Relative Permittivity of Dimethylsulfoxide and *N*,*N*-Dimethylformamide at Temperatures from (278 to 328) K and Pressures from (0.1 to 5) MPa^{\dagger}

Johannes Hunger and Richard Buchner

Institut für Physikalische und Theoretische Chemie, Universität Regensburg, D-93040 Regensburg, Germany

Mohamed E. Kandil, Eric F. May, and Kenneth N. Marsh*

Centre for Energy, School of Mechanical Engineering, The University of Western Australia, Crawley W.A. 6009, Australia

Glenn Hefter

Chemistry Department, Murdoch University, Murdoch, W.A. 6150, Australia

Relative permittivities (ε_r) have been measured at two frequencies with an expanded (k = 2) uncertainty of 0.1 using a re-entrant radio frequency resonator in the pressure range (0.1 to 5) MPa at temperatures from (278 to 328) K for *N*,*N*-dimethylformamide (DMF) and (293 to 328) K for dimethylsulfoxide (DMSO). At 298.15 K and 0.1 MPa, the assessed literature averages of 38.4 ± 1.8 and 47.3 ± 1.8 for DMF and DMSO, respectively, are consistent with the values of 37.2 ± 0.1 and 46.0 ± 0.1 determined in this work. Possible sources of uncertainty are discussed. An empirical description of $\varepsilon_r(p,T)$ is given that can be used to calculate the temperature and pressure derivatives of ε_r . Kirkwood *g* factors calculated using the present data show only minimal dipole-dipole correlations for both DMF and DMSO.

Introduction

Accurate values of the pressure and temperature dependence of relative permittivities (dielectric constants), ε_r , are of scientific and industrial interest, since they are required for the application of various theories and for reliable process simulation. For example, the pressure dependence of ε_r needs to be known to model the compression of a solvent by the electric field of an ion via the Drude–Nernst equation¹ or to apply the Debye– Hückel limiting law to the volumetric properties of electrolyte solutions.² Similar requirements exist for the first and second temperature derivatives of ε_r for modeling enthalpies of solution and heat capacities.

However, reliable studies of $\varepsilon_r(p,T)$ of molecular solvents in the literature are scarce,³ with most of the available experimental data, particularly for solvents suited to electrolyte studies, focused on $(\partial \varepsilon_r / \partial T)_p$, often obtained over very limited temperature ranges. In this work $\varepsilon_r(p,T)$ has been measured for N,Ndimethylformamide (DMF) and dimethylsulfoxide (DMSO), with a particular focus on $(\partial \varepsilon_r / \partial p)_T$. Both of these solvents are widely used in separation processes because they dissolve a very diverse range of organic and inorganic compounds: DMF is used on a large scale as a solvent for polymers and paints, while DMSO has pharmaceutical applications.⁴ Reliable data for $\varepsilon_r(p,T)$ of DMF and DMSO will improve the fundamental models used to describe them, which may in turn lead to better predictions of their thermophysical properties by simulation packages used to design new industrial processes based on these solvents.

The experimental methods available to determine relative permittivity over a range of temperatures and pressures have been summarized recently.⁵ One method well-suited to $\varepsilon_r(p,T)$ measurements of fluids utilizes robust re-entrant cavity resonators. Measurements of $\varepsilon_r(p,T)$ with such instruments have been used to determine high-pressure phase boundaries and liquid volume fractions in binary⁶⁻⁸ and multicomponent hydrocarbon mixtures.9,10 Re-entrant resonators have also been used for accurate measurements of molar polarizability and/or permittivity and dipole moments in nonpolar fluids and mixtures,^{11,12} weakly polar pure fluids¹³ and strongly polar water.^{14–16} In the present study a three-lobed re-entrant radio frequency resonator was used to determine the generalized complex permittivity, $\hat{\eta}(p,T)$, over the pressure range (0.1 to 5) MPa at temperatures from (278 to 328) K for DMF and (293 to 328) K for DMSO. The generalized complex permittivity, $\hat{\eta} = \varepsilon_{\rm r} - i\eta''$, where i = $(-1)^{1/2}$ and $\eta'' = \varepsilon'' + \kappa/2\pi f\varepsilon_0$, comprises the relative permittivity, $\varepsilon_{\rm r}$, the total loss, η'' , the dielectric loss, ε'' , and the Ohmic loss, which is determined by the electrical conductivity, κ , the frequency of the electromagnetic radiation, f, and the electric constant, $\varepsilon_0 = 8.854 \ 187 \ 817... \cdot 10^{-12} \ \text{F} \cdot \text{m}^{-1}.^{17}$

The temperature dependence of ε_r for these two solvents has been studied frequently (see Supporting Information), although the results are not in very good agreement. To the best of our knowledge, apart from the data of Uosaki et al. (see later), for DMSO at 298.15 K, no such measurements have been made for the neat liquids at pressures above ambient.

Apparatus and Materials

[†] Part of the "Josef M. G. Barthel Festschrift".

* To whom correspondence should be addressed. E-mail: ken.marsh@ canterbury.ac.nz.

Analytical grade DMSO (mass fraction w > 0.999) and DMF (w > 0.998) were obtained from Ajax Finechem (Australia) and

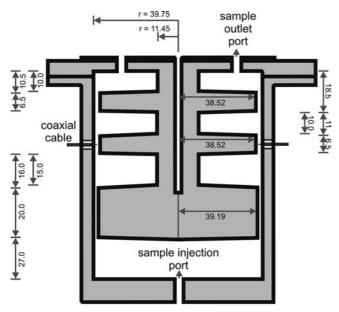


Figure 1. Schematic representation of the three-lobed cavity resonator. Key dimensions for the cavity are given in millimeters.

used without further purification. The water mass fraction, determined by coulometric Karl Fischer titration, was $4 \cdot 10^{-4}$ and $5.5 \cdot 10^{-4}$ for the DMSO and DMF samples, respectively. Approximate conductivities of DMF and DMSO were determined with a relative uncertainty of ± 10 %, with a four-terminal conductivity probe to be ($4 \cdot 10^{-4}$ and $1.3 \cdot 10^{-3}$) S · m⁻¹, respectively, at approximately 297 K.

A schematic of the re-entrant cavity resonator is shown in Figure 1. This cavity had three "lobes" which resulted in three radio frequency modes, with vacuum resonance frequencies of approximately 170 MHz, 675 MHz, and 1.12 GHz. The relative deviations of these vacuum frequencies from those predicted with the nominal cavity dimensions using the extended waveguide model of Goodwin et al.⁶ were -1.5 %, +1.0 %, and +7.8 %, respectively. Such deviations are typical of those reported elsewhere.⁸ While the vacuum resonance frequencies depended sensitively on the cavity dimensions, the measured values of $\varepsilon_r(p,T) \cong (f(p,T)/f(0,T))^2$, being derived from frequency ratios, were insensitive to the cavity dimensions. The small effects of pressure and temperature on the vacuum resonance frequencies were accounted for by calibrating the resonator with helium as described in the next section.

The resonator was constructed from two type 316 stainless steel sections bolted together, with an indium O-ring providing a pressure seal and good electrical contact between the two sections. Unfortunately, the seal was not reliable at p > 8 MPa at temperatures above 328 K. The inner surfaces of the cavity that formed the boundaries for the radio frequency resonances were plated with gold to a thickness of 30 μ m. This increased the quality factor of the resonances by decreasing the resistivity losses that occurred in the bounding conductor. High vacuum quality factors allow more reliable measurements of the imaginary part of $\hat{\eta}(p,T)$. Furthermore, the frequency dependence of the vacuum quality factor of the resonances is simpler to model if the boundary conductor is nonmagnetic.¹⁵

A schematic of the experimental setup used to make the measurements as a function of temperature and pressure is shown in Figure 2. The cavity resonator was placed in a Julabo ME thermostat filled with silicone oil M5 (Carl Roth, Germany), with a long-term temperature stability of \pm 0.02 K. The temperatures of the bath and of the cavity were measured with

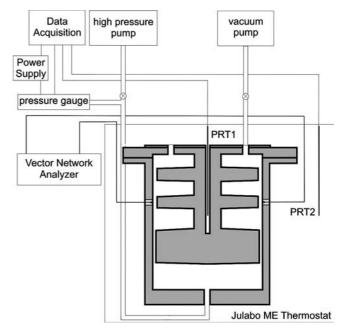


Figure 2. Schematic of the experimental system used for the measurements.

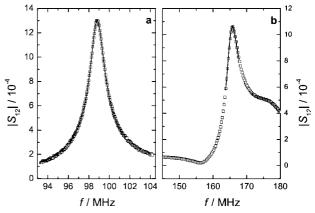


Figure 3. Magnitude of the complex scattering parameter, $|S_{12}|$, for: (a) mode 2 and (b) mode 3, for DMSO at $T \approx 293.15$ K and $p \approx 0.1$ MPa. Symbols represent measured values; line corresponds to fit with eq 1.

two 100 Ω platinum resistance thermometers (PTRs) connected to an Agilent 34970A data acquisition/switch unit using a fourwire configuration. The thermometer PRT1, used to measure the cavity temperature, was placed in the central well as shown in Figure 2. The two PRTs were calibrated against a 25 Ω standard PRT (Hart Scientific model 5681) with a standard uncertainty of \pm 0.05 K. When the bath temperature was close to ambient, the agreement between the temperatures measured with the two PRTs was consistent with this uncertainty; however, at temperatures far from ambient, heat leaks into the resonator from elements located outside the bath resulted in differences of up to 0.2 K. The standard uncertainty in the temperature of the resonator was estimated to be \pm 0.1 K.

