# Use of the Resonance Raman Intensities To Check the Density Functional Theory Derived Force Field of the Free Base Porphine 

Mouhsine Tazi, Philippe Lagant, and Gérard Vergoten*, $\dagger$<br>CRESIMM, Université des Sciences et Technologies de Lille, UFR de Chimie, Bât C8, 59655 Villeneuve d'Ascq, France

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#### Abstract

The vibrational normal modes of the free base porphine (FBP) have been investigated within the framework of the density functional theory (DFT). The scaling of the internal force constants has been performed using a least-squares method, and a general valence force field was deduced for the free base porphine with $D_{2 h}$ symmetry. To check the vibrational assignments for the normal modes having the $\mathrm{A}_{\mathrm{g}}$ symmetry, the resonance Raman intensities have been predicted. It is shown that the $A$ term part of the scattering tensor is able to explain most of the observed resonance Raman enhancements for the electronic transitions lying in the Q band.


## Introduction

The free base porphine (FBP) is the starting point for vibrational studies on metalloporphyrins which constitute a template for very important biological functions such as photosynthesis, oxygen transport, and oxidation/reduction mechanisms. A resonance structure with $D_{2 h}$ symmetry has been shown to stand for the free base porphyrin leading to an electronic delocalized structure for the ground state.

The resonance Raman, visible absorption, fluorescence, and phosphorescence spectra have been largely investigated, ${ }^{1,3}$ and more recently polarized infrared spectra ${ }^{4}$ and Raman ${ }^{5}$ investigations have been performed on the basis of a force field derived from scaled quantum mechanical studies (SQM).

In the present calculations, we used as in previous studies ${ }^{6,8}$ the density functional theory (DFT) approach which takes into account the exchange-correlation corrections needed to correctly reproduce the delocalization effects.

The potential energy distribution (PED) may strongly vary from one specific force field determinated from scaled quantum mechanical studies to another one. To overcome this problem, vibrational studies using isotopomers have been used with success to correctly approach the nature of the normal modes associated with the scaled quantum mechanical force field.

In the present study, we used an additional approach which consists of the prediction of the resonance Raman intensities (RRI) of the vibrational modes belonging to the totally symmetric species. This method permits verification of the potential energy distributions of the $\mathrm{A}_{\mathrm{g}}$ normal modes and was applied previously in our group to study nucleic acids ${ }^{9,12}$ and aromatic amino acids. It will be shown below that such a method is quite easy to use when regarding the difficulty to predict correct infrared or Raman intensities and, consequently, appears as a complementary tool to obtain a correct force field. Unfortunately the infrared vibrational intensities are not available with the DFT procedure in the Jaguar software.

## Materials and Methods

The DFT calculations were performed using the Jaguar software (version 3.0). ${ }^{13}$ The B3-LYP exchange functional

[^0](Becke-3/parameter/HF/Slater/Becke88/VWN and LYP) was used in addition to the $6-31 \mathrm{G}(\mathrm{df}, \mathrm{p})(5 \mathrm{~d}, 7 \mathrm{f})$ basis set.

A calculation at the same level of theory was performed previously by Kozlowski et al., ${ }^{4,5}$ The geometry optimization was first done using the Merck force field included in the Spartan program (version 5.0.2) ${ }^{14}$ under a constrained $D_{2 h}$ geometry. This structure was thereafter treated by the DFT method using a total number of 429 basis functions. No constraints were imposed, and the final geometry remains of the $D_{2 h}$ type.

The matrix of second derivatives of the potential energy with respect to the Cartesian coordinates (Hessian matrix) resulting from the DFT optimization was treated using the Redong program of Allouche and Pourcin. ${ }^{15}$ The method under consideration consists of the determination (by least-squares methods) of the scaling factors corresponding to the internal or symmetry coordinates leading to the best fit of the theoretical to the experimental vibrational wavenumbers. The force constants can then be expressed in terms of internal or symmetry coordinates if removal of local and/or cyclic redundancies is required.

The free base porphine has 38 atoms and $108(3 N-6)$ internal degrees of freedom. Under a $D_{2 h}$ symmetry, with the $x$ and $y$ axes lying in the molecular plane the irreducible representation of the fundamental vibrational modes is given by $19 A_{g}+18 B_{1 g}+9 B_{2 g}+8 B_{3 g}+10 B_{l u}+8 A_{u}+10 B_{l u}+$ $18 B_{2 u}+18 B_{3 u}$ species, where the $A_{g}, B_{1 g}, B_{3 u}$, and $B_{2 u}$ species are related to the in-plane modes.

