $\mathrm{CO}_{2}(1)+$ propane (2) system was developed by fitting the data listed in Table 6. The equation was based on the following functional form:

$$
\begin{equation*}
Z=\frac{p}{\rho R T}=1+B_{\mathrm{m}} \rho+C_{\mathrm{m}} \rho^{2} \tag{7}
\end{equation*}
$$

Table 6. Experimental pvTx Data for the $\mathbf{C O}_{2}(1)+$ Propane (2) Mixtures

| $T$ | $p$ | $\rho$ |  |  | $T$ | $p$ | $\rho$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| K | kPa | $\overline{\mathrm{kg} \cdot \mathrm{m}^{-3}}$ | Z | $x_{1}$ | K | kPa | $\overline{\mathrm{kg} \cdot \mathrm{m}^{-3}}$ | Z | $x_{1}$ |
| 400.028 | 7784.16 | 140.912 | 0.73164 | 0.5158 | 400.037 | 4441.75 | 65.486 | 0.89783 | 0.8017 |
| 400.026 | 6095.48 | 102.176 | 0.79013 | 0.5158 | 400.036 | 3314.32 | 47.495 | 0.92370 | 0.8017 |
| 400.035 | 4696.70 | 74.081 | 0.83968 | 0.5158 | 400.034 | 2454.95 | 34.445 | 0.94341 | 0.8017 |
| 400.034 | 3565.28 | 53.710 | 0.87917 | 0.5158 | 400.032 | 1808.37 | 24.980 | 0.95826 | 0.8017 |
| 400.042 | 2676.02 | 38.937 | 0.91022 | 0.5158 | 400.029 | 1326.55 | 18.115 | 0.96933 | 0.8017 |
| 400.035 | 1989.48 | 28.228 | 0.93346 | 0.5158 | 400.018 | 970.17 | 13.137 | 0.97758 | 0.8017 |
| 400.026 | 1468.73 | 20.463 | 0.95062 | 0.5158 | 400.033 | 707.92 | 9.526 | 0.98369 | 0.8017 |
| 400.034 | 1079.54 | 14.834 | 0.96388 | 0.5158 | 400.028 | 515.70 | 6.908 | 0.98818 | 0.8017 |
| 400.029 | 790.53 | 10.753 | 0.97372 | 0.5158 | 400.029 | 375.15 | 5.009 | 0.99134 | 0.8017 |
| 400.030 | 577.33 | 7.794 | 0.98102 | 0.5158 | 400.034 | 272.65 | 3.632 | 0.99360 | 0.8017 |
| 400.037 | 420.82 | 5.650 | 0.98648 | 0.5158 | 400.035 | 198.07 | 2.634 | 0.99546 | 0.8017 |
| 400.044 | 306.29 | 4.095 | 0.99053 | 0.5158 | 390.029 | 7432.39 | 124.497 | 0.81051 | 0.8017 |
| 400.035 | 222.65 | 2.968 | 0.99342 | 0.5158 | 390.032 | 5688.28 | 90.301 | 0.85521 | 0.8017 |
| 390.027 | 7399.00 | 141.004 | 0.71281 | 0.5158 | 390.029 | 4298.50 | 65.497 | 0.89101 | 0.8017 |
| 390.022 | 5838.53 | 102.241 | 0.77574 | 0.5158 | 390.030 | 3214.68 | 47.503 | 0.91877 | 0.8017 |
| 390.027 | 4522.90 | 74.128 | 0.82883 | 0.5158 | 390.025 | 2384.93 | 34.451 | 0.93987 | 0.8017 |
| 390.025 | 3446.26 | 53.743 | 0.87108 | 0.5158 | 390.033 | 1758.82 | 24.983 | 0.95577 | 0.8017 |
| 390.033 | 2593.45 | 38.961 | 0.90421 | 0.5158 | 390.037 | 1291.27 | 18.117 | 0.96761 | 0.8017 |
| 390.029 | 1931.69 | 28.245 | 0.92903 | 0.5158 | 390.028 | 944.86 | 13.139 | 0.97637 | 0.8017 |
| 390.034 | 1427.95 | 20.475 | 0.94736 | 0.5158 | 390.029 | 689.66 | 9.528 | 0.98276 | 0.8017 |
| 390.029 | 1050.49 | 14.843 | 0.96143 | 0.5158 | 390.027 | 502.51 | 6.909 | 0.98748 | 0.8017 |
| 390.034 | 769.82 | 10.759 | 0.97194 | 0.5158 | 390.033 | 365.64 | 5.010 | 0.99087 | 0.8017 |
| 390.036 | 562.52 | 7.799 | 0.97977 | 0.5158 | 390.029 | 265.87 | 3.633 | 0.99358 | 0.8017 |
| 390.033 | 410.13 | 5.653 | 0.98549 | 0.5158 | 390.030 | 193.15 | 2.634 | 0.99548 | 0.8017 |
