

Measurement and Correlation of Solubility Data for CO₂ in NaHCO₃ Aqueous Solution

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ABSTRACT: To investigate the influence of NaHCO₃ on the CO₂ absorption in aqueous solution, the solubility of CO₂ in NaHCO₃ aqueous solutions [(0, 0.05, 0.1, 0.5, and 1.0) mol·kg⁻¹] was measured in the temperature range from (313 to 333) K with pressure range from (0.3 to 2.0) MPa by employing a new designed batch apparatus. The results showed that the solubility data for CO₂ in NaHCO₃ aqueous solutions agreed well with Henry's law, and the Henry constant appeared to be a function of temperature and the concentration of NaHCO₃. Two thermodynamic models were proposed for correlating the experimental data, that is, the modified Setschenow and Peng–Robinson (PR)-Duan equations. It was proved that the models fitted well in with the experimental data, and the average relative deviations were (4.06 and 3.90) %, respectively. In addition, the Henry constant in pure water can be basically predicted at a certain temperature range. The influence of NaHCO₃ on the solubility of CO₂ is interpreted by “salting-out effect” which is usual for the salt-containing solutions.

INTRODUCTION

The carbonation of aqueous sodium chromate is an attractive alternative to the conventional acidification route for the manufacturing of sodium dichromate which is extensively used in leather, textile, and other industries.^{1–3} This process involves the absorption of carbon dioxide in aqueous sodium chromate solution.^{4,5} However, with taking byproduct NaHCO₃ unceasingly, the carbonation will be affected because NaHCO₃ plays a negative role during the absorption of CO₂, that is, NaHCO₃ obviously decreased the solubility of CO₂ in the carbonization solutions.^{6,7} The objective of this work is to investigate the system CO₂–water in the presence of NaHCO₃ to get enough experimental data to validate a rational thermodynamic model for describing this system. Therefore, it was decided to measure the solubility of CO₂ in aqueous solutions of NaHCO₃ (0, 0.05, 0.1, 0.5, and 1.0 mol·kg⁻¹) within the temperature range from (313 to 333) K and for pressure range from (0.3 to 2.0) MPa. The conditions selected were determined by the carbonization process. For the correlation of the experimental data, two thermodynamic models—modified Setchenow and Peng Robinson (PR)-Duan equations—were proposed.

A large number of experimental studies have been conducted with different techniques to measure the solubility of CO₂ in pure water and more complex aqueous solutions. Table 1 reports the solubility of CO₂ in different aqueous solutions at various temperatures, pressures, and concentrations presented in literature. Among these studies, the solubility of CO₂ in NaCl aqueous solutions was widely studied, such as the data from Koschel et al.,⁸ Takenouchi and Kennedy,⁹ Nighswander et al.,¹⁰ Rumpf et al.,¹¹ Drummond,¹² and Gehrig.¹³ However, the data are scarce on the solubility of CO₂ in other systems. Portuga et al.¹⁴

measured the solubility of CO₂ in aqueous solutions of potassium glycinate with a stirred reactor. Ferrentino et al.¹⁵ used two different setups (semicontinuous equipment and batch equipment) to measure the solubility of CO₂ in NaH₂PO₄ aqueous solutions. Bermejo et al.¹⁶ determined the solubility of CO₂ in pure water and aqueous solutions of Na₂SO₄ with a Cailletet apparatus. Kamps et al.¹⁷ reported the simultaneous solubility of NH₃ and CO₂ in aqueous solutions of NH₄Cl, NH₄NO₃, and NaNO₃. Kamps et al.¹⁸ used a high-pressure view-cell technique based on the synthetic method to determine the solubility of CO₂ in aqueous solutions of KCl and K₂CO₃. Prutton and Savage¹⁹ determined the solubility of CO₂ in aqueous solutions CaCl₂. Gao et al.²⁰ and Wong and Ya²¹ determined the solubility of CO₂ in aqueous solutions of NaHCO₃ using the equilibrium liquid sampling method and a coulometric technique, respectively.