Figure 1 displays the structure under $D_{2 h}$ symmetry, and Table 1 gives the Cartesian coordinates of the optimized geometry. The molecular electrostatic potential (ESP) was fitted to a set of point charges located at the atomic centers. The fit was constrained to reproduce the dipole moment exactly. A total of 160 internal coordinates were used to define the molecule. No symmetry coordinates were defined to remove the redundancies occurring in the pyrrole rings or in the superring for the following reasons: (i) For each pyrrole ring, it is possible to use local symmetry coordinates, but the external substituents $\left(\mathrm{C}_{\beta} \mathrm{H}\right.$ and NH$)$ have to be included for redundancy relations. (ii) The total symmetry coordinates including the external $\mathrm{C}_{\mathrm{m}} \mathrm{H}$ atoms must be linear combinations of these local symmetry


Figure 1. Free base porphine structure under $D_{2 h}$ symmetry (taken in the $x y$ plane).

TABLE 1: Optimized DFT Cartesian Coordinates for FBP Atoms As Calculated under the $D_{2 h}$ Symmetry (xy plane) and Their Corresponding Charges (Atomic Units)

| atom | atomic no. | $x$ | $y$ | $Z$ | atomic charge |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 7 | 0.00000 | -2.036 836 | 0.00000 | -0.450 23 |
| 2 | 1 | 1.35202 | 5.11269 | 0.00000 | 0.16050 |
| 3 | 7 | 0.00000 | 2.03683 | 0.00000 | $-0.45023$ |
| 4 | 1 | -1.098 517 | 0.00000 | 0.00000 | 0.18041 |
| 5 | 1 | 1.09851 | 0.00000 | 0.00000 | 0.18041 |
| 6 | 7 | -2.113 52 | 0.00000 | 0.00000 | -0.189 47 |
| 7 | 7 | 2.11352 | 0.00000 | 0.00000 | -0.189 47 |
| 8 | 6 | 2.89323 | 1.13102 | 0.00000 | 0.28278 |
| 9 | 6 | 2.89323 | -1.131 022 | 0.00000 | 0.28278 |
| 10 | 6 | 1.08596 | -2.861 657 | 0.00000 | 0.38624 |
| 11 | 6 | -1.085 967 | $-2.861657$ | 0.00000 | 0.38624 |
| 12 | 6 | -2.893 237 | $-1.131022$ | 0.00000 | 0.28278 |
| 13 | 6 | -2.893 237 | 1.131022 | 0.00000 | 0.28278 |
| 14 | 6 | -1.085 965 | 2.861657 | 0.00000 | 0.38624 |
| 15 | 6 | 1.08596 | 2.861657 | 0.00000 | 0.38624 |
| 16 | 1 | 3.18283 | 3.21954 | 0.00000 | 0.16388 |
| 17 | 6 | 0.67863 | 4.26508 | 0.00000 | -0.269 12 |
| 18 | 6 | 2.42287 | 2.44395 | 0.00000 | -0.416 53 |
| 19 | 6 | 4.25833 | 0.68641 | 0.00000 | $-0.25023$ |
| 20 | 6 | 2.42287 | -2.443 952 | 0.00000 | -0.416 53 |
| 21 | 6 | -0.678 632 | 4.26508 | 0.00000 | -0.269 12 |
| 22 | 6 | -2.422 877 | 2.44395 | 0.00000 | -0.416 53 |
| 23 | 6 | -4.258 333 | 0.68641073 | 0.00000 | -0.250 23 |
| 24 | 6 | 0.67863 | -4.265 086 | 0.00000 | -0.269 12 |
| 25 | 1 | -3.182839 | 3.219541 | 0.00000 | 0.16388 |
| 26 | 6 | -2.422 877 | -2.443 951 | 0.00000 | -0.416 53 |
| 27 | 6 | -4.258 333 | -0.686 410 | 0.00000 | $-0.25023$ |
| 28 | 6 | 4.25833 | -0.686 410 | 0.00000 | -0.250 23 |
| 29 | 6 | -0.678 632 | -4.265 086 | 0.00000 | -0.269 12 |
| 30 | 1 | 3.18284 | -3.219 541 | 0.00000 | 0.16388 |
| 31 | 1 | -3.182839 | -3.219 541 | 0.00000 | 0.16388 |
| 32 | 1 | 1.35202 | -5.112691 | 0.00000 | 0.16050 |
| 33 | 1 | 5.11385 | -1.347760 | 0.00000 | 0.17211 |
| 34 | 1 | -5.113856 | 1.347760 | 0.00000 | 0.17211 |
| 35 | 1 | 5.11385 | 1.347760 | 0.00000 | 0.17211 |
| 36 | 1 | -1.352022 | -5.112691 | 0.00000 | 0.16050 |
| 37 | 1 | -1.352022 | 5.112691 | 0.00000 | 0.16050 |
| 38 | 1 | -5.113856 | $-1.347760$ | 0.00000 | 0.17211 |
| dipole moment (Debye) |  | 0.000 | 0.000 | 0.000 | 0.000 |

coordinates to respect the $D_{2 h}$ molecular symmetry. (iii) The derived symmetry force constants are typical of the $D_{2 h}$ symmetry and cannot be used for the molecule with a different symmetry. (iv) A transformation from the space of nonredundant