Pressures within the cavity were monitored using a diaphragm strain-gauge type pressure transmitter (General Electric PTX 1400) with a full scale of 40 MPa. The transmitter was calibrated against a reference quartz crystal transducer (Paroscientific, model 1000, 7 MPa full scale) located outside the bath, which was isolated from the resonator during the measurements of DMF and DMSO. The relative uncertainty of the pressure

Table 1. Temperature, *T*, Pressure, *p*, and Resonance Frequencies, f_j , of Modes j = 2 and j = 3 for DMF^{*a*}

| T | | <u>J2</u> | | p f_2 | | | |
|------------------|--------------|--------------------|--------------------|---------------------------|---------|--------|---------------------------|
| K | kPa | MHz | ε_{r2} | $\eta^{\prime\prime}{}_2$ | MHz | €r3 | $\eta^{\prime\prime}{}_3$ |
| 277.74 | 110 | 105.248 | 41.138 | 0.404 | 176.165 | 41.128 | 0.608 |
| 277.74 | 5088 | 105.240 | 41.279 | 0.410 | 176.013 | 41.267 | 0.620 |
| 277.73 | 2589 | 105.240 | 41.211 | 0.407 | 176.083 | 41.200 | 0.614 |
| 277.72 | 111 | 105.240 | | 0.404 | 176.161 | 41.130 | 0.608 |
| | | | 41.140 | | | 41.150 | |
| 277.72 | 290 | 105.244 | 41.146 | 0.404 | 176.153 | 41.136 | 0.608 |
| 277.73 | 589 | 105.245 | 41.153 | 0.405 | 176.147 | 41.143 | 0.609 |
| 277.73 | 1088 | 105.244 | 41.168 | 0.405 | 176.131 | 41.157 | 0.610 |
| 277.73 | 2087 | 105.240 | 41.198 | 0.407 | 176.096 | 41.187 | 0.613 |
| 277.73 | 3086 | 105.238 | 41.227 | 0.408 | 176.064 | 41.216 | 0.615 |
| 277.73 | 4086 | 105.236 | 41.256 | 0.409 | 176.032 | 41.245 | 0.618 |
| 277.73 | 5086 | 105.240 | 41.279 | 0.410 | 176.012 | 41.268 | 0.620 |
| 277.73 | 2587 | 105.241 | 41.211 | 0.407 | 176.083 | 41.200 | 0.614 |
| 277.72 | 106 | 105.246 | 41.140 | 0.404 | 176.162 | 41.129 | 0.608 |
| 287.71 | 100 | 107.833 | 39.177 | 0.355 | 180.488 | 39.169 | 0.518 |
| 287.71 | 5081 | 107.815 | 39.318 | 0.360 | 180.317 | 39.309 | 0.518 |
| | | | 39.244 | | | 39.309 | |
| 287.74 | 2581 | 107.828 | | 0.357 | 180.410 | 39.235 | 0.522 |
| 287.77 | 102 | 107.846 | 39.167 | 0.355 | 180.512 | 39.158 | 0.517 |
| 287.75 | 281 | 107.842 | 39.175 | 0.355 | 180.500 | 39.166 | 0.518 |
| 287.74 | 581 | 107.838 | 39.186 | 0.356 | 180.483 | 39.177 | 0.519 |
| 287.74 | 1080 | 107.834 | 39.201 | 0.356 | 180.463 | 39.192 | 0.520 |
| 287.74 | 2079 | 107.828 | 39.231 | 0.357 | 180.423 | 39.223 | 0.522 |
| 287.75 | 3081 | 107.826 | 39.259 | 0.358 | 180.389 | 39.251 | 0.524 |
| 287.75 | 4083 | 107.822 | 39.287 | 0.359 | 180.356 | 39.278 | 0.526 |
| 287.76 | 5087 | 107.822 | 39.309 | 0.360 | | 39.300 | |
| 287.70 | | | | | 180.336 | 39.300 | 0.527 |
| 287.75 | 2587 | 107.830 | 39.243 | 0.357 | 180.413 | 39.234 | 0.522 |
| 287.75 | 110 | 107.841 | 39.171 | 0.355 | 180.503 | 39.162 | 0.517 |
| 292.67 | 109 | 109.153 | 38.229 | 0.337 | 182.698 | 38.220 | 0.482 |
| 292.68 | 5084 | 109.126 | 38.373 | 0.341 | 182.511 | 38.363 | 0.491 |
| 292.68 | 2583 | 109.140 | 38.300 | 0.339 | 182.607 | 38.291 | 0.486 |
| 292.68 | 105 | 109.155 | 38.228 | 0.337 | 182.702 | 38.219 | 0.482 |
| 292.68 | 284 | 109.152 | 38.234 | 0.337 | 182.693 | 38.225 | 0.483 |
| 292.68 | 583 | 109.152 | 38.243 | 0.338 | 182.680 | 38.234 | 0.483 |
| | | | | | | 38.249 | |
| 292.68 | 1083 | 109.146 | 38.258 | 0.338 | 182.660 | 38.249 | 0.484 |
| 292.68 | 2082 | 109.139 | 38.288 | 0.339 | 182.619 | 38.279 | 0.486 |
| 292.68 | 3081 | 109.135 | 38.317 | 0.340 | 182.582 | 38.307 | 0.488 |
| 292.68 | 4080 | 109.129 | 38.346 | 0.340 | 182.543 | 38.337 | 0.489 |
| 292.68 | 5080 | 109.125 | 38.373 | 0.341 | 182.510 | 38.363 | 0.491 |
| 292.68 | 2582 | 109.137 | 38.302 | 0.339 | 182.601 | 38.293 | 0.487 |
| 292.68 | 103 | 109.153 | 38.229 | 0.338 | 182.700 | 38.220 | 0.482 |
| 292.68 | 5081 | 109.126 | 38.373 | 0.341 | 182.511 | 38.363 | 0.492 |
| 292.68 | 2586 | 109.138 | 38.301 | 0.339 | 182.604 | 38.292 | 0.487 |
| 292.68 | 108 | 109.154 | 38.228 | 0.338 | 182.701 | 38.219 | 0.483 |
| 297.68 | 108 | 110.472 | 37.315 | 0.323 | 184.906 | 37.307 | 0.450 |
| | 109 | 110.472 | | | | 37.307 | |
| 297.69 | 288 | 110.471 | 37.320 | 0.323 | 184.898 | 37.312 | 0.450 |
| 297.69 | 588 | 110.467 | 37.330 | 0.323 | 184.882 | 37.322 | 0.451 |
| 297.68 | 1088 | 110.459 | 37.348 | 0.324 | 184.855 | 37.340 | 0.452 |
| 297.69 | 2089 | 110.454 | 37.376 | 0.324 | 184.816 | 37.368 | 0.453 |
| 297.71 | 3089 | 110.453 | 37.401 | 0.325 | 184.785 | 37.393 | 0.454 |
| 297.72 | 4089 | 110.447 | 37.430 | 0.325 | 184.744 | 37.422 | 0.456 |
| 297.72 | 5090 | 110.442 | 37.458 | 0.326 | 184.707 | 37.450 | 0.457 |
| 297.72 | 3090 | 110.455 | 37.400 | 0.325 | 184.788 | 37.392 | 0.454 |
| 297.71 | 1091 | 110.455 | 37.341 | 0.324 | 184.872 | 37.333 | 0.451 |
| 297.71 | 112 | 110.475 | 37.313 | 0.323 | 184.909 | 37.306 | 0.451 |
| 302.73 | 101 | | 36.471 | 0.323 | 187.016 | | 0.430 |
| | | 111.734 | | | | 36.464 | |
| 302.73 | 5078 | 111.707 | 36.608 | 0.304 | 186.820 | 36.601 | 0.424 |
| 302.73 | 2579 | 111.711 | 36.545 | 0.302 | 186.905 | 36.537 | 0.420 |
| 303.11 | 101 | 111.818 | 36.415 | 0.300 | 187.158 | 36.408 | 0.415 |
| 303.11 | 281 | 111.816 | 36.421 | 0.300 | 187.148 | 36.414 | 0.415 |
| 303.12 | 581 | 111.818 | 36.427 | 0.300 | 187.142 | 36.420 | 0.416 |
| 303.11 | 1082 | 111.810 | 36.444 | 0.300 | 187.113 | 36.437 | 0.416 |
| 303.12 | 2085 | 111.805 | 36.472 | 0.301 | 187.075 | 36.465 | 0.418 |
| 303.13 | 3088 | 111.797 | 36.501 | 0.301 | 187.031 | 36.494 | 0.410 |
| 303.13 | 4088 | 111.797 | 36.529 | 0.302 | 186.990 | 36.522 | 0.419 |
| | | | | | | | |
| 303.13 | 5088 | 111.797 | 36.549 | 0.302 | 186.969 | 36.543 | 0.422 |
| 303.12 | 2589 | 111.800 | 36.487 | 0.301 | 187.052 | 36.480 | 0.418 |
| 303.12 | 112 | 111.821 | 36.414 | 0.300 | 187.162 | 36.406 | 0.414 |
| 307.72 | 111 | 113.056 | 35.617 | 0.290 | 189.229 | 35.610 | 0.392 |
| 307.71 | 5089 | 113.016 | 35.759 | 0.292 | 189.011 | 35.752 | 0.399 |
| 307.71 | 2589 | 113.028 | 35.693 | 0.291 | 189.109 | 35.685 | 0.396 |
| 307.72 | 111 | 113.055 | 35.618 | 0.289 | 189.230 | 35.610 | 0.392 |
| 307.72 | 290 | 113.055 | 35.622 | 0.289 | 189.224 | 35.614 | 0.392 |
| | | | | | | | |
| 307.73 | 588 | 113.050 | 35.632 | 0.290 | 189.206 | 35.624 | 0.393 |
| 307.74 307.76 | 1088 2086 | 113.048 113.040 | 35.645 35.673 | 0.290 | 189.187 | 35.637 | 0.393 |
| | | | | 0.290 | 189.144 | 35.666 | 0.395 |