Modeling of the gas–liquid phase equilibria which has been widely studied can basically be subdivided into four approaches: (1) the empirical approaches, such as Setchenow's salting-out equation²² and Kent and Eisenberg's KE equation;²³ (2) the application of the activity coefficient model, which forms the basis for the electrolyte NRTL (nonrandom two-liquid) model²⁴ and Li–Mather^{25–27} equation; (3) the use of an equation of state (EOS) model, which is a fairly new development, finding application in recent publications. Kiepe et al.²⁸ successfully

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Table 1. Solubility of CO₂ in Different Aqueous Solutions

authors	aqueous solution	$m_s/\text{mol}\cdot\text{kg}^{-1}$	T/K	P/MPa
Koschel et al. ⁸	NaCl	1–3	323–373	0–20
Takenouchi and Kennedy ⁹	NaCl	0–4.28	423–723	10–140
Nighswander et al. ¹⁰	NaCl	0–0.17	353–473	2–10
Rumpf et al. ¹¹	NaCl	4–6	313–433	0.1–10
Drummond ¹²	NaCl	0–6.5	290–673	3.5–40
Gehrig ¹³	NaCl	1–4.3	408–800	3–280
Portuga et al. ¹⁴	NH ₂ CH ₂ COOK	0.1–3.0	293–351	0–0.06
Ferrentino et al. ¹⁵	NaH ₂ PO ₄	0.02–0.40	288–368	7.58–13.10
Bermejo et al. ¹⁶	Na ₂ SO ₄	0.25–1	288–368	0–14
Kamps et al. ¹⁷	NH ₄ Cl+ NH ₄ NO ₃ + NaNO ₃	4	313–393	0–0.7
Kamps et al. ¹⁸	KCl	2–4	313–433	0–9.4
Kamps et al. ¹⁸	K ₂ CO ₃	0.43–1.7	313–393	0.27–9.2
Pruetton and Savage ¹⁹	CaCl ₂	0–3.9	348–394	1–70
Gao et al. ²⁰	NaHCO ₃	0.2–0.8	323–403	5–50
Wong and Ya ²¹	NaHCO ₃	0.1–0.5	278–298	

predicted the gas solubility in the NaCl aqueous solution system by coupling the predictive Soave–Redlich–Kwong (PSRK) EOS with the group contribution model LIFAC. Duan and Sun^{29–32} established a sound thermodynamic model based on a specific particle interaction approach for the chemical potential of CO₂.^{33,34} The fourth approach is the application of the statistical mechanics, for example, scaled particle theory^{35,36} successfully applied for calculating the solubility of nonpolar gas in KOH aqueous solutions (10 to 50 wt %),³⁷ or the molecular thermodynamic model^{38–41} established by Hu et al. for predicting the Henry's constants of gases in electrolyte solutions based on the first-order perturbation theory and a simplified radial distribution function.

EXPERIMENTAL SECTION

Materials. CO₂ had a mole fraction purity of 0.999; NaHCO₃ had a mass fraction purity of 0.998, and deionized water had an electrical conductivity of no more than 0.079 μS·cm⁻¹. NaHCO₃ aqueous solutions were prepared for the concentrations of (0, 0.05, 0.1, 0.5, and 1.0) mol·kg⁻¹.

Apparatus. The solubility was measured at ambient pressure by using a static approach which was described in literature.^{14,15,42,43} A new designed batch apparatus applied for the experiment is shown in Figure 1. Here a gas mass-flow controller was innovatively used which is more convenient and precise to take place of storing vessel for acquiring CO₂ quantity added to the reactor, n_0 . The apparatus consists of a gas cylinder; a GCF equilibrium still (947.21 ± 5.29 mL by calibration), which could bear the high pressure of 30 MPa; a 2XZ-4 vacuum pump, the limited pressure is 6·10⁻² Pa; a Mettler Toledo AL104 electronic balance with an accuracy of 0.0001 g; a CH2015 thermostatic bath, with an accuracy of ± 0.05 K; a SevenStar CS200 gas mass-flow controller, with an uncertainty of ± 1 mL·min⁻¹; and a CYB-36 pressure transducer with an accuracy of ± 0.05 % of full scale (6 MPa).