TABLE 2: Comparison between Optimized Geometrical Parameters (A, deg) As Obtained from Different ab Initio Calculations

|  | DFT/B3LYP <br> (this work) | $\mathrm{LDFT}^{16}$ | SCF/TZP ${ }^{17}$ | MP2/DZP2 ${ }^{18}$ | expt $1^{1}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{N}-\mathrm{H}$ | 1.015 | 1.038 | 0.99 | 0.99 |  |
| $\mathrm{N}-\mathrm{C}_{\alpha}$ | 1.37 | 1.365 | 1.35 | 1.36 | 1.367 |
| $\left(\mathrm{N}-\mathrm{C}_{\alpha}\right)^{a}$ | 1.363 | 1.363 | 1.34 | 1.35 | 1.364 |
| $\mathrm{C}_{\beta}-\mathrm{C}_{\alpha}$ | 1.436 | 1.423 | 1.43 | 1.43 | 1.438 |
| $\left(\mathrm{C}_{\beta}-\mathrm{C}_{\alpha}\right)^{a}$ | 1.462 | 1.445 | 1.45 | 1.46 | 1.463 |
| $\mathrm{C}_{\beta}-\mathrm{C}_{\beta}$ | 1.372 | 1.371 | 1.35 | 1.35 | 1.373 |
| $\left(\mathrm{C}_{\beta}-\mathrm{C}_{\beta}\right)^{a}$ | 1.356 | 1.358 | 1.34 | 1.34 | 1.354 |
| $\mathrm{C}_{\mathrm{m}}-\mathrm{C}_{\alpha}$ | 1.394 | 1.384 | 1.38 | 1.37 | 1.392 |
| $\left(\mathrm{C}_{\mathrm{m}}-\mathrm{C}_{\alpha}\right)^{a}$ | 1.4 | 1.390 | 1.39 | 1.38 | 1.393 |
| $\mathrm{C}_{\beta}-\mathrm{H}$ | 1.080 | 1.094 | 1.07 | 1.06 |  |
| $\left(\mathrm{C}_{\beta}-\mathrm{H}\right)^{a}$ | 1.082 | 1.095 | 1.07 | 1.06 |  |
| $\mathrm{C}_{\mathrm{m}}-\mathrm{H}$ | 1.086 | 1.098 | 1.07 | 1.07 |  |
| $\mathrm{H}-\mathrm{N}-\mathrm{C}_{\alpha}$ | 124.6 | 125.0 | 124.4 | 124.4 |  |
| $\mathrm{C}_{\alpha}-\mathrm{N}-\mathrm{C}_{\alpha}$ | 110.8 | 110.1 | 111.1 | 110.8 | 109.6 |
| $\left(\mathrm{C}_{\alpha}-\mathrm{N}-\mathrm{C}_{\alpha}\right)^{a}$ | 105.5 | 104.9 | 106.4 | 105.1 | 105.7 |
| $\mathrm{N}-\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ | 106.5 | 107.2 | 106.5 | 106.9 | 107.8 |
| $\left(\mathrm{N}-\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}\right)^{a}$ | 111.0 | 111.4 | 110.7 | 111.5 | 110.9 |
| $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}-\mathrm{C}_{\beta}$ | 108.0 | 107.7 | 107.9 | 107.7 | 107.4 |
| $\left(\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}-\mathrm{C}_{\beta}\right)^{a}$ | 106.2 | 106.9 | 108.1 | 105.9 | 106.3 |
| $\mathrm{N}-\mathrm{C}_{\alpha}-\mathrm{C}_{\mathrm{m}}$ | 125.6 | 125.6 | 126.2 | 125.5 | 124.8 |
| $\left(\mathrm{N}-\mathrm{C}_{\alpha}-\mathrm{C}_{\mathrm{m}}\right)^{a}$ | 125.4 | 125.6 | 125.9 | 125.6 | 125.1 |
| $\mathrm{C}_{\alpha}-\mathrm{C}_{\mathrm{m}}-\mathrm{C}_{\alpha}$ | 127.1 | 126.3 | 126.6 | 126.8 | 127.4 |
| $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}-\mathrm{H}$ | 124.2 | 123.9 | 124.5 | 124.5 |  |
| $\left(\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}-\mathrm{H}\right)^{a}$ | 125.3 | 125.2 | 125.5 | 125.6 |  |
| $\mathrm{C}_{\alpha}-\mathrm{C}_{\mathrm{m}}-\mathrm{H}$ | 117.0 | 116.8 | 116.1 | 116.0 |  |
| $\mathrm{C}_{\beta}-\mathrm{C}_{\beta}-\mathrm{H}$ | 127.7 |  |  |  |  |
| $\left(\mathrm{C}_{\beta}-\mathrm{C}_{\beta}-\mathrm{H}\right)^{a}$ | 128.5 |  |  |  |  |