| Table 1. Commuted | Table | 1. | Continued |
|-------------------|-------|----|-----------|
|-------------------|-------|----|-----------|

| T | p | f_2 | | | <i>f</i> ₃ | | |
|--------|------|---------|--------------------|---------------------------|-----------------------|--------------------|---------------------------|
| K | kPa | MHz | \mathcal{E}_{r2} | $\eta^{\prime\prime}{}_2$ | MHz | \mathcal{E}_{r3} | $\eta^{\prime\prime}{}_3$ |
| 307.76 | 3085 | 113.031 | 35.702 | 0.290 | 189.098 | 35.695 | 0.396 |
| 307.74 | 4085 | 113.016 | 35.736 | 0.291 | 189.042 | 35.728 | 0.397 |
| 307.75 | 5084 | 113.024 | 35.754 | 0.291 | 189.023 | 35.747 | 0.399 |
| 307.72 | 2583 | 113.028 | 35.693 | 0.290 | 189.110 | 35.685 | 0.395 |
| 307.72 | 104 | 113.053 | 35.619 | 0.289 | 189.226 | 35.611 | 0.392 |
| 318.12 | 101 | 115.754 | 33.964 | 0.258 | 193.747 | 33.956 | 0.343 |
| 318.15 | 5079 | 115.723 | 34.094 | 0.261 | 193.531 | 34.089 | 0.348 |
| 318.14 | 2586 | 115.724 | 34.037 | 0.260 | 193.620 | 34.029 | 0.346 |
| 318.13 | 109 | 115.756 | 33.964 | 0.259 | 193.751 | 33.955 | 0.343 |
| 318.13 | 288 | 115.752 | 33.969 | 0.259 | 193.740 | 33.961 | 0.343 |
| 318.13 | 588 | 115.747 | 33.979 | 0.259 | 193.722 | 33.971 | 0.344 |
| 318.13 | 1088 | 115.740 | 33.995 | 0.260 | 193.694 | 33.986 | 0.344 |
| 318.12 | 2088 | 115.725 | 34.026 | 0.260 | 193.637 | 34.018 | 0.345 |
| 318.12 | 3088 | 115.711 | 34.056 | 0.261 | 193.582 | 34.048 | 0.346 |
| 318.12 | 4088 | 115.710 | 34.079 | 0.261 | 193.547 | 34.072 | 0.347 |
| 318.12 | 5088 | 115.714 | 34.099 | 0.265 | 193.517 | 34.094 | 0.350 |
| 318.12 | 2591 | 115.716 | 34.042 | 0.264 | 193.607 | 34.034 | 0.348 |
| 318.12 | 113 | 115.749 | 33.968 | 0.264 | 193.740 | 33.959 | 0.346 |
| 328.09 | 111 | 118.427 | 32.438 | 0.245 | 198.222 | 32.429 | 0.310 |
| 328.07 | 5087 | 118.362 | 32.580 | 0.246 | 197.947 | 32.574 | 0.314 |
| 328.07 | 2587 | 118.376 | 32.519 | 0.245 | 198.058 | 32.510 | 0.312 |
| 328.02 | 109 | 118.406 | 32.449 | 0.244 | 198.189 | 32.440 | 0.310 |
| 328.04 | 287 | 118.405 | 32.453 | 0.244 | 198.181 | 32.445 | 0.310 |
| 328.03 | 584 | 118.397 | 32.464 | 0.244 | 198.157 | 32.456 | 0.310 |
| 328.04 | 1084 | 118.389 | 32.479 | 0.244 | 198.127 | 32.471 | 0.310 |
| 328.05 | 2082 | 118.374 | 32.509 | 0.244 | 198.070 | 32.501 | 0.311 |
| 328.05 | 3081 | 118.355 | 32.541 | 0.244 | 198.004 | 32.533 | 0.312 |
| 328.04 | 4080 | 118.346 | 32.567 | 0.244 | 197.956 | 32.560 | 0.313 |
| 328.04 | 5079 | 118.349 | 32.587 | 0.244 | 197.923 | 32.582 | 0.313 |
| 328.05 | 2580 | 118.362 | 32.526 | 0.243 | 198.034 | 32.518 | 0.311 |
| 328.07 | 101 | 118.411 | 32.447 | 0.242 | 198.195 | 32.438 | 0.309 |

^{*a*} ε_{ij} and η''_{j} are the real and imaginary parts of the generalized complex permittivity obtained with eq 2.

measurements made with the diaphragm strain-gauge transducer was \pm 0.25 % of the reading, while the repeatability of the transducer was better than \pm 1 kPa.

A computer-controlled high-pressure positive displacement pump (Quizix QX-6000, maximum pressure 40 MPa) was used to fill and then pressurize the solvent in the cavity. The filling process consisted of injecting about 240 cm³ of liquid into the cavity, which had a total internal volume of 260 cm³. A vacuum was then applied to the space above the liquid to degas the solvent. The remaining solvent volume was injected using the positive displacement pump, and once full, the pump was used to check for trapped gas bubbles by measuring the effective compressibility of the liquid. In all of the experiments reported, the apparent compressibility of the liquids, determined from the measured change in pressure corresponding to a known displaced volume, agreed with the expected value^{18–20} within the experimental uncertainty.

The electromagnetic resonances of the re-entrant cavity were measured in transmission using a HP 8719ET vector network analyzer, with a frequency range of (0.05 to 13.5) GHz. The network analyzer recorded the complex scattering parameter \hat{S}_{12} at 201 frequencies, centered on the approximate resonance frequency and spanning a range of approximately 10 times the resonance frequency. A typical sweep took about 50 s, and about 10 sweeps were averaged when obtaining the \hat{S}_{12} used to determine the resonance parameters.

Method

Measurements of $\hat{\eta}(p,T)$ were made along isotherms. Following a change in bath temperature, approximately 3 h was required before the system was deemed to have achieved equilibrium, on the basis of the rates of change of the measured

pressure, temperature, and resonance frequency. Following a change in pressure, approximately 0.8 h was required. The complex scattering parameters \hat{S}_{12} , measured once the system had equilibrated, were fit to the theoretical resonance function:⁶

$$\hat{S}_{12}(f) = \frac{\hat{A}f}{f^2 + (f_j + ig_j)^2} + \hat{B}$$
(1)

Here f is the stimulus frequency, \hat{A} and \hat{B} are complex adjustable parameters, and $(f_i + ig_i)$ is the complex resonance frequency of mode j (= 1, 2, or 3). Nonlinear least-squares regression of \hat{S}_{12} to eq 1 was used to determine the six parameters in the quantities \hat{A} , \hat{B} , and $(f_i + ig_i)$. Figure 3 shows values of $|\hat{S}_{12}|$ measured for the second and third modes with the cavity filled with DMSO at 293 K and 0.1 MPa. While mode 1 was measurable when the cavity was evacuated or filled with helium, the high permittivity of the target solvents meant that mode 1 was below the low-frequency limit of the network analyzer when the cavity was filled with either DMSO or DMF. When the cavity was filled with these solvents, the mode 2 resonance was located at approximately (95 to 120) MHz (Figure 3) and was isolated from other cavity resonances. In contrast, mode 3, which was located at approximately (165 to 200) MHz, was affected by interference from higher order modes. However, the interference did not seem to cause values of $\hat{\eta}(p,T)$ obtained from mode 3 to differ significantly from those obtained from mode 2, within the estimated experimental uncertainty. Accordingly, the real and imaginary parts of $\hat{\eta}(p,T)$ determined with both modes 2 and 3 are reported in Tables 1 and 2.

The complex total permittivity of each fluid was determined from the measured resonance frequencies, half-widths, and quality

Table 2. Temperature, *T*, Pressure, *p*, and Resonance Frequencies, f_j , of Modes j = 2 and j = 3 for DMSO^{*a*}

