

Ab Initio Density Functional Calculations of Deuterium Kinetic Isotope Effects for Decomposition of Dimethylnitramine

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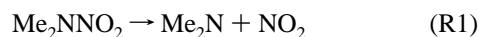
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Ab initio harmonic force fields were computed using the Becke3–Lee–Yang–Parr hybrid density functional with the standard 6-31G* basis set for dimethylnitramine, for dimethylamino radical, and for the transition structure for five-center elimination of HONO from dimethylnitramine. These force fields were used to calculate the primary deuterium kinetic isotope effect for the HONO elimination, and the secondary isotope effect for the N–N bond homolysis of dimethylnitramine. The computed primary effect is $k^H/k^{D6} = 4.21$, and the computed secondary effect is $k^H/k^{D6} = 1.40$, both at 240 °C. Comparison with the experimentally observed isotope effect of 1.57 for decomposition of dimethylnitramine-*d*₆ in solution at 240 °C suggests a significant part of the observed effect is due to the secondary effect on N–N bond homolysis. Similar β secondary deuterium isotope effects are expected for the N–NO₂ cleavages that initiate the decompositions of the nitramine explosives HMX and RDX.

Introduction

The decomposition of dimethylnitramine (DMNA) has been studied as a model for decomposition of more complex nitramine explosives such as hexahydro-1,3,5-trinitro-*s*-triazine (RDX) and octahydro-1,3,5,7-tetranitro-1,3,5,7-tetrazocine (HMX).¹ McQuaid identified three possible unimolecular pathways² for DMNA decomposition: (1) simple N–N homolysis, (2) rearrangement to a nitrite ester, Me₂NNO, and (3) concerted elimination of nitrous acid, HONO, through a five-center transition structure.



The N–N bond homolysis is the predominant pathway in the gas phase decomposition of DMNA using infrared multiphoton decomposition (IRMPD).^{1,3} The N–N homolysis also is the main pathway in the solution phase decomposition at 200–300 °C.⁴ Botcher and Wight⁵ found N–NO₂ homolysis was the initial reaction in the laser pyrolysis of solid RDX. Rearrangement to the nitrite was reported in one instance,^{3b,6} when DMNA was decomposed by IRMPD under collisional conditions. In IRMPD of nitromethane the C–N homolysis and rearrangement to nitrite are competitive pathways.^{6b,7} The third pathway, concerted HONO elimination, has not been observed directly for DMNA. Oxley suggested the elimination competes with N–N cleavage in solution.⁴ This conclusion was based on observation of a deuterium kinetic isotope effect (KIE) of $k^H/k^{D6} = 1.57$ at 240 °C. Primary KIEs are also observed in the condensed phase decompositions of RDX and HMX.⁸ Shaw and Walker speculated that HONO elimination could be a minor pathway in unimolecular decomposition of HMX.⁹ Also, Capellos^{10a} and Zuckermann^{10b} have suggested RDX reacts by HONO elimination in the gas phase. The elimination certainly takes place in the hydrocarbon analogue 2-nitropropane, and

the kinetic barrier for this process was determined by Benson¹¹ and later by Wodtke et. al.⁷

In the present work, we study the competing N–N cleavage and HONO elimination pathways using ab initio MO theory. Theoretical deuterium kinetic isotope effects are computed for these two pathways. Interestingly, we find the N–N bond cleavage has a significant secondary KIE for β deuterium substitution that arises from hyperconjugation of the amino radical with the adjacent C–H bonds. Although previous explanations^{4,8} focus on a primary KIE for rate-determining C–H bond cleavage, we suggest the secondary effect on N–N bond cleavage contributes significantly to the KIE in unimolecular dimethylnitramine decomposition.