${ }^{a}$ For bonds belonging to the unprotonated pyrrole rings.
symmetry coordinates (108) to the space of internal coordinates (160) would reintroduce ring redundancies. As the aim of this work was to select a possible set of internal force constants and transferable scaling factors, no further attempt was done to treat the problem in this way. Comparable assignments in the potential energy distribution can be made between the present work and those obtained from Koslowski et al. ${ }^{4,5}$

## Results and Discussion

The atomic definitions for FBP were taken according to Zgierski's notations ${ }^{16}$ with $\mathrm{C}_{\alpha}, \mathrm{C}_{\beta}$, and $\mathrm{C}_{\mathrm{m}}$ being the carbon atoms in the $\alpha, \beta$, and meso positions. The optimized structure obtained on the isolated molecule using the DFT method is in good agreement with the results of X-ray studies, ${ }^{17}$ and this fact shows that only weak distortions would appear in the crystal state (Table 2).

The optimized parameters are compared in Table 2 to other theoretical values obtained from studies using the LDFT, SCF/ TZDP, and MP2/DZP2 methods. ${ }^{18,20}$ It can be easily seen that the calculated values are in quite agreement with the experimental ones, the mean deviations being $0.005 \AA$ for bonds and $1.3^{\circ}$ for angles.

Table 3 displays a set of scaling factors referring to different groups of internal coordinates. Ten different values were retained after the fitting of the theoretical wavenumbers to the experimental ones. Their values lie in the $0.92-0.98$ range except for those corresponding to the NH stretching value which displays a lower value ( 0.87 ). The derived diagonal force constants expressed in the internal coordinate space are displayed in Table 4.

These scaling factors have to be compared to the corresponding values given in ref 5 . The $\mathrm{N}-\mathrm{C}$ and $\mathrm{C}-\mathrm{C}$ stretchings coordinates have a calculated value of 0.93 , which is to be compared to the value of 0.927 obtained in this work. The values

TABLE 3: Calculated Scaling Factors for Force Constants According to the Different Groups of Internal Coordinates (IC)

| IC | $\begin{aligned} & \text { in } \\ & \text { plane } \end{aligned}$ | scaling <br> factor | IC | out of plane | scaling <br> factor |
| :---: | :---: | :---: | :---: | :---: | :---: |
| R1,R2 | NH | 0.8695 | R111,R112 | NH opb | 0.95 |
| R3,R6 | $\mathrm{C}_{\mathrm{m}} \mathrm{H}$ | 0.9165 | R113,R116 | $\mathrm{C}_{\mathrm{m}} \mathrm{H}$ opb | 0.92 |
| R7,R14 | $\mathrm{C}_{\beta} \mathrm{H}$ | 0.9165 | R117,R124 | $\mathrm{C}_{\beta} \mathrm{H}$ opb | 0.92 |
| R15,R22 | NC | 0.927 | R125,R132 | $\mathrm{C}_{\alpha} \mathrm{C}_{\mathrm{m}} \mathrm{Opb}$ | 0.99 |
| R23,R30 | $\mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}$ | 0.927 | R133,R140 | NCtor | 0.95 |
| R31,R38 | $\mathrm{C}_{\beta} \mathrm{C}_{\alpha}$ | 0.927 | R141,R148 | $\mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}$ tor | 0.935 |
| R39,R42 | $\mathrm{C}_{\beta} \mathrm{C}_{\beta}$ | 0.927 | R149,R156 | $\mathrm{C}_{\beta} \mathrm{C}_{\alpha}$ tor | 0.935 |
| R43,R46 | CNH | 0.952 | R157,R160 | $\mathrm{C}_{\beta} \mathrm{C}_{\beta}$ tor | 0.935 |
| R47,R54 | $\mathrm{C}_{\alpha} \mathrm{C}_{\mathrm{m}} \mathrm{H}$ | 0.952 |  |  |  |
| R55,R62 | $\mathrm{C}_{\alpha} \mathrm{C}_{\beta} \mathrm{H}$ | 0.952 |  |  |  |
| R63,R70 | $\mathrm{C}_{\beta} \mathrm{C}_{\beta} \mathrm{H}$ | 0.952 |  |  |  |
| R71,R74 | CNC | 0.98 |  |  |  |
| R75,R82 | $\mathrm{NC}_{\alpha} \mathrm{C}_{\mathrm{m}}$ | 0.98 |  |  |  |
| R83,R90 | $\mathrm{NC}_{\alpha} \mathrm{C}_{\beta}$ | 0.98 |  |  |  |
| R91,R98 | $\mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha} \mathrm{C}_{\beta}$ | 0.98 |  |  |  |
| R99,R102 | $\mathrm{C}_{\alpha} \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}$ | 0.98 |  |  |  |
| R103,R110 | $\mathrm{C}_{\alpha} \mathrm{C}_{\beta} \mathrm{C}_{\beta}$ | 0.98 |  |  |  |