Procedure. First, a known volume (400 mL) of fresh NaHCO₃ aqueous solutions, m_{sol} , V_{sol} previously degassed was injected into the equilibrium still, V_i . The thermostatic bath was started which was used to adjust the temperature in the still to the desired value. Then, the still was purged by operating the

vacuum pump to make it completely empty and remove the remaining air. The values were turned on: V1, V2, and V3. A certain amount of gas was pushed into the still, which was recorded by gas mass-flow controller, V_0 . Value V_3 was turned off. Then, the stirring system was started until the equilibrium of the gas–liquid achieved, which happened when the pressure recorded, P_{eq} in the equilibrium still became constant. The solubility of CO₂ in NaHCO₃ aqueous solutions was computed as eqs 1 to 6.

$$n_0 = \frac{V_0 \cdot \rho(\text{CO}_2)}{M(\text{CO}_2)} \quad (1)$$

Here, $\rho(\text{CO}_2)$ and $M(\text{CO}_2)$ represent the density and molar mass of CO₂, respectively.

The amount of CO₂, n_{eq} remaining in the gas phase when the equilibrium happened was calculated by the Peng–Robinson cubic equation of state^{44,45} with the CO₂ partial pressure in the gas phase, P_{CO_2} , temperature, T , volume of gas phase in the still, V_g , and the volume per mole of CO₂, V_m . Here P_{CO_2} was computed by assuming that the gas phase obeyed Dalton's law and the partial pressure of water in vapor mixture, $P_{\text{H}_2\text{O}}$, is the same as the saturation pressure of pure water. Therefore, n_{eq} was obtained as follows,

$$P_{\text{CO}_2} = P_{\text{eq}} - P_{\text{H}_2\text{O}} \quad (2)$$

$$V_g = V_t - V_{\text{sol}} \quad (3)$$

$$P_{\text{CO}_2} = \frac{RT}{V_m - b} - \frac{a}{V_m(V_m + b) + b(V_m - b)} \quad (4)$$

$$n_{\text{eq}} = \frac{V_g}{V_m} \quad (5)$$

The solubility of CO₂ in NaHCO₃ aqueous solutions, m_{ex} , was then acquired,

$$m_{\text{ex}} = \frac{n_0 - n_{\text{eq}}}{m_{\text{sol}}} \quad (6)$$

The uncertainty of m_{ex} was determined from the uncertainty in temperature, pressure, and volume, which were ± 0.1, ± 0.05,

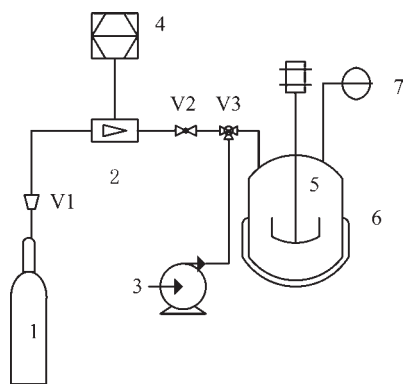


Figure 1. Schematic diagram of the experimental equipment: 1, gas cylinder; 2, gas mass-flow controller; 3, vacuum pump; 4, computer; 5, equilibrium still; 6, thermostatic bath; 7, pressure transducer; V1~V3, valves.

Table 2. Solubility of CO₂ in Pure Water Compared with Literature at $T = 323$ K

	P_{CO_2}	m_{CO_2}
	MPa	mol·kg ⁻¹
experiment	0.105	0.0208
	2.502	0.5111
literature ⁴⁶	0.1	0.0196
	2.5	0.5187

and ± 1 %, respectively, to give the estimated maximum uncertainty of ± 4 %.

RESULTS

To demonstrate the accuracy and precision of CO₂ solubility equipment and measurement procedures, the experimental results for the solubility of CO₂ in pure water were compared with the values presented in the literature.⁴⁶ Table 2 reports the experimental values of the solubility of CO₂ in pure water at 323 K.

It can be concluded from Table 2 that the experiment values differ from the literature values by 1.1 % and -1.5 % at (0.1 and 2.5) MPa, respectively. Therefore, it indicates that this equipment is able to reproduce the accurate solubility results which were very close to the experimental values of the solubility of CO₂ in pure water reported in previously published works.

Table 3 reports the experimental values of the solubility of CO₂ in NaHCO₃ aqueous solutions (0, 0.05, 0.1, 0.5, 1.0 mol·kg⁻¹) at a temperature range from (313 to 333) K with a pressure range from (0.3 to 2) MPa.