| T | p | f_2 | | | f_3 | | |
|--------------------------------------|------|---------|--------------------|---------------------------|---------|--------------------|----------------|
| Κ | kPa | MHz | \mathcal{E}_{r2} | $\eta^{\prime\prime}{}_2$ | MHz | \mathcal{E}_{r3} | η''_3 |
| 292.85 | 110 | 98.751 | 46.701 | 0.564 | 165.344 | 46.655 | 0.895 |
| 292.85 | 5090 | 98.871 | 46.740 | 0.572 | 165.415 | 46.692 | 0.909 |
| 292.84 | 2591 | 98.810 | 46.721 | 0.568 | 165.378 | 46.674 | 0.902 |
| | | | | | | | |
| 292.85 | 113 | 98.752 | 46.700 | 0.565 | 165.344 | 46.654 | 0.895 |
| 292.84 | 293 | 98.755 | 46.702 | 0.565 | 165.345 | 46.657 | 0.895 |
| 292.85 | 592 | 98.762 | 46.705 | 0.565 | 165.348 | 46.660 | 0.890 |
| 292.84 | 1092 | 98.773 | 46.710 | 0.566 | 165.353 | 46.665 | 0.898 |
| 292.83 | 2091 | 98.795 | 46.720 | 0.568 | 165.364 | 46.674 | 0.90 |
| 292.84 | 3091 | 98.820 | 46.727 | 0.569 | 165.379 | 46.682 | 0.904 |
| 292.84 | 4091 | 98.844 | 46.735 | 0.571 | 165.394 | 46.689 | 0.90 |
| | | | | | | | |
| 292.84 | 5091 | 98.870 | 46.741 | 0.573 | 165.411 | 46.695 | 0.910 |
| 292.84 | 2591 | 98.810 | 46.721 | 0.568 | 165.374 | 46.676 | 0.902 |
| 292.84 | 112 | 98.751 | 46.701 | 0.565 | 165.341 | 46.656 | 0.895 |
| 297.86 | 111 | 99.426 | 46.062 | 0.523 | 166.462 | 46.024 | 0.810 |
| 297.86 | 5090 | 99.537 | 46.109 | 0.529 | 166.516 | 46.070 | 0.829 |
| 297.86 | 2590 | 99.479 | 46.087 | 0.526 | 166.484 | 46.050 | 0.823 |
| | 111 | 99.422 | 46.065 | 0.523 | 166.453 | 46.028 | 0.810 |
| 297.85 | | | | | | | |
| 297.86 | 291 | 99.425 | 46.068 | 0.523 | 166.453 | 46.031 | 0.817 |
| 297.86 | 591 | 99.431 | 46.071 | 0.523 | 166.455 | 46.035 | 0.818 |
| 297.86 | 1089 | 99.441 | 46.077 | 0.524 | 166.458 | 46.041 | 0.819 |
| 297.86 | 2089 | 99.464 | 46.086 | 0.525 | 166.469 | 46.050 | 0.82 |
| 297.86 | 3089 | 99.486 | 46.095 | 0.526 | 166.480 | 46.059 | 0.824 |
| 297.86 | 4089 | 99.509 | 46.104 | 0.528 | 166.492 | | 0.82 |
| | | | | | | 46.068 | |
| 297.86 | 5091 | 99.533 | 46.113 | 0.529 | 166.507 | 46.075 | 0.829 |
| 297.85 | 2591 | 99.475 | 46.091 | 0.526 | 166.474 | 46.055 | 0.823 |
| 297.86 | 114 | 99.419 | 46.068 | 0.523 | 166.446 | 46.032 | 0.81 |
| 302.77 | 112 | 100.089 | 45.446 | 0.489 | 167.566 | 45.412 | 0.750 |
| 302.78 | 5089 | 100.208 | 45.487 | 0.494 | 167.632 | 45.452 | 0.76 |
| 302.82 | 2589 | 100.154 | 45.461 | 0.491 | 167.607 | 45.428 | 0.755 |
| | | | | | | 45.428 | |
| 302.84 | 111 | 100.103 | 45.433 | 0.489 | 167.587 | 45.401 | 0.749 |
| 302.84 | 291 | 100.107 | 45.435 | 0.489 | 167.588 | 45.403 | 0.750 |
| 302.85 | 591 | 100.114 | 45.438 | 0.489 | 167.592 | 45.406 | 0.750 |
| 302.84 | 1091 | 100.123 | 45.444 | 0.490 | 167.594 | 45.412 | 0.751 |
| 302.83 | 2090 | 100.143 | 45.456 | 0.491 | 167.600 | 45.424 | 0.754 |
| 302.63 | 3090 | 100.145 | 45.488 | 0.493 | 167.569 | 45.456 | 0.75 |
| | | | | | | | |
| 302.62 | 4091 | 100.163 | 45.498 | 0.495 | 167.580 | 45.466 | 0.76 |
| 302.62 | 5091 | 100.191 | 45.503 | 0.496 | 167.599 | 45.471 | 0.762 |
| 302.61 | 2591 | 100.129 | 45.484 | 0.493 | 167.561 | 45.453 | 0.75 |
| 302.6 | 101 | 100.072 | 45.461 | 0.489 | 167.532 | 45.431 | 0.751 |
| 307.85 | 111 | 100.868 | 44.739 | 0.457 | 168.902 | 44.690 | 0.690 |
| 307.85 | 5087 | 100.964 | 44.801 | 0.461 | 168.927 | 44.752 | 0.700 |
| 307.84 | 2587 | 100.904 | 44.774 | 0.459 | 168.905 | 44.726 | 0.694 |
| | | | | | | | |
| 307.84 | 109 | 100.859 | 44.747 | 0.457 | 168.884 | 44.700 | 0.690 |
| 307.85 | 288 | 100.862 | 44.750 | 0.457 | 168.883 | 44.703 | 0.690 |
| 307.85 | 587 | 100.866 | 44.755 | 0.457 | 168.882 | 44.708 | 0.69 |
| 307.85 | 1086 | 100.874 | 44.763 | 0.458 | 168.882 | 44.715 | 0.692 |
| 307.85 | 2086 | 100.894 | 44.775 | 0.459 | 168.888 | 44.727 | 0.69 |
| 307.84 | 3086 | | 44.787 | 0.459 | | 44.740 | 0.695 |
| | | 100.913 | | | 168.893 | | |
| 307.84 | 4086 | 100.934 | 44.797 | 0.460 | 168.902 | 44.750 | 0.69 |
| 307.85 | 5085 | 100.956 | 44.807 | 0.461 | 168.912 | 44.759 | 0.699 |
| 307.85 | 2584 | 100.906 | 44.778 | 0.459 | 168.894 | 44.731 | 0.694 |
| 307.84 | 107 | 100.854 | 44.751 | 0.457 | 168.873 | 44.705 | 0.689 |
| 317.75 | 116 | 102.326 | 43.459 | 0.411 | 171.296 | 43.436 | 0.599 |
| 317.75 | 5093 | 102.415 | 43.526 | 0.414 | 171.315 | 43.499 | 0.60 |
| 317.74 | 2595 | 102.415 | 43.496 | 0.413 | | 43.499 | 0.602 |
| | | | | | 171.299 | | |
| 317.73 | 117 | 102.320 | 43.464 | 0.411 | 171.289 | 43.439 | 0.599 |
| 317.74 | 296 | 102.325 | 43.466 | 0.411 | 171.292 | 43.440 | 0.599 |
| 317.77 | 595 | 102.332 | 43.468 | 0.411 | 171.298 | 43.442 | 0.600 |
| 317.75 | 1094 | 102.338 | 43.477 | 0.412 | 171.295 | 43.451 | 0.600 |
| 317.76 | 2093 | 102.357 | 43.490 | 0.412 | 171.299 | 43.463 | 0.602 |
| | | | | | | | |
| 317.78 | 3092 | 102.379 | 43.499 | 0.413 | 171.309 | 43.473 | 0.603 |
| 317.78 | 4092 | 102.396 | 43.513 | 0.414 | 171.312 | 43.486 | 0.60 |
| 317.78 | 5092 | 102.420 | 43.522 | 0.414 | 171.326 | 43.493 | 0.60 |
| 317.75 | 2592 | 102.367 | 43.495 | 0.413 | 171.304 | 43.468 | 0.60 |
| 317.73 | 113 | 102.318 | 43.466 | 0.412 | 171.289 | 43.439 | 0.599 |
| 327.57 | 99 | 102.318 | | 0.376 | | 42.138 | 0.52 |
| | | | 42.150 | | 173.884 | | |
| 327.57 | 5073 | 103.972 | 42.218 | 0.379 | 173.895 | 42.204 | 0.534 |
| 327.54 | 2573 | 103.918 | 42.193 | 0.378 | 173.874 | 42.179 | 0.532 |
| 327.54 | 95 | 103.877 | 42.157 | 0.377 | 173.874 | 42.143 | 0.529 |
| | 274 | 103.881 | 42.159 | 0.378 | 173.876 | 42.145 | 0.529 |
| 327.33 | | 103.885 | 42.164 | 0.378 | 173.875 | 42.150 | 0.53 |
| | 577 | | | | 113.013 | 74.100 | 0.550 |
| 327.56 | 572 | | | | | | |
| 327.56 327.57 | 1071 | 103.893 | 42.171 | 0.378 | 173.875 | 42.157 | 0.530 0.531 |
| 327.55 327.56 327.57 327.56 | | | | | | | |

 Table 2.
 Continued

| T | <u>p</u> | f_2 | | | f_3 | | |
|--------|----------|---------|--------------------|---------------------------|---------|--------------------|---------------------------|
| К | kPa | MHz | \mathcal{E}_{r2} | $\eta^{\prime\prime}{}_2$ | MHz | \mathcal{E}_{r3} | $\eta^{\prime\prime}{}_3$ |
| 327.56 | 4068 | 103.940 | 42.216 | 0.380 | 173.874 | 42.200 | 0.534 |
| 327.57 | 5067 | 103.968 | 42.221 | 0.380 | 173.894 | 42.204 | 0.535 |
| 327.57 | 2569 | 103.916 | 42.194 | 0.379 | 173.876 | 42.177 | 0.532 |
| 327.57 | 91 | 103.877 | 42.157 | 0.379 | 173.878 | 42.141 | 0.529 |

 $a_{i} \epsilon_{i}$ and η''_{i} are the real and imaginary parts of the generalized complex permittivity obtained with eq 2.

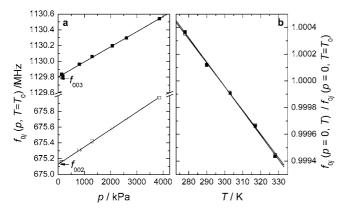


Figure 4. (a) Pressure calibration at $T_0 = 297.69$ K and (b) temperature calibration: \Box , mode 2; \blacksquare , mode 3 of the three-lobed reentrant cavity resonator. Lines represent linear regressions, and f_{0j} are the resonance frequencies corrected for the relative permittivity of He.