Methods

Ab initio calculations were carried out using the Gaussian 94 programs.¹² Energies, geometries, and harmonic vibrational frequencies were computed using the Becke3–Lee–Yang–Parr (B3LYP) hybrid density functional¹³ with the standard 6-31G* basis set.^{14,15a} Computations were carried out on dimethylnitramine (DMNA), dimethylamino radical (Me₂N), NO₂ radical, the transition structure (TS) for elimination of HONO from DMNA, nitrous acid (HONO), and *N*-methylmethylenimine (MeNCH₂). Geometries for DMNA and TS are described in Tables 1 and 2. Absolute energies and zero-point vibrational energies for all structures are given in Table 3. B3LYP harmonic frequencies were computed as well for the perdeuterated analogues DMNA-*d*₆, Me₂N-*d*₆, and TS-*d*₆. The same calculations were also done using second-order Moller–Plesset theory,^{15a} with the frozen core approximation, again using the 6-31G* basis set (i.e., MP2(fc)/6-31G*^{15b}).

The harmonic frequencies for the isotopic pairs (DMNA/DMNA-*d*₆), (TS/TS-*d*₆), and (Me₂N/Me₂N-*d*₆) were used to compute the KIE for the concerted elimination of HONO and for the N–N bond homolysis.^{16,17} A FORTRAN program for computing isotope effects from frequencies is included in the Supporting Information, along with a table of harmonic frequencies for TS and TS-*d*₆.

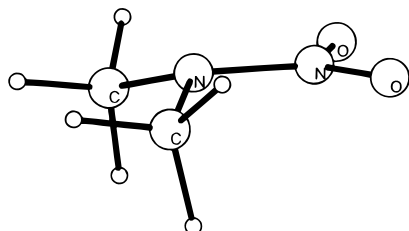
Briefly, the reduced isotopic partition function ratios^{16a,c} (s_2/s_1)^f were computed using the computed harmonic frequencies

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TABLE 1: B3LYP/6-31G* Geometries for DMNA (See Figure 1) Compared with Experimental Geometries from Ref 19 (Bond Lengths, angstroms; Angles, degrees)

	B3LYP	expt			B3LYP	expt	
		<i>a</i>	<i>b</i>			<i>a</i>	<i>b</i>
N–N	1.384	1.331(3)	1.383(3)	C–N–C	120.3	124.6(2)	127.6(6)
N–C	1.458	1.452(3)	1.460(3)	C–N–N	115.5	117.7(2)	116.2(3)
N–O	1.232	1.240(2)	1.223(2)	C–N–O	126.0	124.0(2)	130.4(3)
				O–O–N	117.0	118.0(2)	114.8(2)
				γ^c	30.3	0.00	0.00

^a X-ray crystal structure from ref 19a. ^b Gas phase geometry from electron diffraction.^{19b} ^c γ is the pyramidalization of the amine nitrogen, expressed as the angle between the CNC plane and the NN bond axis.

**Figure 1.** B3LYP/6-31G* geometry for dimethylnitramine (DMNA).**TABLE 2: B3LYP/6-31G* Geometries for TS (See Figure 2 for Numbering of Atoms) (Bond Lengths, angstroms; Bond Angles, degrees)**

N1–N2	2.190	N2–O2	1.206
N1–C1	1.343	O1–H1	1.320
N1–C2	1.451	H1–C1	1.314
N2–O1	1.270		
C–N1–C	117.1	N1–N2–O1	101.6
C1–N1–N2	94.6	N1–N2–O2	135.9
C2–N1–N2	97.2	H1–C1–N1	97.0
O–N2–O	122.2	H2–C1–N1	115.0
O1–H1–C1	152.3	H3–C1–N1	119.7
C1–N1–N2–O1	6.5	C1–N1–N2–O2	180.1
γ^a			29.6

^a γ is pyramidalization of C1, expressed as the angle between the H2C1H3 plane and the C1N1 bond axis.