TABLE 4: Scaled General Valence Diagonal Force Constants Obtained for FBP

| $\mathrm{IC}^{a}$ | bond stretching <br> $(\mathrm{mdyn} / \AA)$ | $\mathrm{IC}^{a}$ | angle bending <br> $($ mdyn $\AA)$ |
| :--- | :---: | :--- | :---: |
| $\mathrm{N}-\mathrm{H}$ | 6.21 | $\mathrm{H}^{2}-\mathrm{N}-\mathrm{C}_{\alpha}$ | 0.38 |
| $\mathrm{~N}-\mathrm{C}_{\alpha}$ | 4.12 | $\mathrm{C}_{\alpha}-\mathrm{N}-\mathrm{C}_{\alpha}$ | 0.74 |
| $\left(\mathrm{~N}-\mathrm{C}_{\alpha}\right)^{b}$ | 3.95 | $\left(\mathrm{C}_{\alpha}-\mathrm{N}-\mathrm{C}_{\alpha}\right)^{b}$ | 1.10 |
| $\mathrm{C}_{\beta}-\mathrm{C}_{\alpha}$ | 3.66 | $\mathrm{~N}-\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ | 0.72 |
| $\left(\mathrm{C}_{\beta}-\mathrm{C}_{\alpha}\right)^{b}$ | 3.25 | $\left(\mathrm{~N}-\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}\right)^{b}$ | 0.75 |
| $\left.\mathrm{C}_{\beta}-\mathrm{C}_{\beta}\right)^{2}$ | 4.90 | $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}-\mathrm{C}_{\beta}$ | 0.7 |
| $\left(\mathrm{C}_{\beta}-\mathrm{C}_{\beta}\right)^{b}$ | 5.52 | $\left(\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}-\mathrm{C}_{\beta}\right)^{b}$ | 0.68 |
| $\mathrm{C}_{\mathrm{m}}-\mathrm{C}_{\alpha}$ | 6.28 | $\mathrm{~N}^{-}-\mathrm{C}_{\alpha}-\mathrm{C}_{\mathrm{m}}$ | 0.527 |
| $\left(\mathrm{C}_{\mathrm{m}}-\mathrm{C}_{\alpha}\right)$ | 6.06 | $\left(\mathrm{~N}-\mathrm{C}_{\alpha}-\mathrm{C}_{\mathrm{m}}\right)^{b}$ | 0.59 |
| $\mathrm{C}_{\beta}-\mathrm{H}$ | 5.27 | $\mathrm{C}_{\alpha}-\mathrm{C}_{\mathrm{m}}-\mathrm{C}_{\alpha}$ | 0.526 |
| $\left(\mathrm{C}_{\beta}-\mathrm{H}\right)^{b}$ | 5.27 | $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}-\mathrm{H}$ | 0.396 |
| $\mathrm{C}_{\mathrm{m}}-\mathrm{H}$ | 5.13 | $\left(\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}-\mathrm{H}\right)^{b}$ | 0.38 |
|  |  | $\mathrm{C}_{\alpha}-\mathrm{C}_{\mathrm{m}}-\mathrm{H}$ | 0.4 |
|  |  | $\mathrm{C}_{\beta}-\mathrm{C}_{\beta}-\mathrm{H}$ | 0.38 |
|  |  | $\left(\mathrm{C}_{\beta}-\mathrm{C}_{\beta}-\mathrm{H}\right)^{b}$ | 0.38 |

${ }^{a}$ IC: internal coordinate. ${ }^{b}$ For bonds belonging to the unprotonated pyrrole rings.
for the $\mathrm{C}-\mathrm{H}$ stretching given our work and in the reference ${ }^{5}$ are in good agreement ( 0.916 and 0.912 , respectively). The values for the $\mathrm{N}-\mathrm{H}$ rocking in-plane coordinate are comparable ( 0.95 and 0.94 ), and likewise values corresponding to the out of plane wagging ( 0.95 and 9486). A discrepancy can be noted for the in-plane CH deformation ( 0.952 and 0.934 ). The scaling factors applying to the ring stretching coordinates have quite comparable values: 0.98 (this work) and $0.988 .{ }^{5}$

No great differences between the scaling factors can be noted when one uses a set of redundant or nonredundant internal coordinates.

Vibrational Analysis. The calculated frequencies and normal mode symmetries ( $D_{2 h}$ molecular geometry) for FBP are given in Table 5. Only the highest contributions to the potential energy distribution (PED) among the internal coordinates were reported.

The theoretical wavenumbers for the $d_{0}, d_{2}(\mathrm{NH}), d_{4}\left(\mathrm{C}_{\mathrm{m}} \mathrm{H}\right)$, $d_{8}\left(\mathrm{C}_{\beta} \mathrm{H}\right)$, and $d_{12}\left(\mathrm{C}_{\mathrm{m}} \mathrm{H}, \mathrm{C}_{\beta} \mathrm{H}\right)$ isotopomers are compared to their corresponding experimental values ${ }^{4,5}$ in Table 6. It is noteworthy that the same set of scaling factors was kept for the five isotopomers.