| 390.038 | 298.57 | 4.098 | 0.98973 | 0.5158 | 380.019 | 7122.68 | 124.564 | 0.79677 | 0.8017 |
| 390.028 | 217.06 | 2.970 | 0.99273 | 0.5158 | 380.024 | 5478.48 | 90.348 | 0.84492 | 0.8017 |
| 380.026 | 7010.29 | 141.070 | 0.69281 | 0.5158 | 380.021 | 4154.26 | 65.530 | 0.88335 | 0.8017 |
| 380.020 | 5579.29 | 102.287 | 0.76047 | 0.5158 | 380.021 | 3114.53 | 47.526 | 0.91314 | 0.8017 |
| 380.017 | 4347.62 | 74.161 | 0.81733 | 0.5158 | 380.026 | 2314.67 | 34.467 | 0.93575 | 0.8017 |
| 380.025 | 3326.52 | 53.766 | 0.86258 | 0.5158 | 380.021 | 1709.04 | 24.996 | 0.95272 | 0.8017 |
| 380.026 | 2510.44 | 38.978 | 0.89793 | 0.5158 | 380.023 | 1255.86 | 18.126 | 0.96539 | 0.8017 |
| 380.020 | 1873.61 | 28.257 | 0.92443 | 0.5158 | 380.022 | 919.55 | 13.145 | 0.97476 | 0.8017 |
| 380.021 | 1386.94 | 20.484 | 0.94399 | 0.5158 | 380.025 | 671.46 | 9.532 | 0.98155 | 0.8017 |
| 380.026 | 1021.40 | 14.849 | 0.95902 | 0.5158 | 380.026 | 489.43 | 6.912 | 0.98664 | 0.8017 |
| 380.033 | 749.01 | 10.763 | 0.97018 | 0.5158 | 380.029 | 356.25 | 5.012 | 0.99036 | 0.8017 |
| 380.032 | 547.58 | 7.802 | 0.97847 | 0.5158 | 380.025 | 259.02 | 3.635 | 0.99302 | 0.8017 |
| 380.025 | 399.41 | 5.656 | 0.98459 | 0.5158 | 380.025 | 188.21 | 2.635 | 0.99508 | 0.8017 |
| 380.039 | 290.81 | 4.099 | 0.98900 | 0.5158 | 370.021 | 6810.40 | 124.620 | 0.78207 | 0.8017 |
| 380.039 | 211.45 | 2.971 | 0.99212 | 0.5158 | 370.009 | 5266.97 | 90.391 | 0.83389 | 0.8017 |
| 370.020 | 6617.03 | 141.135 | 0.67132 | 0.5158 | 370.020 | 4009.41 | 65.558 | 0.87522 | 0.8017 |
| 370.017 | 5317.21 | 102.331 | 0.74401 | 0.5158 | 370.011 | 3013.86 | 47.548 | 0.90712 | 0.8017 |
| 370.016 | 4171.02 | 74.192 | 0.80499 | 0.5158 | 370.011 | 2244.05 | 34.483 | 0.93133 | 0.8017 |
| 370.018 | 3205.97 | 53.788 | 0.85345 | 0.5158 | 370.004 | 1659.14 | 25.007 | 0.94950 | 0.8017 |
| 370.020 | 2426.93 | 38.994 | 0.89117 | 0.5158 | 370.013 | 1220.32 | 18.134 | 0.96303 | 0.8017 |
| 370.016 | 1815.28 | 28.268 | 0.91949 | 0.5158 | 370.015 | 894.13 | 13.150 | 0.97304 | 0.8017 |
| 370.016 | 1345.82 | 20.492 | 0.94039 | 0.5158 | 370.013 | 653.23 | 9.536 | 0.98031 | 0.8017 |
| 370.020 | 992.19 | 14.855 | 0.95640 | 0.5158 | 370.011 | 476.31 | 6.915 | 0.98573 | 0.8017 |
| 370.028 | 728.17 | 10.768 | 0.96830 | 0.5158 | 370.022 | 346.79 | 5.014 | 0.98973 | 0.8017 |
| 370.027 | 532.61 | 7.805 | 0.97706 | 0.5158 | 370.016 | 252.19 | 3.636 | 0.99254 | 0.8017 |
| 370.023 | 388.65 | 5.658 | 0.98360 | 0.5158 | 370.018 | 183.24 | 2.637 | 0.99461 | 0.8017 |
| 370.023 | 283.04 | 4.101 | 0.98819 | 0.5158 | 360.023 | 6494.96 | 124.685 | 0.76616 | 0.8017 |
| 370.021 | 205.87 | 2.973 | 0.99167 | 0.5158 | 360.014 | 5054.02 | 90.435 | 0.82198 | 0.8017 |
| 360.011 | 6218.19 | 141.203 | 0.64809 | 0.5158 | 360.016 | 3863.46 | 65.591 | 0.86635 | 0.8017 |
| 360.011 | 5051.96 | 102.377 | 0.72622 | 0.5158 | 360.010 | 2912.64 | 47.571 | 0.90057 | 0.8017 |