TABLE 3: Absolute B3LYP/6-31G* energies (hartrees, 1 hartree = 627.51 kcal/mol), and Zero-Point Vibrational Energies (ZPVE; kcal/mol)

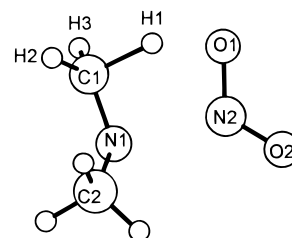
	energy	ZPE	energy	ZPE
DMNA	–339.656 546	60.08	HONO	–205.696 797 12.75
TS	–339.576 607	55.12	MeNCH ₂	–133.942 339 43.04
Me ₂ N	–134.509 485	48.66	NO ₂	–205.072 205 5.54

for DMNA/DMNA-*d*₆, TS/TS-*d*₆, and Me₂N/Me₂N-*d*₆. The KIE for the N–N dissociation reaction (eq R1) was computed from the ratio $(s_2/s_1)_{\text{DMNA}}/(s_2/s_1)_{\text{Me}_2\text{N}}$. Similarly, the KIE for the HONO elimination (eq R2) was computed from $\text{KIE} = (Q_t^{\text{H}}/Q_t^{\text{D}})(s_2/s_1)_{\text{DMNA}}/(s_2/s_1)_{\text{TS}}$.¹⁷ The factor $(Q_t^{\text{H}}/Q_t^{\text{D}})$ is a tunneling correction calculated with Bell's equation.^{17b,18}

The tunneling correction factor is given by $Q_t^{\text{H}}/Q_t^{\text{D}} = (|u^{\text{H}}/2|/\sin|u^{\text{H}}/2|)/(|u^{\text{D}}/2|/\sin|u^{\text{D}}/2|)$, where $|u| = h|\nu^*|/kT$, and ν^* is the imaginary frequency in the transition structure.¹⁸ This correction is valid if $|u| < 2\pi$ and if the potential energy is a quadratic function of the reaction coordinate in the region of the saddle point.

Results and Discussion

Geometries and Energies. The theoretical geometry for dimethylnitramine is compared with the experimental gas phase and solid phase geometries¹⁹ in Table 1. Both experimental geometries are planar ($\gamma = 0.00^\circ$), with *C*_{2v} symmetry, while the B3LYP/6-31G* structure (Figure 1) is pyramidal at the amine nitrogen ($\gamma = 30.3^\circ$; see Table 1), with *C*_s symmetry.

**Figure 2.** B3LYP/6-31G* geometry for the transition structure (TS) for elimination of HONO from dimethylnitramine

The MP2/6-31G* and B3LYP/6-31G* geometries are very similar, except the amine is more pyramidal ($\gamma = 38.5^\circ$) and the N–O bonds are 0.009 Å longer in the MP2 geometry.

Compared with the theoretical structure, the experimental X-ray crystal structure^{19a} has a short N–N bond, long N–O bonds, and a wide C–N–C angle (Table 1). These differences, and the planar geometry in the solid, suggest that electron donation from the amine lone pair to the nitro group is more important in the solid than in the gas phase.²⁰ This might be caused by intermolecular electrostatic interactions which lead to enhanced resonance in the crystalline state.

The experimental gas phase structure for DMNA^{19b} also differs considerably from the theoretical gas phase geometry. The large differences in the C–N–C and O–N–O angles and in the pyramidalization of the amine²⁰ suggest the experimental gas phase geometry is inaccurate.

In the transition structure for HONO elimination (see Figure 2 and Table 2) the breaking CH bond and the forming OH bond have nearly equal lengths. The N–N bond in TS is stretched to 2.19 Å, and the nitro group and N1, C1, and H1 atoms form a nearly planar five-membered ring. The C–H–O angle around the transferred hydrogen is nonlinear at 152.3°. In the MP2/6-31G* transition structure the breaking C–H bond is longer by 0.024 Å, the forming O–H bond is shorter by 0.028 Å, and the breaking N–N bond is shorter by 0.150 Å than in the B3LYP/6-31G* structure.