THERMODYNAMIC MODELS

Modified Setschenow Equation. From the solubility data presented in Table 3, it can be seen that a linear equilibrium relationship between CO₂ concentration and the equilibrium CO₂ partial pressure is obvious, which is described as Henry's law. For simplicity, the nonideality for gas phase is neglected in this work, because calculation is limited in the low-medium pressures, consequently, using P_{CO_2} to replace the fugacity of CO₂, f_{CO_2} , as eq 7,

$$P_{\text{CO}_2} = H \cdot m_{\text{CO}_2} \quad (7)$$

Table 3. Solubility of CO₂ in NaHCO₃ Aqueous Solutions

m_{NaHCO_3}	$T = 313$ K		$T = 323$ K		$T = 333$ K	
	P_{CO_2}	m_{CO_2}	P_{CO_2}	m_{CO_2}	P_{CO_2}	m_{CO_2}
mol·kg ⁻¹	MPa	mol·kg ⁻¹	MPa	mol·kg ⁻¹	MPa	mol·kg ⁻¹
0	0.369	0.1006	0.392	0.0673	0.380	0.0598
	0.792	0.1798	0.798	0.1487	0.784	0.1281
	1.204	0.2751	1.196	0.2330	1.209	0.1948
	1.595	0.3916	1.602	0.3204	1.602	0.2626
	1.993	0.4736	1.997	0.4014	2.000	0.3198
0.05	0.357	0.0806	0.579	0.1091	0.369	0.0565
	0.708	0.1595	0.939	0.1745	0.762	0.1196
	0.913	0.2104	1.292	0.2447	1.363	0.2157
	1.289	0.3014	1.695	0.3223	1.592	0.2539
	1.990	0.4604	1.975	0.3816	1.792	0.2756
0.1	0.310	0.0725	0.362	0.0655	0.378	0.0471
	0.856	0.1950	0.793	0.1440	0.822	0.1117
	1.200	0.2720	1.210	0.2257	1.185	0.1670
	1.605	0.3608	1.599	0.3024	1.593	0.2268
	1.901	0.4344	2.017	0.3866	1.988	0.2997
0.5	0.371	0.0725	0.399	0.0769	0.404	0.0516
	0.824	0.1617	0.807	0.1417	0.790	0.0984
	1.221	0.2349	1.188	0.2010	1.191	0.1460
	1.605	0.3082	1.605	0.2682	1.598	0.1963
	1.990	0.3900	1.993	0.3363	2.016	0.2564
1.0	0.376	0.0793	0.346	0.0667	0.342	0.0418
	0.826	0.1529	0.830	0.1331	0.853	0.0964
	1.222	0.2161	1.204	0.1816	1.200	0.1277
	1.619	0.2806	1.603	0.2380	1.595	0.1663
	2.035	0.3462	1.958	0.2884	1.955	0.1959

Therefore, as soon as Henry's constant, H , is predicted by building a credible thermodynamic model and the ambient pressure is given, the solubility of CO₂ in NaHCO₃ aqueous solutions will be known. It is well-known that the Setschenow equation⁴⁷ is applied for describing the relationship between the concentrations of aqueous solution and gas solute when the ambient pressure is certain. The modified Setchenow equation is proposed in this work for calculating H , which is determined by the concentration of the salt solutions, m_s , and T , as eq 8,

$$\log H = k_s \cdot m_s + k_0 \quad (8)$$

Combined eqs 7 and 8, it obtain eq 9,

$$\log \frac{P_{\text{CO}_2}}{m_{\text{CO}_2}} = k_s \cdot m_s + k_0 \quad (9)$$

To calculate the solubility of CO₂ as a function of T , P_{CO_2} , and m_s , it needs to determine the parameters, k_s and k_0 , which are dependent upon T . Following Li and Mather,²⁶ the parameters are selected as eq 10,