| 360.011 | 3992.60 | 74.224 | 0.79163 | 0.5158 | 360.010 | 2173.16 | 34.499 | 0.92651 | 0.8017 |
| 360.013 | 3084.26 | 53.811 | 0.84351 | 0.5158 | 360.006 | 1608.88 | 25.019 | 0.94586 | 0.8017 |
| 360.015 | 2342.90 | 39.010 | 0.88386 | 0.5158 | 360.010 | 1184.71 | 18.143 | 0.96043 | 0.8017 |
| 360.014 | 1756.62 | 28.280 | 0.91413 | 0.5158 | 360.016 | 868.69 | 13.157 | 0.97115 | 0.8017 |
| 360.009 | 1304.50 | 20.501 | 0.93647 | 0.5158 | 360.016 | 634.97 | 9.541 | 0.97891 | 0.8017 |
| 360.011 | 962.87 | 14.861 | 0.95355 | 0.5158 | 360.016 | 463.19 | 6.918 | 0.98473 | 0.8017 |
| 360.006 | 707.21 | 10.772 | 0.96618 | 0.5158 | 360.022 | 337.31 | 5.017 | 0.98893 | 0.8017 |
| 360.012 | 517.62 | 7.809 | 0.97556 | 0.5158 | 360.019 | 245.35 | 3.638 | 0.99197 | 0.8017 |
| 360.015 | 377.87 | 5.660 | 0.98250 | 0.5158 | 360.016 | 178.29 | 2.638 | 0.99415 | 0.8017 |
| 360.008 | 275.27 | 4.103 | 0.98739 | 0.5158 | 350.018 | 6175.26 | 124.740 | 0.74894 | 0.8017 |
| 360.015 | 200.24 | 2.974 | 0.99096 | 0.5158 | 350.012 | 4838.83 | 90.473 | 0.80914 | 0.8017 |
| 350.010 | 5812.83 | 141.262 | 0.62289 | 0.5158 | 350.013 | 3716.34 | 65.618 | 0.85683 | 0.8017 |
| 350.010 | 4782.86 | 102.417 | 0.70691 | 0.5158 | 350.011 | 2810.84 | 47.589 | 0.89357 | 0.8017 |
| 350.009 | 3811.99 | 74.253 | 0.77712 | 0.5158 | 350.007 | 2101.90 | 34.513 | 0.92138 | 0.8017 |
| 350.012 | 2961.46 | 53.831 | 0.83276 | 0.5158 | 350.011 | 1558.64 | 25.028 | 0.94214 | 0.8017 |
| 350.014 | 2258.25 | 39.024 | 0.87595 | 0.5158 | 350.015 | 1148.99 | 18.150 | 0.95772 | 0.8017 |
| 350.013 | 1697.65 | 28.290 | 0.90837 | 0.5158 | 350.012 | 843.17 | 13.162 | 0.96917 | 0.8017 |
| 350.009 | 1263.00 | 20.508 | 0.93226 | 0.5158 | 350.009 | 616.66 | 9.544 | 0.97747 | 0.8017 |
| 350.010 | 933.45 | 14.866 | 0.95050 | 0.5158 | 350.020 | 450.01 | 6.921 | 0.98369 | 0.8017 |
| 350.008 | 686.24 | 10.776 | 0.96398 | 0.5158 | 350.017 | 327.80 | 5.019 | 0.98814 | 0.8017 |
| 350.009 | 502.56 | 7.811 | 0.97391 | 0.5158 | 350.020 | 238.49 | 3.639 | 0.99140 | 0.8017 |
| 350.013 | 367.05 | 5.662 | 0.98128 | 0.5158 | 350.011 | 173.33 | 2.639 | 0.99374 | 0.8017 |
| 350.011 | 267.49 | 4.104 | 0.98655 | 0.5158 | 340.010 | 5849.82 | 124.787 | 0.73008 | 0.8017 |
| 350.014 | 194.63 | 2.975 | 0.99034 | 0.5158 | 340.005 | 4621.28 | 90.506 | 0.79522 | 0.8017 |
| 340.008 | 4508.97 | 102.472 | 0.68566 | 0.5158 | 339.995 | 3567.86 | 65.643 | 0.84651 | 0.8017 |
| 340.012 | 3628.80 | 74.290 | 0.76114 | 0.5158 | 340.001 | 2708.23 | 47.606 | 0.88599 | 0.8017 |
| 340.009 | 2837.32 | 53.858 | 0.82090 | 0.5158 | 339.996 | 2030.23 | 34.525 | 0.91584 | 0.8017 |
| 340.015 | 2172.91 | 39.044 | 0.86721 | 0.5158 | 339.990 | 1508.12 | 25.038 | 0.93812 | 0.8017 |
| 340.015 | 1638.30 | 28.304 | 0.90195 | 0.5158 | 340.006 | 1113.10 | 18.156 | 0.95480 | 0.8017 |
| 340.008 | 1221.28 | 20.518 | 0.92752 | 0.5158 | 339.987 | 817.54 | 13.167 | 0.96705 | 0.8017 |