In refs 4 and 5 a particular detailed analysis of the vibrational (infrared and nonresonant Raman) activities was performed and a correlation was established between some of them and their appearance in the fluorescence and phosphorescence emissions according to their symmetry properties. The present work was done using the same basis and correlation functions as in ref 4.

It can be easily deduced from Tables 5 and 6 that the calculated wavenumbers and PED for all the isotopomers are quite in correspondence with the experimental bands. The assignments for the $d_{2}, d_{4}, d_{8}$, and $d_{12}$ analogues were done according to their potential energy distribution. Only a few calculated frequencies are in disagreement with the previous assignments. In particular, the calculated wavenumber at $776 \mathrm{~cm}^{-1}$ for the $\mathrm{B}_{1 \mathrm{u}}$ mode ( $D_{2 h}$ ) in the $d_{2}$ isotopomer corresponds to the observed band at $785 \mathrm{~cm}^{-1}$ in $d_{0}$. For this band, Kozlowski et al. ${ }^{4,5}$ discussed the validity of the calculated dipole moments and preferred to assign the $d_{2}$ wavenumber at $535 \mathrm{~cm}^{-1}$. This explanation is somewhat difficult to understand since the potential energy distribution for the $d_{0}$ and $d_{2}$ isotopomers does not show any participation of the $\mathrm{C}_{\alpha} \mathrm{NH}$ group to this mode (no shift) and any dependence on the type of basis sets.

Resonance Raman Intensities. Simplified Theory for the Resonance Raman Intensities. For molecules containing $\pi$-electron conjugated systems, the first allowed electronic transitions are generally of the $\pi \rightarrow \pi^{*}$ type. Along these electronic transitions, some normal modes can be perturbed by the changes occurring in the molecular geometry and electronic bonding. Such changes principally affect the atomic equilibrium displacements in the excited electronic state with respect to the ground state. To follow such geometrical perturbations, the vibrational analysis appears to be a powerful method to investigate the changes taking place in the atomic distances and valence angles. Wilson's GF method ${ }^{21}$ was until now extensively used to deal with the normal modes determination as its relates the internal coordinates $R$ (stretching, in-plane and out-of-plane bending, torsion) to the $3 N-6$ normal coordinates $Q_{i}$ of a molecule containing $N$ atoms according to the matrix relation $Q=L^{-1} R$. In this last formulation, $L$ stands for the eigenvector matrix that can be derived from the resolution of the well-known relationship $G F L=L \Lambda$, where $G$ and $F$ represent the inverse kinetic energy and potential energy matrices, respectively. The matrix of internal coordinates $R$ can be obtained from the $3 N$ Cartesian coordinates via the $B$ matrix involving the Wilson's vectors and the relationship $R=B X$. Along an electronic transition, the variations $\Delta R$ occurring in the internal coordinates are related to the shifts in the normal coordinates $\Delta Q$ according to the following expression: $\Delta Q=L^{-1}(\Delta R)=L^{-1} B(\Delta X)$.

Using quantum mechanical methods (semiempirical or ab initio) it is relatively easy to calculate the bond lengths and bond angles of a molecule at its potential energy minimum for the ground and excited electronic states. From this, it is possible to deduce the displacements of the potential energy minimum along some particular normal modes from those occurring in the internal coordinates. It has been suggested that the changes in bond lengths $\Delta r_{i}$ along a particular electronic transition are proportional to the corresponding changes ( $\Delta \mathrm{bo}$ ) of the bond orders; i.e., $\Delta R_{i}=C(\Delta \mathrm{bo})_{i}$, where the subscript $i$ corresponds to the $i$ th bond and $C$ is a constant. For molecules having totally symmetric modes, the main origin of the resonance Raman enhancements arises from the $A$ term of the scattering tensor and the associated intensity $I_{j}$ of the $j$ th normal mode can be shown to be approximatively proportional to the square of the shift $\Delta Q_{j}$ appearing along this normal mode between the ground and the excited electronic state; i.e., $I_{j}=K\left(\Delta Q_{j}\right)^{2} v_{j}^{2}$, where $v_{j}$ refers to the associated linear frequency of the normal mode. ${ }^{9,22,23}$ Then, considering the linear relationship between the $k$ th change in bond length and its associated change in bond order, the resonance Raman intensity of the $j$ th normal mode is given by

$$
I_{j}=C K v_{j}^{2} \sum_{k}\left(L_{k}^{-1}\right)\left(\Delta \mathrm{bo}_{k}\right)^{2}
$$