The B3LYP/6-31G* harmonic frequencies for DMNA and DMNA-*d*₆ are given in Table 4a, and the observed infrared frequencies for DMNA^{3a} are given in Table 4b. The most intense bands in the theoretical spectrum are assigned to the NO₂ symmetric and asymmetric stretching modes at 1355 and 1652 cm^{–1}, respectively. These are in good agreement with the observed bands at 1300 and 1560 cm^{–1}, after allowance is made for vibrational anharmonicity, which tends to make the observed frequencies about 5% smaller than the theoretical harmonic frequencies.^{16c}

The B3LYP/6-31G* enthalpy barrier at 0 K for the N–N cleavage is 41.08 kcal/mol (Table 5). At PMP2/6-31G* the bond enthalpy increases to 45.11 kcal/mol. Some experimental estimates for the N–N bond dissociation enthalpy for DMNA at 298 K are 45.9,²¹ 46.5,^{3b} and 46.2 kcal/mol.⁹ These are smaller than the C–N bond dissociation enthalpy of 53 kcal/mol for the carbon analogue 2-nitropropane.⁷

TABLE 4

(a) B3LYP/6-31G* Harmonic Vibrational Frequencies for Dimethylnitramine and Dimethylnitramine-*d*₆ (IR intensities (kM/mol) in parentheses)

ν^H (cm ⁻¹)	ν^D (cm ⁻¹)	assignment
118 (0.1)	91	a'' NN torsion + CN torsion
123 (3)	92	a' CN torsion
137 (0.3)	121	a'' CN torsion
205 (9)	185	a' amine inversion
358 (2)	324	a'' CNN bend
421 (4)	360	a' CNC bend
615 (10)	588	a'' skeletal def
623 (1)	589	a' skeletal def
778 (20)	774	a' NO ₂ out of plane def
859 (10)	799	a' ONO bend + CN str
1011 (68)	835	a' HCN bend + NN str + CN str
1064 (13)	867	a'' HCN bend
1138 (3)	895	a'' HCN bend
1165 (50)	927	a' HCN bend
1284 (4)	1080	a' NN str + HCN bend + CNC bend
1325 (2)	1089	a'' CN str + HCN bend
1355 (278)	1092	a' NO ₂ sym str + N-N str + HCH bend
1457 (6)	1101	a'' HCH bend
1497 (35)	1108	a' HCH bend
1504 (12)	1138	a'' HCH bend
1522 (11)	1198	a' HCH bend
1524 (1)	1300	a'' HCH bend
1543 (38)	1376	a' HCH bend
1652 (265)	1649	a'' NO ₂ assym str
3041 (23)	2189	a'' CH str
3046 (44)	2195	a' CH str
3136 (0.1)	2319	a'' CH str
3142 (33)	2321	a' CH str
3190 (2)	2365	a'' CH str
3192 (5)	2369	a' CH str

(b) Experimental Fundamental Frequencies (cm⁻¹) for Dimethylnitramine from Ref 3a (Degeneracies in Parentheses)

2940 (6)	C-H str	1150 (6)	H-C-N bend
1560	N-O str	1100 (2)	C-N str
1430 (4)	H-C-H bend	800 (2)	C-N-N bend
1300	N-O str	640 (3)	N-N-O bend
1250	N-N str	230 (2)	C-N torsion
1200	C-N-C bend	150	N-N torsion

TABLE 5: B3LYP/6-31G* Energies in kcal/mol, Corrected for ZVPE

DMNA → Me ₂ N + NO ₂	ΔE = 41.08 kcal/mol
DMNA → [TS]	ΔE = 45.20 kcal/mol
DMNA → MeNCH ₂ + HONO	ΔE = 6.64 kcal/mol

The bond dissociation enthalpy at 0 K for the parent nitramine, NH₂NO₂, is 51.1 kcal/mol using the accurate G2 theory,²² compared to 47.0 kcal/mol computed with B3LYP/6-31G*. This suggests the B3LYP/6-31G* enthalpy for N-N cleavage in DMNA should be adjusted upward to 45.2 kcal/mol, which increases to 47 kcal/mol after a temperature correction to 298 K. This gives better agreement with the experimental data.

The HONO elimination has never been observed directly for DMNA or other nitramines. The B3LYP/6-31G* enthalpy barrier at 0 K is 45.20 kcal/mol (Table 5). At MP2/6-31G* this increases to 53.83 kcal/mol. Lazarou^{3a} suggests the barrier should be the same as the 41–43 kcal/mol barrier for HONO elimination in 2-nitropropane,⁷ but Melius²¹ suggests the barrier for the nitramine should be 2 kcal/mol lower than for the carbon analogue. The computed enthalpy change for formation of HONO + MeNCH₂ is 6.64 kcal/mol at 0 K, compared with other estimates of -1⁹ and +3 kcal/mol^{3a} for the enthalpy change at 298 K.