Table 6. Continued

| $T$ | $p$ | $\rho$ |  |  | $T$ | $p$ | $\rho$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| K | kPa | $\mathrm{kg} \cdot \mathrm{m}^{-3}$ | Z | $x_{1}$ | K | kPa | $\mathrm{kg} \cdot \mathrm{m}^{-3}$ | Z | $x_{1}$ |
| 340.012 | 903.91 | 14.873 | 0.94702 | 0.5158 | 339.990 | 598.29 | 9.548 | 0.97595 | 0.8017 |
| 340.010 | 665.18 | 10.781 | 0.96141 | 0.5158 | 340.002 | 436.79 | 6.923 | 0.98255 | 0.8017 |
| 340.007 | 487.50 | 7.815 | 0.97202 | 0.5158 | 340.013 | 318.30 | 5.020 | 0.98742 | 0.8017 |
| 340.016 | 356.19 | 5.665 | 0.97978 | 0.5158 | 340.003 | 231.59 | 3.641 | 0.99077 | 0.8017 |
| 340.009 | 259.67 | 4.106 | 0.98542 | 0.5158 | 340.008 | 168.38 | 2.640 | 0.99340 | 0.8017 |
| 340.013 | 189.01 | 2.976 | 0.98956 | 0.5158 | 329.999 | 4401.15 | 90.545 | 0.77997 | 0.8017 |
| 330.011 | 3442.62 | 74.321 | 0.74366 | 0.5158 | 329.991 | 3418.11 | 65.670 | 0.83522 | 0.8017 |
| 330.014 | 2711.71 | 53.880 | 0.80801 | 0.5158 | 329.999 | 2604.89 | 47.625 | 0.87766 | 0.8017 |
| 330.014 | 2086.76 | 39.059 | 0.85771 | 0.5158 | 330.001 | 1958.15 | 34.538 | 0.90975 | 0.8017 |
| 330.010 | 1578.47 | 28.315 | 0.89498 | 0.5158 | 329.987 | 1457.41 | 25.048 | 0.93369 | 0.8017 |
| 330.009 | 1179.41 | 20.526 | 0.92249 | 0.5158 | 330.006 | 1077.12 | 18.163 | 0.95157 | 0.8017 |
| 330.008 | 874.20 | 14.879 | 0.94328 | 0.5158 | 329.985 | 791.85 | 13.172 | 0.96468 | 0.8017 |
| 330.006 | 644.04 | 10.786 | 0.95869 | 0.5158 | 329.983 | 579.89 | 9.552 | 0.97422 | 0.8017 |
| 330.008 | 472.35 | 7.818 | 0.96999 | 0.5158 | 329.997 | 423.55 | 6.926 | 0.98128 | 0.8017 |
| 330.010 | 345.31 | 5.667 | 0.97826 | 0.5158 | 330.003 | 308.75 | 5.022 | 0.98644 | 0.8017 |
| 330.010 | 251.86 | 4.108 | 0.98436 | 0.5158 | 330.009 | 224.73 | 3.642 | 0.99017 | 0.8017 |
| 330.011 | 183.36 | 2.977 | 0.98871 | 0.5158 | 330.010 | 163.40 | 2.641 | 0.99284 | 0.8017 |
| 320.009 | 2584.00 | 53.913 | 0.79354 | 0.5158 | 320.002 | 3266.52 | 65.693 | 0.82281 | 0.8017 |
| 320.008 | 1999.59 | 39.083 | 0.84707 | 0.5158 | 320.003 | 2500.61 | 47.642 | 0.86853 | 0.8017 |
| 320.008 | 1518.12 | 28.332 | 0.88714 | 0.5158 | 320.001 | 1885.55 | 34.551 | 0.90306 | 0.8017 |
| 320.000 | 1137.15 | 20.539 | 0.91670 | 0.5158 | 319.998 | 1406.42 | 25.056 | 0.92884 | 0.8017 |
| 320.007 | 844.37 | 14.888 | 0.93902 | 0.5158 | 319.999 | 1040.92 | 18.170 | 0.94799 | 0.8017 |
| 320.009 | 622.82 | 10.792 | 0.95552 | 0.5158 | 319.992 | 766.06 | 13.176 | 0.96208 | 0.8017 |
| 320.007 | 457.20 | 7.823 | 0.96766 | 0.5158 | 320.001 | 561.41 | 9.555 | 0.97230 | 0.8017 |
| 320.007 | 334.43 | 5.670 | 0.97647 | 0.5158 | 319.999 | 410.29 | 6.929 | 0.97990 | 0.8017 |
| 320.010 | 244.02 | 4.110 | 0.98293 | 0.5158 | 320.013 | 299.21 | 5.024 | 0.98548 | 0.8017 |
| 320.012 | 177.71 | 2.979 | 0.98760 | 0.5158 | 320.011 | 217.81 | 3.643 | 0.98933 | 0.8017 |
| 400.029 | 7739.41 | 124.476 | 0.82303 | 0.8017 | 320.008 | 158.39 | 2.642 | 0.99217 | 0.8017 |
| 400.040 | 5896.58 | 90.285 | 0.86450 | 0.8017 |  |  |  |  |  |