Table 3. Vacuum Resonance Frequencies f_{00j} at $T_0 = 297.69$ K, Measured Vacuum Half-Widths, g_{0j} , Pressure Coefficients, ϕ_j , and Temperature Coefficients, α_j , for Modes 2 and 3

| | f_{00j} | g_{0j} | $10^{7} \phi_{j}$ | $10^5 \alpha_j$ |
|---|----------------------|--------------------|-------------------|------------------|
| j | MHz | MHz | kPa ⁻¹ | K ⁻¹ |
| 2 | 675.128 ± 0.004 | 0.2063 ± 0.004 | 3.29 ± 0.03 | -1.77 ± 0.04 |
| 3 | 1129.803 ± 0.008 | 0.2567 ± 0.008 | 1.68 ± 0.03 | -1.83 ± 0.04 |

factors using the implicit model developed by Hamelin et al.¹⁴ for the case of weak coupling to the measurement circuit.

$$\hat{\eta} = \left(\frac{f_{0j} + ig_{0j}}{f_j + ig_j}\right)^2 \frac{1 + (-1 + i)(f_j/f_{0j})^{3/2}\hat{\eta}/Q_{sj}^0}{1 + (-1 + i)/Q_{sj}^0}$$
(2)

In eq 2 subscripts or superscripts "0" indicate properties of the vacuum resonance, and $Q_{sj}^0 \equiv f_{0j}/2g_{0j}$ (≈ 2000) is the vacuum quality factor of mode *j*, determined by the effective resistivity of the bounding metal surface. The measured vacuum halfwidths, g_{0j} , were about 2 to 10 times larger than expected on the basis of the literature electrical conductivity of gold.²¹ This discrepancy can be attributed to the surface finish of the cavity's internal walls and is not critical to the measurements of $\hat{\eta}(p,T)$ because the values of $Q_{s,j}^0$ were stable. However, it was important to account for the changes in f_{0j} that occurred as the cavity temperature and fluid pressure were varied.

Helium Calibration. The relative permittivity of helium can be calculated as a function of temperature and pressure with an uncertainty smaller than the corresponding measurements of $\varepsilon_r(p,T)$.²² Thus, resonance measurements when the cavity was filled with helium could be used to determine the effects of the cavity's thermal expansion and pressure dilation on the vacuum

frequencies, thereby calibrating the resonator. For lossless fluids such as helium, with $\varepsilon_r \approx 1$, eq 2 simplifies to

$$\varepsilon_{\rm r}(p,T) = \left(\frac{f_{0j} + ig_{0j}}{f_j + ig_j}\right)^2 \left(\frac{1 + (-1+i)Q_j}{1 + (-1+i)Q_{\rm s,j}^0}\right) \tag{3}$$

where Q_j is the mode's measured quality factor at a given (p,T). The vacuum resonance half-width is essentially independent of pressure and temperature, but the vacuum resonance frequency has the dependence

$$f_{0j} = f_{00j}(1 + \alpha_j(T - T_0) + \phi_j p) \tag{4}$$

Here f_{00j} is the resonance frequency of mode j at p = 0 and an arbitrary reference temperature T_0 , α_i is the effective temperature coefficient of the mode, and ϕ_i is the effective pressure coefficient of the mode. Measurements of $(f_i + ig_i)$ were made with the cavity filled with helium (mole fraction purity of 0.999999) at pressures ranging from (0.1 to 3.9) MPa at $T_0 =$ 297.69 K and also at temperatures from (278 to 328) K at 2 MPa. At each condition, the value of $\varepsilon_r(p,T)$ for helium was calculated using the equation of state of McCarty and Arp²³ and the polarizability correlation of Harvey and Lemmon²⁴ as implemented in the software Refprop 8.0.25 The calculated values of $\varepsilon_r(p,T)$ for helium were used in eq 3 to determine a value of f_{0i} at each pressure and temperature. The results of the pressure and temperature calibrations are shown in Figure 4. Linear least-squares regression of the data shown in Figure 4 was used to derive the parameters f_{00j} , α_j , and ϕ_j for each mode. The results for modes 2 and 3 are summarized in Table 3 and are comparable to those measured by other workers^{8,11} with similar re-entrant cavities. The effective temperature coefficients of both modes are also in reasonable agreement with the coefficient of thermal expansion for stainless steel (α = $1.59 \cdot 10^{-5}$ K⁻¹).²⁶ Also shown in Table 3 are the measured vacuum resonance half-widths that were used in eqs 2 and 3 for the analysis of all of the data obtained for helium, DMF, and DMSO.

Results and Discussion

Temperatures, pressures, frequencies, and the ε_r and $\hat{\eta}$ values obtained from the analysis with eq 2 are presented in Table 1 for DMF and Table 2 for DMSO, with pressures listed in temporal order. An analysis of the effects of uncertainties in the measured variables on the uncertainty in ε_r is given below.

Modeling. A least-squares regression of $\varepsilon_r(p,T)$ via the empirical eq 5 was used to determine the adjustable parameters A_1, A_2, B_1, B_2 , and C_1

$$\varepsilon_{\rm r}(p,T) = A_1 + A_2 p + (B_1 + B_2 p)T + C_1 T^2 \qquad (5)$$

The parameters B_2 (for DMF) and C_1 (for DMSO) were not statistically significant and thus were set equal to zero for DMF and DMSO, respectively. The other parameters, together with fit qualities, are summarized in Table 4. The derivatives

Table 4. Regression Parameters for the Three-Dimensional Fit of $\varepsilon_r(p,T)$ Using Equation 5 for Mode 2 for DMF and DMSO^a

| | | $A_2 \cdot 10^6$ | <i>B</i> ₁ | $B_2 \cdot 10^7$ | $C_1 \cdot 10^4$ | |
|---------------------------|--|---------------------------------|---|------------------|------------------|----------------|
| | A_1 | kPa | K | kPa•K | K ² | σ |
| DMF mode 2 DMSO mode 2 | $\begin{array}{c} 141.31 \pm 0.66 \\ 85.13 \pm 0.06 \end{array}$ | $28.6 \pm 1.0 \\ -43.8 \pm 2.4$ | $\begin{array}{c} -0.520 \pm 0.004 \\ -0.1312 \pm 0.0002 \end{array}$ | 1.8 ± 0.8 | 5.75 ± 0.07 | 0.018 0.014 |

^{*a*} The standard error of the regression, σ , is also shown.

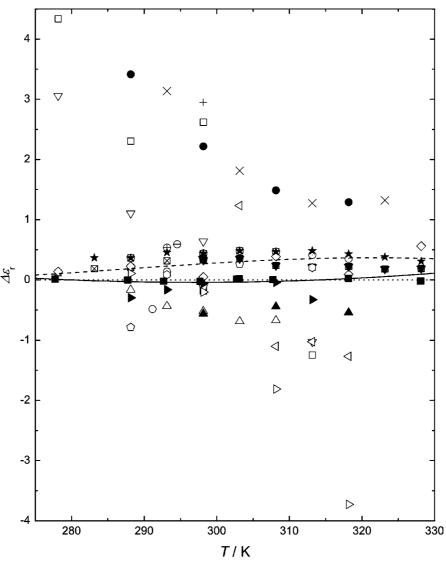


Figure 5. Absolute deviations, $\Delta \varepsilon_r = \varepsilon_{r,\text{lit}} - \varepsilon_r$, of literature data for DMF at p = 101.3 kPa MPa from permittivities, ε_r , calculated from eq 5 of this work using parameters obtained from mode 2: \blacksquare , measured values from this work; solid line represents $\varepsilon_r(T)$ recommended in ref 27; dashed line, recommended in ref 46. For details of the literature data see Supporting Information.

 $(\partial \varepsilon_r / \partial T)_p$ and $(\partial \varepsilon_r / \partial p)_T$ are much smaller for DMSO than for DMF. For solvents of similar "character" (structure, molecular size, dipole moment, etc.) the magnitudes of $(\partial \varepsilon_r / \partial p)_T$ and $(\partial \varepsilon_r / \partial T)_p$ largely reflect changes in the dipole density (and hence the liquid density) with *T* and *p*. Consistent with this notion, both the isobaric expansivity, α_p , and the isothermal compressibility, κ_T , of DMF are larger than those of DMSO.²⁷ The small magnitude of the derivatives and the rather limited temperature range in the present study inevitably result in higher uncertainties in the parameters of eq 5 for DMSO compared with DMF (Table 4). It is notable that the pressure and temperature derivatives for both solvents are significantly lower than for water,²⁸ which is basically a reflection of the higher dipole density (low molecular weight) of water.

Literature Comparison. The existing relative permittivity data for both DMF and DMSO have been compiled recently by

Wohlfarth.^{29,30} However, many of the values listed by Wohlfarth are replicates, in that they are pure component data extracted from papers (from the same laboratory) reporting results for liquid mixtures. Some of the pure component ε_r values reported in these papers, mostly without comment, differ by as much as 2, which suggests they are of low accuracy. Unfortunately, the equations recommended by Wohlfarth²⁷ appear to have been fit to all of the data without weighting for uncertainty.