TABLE 5: Wavenumbers and Potential Energy Distribution for the $d_{0}$ Isotopomer of FBP $\left(D_{2 h}\right)$ Obtained after Scaling of the Force Constant ${ }^{a}$

| no. | sym | calc | PED | no. | sym | calc | PED |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | $\mathrm{B}_{1 \mathrm{u}}$ | 51.7 | $39 \tau \mathrm{NC}, 17 \tau \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 10 \tau \mathrm{C}_{\beta} \mathrm{C}_{\alpha}, 27 \pi \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}$ | 57 | $\mathrm{B}_{2 \mathrm{u}}$ | 981.7 | $53 v \mathrm{C}_{\beta} \mathrm{C}_{\alpha}, 15 v \mathrm{CN}$ |
| 2 | $\mathrm{B}_{1 \mathrm{~g}}$ | 72.3 | $29 \delta \mathrm{CNH}, 24 \delta \mathrm{C}_{\alpha} \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 18 \delta \mathrm{NC}_{\alpha} \mathrm{C}_{\mathrm{m}}, 16 \delta \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha} \mathrm{C}_{\beta}$ | 58 | $\mathrm{Ag}_{\mathrm{g}}$ | 984.5 | $35 v \mathrm{CN}, 16 v \mathrm{C}_{\beta} \mathrm{C}_{\alpha}, 14 \delta \mathrm{HC}_{\beta} \mathrm{C}_{\alpha}, 14 \delta \mathrm{HNC}$ |
| 3 | $\mathrm{A}_{\mathrm{u}}$ | 92.0 | $38 \tau \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 25 \pi \mathrm{C}_{\mathrm{m}} \mathrm{H}, 21 \pi \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}$ | 59 | $\mathrm{B}_{3 \mathrm{u}}$ | 1002.4 | $30 \nu \mathrm{C}_{\beta} \mathrm{C}_{\alpha}, 20 \nu \mathrm{CN}, 17 \delta \mathrm{HC}_{\beta} \mathrm{C}_{\alpha}$ |
| 4 | $\mathrm{B}_{1 \mathrm{u}}$ | 117.8 | $35 \tau \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 28 \pi \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 14 \pi \mathrm{C}_{\mathrm{m}} \mathrm{H}, 11 \pi \mathrm{NH}$ | 60 | $\mathrm{B}_{1 \mathrm{~g}}$ | 1004.4 | $23 v \mathrm{C}_{\beta} \mathrm{C}_{\alpha}, 16 v \mathrm{CN}, \delta \mathrm{HNC}$ |
| 5 | $\mathrm{B}_{2 \mathrm{~g}}$ | 135.1 | $69 \tau \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 16 \pi \mathrm{NH}, 16 \pi \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}$ | 61 | $\mathrm{B}_{2 \mathrm{u}}$ | 1052.1 | $45 \delta \mathrm{HC}_{\beta} \mathrm{C}_{\beta}, 39 \delta \mathrm{HC}_{\beta} \mathrm{C}_{\alpha}$ |
| 6 | $\mathrm{B}_{3 \mathrm{~g}}$ | 138.1 | $59 \tau \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 16 \pi \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 14 \pi \mathrm{C}_{\mathrm{m}} \mathrm{H}$ | 62 | $\mathrm{B}_{3 \mathrm{u}}$ | 1053.5 | $39 \delta \mathrm{HC}_{\beta} \mathrm{C}_{\beta}, 32 \delta \mathrm{HC}_{\beta} \mathrm{C}_{\alpha}$ |
| 7 | $\mathrm{Ag}_{\mathrm{g}}$ | 160.9 | $42 \delta \mathrm{NC}_{\alpha} \mathrm{C}_{\mathrm{m}}, 40 \delta \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha} \mathrm{C}_{\beta}$ | 63 | $\mathrm{Ag}_{\mathrm{g}}$ | 1054.9 | $44 \delta \mathrm{HC}_{\beta} \mathrm{C}_{\beta}, 38 \delta \mathrm{HC}_{\beta} \mathrm{C}_{\alpha}$ |
| 8 | $\mathrm{B}_{2 \mathrm{~g}}$ | 192.4 | $32 \pi \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 22 \tau \mathrm{C}_{\beta} \mathrm{C}_{\alpha}, 17 \tau \mathrm{NC}, 14 \tau \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}$ | 64 | $\mathrm{Ag}_{\mathrm{g}}$ | 1063.7 | $44 \delta \mathrm{HC}_{\beta} \mathrm{C}_{\beta}, 37 \delta \mathrm{HC}_{\beta} \mathrm{C}_{\alpha}$ |
| 9 | $\mathrm{B}_{3 \mathrm{~g}}$ | 212.6 | $50 \tau \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 22 \pi \mathrm{NH}, 14 \pi \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}$ | 65 | $\mathrm{B}_{1 \mathrm{~g}}$ | 1132.6 | $27 v \mathrm{CN}, 13 v \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 10 v \mathrm{C}_{\beta} \mathrm{C}_{\alpha}, 19 \delta \mathrm{HC}_{\mathrm{m}} \mathrm{C}_{\alpha}$ |