Table 7. Numerical Constants in Equations 10 and 11 for the $\mathbf{C O}_{2}$ (1) + Propane (2) Mixtures

where $B_{\mathrm{m}}$ and $C_{\mathrm{m}}$ denote the second and third mixture virial coefficients given by:

$$
\begin{gather*}
B_{\mathrm{m}}=\sum_{i}^{2} \sum_{j}^{2} x_{i} x_{j} B_{i j}  \tag{8}\\
C_{\mathrm{m}}=\sum_{i}^{2} \sum_{j}^{2} \sum_{k}^{2} x_{i} x_{j} x_{k} C_{i j k} \tag{9}
\end{gather*}
$$

Note that if $i=j=k, B_{i j}$ and $C_{i j k}$ correspond to the virial coefficients for the pure components. The virial coefficients $B_{11}$, $C_{111}, B_{22}$, and $C_{222}$ of the pure $\mathrm{CO}_{2}$ and propane were calculated from equations of Span and Wagner ${ }^{27}$ and Lemmon et al. ${ }^{21}$ with temperatures from ( 220 to 450 ) K. Both $B_{i j}$ and $C_{i j k}$ were expressed as functions of the reduced temperature $T_{\mathrm{r}, j(k)}=$ $T / T_{\mathrm{c}, i j(k)}$ as:

$$
\begin{array}{r}
B_{i j}=B_{0, i j}+B_{1, i j} T_{r, i j}{ }^{-1}+B_{2, i j} T_{r, i j}{ }^{-2}+B_{3, i j} T_{r, i j}{ }^{-3}+ \\
B_{4, i j} T_{r, i j}{ }^{-6}+B_{5, i j} T_{r, i j}{ }^{-8} \\
C_{i j k}=C_{0, i j k}+C_{1, i j k} T_{\mathrm{r}, i j k}{ }^{-0.5}+C_{2, i j k} T_{\mathrm{r}, i j k}{ }^{-1}+C_{3, i j k} T_{\mathrm{r}, i j k}{ }^{-2} \tag{11}
\end{array}
$$

The characteristic temperature, $T_{\mathrm{c}, i j(k)}$, was defined for the cross second and third virial coefficients of the mixture as:

$$
\begin{gather*}
T_{\mathrm{c}, i j}=\sqrt{T_{\mathrm{c}, i} T_{\mathrm{c}, j}}  \tag{12}\\
T_{\mathrm{c}, j j k}=\sqrt[3]{T_{\mathrm{c}, i} T_{\mathrm{c}, j} T_{\mathrm{c}, k}}
\end{gather*}
$$

The critical temperature of $\mathrm{CO}_{2}$ is $304.128 \mathrm{~K},{ }^{29}$ and that of propane is $369.89 \mathrm{~K} .{ }^{21}$ The coefficients in eqs 10 and 11 for the $\mathrm{CO}_{2}+$ propane mixtures are listed in Table 7 .