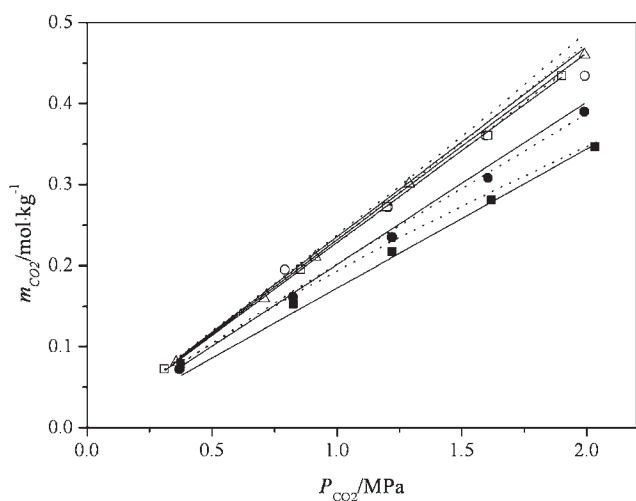
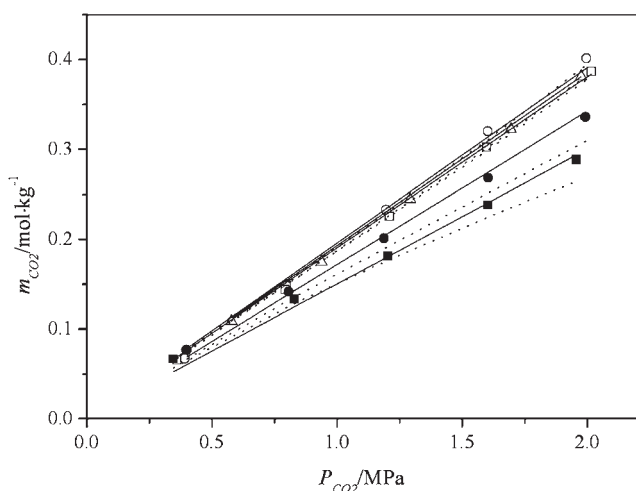
$$f(T) = a \ln T + b/T + c \quad (10)$$

Equations 9 and 10 form the basis of parametrization for the model; the objective function for regression is as eq 11,

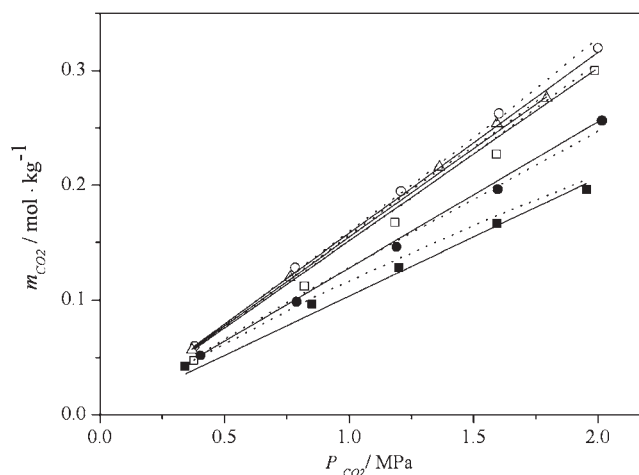
$$F_{\text{obj}} = \sum \left| \frac{m_{\text{ex}} - m_{\text{CO}}}{m_{\text{ex}}} \right| \quad (11)$$

Table 4. Fitted Values for Henry's Constants of the CO₂–NaHCO₃–H₂O System

	<i>a</i>	<i>b</i>	<i>c</i>
<i>k_s</i>	96.5800	30934.3165	−653.6629
<i>k₀</i>	19.1934	5295.9216	−126.5809

**Figure 2.** Solubility of CO₂ in NaHCO₃ aqueous solutions as a function of P_{CO_2} at $T = 313$ K. The points show the experimental data. The solid and dot lines show the modified Setschenow equation and PR-Duan equation correlated values, respectively. \circ , 0 mol·kg^{−1}; Δ , 0.05 mol·kg^{−1}; \square , 0.1 mol·kg^{−1}; \bullet , 0.5 mol·kg^{−1}; \blacksquare , 1.0 mol·kg^{−1} NaHCO₃ aqueous solutions.**Figure 3.** Solubility of CO₂ in NaHCO₃ aqueous solutions as a function of P_{CO_2} at $T = 323$ K. The points show the experimental data. The solid and dot lines show the modified Setschenow equation and PR-Duan equation correlated values, respectively. \circ , 0 mol·kg^{−1}; Δ , 0.05 mol·kg^{−1}; \square , 0.1 mol·kg^{−1}; \bullet , 0.5 mol·kg^{−1}; \blacksquare , 1.0 mol·kg^{−1} NaHCO₃ aqueous solutions.