The available literature results for DMF are summarized in Table S1 in the Supporting Information and graphed in Figure 5. At T = 298.15 K and p = 0.1 MPa the reported ε_r values vary from 36.7 to 40.21, with values grouped around 39.4 \pm 0.4 and 37.3 \pm 0.6, the latter agreeing well with the present value of 37.26 \pm 0.02. Probably fortuitously, the present $\varepsilon_r(T)$ values agree well (Figure 5) with the equation given by Wohlfarth.²⁷ Assuming no uncertainty for water impurity and

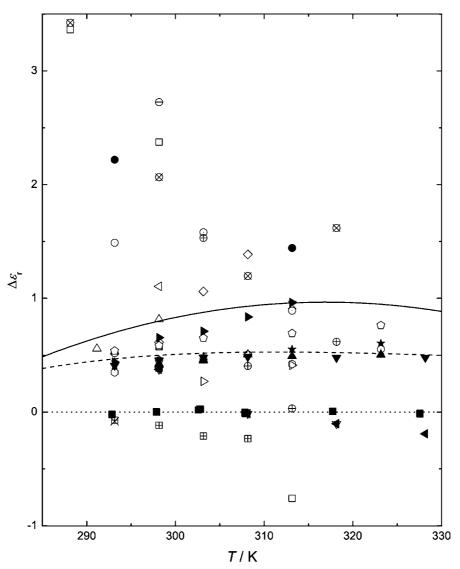


Figure 6. Absolute deviations, $\Delta \varepsilon_r = \varepsilon_{r,\text{lit}} - \varepsilon_r$, of literature data for DMSO at p = 101.3 kPa from permittivities, ε_r , calculated from eq 5 of this work obtained from mode 2: \blacksquare , measured values from this work; solid line represents $\varepsilon_r(T)$ recommended in ref 27; dashed line, recommended in ref 47; dotted line equals zero. For details of the literature data see Supporting Information.

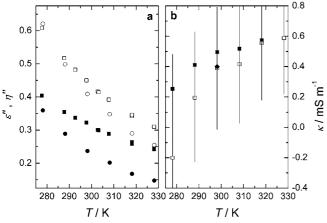


Figure 7. (a) Total loss, η'' , for DMF, this work: \blacksquare , ≈ 110 MHz; \Box , ≈ 185 MHz. Dielectric loss, ε'' , derived from ref 33: \bullet , ≈ 110 MHz; \bigcirc , ≈ 185 MHz. (b) Conductivity, κ , calculated from the difference $\eta'' - \varepsilon''(\kappa/2\pi f \varepsilon_0)$: \blacksquare , ≈ 110 MHz; \Box , ≈ 185 MHz; \bullet , measured value. Vertical lines, estimated uncertainty.

values of ε_r in Table 1 adjusted to a constant temperature within 0.01 K gave a value of $(\partial \varepsilon_r / \partial p)_T = (28.6 \pm 1.0)$ TPa⁻¹ for DMF that is virtually constant over the temperature range studied.

Similarly, assuming no uncertainties for water impurities and 0.1 K temperature uncertainty, the temperature derivatives, $(\partial \varepsilon_r / \partial T)_p = (-0.177 \pm 0.006) \text{ K}^{-1}$ and $(\partial^2 \varepsilon_r / \partial T^2)_p = (11.5 \pm 0.1) \cdot 10^{-4} \text{ K}^{-2}$ (both at T = 298.15 K), did not show a significant variation with pressure. This compares with literature values at 298.15 K of $(\partial \varepsilon_r / \partial T)_p = (-0.177^{27} \text{ and } -0.170^{47}) \text{ K}^{-1}$ and $(\partial^2 \varepsilon_r / \partial T^2)_p = (14.3^{27} \text{ and } 9.7^{47}) \cdot 10^{-4} \text{ K}^{-2}$ both derived from the fit equations. The agreement is probably within the combined uncertainties.

Literature values for DMSO³⁰ are presented in Table S2 in the Supporting Information and plotted in Figure 6. There is considerable scatter in these data. Although most of the literature values are higher than the present results, there are five sets of data that agree with our ε_r values within our estimated uncertainty (see below) of 0.1. In particular, it should be noted that the greatest differences occur for the ε_r values determined by time domain spectroscopy, which have a high uncertainty. The differences between the present values and most of the literature data at p = 0.1 MPa are too large to be due to water contamination, even though the water content of the literature samples is often not stated, whereas that of the present sample is known to be low, { $x(H_2O) \approx 0.002$ }. Further discussion of possible sources of this discrepancy is given in the following section. As noted in the Introduction, Uosaki et al.³¹ determined $\varepsilon_r(p)$ for DMSO at 298.15 K and p up to p = 50 MPa. A graphical representation of their data gives $(\partial \varepsilon_r / \partial p)_T = (12.3 \pm 0.3)$ TPa⁻¹. This value agrees with the present result of (12 ± 2) TPa⁻¹ within our large experimental uncertainty (bearing in mind the limited pressure range of the present study). The value of $(\partial \varepsilon_r / \partial T)_p = (-0.131 \pm 0.002)$ K⁻¹ for DMSO obtained at p = 0.1 MPa is considerably smaller than the corresponding value for DMF and was constant over the temperature and pressure range studied within the experimental uncertainties. Literature values at 298.15 K for $(\partial \varepsilon_r / \partial T)_p$ are $(-0.113^{27}$ and $-0.126^{47})$ K⁻¹ and $(\partial^2 \varepsilon_r / \partial T^2)_p$ of $(9.4^{27}$ and $4.9^{47}) \cdot 10^{-4}$ K⁻². The last value in ref 47 is based on a critical selection of reliable values and is probably more accurate.

Sources of Uncertainty. The presence of air in the cavity would produce low permittivities, but the pressure test agreed well with the calculated compressibilities of the solvents; in addition, hysteresis would be expected within a pressure cycle. Since almost no hysteresis was observed, it is unlikely that the cavity was not filled completely. Uncertainties in the temperature of ± 0.1 K result in an uncertainty in ε_r of about ± 0.03 .

The data analysis model makes a small contribution to the overall uncertainty.⁹ Equation 3 is only valid for weak coupling to the external circuit; however, at the resonance frequency, $|S_{12}|$ was about 0.001, which is far from the critical value of 1, and thus, coupling effects were negligible. The model is also only accurate to first order in 1/Q; for DMF and DMSO, terms of order $(1/Q)^2$ would amount to an uncertainty in ε_r of about 0.02. However, traditional methods like capacitor techniques also have to assume equivalent circuits, and the results so obtained may be biased by parasitic capacitances in the experimental setup especially if the solvent conductivity is high.

Another source of uncertainty is the possible dispersion of the permittivity at the relatively high measurement frequencies: \approx (95 to 120) MHz for mode 2 and \approx (165 to 200) MHz for mode 3. However, dielectric relaxation (DR) data for DMF³² suggest that frequency dispersion should only produce differences from the static relative permittivity ranging from 0.001 to 0.004 at ambient pressure. Dispersion can, however, explain the difference between the values obtained from mode 2, ε_{r2} , and mode 3, ε_{r3} . Values of $\varepsilon_{r2} - \varepsilon_{r3}$ varying from 0.007 to 0.011 were observed, which are broadly consistent, given the uncertainties in both techniques, with the DR spectroscopic values of 0.0015 to 0.007 at temperatures from (278 to 328) K.

Sample impurities, primarily water, can be a source of uncertainty. For DMSO and DMF the addition of water leads to a higher relative permittivity as shown in several studies in the literature on the relative permittivity of binary DMSO + water^{31,33,34} and DMF + water.³⁵ However, such effects will be very small ($\partial \varepsilon_r \approx 0.06$) on the basis of the measured water contents { $x(H_2O) \approx 0.002$ }. In summary the estimated standard uncertainty at a 95 % confidence limit in ε_r accounting for all uncertainties including water content is estimated at 0.1.

The conductivity, κ , can be estimated at the frequencies studied by combining the measured $\hat{\eta}$ with DR estimates of the dielectric loss, ε'' . For DMF Figure 7a shows that the difference $\eta'' - \varepsilon''$ is smaller for mode 3 than for mode 2. This is because the ohmic loss (conductivity) contribution scales with 1/f. The uncertainty in η'' measured with the resonator is approximately 0.03 (equal to that of ε''), whereas the relative uncertainty of the DR ε'' values is ≈ 2 %. The conductivity calculated from the difference $\eta'' - \varepsilon''$ is shown in Figure 7b. Taking all sources of error into account, the uncertainties of the conductivities obtained are $2 \cdot 10^{-4}$ S·m⁻¹ at 110 MHz and $4 \cdot 10^{-4}$ S·m⁻¹ at 185 MHz. Thus, the deviation in the two conductivities determined using the two modes and the DR data is within the uncertainty of the determination and agrees with the experimental value. The deviation increases at lower temperatures, but this may be because κ is smaller at lower temperatures, causing the relative uncertainty to increase. For DMSO the DR spectrum is only available at 298 K,³⁶ but the slower dynamics of DMSO can explain the larger discrepancy between ε_{r2} and ε_{r3} , which ranges from 0.04 to 0.05 and also the higher absolute values of ε'' compared with DMF. The conductivity values obtained from mode 2 and mode 3, respectively, [(2.2 \pm 1.1) $\cdot 10^{-4}$ and $(0.5 \pm 1.3) \cdot 10^{-4}$] S \cdot m⁻¹, are somewhat lower than the values measured at room temperature with a conductivity probe.