Figure 10 shows the relative pressure deviations of the experimental data from eq 7. Thus, the data can be wellrepresented by the truncated virial equation with a root-meansquare (rms) deviation of $0.028 \%$ over the entire range. The deviations of the density measurements from the present virial EOS are also shown in Figure 11. The detailed maximum and rms deviations are listed in Table 8.
The published $p v T x$ data from Reamer et al., ${ }^{5}$ Niesen and Rainwater, ${ }^{6}$ de la Cruz de Dios et al., ${ }^{8}$ and Blanco et al. ${ }^{9}$ with temperatures from ( 278 to 511 ) K are compared to eq 7 with the relative pressure and density deviations shown in Figures 12 and 13. The mole fractions of $\mathrm{CO}_{2}$ for the published experimental data varied from (0 to 1 ). The deviations of the published data show much larger random errors than the data from this work. The maximum relative pressure deviation of the experimental data from Reamer et al. ${ }^{5}$ is $1.0 \%$ with $\mathrm{CO}_{2}$ mole fractions of $0.7936,0.5884$, and 0.4017 at pressures below 5000 kPa . The experimental pressures from Reamer et al. ${ }^{5}$ are


Figure 10. Pressure deviations of experimental $p v T x$ data from eq 7 for $\mathrm{CO}_{2}(1)+$ propane (2) mixtures: $\square, x_{1}=0.5158 ; \Delta, x_{1}=0.8017$.


Figure 11. Density deviations of experimental $p v T x$ data from eq 7 for $\mathrm{CO}_{2}(1)+$ propane (2) mixtures: $\square, x_{1}=0.5158 ; \Delta, x_{1}=0.8017$.

Table 8. Deviations of the Present $p v T x$ Data from Equation 7 for $\mathrm{CO}_{2}$ (1) + Propane (2) Mixtures ${ }^{a}$

| $100 \cdot \delta_{\max }(p)$ | $100 \cdot \delta_{\text {rms }}(p)$ | $100 \cdot \delta_{\max }(\rho)$ | $100 \cdot \delta_{\text {rms }}(\rho)$ |
| :---: | :---: | :---: | :---: |
| 0.071 | 0.028 | 0.082 | 0.033 | a

$$
\begin{gathered}
\delta_{\max }(p)=\max \left(p_{i, \exp } / p_{i, \mathrm{cal}}-1\right) \\
\delta_{\mathrm{rms}}(p)=\sqrt{\sum_{i=1}^{n}\left(p_{i, \exp } / p_{i, \mathrm{cal}}-1\right)^{2} /(n-1)} \\
\delta_{\max }(\rho)=\max \left(\rho_{i, \exp } / \rho_{i, \mathrm{cal}}-1\right) \\
\delta_{\mathrm{rms}}(\rho)=\sqrt{\sum_{i=1}^{n}\left(\rho_{i, \exp } / \rho_{i, \mathrm{cal}}-1\right)^{2} /(n-1)}
\end{gathered}
$$

lower than eq 7 at $x_{1}=0.1962$ from ( 310 to 510 ) K. Note that eq 7 was correlated from present $p v T x$ data at temperatures from (320 to 400 ) K ; nevertheless eq 7 can represent experimental data well at temperatures up to 450 K . At temperatures above 450 K , the experimental pressures from Reamer et al. ${ }^{5}$ show increasing systematic discrepancies. The maximum densities deviation of the experimental data from Niesen and Rainwater ${ }^{6}$ is $1.0 \%$ at pressures lower than 4000 kPa with larger deviations at higher pressures. Most of the experimental data from de la Cruz de Dios et al. ${ }^{8}$ show good agreement with eq 7 except at atmospheric pressure because de la Cruz de Dios et al. ${ }^{8}$ measured the properties at high pressures up to 70 MPa with a pressure uncertainty of $\pm 1.3 \mathrm{kPa}$. Blanco et al. ${ }^{9}$ measured the densities of $\mathrm{CO}_{2}+$ propane at 308.15 K with larger random errors than the other data. The pressure and densities show larger


Figure 12. Pressure deviations of experimental $p v T x$ data from eq 7 for $\mathrm{CO}_{2}(1)+$ propane (2) mixtures: $\bigcirc$, Reamer et al. $5^{5}+$, Niesen and Rainwater; ${ }^{6} \times$, de la Cruz de Dios et al.; ${ }^{8} \Delta$, Blanco et al. ${ }^{9}$