Here m_{CO} represents the correlated solubility of CO₂ by equation. Results of the parameters are listed in Table 4, and the correlation results are shown in Figures 2 to 4. The average relative deviation for the solubility of CO₂ from experimental data is 4.06 %.

**Figure 4.** Solubility of CO₂ in NaHCO₃ aqueous solutions as a function of P_{CO_2} at $T = 333$ K. The points show the experimental data. The solid and dot lines show the modified Setschenow equation and PR-Duan equation correlated values, respectively. \circ , 0 mol·kg^{−1}; Δ , 0.05 mol·kg^{−1}; \square , 0.1 mol·kg^{−1}; \bullet , 0.5 mol·kg^{−1}; \blacksquare , 1.0 mol·kg^{−1} NaHCO₃ aqueous solutions.

PR-Duan Equation. The solubility of CO₂ in aqueous solutions is determined from the balance of chemical potential between in the liquid phase, $\mu_{\text{CO}_2}^{\text{l}}$ and in the gas phase, $\mu_{\text{CO}_2}^{\text{g}}$. The chemical potential can be expressed in terms of fugacity, f_{CO_2} in the gas phase and activity, a_{CO_2} in the liquid phase, as eqs 12 and 13,

$$\begin{aligned} \mu_{\text{CO}_2}^{\text{l}}(T, P, m) &= \mu_{\text{CO}_2}^{\text{l}(0)}(T, P) + RT \ln a_{\text{CO}_2}(T, P, m) \\ &= \mu_{\text{CO}_2}^{\text{l}(0)}(T, P) + RT \ln m_{\text{CO}_2} + RT \ln \gamma_{\text{CO}_2}(T, P, m) \end{aligned} \quad (12)$$

$$\begin{aligned} \mu_{\text{CO}_2}^{\text{g}}(T, P, m) &= \mu_{\text{CO}_2}^{\text{g}(0)}(T) + RT \ln f_{\text{CO}_2}(T, P, y) \\ &= \mu_{\text{CO}_2}^{\text{g}(0)}(T) + RT \ln P_{\text{CO}_2} + RT \ln \varphi_{\text{CO}_2}(T, P, y) \end{aligned} \quad (13)$$

At equilibrium, $\mu_{\text{CO}_2}^{\text{l}} = \mu_{\text{CO}_2}^{\text{g}}$ to obtain eq 14,

$$\begin{aligned} \ln \frac{P_{\text{CO}_2}}{m_{\text{CO}_2}} &= \frac{\mu_{\text{CO}_2}^{\text{l}(0)}(T, P) - \mu_{\text{CO}_2}^{\text{l}(0)}(T)}{RT} - \ln \varphi_{\text{CO}_2}(T, P, y) \\ &\quad + \ln \gamma_{\text{CO}_2}(T, P, m) \end{aligned} \quad (14)$$

where $\mu_{\text{CO}_2}^{\text{l}(0)}$ and $\mu_{\text{CO}_2}^{\text{g}(0)}$ are the standard chemical potential of CO₂ in the ideal liquid phase ($m_{\text{CO}_2} = 1$ mol·kg^{−1}) and that in the ideal gas phase ($P_{\text{CO}_2} = 1$ MPa), respectively. The difference between $\mu_{\text{CO}_2}^{\text{l}(0)}$ and $\mu_{\text{CO}_2}^{\text{g}(0)}$ is defined as $\Delta G_{\text{m,CO}_2}^0$ for the CO₂ absorption process.