It appears that our B3LYP/6-31G* barrier for N-N cleavage is underestimated by 5 kcal/mol and our barrier for HONO elimination is overestimated by 2–6 kcal/mol. The MP2/6-

TABLE 6: Computed Isotope Effects at 240 °C

DMNA → Me ₂ N + NO ₂	$k^H/k^{D6} = 1.40$ (1.37 ^a)
DMNA → [TS] → CH ₂ NMe + HONO	$k^H/k^{D6} = 4.21$ (4.02 ^a)

^a Computed using 0.95 scaled B3LYP/6-31G* frequencies.

31G* theory also incorrectly indicates the HONO elimination barrier to be higher in energy than the barrier for N-N cleavage. We suspect that a multireference configuration interaction approach would be better than B3LYP or MP2 for computing the energy difference between the two competing pathways,^{23,6} but such calculations are presently beyond our means.

The HONO elimination pathway is entropically more demanding than the N-N cleavage. This is reflected in the difference in preexponential Arrhenius factors—log *A* = 12 for HONO elimination and log *A* = 15.5 for N-N cleavage.^{3a,7,11}

Uncertainty in the Arrhenius parameters, especially in the activation barrier for the HONO elimination, makes it difficult to estimate the branching ratio for the two pathways, but it has been suggested that the elimination is a minor pathway if it is present at all.^{3c,4,9}

The branching ratio is given by the Arrhenius expression $k_1/k_2 = (A_1/A_2) \exp(-\Delta E_a/RT)$. Both the preexponential factor and the activation energy are larger for the N-N cleavage pathway (*k*₁) than for the elimination pathway (*k*₂). We can estimate the difference Δ*E*_a = 4 kcal/mol in activation barriers and the difference Δlog *A* = 3 in preexponential factors. This gives a branching ratio of *k*₁/*k*₂ = 14 at 200 °C and *k*₁/*k*₂ = 30 at 300 °C in favor of N-N cleavage. However, small uncertainties of 0.5 in Δlog *A* and 1 kcal/mol in Δ*E*_a lead to a factor of 9 uncertainty in the branching ratio.

Kinetic Isotope Effects. The computed KIEs for the N-N bond cleavage and HONO elimination are presented in Table 6. The computed primary KIE for HONO elimination is 4.21 at 240 °C, which includes a correction factor of 1.41 for quantum tunneling. The MP2/6-31G* primary KIE is 4.42, including tunneling. Superimposed on the primary KIE for the HONO elimination is a secondary KIE for the remaining hydrogens (or deuteriums) which are not transferred.

The true primary KIE can be computed from the vibrational frequencies of the monodeuterated DMNA-*d*₁ and TS-*d*₁ as $k^H/k^{D1} = 3.36$, including a correction factor of 1.39 for tunneling. The remaining KIE of 4.21/3.36 = 1.25 represents the superimposed secondary KIE due to the five hydrogens or deuteriums that are not transferred.

The B3LYP/6-31G* β secondary KIE for N-N cleavage (Table 6) is 1.40 at 240 °C. The MP2/6-31G* secondary KIE is 1.29. This is a significant effect compared with the observed KIE of 1.57 in solution at 240 °C.⁴

Observed fundamental frequencies tend to be about 5% smaller than harmonic frequencies, due to anharmonicity.^{16c} The simplest method for correcting for anharmonic effects is to uniformly scale the theoretical harmonic frequencies. The primary KIE computed using a scaling factor of 0.95 is 4.02 (including tunneling), and the secondary KIE is 1.37. As expected, uniform scaling of frequencies has little impact on the computed isotope effects.^{16c}

The secondary KIE is caused by hyperconjugation of the nitrogen radical with the six adjacent C-H or C-D bonds. The resulting weakening of these bonds causes fractionation²⁴ of the lighter isotope in the amino radical. A similar effect causes a decrease in the gas phase acidity of CD₃OH relative to CH₃-OH.²⁵ Conjugation with the oxyanion leads to weakening of the adjacent C-H or C-D bonds in the isotopic methoxides.²⁵