Figure 13. Density deviations of experimental $p v T x$ data from eq 7 for $\mathrm{CO}_{2}$ (1) + propane (2) mixtures: $\bigcirc$, Reamer et al. $;^{5}+$, Niesen and Rainwater. ${ }^{6} \times$, de la Cruz de Dios et al. $;^{8} \nabla$, Blanco et al.; ${ }^{9}-$, REFPROP $8.0,{ }^{24} x_{1}=0.2500$ at (350 and 400) K; ---, REFPROP 8.0, ${ }^{24} x_{1}=0.5158$ at $(350$ and 400$) \mathrm{K} ; \cdots$, REFPROP 8.0, ${ }^{24} x_{1}=0.8017$ at $(350$ and 400) K.
deviations near the dew point because the virial equation of state is best used to describe the $p v T x$ properties in the gaseous phase with densities lower than half of the critical density. The $p v T x$ properties from REFPROP $8.0^{24}$ are compared to eq 7 at

Table 9. Experimental Second and Third Virial Coefficients for the $\mathrm{CO}_{2}$ (1) + Propane (2) Mixtures from the Burnett Analysis

| $T$ | $\frac{B_{\mathrm{m}}}{\mathrm{cm}^{3} \cdot \mathrm{~mol}^{-1}}$ | $C_{\mathrm{m}}$ <br> K |
| :---: | :---: | :---: |
|  | $x_{1}=0.5158$ |  |
| 320.008 | -184.7 | 13378 |
| 330.010 | -171.4 | 11746 |
| 340.011 | -160.0 | 10862 |
| 350.011 | -149.4 | 10037 |
| 360.012 | -140.2 | 9629 |
| 370.020 | -131.7 | 9203 |
| 380.027 | -123.8 | 8846 |
| 390.030 | -116.5 | 8510 |
| 400.033 | -109.3 | 8074 |
|  | $x_{1}=0.8017$ |  |
| 320.003 | -128.9 | 6799 |
| 329.998 | -120.1 | 6388 |
| 340.000 | -112.0 | 5982 |
| 350.014 | -104.9 | 5809 |
| 360.015 | -98.2 | 5602 |
| 370.014 | -91.8 | 5297 |
| 380.024 | -86.1 | 5084 |
| 390.030 | -80.6 | 4861 |
| 400.032 | -76.3 | 4952 |



Figure 14. Temperature dependence of the second virial coefficients for $\mathrm{CO}_{2}(1)+$ propane (2) mixtures: $\square, x_{1}=0.5158 ; \Delta, x_{1}=0.8017 ;-$ eq $10 ; \cdots-B_{12}$ from eq $10 ; \cdots$, the second virial coefficient of $\mathrm{CO}_{2} ;{ }^{27}---$, the second virial coefficient of propane. ${ }^{21}$
$x_{1}=0.2500,0.5158$, and 0.8017 in Figure 13. The maximum relative density deviation at 400 K is $0.4 \%$ for $x_{1}=0.2500$ and 0.8017 with the discrepancies increasing as the temperature decreases. The difference between REFPROP $8.0^{24}$ and eq 7 for $x_{1}=0.2500$ at 350 K reaches $-2.4 \%$ at 4400 kPa . The relative density deviations for mixture $x_{1}=0.5158$ are $-1.0 \%$ at 400 K and $-1.5 \%$ at 350 K .
The experimental second and third coefficients, $B_{\mathrm{m}}(T)$ and $C_{\mathrm{m}}(T)$, were obtained by directly fitting eq 7 to the experimental data along isotherms with the results listed in Table 9.

Table 10 and Figures 14 to 16 show the temperature dependence of the experimental and the values of $B_{\mathrm{m}}$ and $C_{\mathrm{m}}$ correlated using eqs 10 and 11 along with the virial coefficients of the pure components and cross virial coefficients of the $\mathrm{CO}_{2}$ (1) + propane (2) mixture. The estimated uncertainties for a $95 \%$ confidence level are $\pm 1 \mathrm{~cm}^{3} \cdot \mathrm{~mol}^{-1}$ for $B_{\mathrm{m}}$ and $\pm 500$ $\mathrm{cm}^{6} \cdot \mathrm{~mol}^{-2}$ for $C_{\mathrm{m}}$. The calculated second and third virial coefficients are both in good agreement with the experimental data after the careful measurements. The second cross virial coefficients from Mason and Eakin, ${ }^{10}$ Sie et al., ${ }^{11}$ Bougard and Jadot, ${ }^{12}$ Michels et al., ${ }^{13}$ and McElroy et al. ${ }^{14}$ are also plotted in Figure 15. The second cross virial coefficients from eq 10 show good agreement with data from Michels et al. ${ }^{13}$ and McElroy et al. ${ }^{14}$ at temperatures from (293 to 333) K. The three data points from Mason and Eakin, ${ }^{10}$ Sie et al., ${ }^{11}$ and Bougard and Jadot ${ }^{12}$ show larger discrepancies than the others. The second cross virial coefficients from eq 10 at temperatures below 290 K are more negative than those from McElroy et al. ${ }^{14}$ which may result in larger uncertainties of the extrapolated third virial coefficients at temperatures lower than 290 K .