Kirkwood Correlation Factors. The Kirkwood–Fröhlich theory, 37,38 derived from statistical mechanics, can be used to gain insight into the molecular interactions in a single component dipolar liquid through the Kirkwood *g* factor obtained from:

$$g\mu^{2} = \frac{9\varepsilon_{0}k_{\rm B}TM}{\rho N_{\rm A}} \frac{(\varepsilon_{\rm r} - \varepsilon_{\rm r\infty})(2\varepsilon_{\rm r} + \varepsilon_{\rm r\infty})}{\varepsilon_{\rm r}(\varepsilon_{\rm r\infty} + 2)^{2}}$$
(6)

where $k_{\rm B}$ and $N_{\rm A}$ are the Boltzmann and Avogadro constants, respectively, *M* is the molar mass, ρ is the molar density, $\varepsilon_{\rm ros}$ is the infinite frequency permittivity of the liquid, and μ is the dipole moment of the isolated molecule. For a random alignment of the molecular-level dipoles in a liquid g = 1, whereas values of g < 1 or g > 1 respectively indicate antiparallel and parallel statistical alignments. Kirkwood *g* factors thus yield indirect information on liquid structure. For the calculation of *g* as a function of temperature and pressure, density data $\rho(p,T)$ as well as $\varepsilon_{\rm ros}$ values are required.

Table 5. Interpolated Relative Permittivity, ε_r , Obtained from Mode 2, Densities, ρ , Interpolated from Literature Data,^{18–20} and Kirkwood Correlation Factors, *g*, Calculated According to Equation 6 for DMF and DMSO

| Т | £r | | ρ/kg•c | $\rho/\text{kg}\cdot\text{dm}^{-3}$ | | |
|--------|-------------|------------|-------------|-------------------------------------|-------------|------------|
| K | p = 0.1 MPa | p = 5 MPa | p = 0.1 MPa | p = 5 MPa | p = 0.1 MPa | p = 5 MPa |
| | | | DMF | | | |
| 278.15 | 41.04 | 41.18 | 0.9628 | 0.9655 | 1.03 | 1.03 |
| 288.15 | 39.09 | 39.23 | 0.9535 | 0.9564 | 1.04 | 1.04 |
| 298.15 | 37.26 | 37.40 | 0.9441 | 0.9471 | 1.04 | 1.04 |
| 308.15 | 35.54 | 35.68 | 0.9346 | 0.9378 | 1.04 | 1.04 |
| 318.15 | 33.94 | 34.08 | 0.9250 | 0.9284 | 1.04 | 1.04 |
| 328.15 | 32.45 | 32.59 | 0.9153 | 0.9189 | 1.05 | 1.04 |
| | | | DMSO | | | |
| 293.15 | 46.68 | 46.72 | 1.0997 | 1.1023 | 1.02 | 1.01 |
| 298.15 | 46.02 | 46.07 | 1.0954 | 1.0980 | 1.03 | 1.02 |
| 308.15 | 44.71 | 44.77 | 1.0866 | 1.0893 | 1.05 | 1.04 |
| 318.15 | 43.40 | 43.46 | 1.0779 | 1.0807 | 1.06 | 1.06 |
| 328.15 | 42.09 | 42.16 | 1.0691 | 1.0720 | 1.08 | 1.07 |

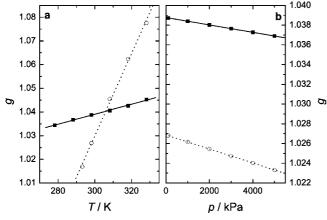


Figure 8. Kirkwood correlation factors *g* calculated from eq 6 at (a) p = 0.1 MPa: \blacksquare , DMF; \bigcirc , DMSO. (b) T = 298.15 K: \blacksquare , DMF; \bigcirc , DMSO. Lines are for visual aid.

The various $\rho(p,T)$ data sets available for DMF^{19,20} at 288.15 $\leq T/K \leq 313.15$ were combined and interpolated or extrapolated to give the densities listed in Table 5. For DMSO $\rho(p,T)$ was taken from ref 18. For both DMF and DMSO, ε_{ree} was approximated as $1.1n^2$ where *n* is the refractive index of the liquid at the sodium D line.³⁹ The multiplicative factor of 1.1 accounts approximately for vibrational modes not excited by the Na D line. Values of n(p,T) were calculated from the Lorentz–Lorenz⁴⁰ equation:

$$[R] = \frac{n^2 - 1}{n^2 + 2\rho N_A} \tag{7}$$

assuming a constant molar refraction, [*R*], of 19.97 cm³·mol⁻¹ for DMF and 20.23 cm³·mol⁻¹ for DMSO.⁴¹ The dipole moments of DMF and DMSO were taken as $\mu = 12.7 \cdot 10^{-30}$ C·m and $\mu = 13.2 \cdot 10^{-30}$ C·m, respectively.²⁷

The calculated correlation factors are summarized in Table 5. For both liquids the present correlation factors agree well with the values obtained with other experimental techniques^{32,42–44} and molecular dynamic simulations.⁴⁵ At all temperatures and pressures g values are slightly higher than unity, suggesting a marginal preference for parallel alignment of the molecular dipoles in both solvents. The effects of temperature (at p = 0.1MPa) and pressure (at T = 298.15 K) on the correlation factor are plotted in Figure 8. The present data indicate that g increases with increasing temperature and decreasing pressure, which yields a small negative activation energy for the dipole-dipole interaction. However, the variation of g with T and p is very small (Table 5), so these trends may well be just a reflection of the uncertainties in $\varepsilon_{r\infty}$ and ρ . In particular, $\varepsilon_{r\infty}$ could be greater than $1.1n^2$ because of atomic polarization and the neglect of effects due to inter- and intramolecular vibrations (it is known that DMF exhibits a high frequency mode at $\approx 160 \text{ GHz}^{32}$).

Conclusions

The relative permittivity of DMF measured with a re-entrant radio frequency resonator at p = 0.1 MPa agreed with reliable literature values. A value of $(\partial \varepsilon_r / \partial p)_T = (28.6 \pm 1.0)$ TPa⁻¹ was obtained for DMF from measurements at $p \le 5$ MPa. For DMSO the measured ε_r was lower than most literature values, while $(\partial \varepsilon_r / \partial p)_T$ agreed within an extrapolated value with the combined uncertainties. For both solvents the Kirkwood *g* factor was slightly higher than 1, indicating a slight tendency for parallel alignment of the dipoles. Radio-frequency and microwave resonant cavities are probably the most precise technique currently available for measuring $\varepsilon_r(p,T)$ of fluids of conductance of $\leq 1 \cdot 10^{-2} \, \text{S} \cdot \text{m}^{-1}$. The present cavity is limited in both its temperature and pressure range, so results were not as precise as expected. Ideally, for measurements of $\varepsilon_r(p,T)$ a cavity should be usable at pressures up to at least 100 MPa and be capable of operating over a 200 K temperature range. It should have at least two modes with vacuum frequencies sufficiently high so that the instrumentation can cope with the addition of a high permittivity fluid. The need to minimize high purity sample consumption will influence the design.

Supporting Information Available:

Literature data on the permittivity of DMF and DMSO and comparison with the present data in both tabular and graphical form. This material is available free of charge via the Internet at http:// pubs.acs.org.

Literature Cited

- Drude, P.; Nernst, W. On the electrostriction induced by free ions. Z. Phys. Chem. (München, Ger.) 1894, 15, 79–85.
- (2) Brouillette, D.; Perron, G.; Desnoyers, J. E. Apparent molar volume, heat capacity, and conductance of lithium bis(trifluoromethylsulfone)imide in glymes and other aprotic solvents. *J. Solution Chem.* 1998, 27, 151–182.
- (3) Marcus, Y.; Hefter, G. On the pressure and electric field dependencies of the relative permittivity of liquids. J. Solution Chem. 1999, 28, 575–592.
- (4) Chadwick, S. S. Ullmann's Encyclopedia of Industrial Chemistry; Wiley-VCH: Weinheim, 2006.
- (5) Moldover, M. R.; Marsh, K. N.; Barthel, J.; Buchner, R. Relative permittivity and refractive index. In *Experimental Thermodynamics*; Goodwin, A. R. H., Marsh, K. N., Wakeham, W. A., Eds.; Elsevier: Amsterdam, 2003; Vol. VI.
- (6) Goodwin, A. R. H.; Mehl, J. B.; Moldover, M. R. Reentrant radiofrequency resonator for automated phase-equilibria and dielectric measurements in fluids. *Rev. Sci. Instrum.* **1996**, 67, 4294–4303.
- (7) Kandil, M. E.; Marsh, K. N.; Goodwin, A. R. H. Determination of the relative permittivity and density within the gas phase and liquid volume fraction formed within the two-phase region for (0.4026 CH₄ + 0.5974 C₃H₈) with a radio frequency re-entrant cavity. *J. Chem. Eng. Data* **2007**, *52*, 1660–1671.
- (8) May, E. F.; Edwards, T. J.; Mann, T. J.; Edwards, C. Dew point, liquid volumes and dielectric constant measurements in a vapor mixture of methane + propane using a microwave apparatus. *Int. J. Thermophys.* 2003, 24, 1509–1525.
- (9) May, E. F.; Edwards, T. J.; Mann, T. J.; Edwards, C.; Miller, R. C. Development of an automated phase behaviour measurement system for lean hydrocarbon fluid mixtures, using re-entrant rf/microwave resonant cavities. *Fluid Phase Equilib.* 2001, 185, 339–347.
- (10) May, E. F.; Edwards, T. J.; Mann, T. J.; Edwards, C. An improved microwave apparatus for phase behaviour measurements in lean gas condensate fluids. *Fluid Phase Equilib.* **2004**, *215*, 245–252.
- (11) May, E. F.; Miller, R. C.; Goodwin, A. R. H. Dielectric constants and molar polarizabilities for vapor mixtures of methane + propane, and methane + propane + hexane obtained with a radio frequency reentrant cavity. J. Chem. Eng. Data 2002, 47, 102–105.
- (12) Kandil, M. E.; Marsh, K. N.; Goodwin, A. R. H. Determination of the relative permittivity, ε', of methylbenzene at temperatures between (290 and 406) K, and pressures below 20 MPa with a radio frequency re-entrant cavity and evaluation of a MEMS capacitor for the measurement of ε'. J. Chem. Eng. Data 2008, 53, 1056–1065.
- (13) Goodwin, A. R. H.; Mehl, J. B. Measurement of the dipole moments of seven partially fluorinated hydrocarbons with a radiofrequency reentrant cavity resonator. *Int. J. Thermophys.* **1997**, *18*, 795–806.
- (14) Hamelin, J.; Mehl, J. B.; Moldover, M. R. The static dielectric constant of liquid water between 274 and 418 K near the saturated vapor pressure. *Int. J. Thermophys.* **1998**, *19*, 1359–1380.
- (15) Hamelin, J.; Mehl, J. B.; Moldover, M. R. Resonators for accurate dielectric measurements in conducting liquids. *Rev. Sci. Instrum.* 1998, 69, 255–260.
- (16) Anderson, G. S.; Miller, R. C.; Goodwin, A. R. H. Static dielectric constants for liquid water from 300 to 350 K at pressures to 13 MPa using a new radio-frequency resonator. J. Chem. Eng. Data 2000, 45, 549–554.