Using Oxley's observed KIE⁴ of $(k^H/k^{D6})_{\text{obs}} = 1.57$ and our calculated KIEs of $(k_1^H/k_1^{D6}) = 1.40$ and $(k_2^H/k_2^{D6}) = 4.21$ for the two pathways, we can compute the branching ratios k_1^H/k_1^D

$k_2^H = 5.2$ and $k_1^{D6}/k_2^{D6} = 15.26^a$. These are the ratios of N–N cleavage (k_1) to HONO elimination (k_2) for the protio and deuterio species at 240 °C. The branching ratio favors the N–N cleavage over the HONO elimination, as expected. Deuterium substitution increases the preference for the N–N cleavage pathway.

Small errors in the observed KIE or the calculated secondary KIE would change the estimated branching ratio considerably.^{26b} A further source of ambiguity is that other minor reaction pathways besides the HONO elimination might exist. Certainly the condensed phase decompositions of RDX and HMX are complex and involve several parallel reaction pathways.²⁷

The observed isotope effects for decomposition of RDX- d_6 and HMX- d_8 have been interpreted as primary effects operating on decomposition pathways involving rate-determining C–H (or C–D) bond breaking.⁸ These isotope effects, measured by isothermal differential scanning calorimetry,⁸ are isotope effects on the *global* rates for release of energy from HMX or RDX. These global rates are not related in a simple way to the rate for an initiating chemical reaction such as N–NO₂ cleavage. Although the β secondary isotope effect for N–NO₂ cleavage in DMNA also acts on the N–NO₂ cleavages in the nitramine explosives, this effect is unlikely to contribute to the overall isotope effect on the global decomposition rate.

Conclusion

Our theoretical results suggest that significant part of the overall deuterium isotope effect for unimolecular dimethylnitramine decomposition is a β secondary effect operating on the N–NO₂ bond homolysis. The same secondary effect should act on the initiation of decomposition of the nitramine explosives HMX and RDX. However, the experimentally observed isotope effects on the global decomposition rates of HMX and RDX in the condensed phase are best interpreted as primary effects operating on pathways that involve rate-determining C–H (or C–D) homolysis.

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Supporting Information Available: A table listing B3LYP/6-31G* harmonic frequencies for TS and TS- d_6 and text giving a 130 line FORTRAN program for computing the reduced isotopic partition function ratio $(s_2/s_1)^f$ for two isotopomers (8 pages). Ordering information is given on any current masthead page.

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$$\alpha^H = \alpha^{D6} [(k_1^H/k_1^{D6}) / (k_{\text{obs}}^H/k_{\text{obs}}^{D6})] \quad (1)$$

$$1 - \alpha^H = (1 - \alpha^{D6}) [(k_2^H/k_2^{D6}) / (k_{\text{obs}}^H/k_{\text{obs}}^{D6})] \quad (2)$$

Adding eqs 1 and 2 and solving for α^{D6} gives $\alpha^{D6} = (k_2^H/k_2^{D6} - k_{\text{obs}}^H/k_{\text{obs}}^{D6}) / (k_2^H/k_2^{D6} - k_1^H/k_1^{D6}) = (4.21 - 1.57) / (4.21 - 1.40) = 0.939$. We can now compute α^H , by substituting the known value of α^{D6} into eq 1: $\alpha^H = 0.939(1.40/1.57) = 0.838$. Thus $\alpha^H = 0.838$ and $\alpha^{D6} = 0.939$. The branching ratios for H and D are then given by $k_1^H/k_2^H = \alpha^H/(1 - \alpha^H)$ and $k_1^{D6}/k_2^{D6} = \alpha^{D6}/(1 - \alpha^{D6})$. (b) For example, if the error range in the observed KIE is 0.15, then the value for α^{D6} could be as large as 0.99 or as small as 0.89. Of course, error in the theoretical isotope effects must also be considered.

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