Figure 15. Second cross virial coefficients $B_{12}$ for $\mathrm{CO}_{2}(1)+$ propane (2) mixtures: $-\bullet$, eq 10; $\square$, Mason and Eakin; ${ }^{10} \bullet$, Sie et al.; ${ }^{11} \square$, Bougard and Jadot; ${ }^{12} \mathrm{O}$, Michels et al.; ${ }^{13} \Delta$, McElroy et al. ${ }^{14}$


Figure 16. Temperature dependence of the third virial coefficients for $\mathrm{CO}_{2}$ (1) + propane (2) mixtures: $\square, x_{1}=0.5158 ; \Delta, x_{1}=0.8017 ;-$ eq $11 ; \cdots$, third virial coefficient of $\mathrm{CO}_{2} ;{ }^{27}---$, third virial coefficient of propane. ${ }^{21}$

## Conclusions

The Burnett isochoric method was used to measure a total of $225 p v T x$ data points in the gaseous phase for $\mathrm{CO}_{2}+$ propane mixtures with $\mathrm{CO}_{2}$ mole compositions of 0.5158 and 0.8017 , temperatures from ( 320 to 400 ) K, and pressures up to 7784 kPa . The temperature and pressure measurement uncertainties were less than $\pm 5 \mathrm{mK}$ and $\pm 300 \mathrm{~Pa}$. Burnett measurements for pure helium, argon, and $\mathrm{CO}_{2}$ were also conducted at 318 K and/or 343 K to validate the reliability of the experimental system and data reduction procedure. A truncated virial EOS was used to fit the experimental data with rms deviations of $\pm$ $0.03 \%$. The present virial equation of state compares well with

Table 10. Cross Second and Third Virial Coefficients Calculated from Virial Equations for $\mathrm{CO}_{\mathbf{2}}$ (1) + Propane (2) Mixtures

|  | $B_{11}$ | $B_{12}$ | $B_{22}$ | $C_{111}$ | $C_{112}$ | $C_{122}$ | $C_{222}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| T/K | $\overline{\mathrm{cm}^{3} \cdot \mathrm{~mol}^{-1}}$ | $\overline{\mathrm{cm}^{3} \cdot \mathrm{~mol}^{-1}}$ | $\overline{\mathrm{cm}^{3} \cdot \mathrm{~mol}^{-1}}$ | $\overline{\mathrm{cm}^{6} \cdot \mathrm{~mol}^{-2}}$ | $\overline{\mathrm{cm}^{6} \cdot \mathrm{~mol}^{-2}}$ | $\overline{\mathrm{cm}^{6} \cdot \mathrm{~mol}^{-2}}$ | $\overline{\mathrm{cm}^{6} \cdot \mathrm{~mol}^{-2}}$ |
| 320.000 | -104.4 | -154.0 | -335.7 | 4388 | 8226 | 16123 | 21572 |
| 330.000 | -97.1 | -142.5 | -314.3 | 4215 | 6892 | 14978 | 21722 |
| 340.000 | -90.5 | -132.3 | -294.8 | 4050 | 6066 | 13917 | 21605 |
| 350.000 | -84.4 | -123.3 | -277.0 | 3894 | 5572 | 12957 | 21301 |
| 360.000 | -78.8 | -115.2 | -260.6 | 3748 | 5272 | 12112 | 20875 |
| 370.000 | -73.6 | -107.8 | -245.6 | 3613 | 5060 | 11391 | 20377 |
| 380.000 | -68.8 | -101.1 | -231.7 | 3489 | 4851 | 10796 | 19848 |
| 390.000 | -64.4 | -94.8 | -218.9 | 3376 | 4581 | 10332 | 19318 |
| 400.000 | -60.3 | -88.7 | -206.9 | 3274 | 4200 | 9997 | 18813 |

The second and third virial coefficients of pure $\mathrm{CO}_{2}$ were calculated from Span and Wagner, ${ }^{27}$ and those of propane were obtained from Lemmon et al. ${ }^{21}$ by fitting the data from ( 220 to 450 ) K.
published pvTx data. The calculated virial coefficients $B_{\mathrm{m}}$ and $C_{\mathrm{m}}$ agree well with the experimental values.

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