- (17) http://physics.nist.gov/cuu/Constants/index.html (accessed Jan 26, 2010).
- (18) Petitet, J. P.; Bezot, P.; Hesse-Bezot, C. Thermodynamic properties of (0.32 DMSO-H₂O) mixture and pure DMSO under pressure. *Physica B* (*Amsterdam, Neth.*) **1988**, *153*, 181–190.
- (19) García-Giménez, P.; Martínez-López, J. F.; Blanco, S. T.; Velasco, I.; Otín, S. Densities and isothermal compressibilities at pressures up to 20 MPa of the systems *N*,*N*-dimethylformamide or *N*,*N*-dimethylacetamide + α,ω-dichloroalkane. *J. Chem. Eng. Data* **2007**, *52*, 2368– 2374.
- (20) Zúñiga-Moreno, A.; Galicia-Luna, L. A. Compressed liquid densities and excess volumes for the binary system CO₂ + *N*,*N*-dimethylformamide (DMF) from (313 to 363) K and pressures up to 25 MPa. *J. Chem. Eng. Data* **2005**, *50*, 1224–1233.
- (21) http://www.kayelaby.npl.co.uk/general_physics/2_6/2_6_1.html (accessed Jan 26, 2010).
- (22) Schmidt, J. W.; Gavioso, R. M.; May, E. F.; Moldover, M. R. Polarizability of helium and gas metrology. *Phys. Rev. Lett.* 2007, 98, 254504.
- (23) McCarty, R. D.; Arp, V. D. A new wide range equation of state for helium. Adv. Cryog. Eng. 1990, 35, 1465–1475.
- (24) Harvey, A. H.; Lemmon, E. W. Method for estimating the dielectric constant of natural gas mixtures. *Int. J. Thermophys.* 2005, 26, 31– 46.
- (25) Lemmon, E. W.; McLinden, M. O.; Huber, M. L. Reference fluid thermodynamic and transport properties, NIST Standard Reference Database 23, Version 8.0; NIST: Gaithersburg, MD, 2007.
- (26) Bauccio, M. ASM Metals Reference Book; ASM International: Akron, OH, 1993.
- (27) CRC-Handbook of Chemistry and Physics, 85th ed.; Lide, D. R., Ed.; CRC Press: Boca Raton, FL, 2004.
- (28) Fernandez, D. P.; Goodwin, A. R. H.; Lemmon, E. W.; Levelt Sengers, J. M. H.; Williams, R. C. A Formulation for the static permittivity of water and steam at temperatures from 238 to 873 K at pressures up to 1200 MPa, including derivatives and Debye-Hückel coefficients. J. Phys. Chem. Ref. Data 1997, 26, 1125–1166.
- (29) Wohlfarth, C. Dielectric constant of N,N-dimethylformamide. In Landolt-Börnstein: Numerical Data and Functional Relationships in Science and Technology - New Series: Static Dielectric Constants of Pure Liquids and Binary Liquid Mixtures; Madelung, O., Ed.; Springer: Berlin, 2008; Vol. 17, pp 175–182.
- (30) Wohlfarth, C. Dielectric constant of dimethylsulfoxide. In Landolt-Börnstein: Numerical Data and Functional Relationships in Science and Technology - New Series: Static Dielectric Constants of Pure Liquids and Binary Liquid Mixtures; Madelung, O., Ed.; Springer: Berlin, 2008; Vol. 17, pp 140–143.
- (31) Uosaki, Y.; Kitaura, S.; Moriyoshi, T. Static relative permittivities of water + acetone and water + dimethyl sulfoxide under pressures up to 300 MPa at 298.15 K. J. Chem. Eng. Data 1997, 42, 580–584.
- (32) Barthel, J.; Buchner, R.; Wurm, B. The dynamics of liquid formamide, *N*-methylformamide, *N*,*N*-dimethylformamide, and *N*,*N*-dimethylacetamide. A dielectric relaxation study. *J. Mol. Liq.* 2002, *98*, 51–69.
- (33) Kaatze, U.; Pottel, R.; Schäfer, M. Dielectric spectrum of dimethyl sulfoxide/water mixtures as a function of composition. *J. Phys. Chem.* 1989, 93, 5623–5627.

- (34) Puranik, S. M.; Kumbharkhane, A. C.; Mehrotra, S. C. Dielectric study of dimethyl sulfoxide-water mixtures using the time-domain technique. *J. Chem. Soc., Faraday Trans.* **1992**, 88, 433–435.
- (35) Cooke, C.; McCallum, C.; Pethybridge, A. D.; Prue, J. E. Conductance of acids in dimethylsulphoxide-I: Conductance of hydrochloric acid in DMSO-water mixtures at 25 °C. *Electrochim. Acta* **1975**, *20*, 591– 598. (a) Kim, J. I.; Cecal, A.; Born, H. J.; Gomaa, E. A. Preferential solvation of single ions: A critical study of the Ph₄AsBPh₄ assumption for single ion thermodynamics in mixed aqueous-acetonitrile and aqueous-*N*,*N*-dimethylformamide solvents. *Z. Phys. Chem. (München, Ger.)* **1978**, *110*, 209–227.
- (36) Barthel, J.; Bachhuber, K.; Buchner, R.; Gill, J. B.; Kleebauer, M. Dielectric spectra of some common solvents in the microwave region. Dipolar aprotic solvents and amides. *Chem. Phys. Lett.* **1990**, *167*, 62–66.
- (37) Fröhlich, H. *Theory of Dielectrics*, 2nd ed.; Oxford University Press: Oxford, 1965.
- (38) Kirkwood, J. G. The dielectric polarization of polar liquids. J. Chem. Phys. 1939, 7, 911–919.
- (39) Stokes, R. H.; Marsh, K. N. A stepwise dilution technique for measuring the static dielectric properties of liquid mixtures. Dielectric behavior of ethanol in cyclohexane, *n*-hexane, carbon tetrachloride, benzene, *p*-xylene, and carbon disulphide. *J. Chem. Thermodyn.* **1976**, 8, 709–723.
- (40) Böttcher, C. F. J. *Theory of Electrical Polarization*; Ed.; Elsevier: Amsterdam, 1973, Vol. 1, and 1978, Vol. 2 (with Bordewijk, P.).
- (41) Pacak, P. Polarizability and molecular radius of dimethyl-sulfoxide and dimethylformamide from refractive index data. J. Solution Chem. 1987, 16, 71–77.
- (42) Bass, S. J.; Nathan, W. I.; Meighan, R. M.; Cole, R. H. Dielectric properties of alkyl amides. II. Liquid dielectric constant and loss. J. Phys. Chem. 1964, 68, 509–515.
- (43) Kinart, M. C.; Bald, A.; Kinart, W. J.; Kolasinski, A. Dimethylsulfoxide-*N*,*N*-dimethylformamide binary mixtures and their physicochemical properties. *Phys. Chem. Liq.* **1998**, *36*, 245–256.
- (44) Prestbo, E. W.; McHale, J. L. Static dielectric constants and Kirkwood correlation factors of dimethyl sulfoxide/carbon tetrachloride solutions. *J. Chem. Eng. Data* **1984**, *29*, 387–389.
- (45) Richardi, J.; Krienke, H.; Fries, P. H. Dielectric constants of liquid formamide, *N*-methylformamide and dimethylformamide via molecular Ornstein-Zernike theory. *Chem. Phys. Lett.* **1997**, *273*, 115–121.
- (46) Barthel, J.; Neueder, R. Conductivities, transference numbers, and limiting ionic conductivities of protophilic H-bond donor and aprotic solvents. I: Amides. In *Electrolyte Data Collection* (Part 1g); Kreysa, G., Ed.; DECHEMA: Frankfurt, 2001; Vol. XII.
- (47) Barthel, J.; Neueder, R. Conductivities, transference numbers, and limiting ionic conductivities of protophilic H-bond donor and aprotic solvents. II: Aprotic solvents, except amides. In *Electrolyte Data Collection* (Part 1h); Kreysa, G., Ed.; DECHEMA: Frankfurt, 2003; Vol. XII.

Received for review December 22, 2009. Accepted January 11, 2010. K.M. acknowledges the award of a Gledden Fellowship by the University of Western Australia. J.H.'s time in Perth was funded by Murdoch University.

JE9010773