$\ln \varphi_{\text{CO}_2}$ can be acquired from the PR equation for pure CO₂, because the fugacity coefficient of CO₂, φ_{CO_2} , in the gas phase of CO₂–H₂O mixtures differs little from that of pure CO₂ at the experimental region. $\ln \varphi_{\text{CO}_2}$ can be calculated by eqs 15 and 16,

$$\ln \varphi_i = \frac{1}{RT} \int_{V_m}^{\infty} \left[\left(\frac{\partial P}{\partial n_i} \right)_{T, V, n_j} - \left(\frac{RT}{V_i} \right) \right] dV_i - \ln Z \quad (15)$$

Table 5. T and P_{CO_2} Dependence of Parameters for the PR-Duan Equation

	$\Delta G_{\text{m,CO}_2}^0/RT$	$\lambda_{\text{CO}_2-\text{Na}}$	$\zeta_{\text{CO}_2-\text{Na}-\text{HCO}_3}$
c_1	8.5921	1.0646	-0.2418
c_2	-2239.6877	-285.6020	
c_3	-0.0591	0.06984	

Peng and Robinson⁴⁸ defined the parameters A and B . Therefore, eq 16 for calculating $\ln \varphi_{\text{CO}_2}$ can be acquired,

$$A = \frac{aP}{(RT)^2} \quad B = \frac{bP}{RT} \quad Z = \frac{PV_{\text{m}}}{RT}$$

$$\ln \varphi_{\text{CO}_2} = Z - 1 - \ln(Z - B) - \frac{A}{2\sqrt{2}B} \ln \left[\frac{Z + (1 + \sqrt{2})B}{Z + (1 - \sqrt{2})B} \right] \quad (16)$$

$\ln \gamma_{\text{CO}_2}$ can be obtained from the Pitzer^{34,49,50} and Duan^{29–32} equations, as eq 17,

$$\begin{aligned} \ln \gamma_{\text{CO}_2} = & \sum_{\text{c}} 2\lambda_{\text{CO}_2-\text{c}} m_{\text{a}} + \sum_{\text{a}} 2\lambda_{\text{CO}_2-\text{a}} m_{\text{a}} \\ & + \sum_{\text{c}} \sum_{\text{a}} \zeta_{\text{CO}_2-\text{a}-\text{c}} m_{\text{c}} m_{\text{a}} \end{aligned} \quad (17)$$

where c and a represent cations and anions, respectively. λ and ζ are the second-order and third-order interaction parameters, respectively. Substituting eq 17 in eq 14, we obtain eq 18,

$$\begin{aligned} \ln \frac{P_{\text{CO}_2}}{m_{\text{CO}_2}} = & \frac{\Delta G_{\text{m,CO}_2}^0}{RT} - \ln \varphi_{\text{CO}_2} + \sum_{\text{c}} 2\lambda_{\text{CO}_2-\text{c}} m_{\text{c}} \\ & + \sum_{\text{a}} 2\lambda_{\text{CO}_2-\text{c}} m_{\text{a}} + \sum_{\text{c}} \sum_{\text{a}} \zeta_{\text{CO}_2-\text{a}-\text{c}} m_{\text{c}} m_{\text{a}} \end{aligned} \quad (18)$$

In the above equation, $\lambda_{\text{CO}_2-\text{HCO}_3}$ is set to zero; because measurements can only be made in electronically neutral solutions ($m_{\text{c}} = m_{\text{a}}$), one of the λ parameters can be deleted. Therefore, to calculate the solubility of CO_2 in NaHCO_3 aqueous solutions, the parameters, $\lambda_{\text{CO}_2-\text{Na}}$, $\zeta_{\text{CO}_2-\text{Na}-\text{HCO}_3}$, and $\Delta G_{\text{m,CO}_2}^0/RT$ need to be determined, which are all dependent upon T and P_{CO_2} . Following Pitzer et al.⁵¹ and Li and Mather,²⁶ eq 19 for the parameters is selected,

$$f(T, P_{\text{CO}_2}) = c_1 + c_2/T + c_3 P_{\text{CO}_2} \quad (19)$$

Equations 18 and 19 form the basis of parametrization for the model. According to the objective function—eq 11, the term $\Delta G_{\text{m,CO}_2}^0/RT$ was first evaluated by using the CO_2 solubility data in pure water with an average relative deviation of 3.85%. Then, $\lambda_{\text{CO}_2-\text{Na}}$ and $\zeta_{\text{CO}_2-\text{Na}-\text{HCO}_3}$ were evaluated simultaneously by fitting eq 18 using the CO_2 solubility data in NaHCO_3 aqueous solutions with average relative deviation of 3.90%. T and P_{CO_2} dependence of parameters are listed in Table 5, and the deviations of correlation for the solubility of CO_2 from experimental data are shown in Figures 2 to 4. The model, which is calculated by use of the PR equation in the gas phase and described by Duan's specific interaction model^{29–33} in the liquid phase, is an application of the EOS approach and defined as the PR-Duan equation in this work.

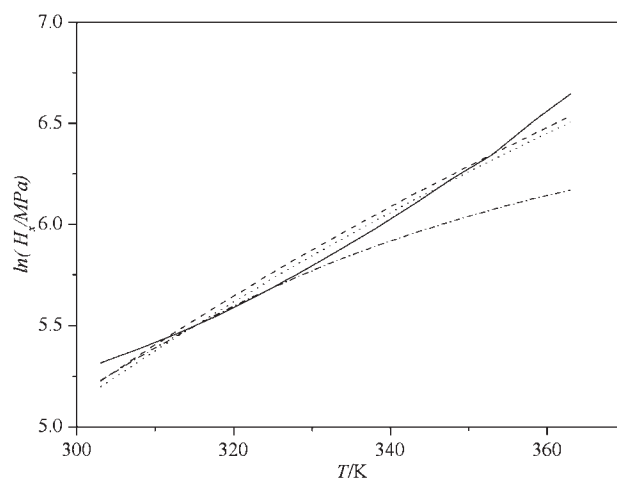


Figure 5. Correlated Henry constants for CO_2 in pure water as a function of T . The solid, dash, dot, and dash-dot lines show the eq 20, Lelieveld, Lide, and Harvey results, respectively.

DISCUSSION

Experimental data in Table 3 and curves in Figures 2 to 4 demonstrate the influence of NaHCO_3 on the solubility of CO_2 . Comparing the results with the solubility of CO_2 in pure water ($0 \text{ mol} \cdot \text{kg}^{-1} \text{ NaHCO}_3$), these values were lower and decreased with the increase of salt concentration in the solutions at a certain temperature and pressure. It can be interpreted by hydration. Because so much salt NaHCO_3 joins in the water, there will be a significant quantity of H_2O coming forth to associate with the ions in solutions as ionic hydration. Furthermore, with increasing the concentration of the saline solution, the water bonded to ions Na^+ and HCO_3^- is increasing, while the free water for dissolving CO_2 is decreasing. Therefore, a given total volume of water will dissolve a smaller concentration of CO_2 at equilibrium. The phenomenon—the effect of decreasing the solubility of molecular species by increasing salt concentration—is known as the “salting-out effect”, which in most case is not concerned with the composition in the aqueous solution.^{52,53}

The modified Setchenow equation is also applicable to the prediction of the Henry constant of CO_2 in pure water, H_0 , at a certain situation. According to eqs 9 and 10, H_0 can be obtained,

$$\log H_0 = k_0 \quad (20)$$

H_0 calculated by this model was compared with literature values which were reported by Harvey,⁵⁴ Lide and Frederikse,⁵⁵ and Lelieveld and Crutzen⁵⁶ as Figure 5. Here, the unit of H_0 is expressed as mole fraction based on Harvey's model.

It can be seen from Figure 5 that H_0 calculated by eq 20 basically approach the values which were correlated by Lide and Frederikse and Lelieveld and Crutzen in the temperature range from (303 to 363) K. By comparison, the difference between Harvey and eq 20 is small in the temperature range from (303 to 338) K and becomes a little obvious in the higher temperature range, because the measurements are only carried out at three temperatures. Therefore, it indicates that eq 20 is able to predict Henry constant of CO_2 in pure water in a certain temperature range.

CONCLUSION

The solubility of CO_2 in pure water and NaHCO_3 aqueous solution was measured within the temperature range from (313 to 333) K

and pressure range from (0.3 to 2.0) MPa by using a new designed static setup. Two thermodynamic models—the modified Setchenow and PR-Duan equations—were proposed with average relative deviation of (4.06 and 3.90) %, respectively. In addition, the Henry constant can be basically predicted at a certain temperature range. The influence of NaHCO_3 on the solubility of CO_2 is obvious, and it can be interpreted by “salting-out effect” which is usual for the salt-containing solutions.

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