| 10 | $\mathrm{B}_{1 \mathrm{u}}$ | 213.5 | $36 \pi \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 27 \tau \mathrm{NC}, 16 \tau \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 16 \tau \mathrm{C}_{\beta} \mathrm{C}_{\alpha}$ | 66 | $\mathrm{B}_{3 \mathrm{u}}$ | 1136.0 | $32 \nu \mathrm{CN}, 12 v \mathrm{C}_{\beta} \mathrm{C}_{\alpha}, 9 v \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}$ |
| 11 | $\mathrm{B}_{2 \mathrm{u}}$ | 290.2 | $40 \delta \mathrm{NC}_{\alpha} \mathrm{C}_{\mathrm{m}}, 36 \delta \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha} \mathrm{C}_{\beta}$ | 67 | $\mathrm{B}_{2 \mathrm{u}}$ | 1155.1 | $17 \nu \mathrm{CN}, 15 \nu \mathrm{C}_{\beta} \mathrm{C}_{\alpha}, 26 \delta \mathrm{HC}_{\mathrm{m}} \mathrm{C}_{\alpha}, 14 \delta \mathrm{HC}_{\beta} \mathrm{C}_{\alpha}$, |
| 12 | $\mathrm{A}_{\mathrm{u}}$ | 296.0 | $45 \pi \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 25 \tau \mathrm{C}_{\beta} \mathrm{C}_{\alpha}, 18 \tau \mathrm{NC}$ |  |  |  | $10 \delta \mathrm{HC}_{\beta} \mathrm{C}_{\beta}$ |
| 13 | $\mathrm{A}_{\mathrm{g}}$ | 301.3 | $41 \nu \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 11 \nu \mathrm{C}_{\beta} \mathrm{C}_{\alpha}, 10 \delta \mathrm{C}_{\alpha} \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}$ | 68 | $\mathrm{Ag}_{\mathrm{g}}$ | 1177.7 | $26 \nu \mathrm{C}_{\beta} \mathrm{C}_{\alpha}, 15 \mathrm{CN}, 35 \delta \mathrm{HC}_{\mathrm{m}} \mathrm{C}_{\alpha}, 10 \delta \mathrm{CNC}$ |
| 14 | $\mathrm{B}_{3 \mathrm{u}}$ | 310.5 | $36 \delta \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha} \mathrm{C}_{\beta}, 35 \delta \mathrm{NC}_{\alpha} \mathrm{C}_{\mathrm{m}}$ | 69 | $\mathrm{B}_{1 \mathrm{~g}}$ | 1183.9 | $20 v \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 11 \nu \mathrm{C}_{\beta} \mathrm{C}_{\alpha}, 10 v \mathrm{CN}, 21 \delta \mathrm{HC}_{\beta} \mathrm{C}_{\beta}$, |
| 15 | $\mathrm{B}_{1 \mathrm{u}}$ | 331.8 | $42 \tau \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 16 \tau \mathrm{NC}, 14 \tau \mathrm{C}_{\beta} \mathrm{C}_{\alpha}$ |  |  |  | $20 \delta \mathrm{HC}_{\beta} \mathrm{C}_{\alpha}, 10 \delta \mathrm{HC}_{\mathrm{m}} \mathrm{C}_{\alpha}$ |
| 16 | $\mathrm{B}_{3 \mathrm{u}}$ | 344.0 | $36 \nu \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 12 \nu \mathrm{C}_{\beta} \mathrm{C}_{\alpha}, 18 \delta \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha} \mathrm{C}_{\beta}$ | 70 | $\mathrm{B}_{1 \mathrm{~g}}$ | 1225.9 | $33 v \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 47 \delta \mathrm{HNC}$ |
| 17 | $\mathrm{B}_{2 \mathrm{u}}$ | 347.8 | $37 \nu \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 12 \nu \mathrm{C}_{\beta} \mathrm{C}_{\alpha}, 19 \delta \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha} \mathrm{C}_{\beta}$ | 71 | $\mathrm{B}_{3 \mathrm{u}}$ | 1226.6 | $24 \nu \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 24 \nu \mathrm{CN}, 12 \nu \mathrm{C}_{\beta} \mathrm{C}_{\alpha}$ |
| 18 | $\mathrm{B}_{1 \mathrm{~g}}$ | 389.9 | $45 \delta \mathrm{NC}_{\alpha} \mathrm{C}_{\mathrm{m}}, 45 \delta \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha} \mathrm{C}_{\beta}$ | 72 | $\mathrm{B}_{2 \mathrm{u}}$ | 1226.9 | $12 \nu \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 51 \delta \mathrm{HNC}$ |
| 19 | $\mathrm{B}_{1 \mathrm{~g}}$ | 407.8 | $35 \nu \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 19 \nu \mathrm{C}_{\beta} \mathrm{C}_{\alpha}, 24 \delta \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha} \mathrm{C}_{\beta}$ | 73 | $\mathrm{B}_{2} \mathrm{u}$ | 1254.6 | $12 \nu \mathrm{CN}, 9 \nu \mathrm{C}_{\beta} \mathrm{C}_{\alpha}, 13 \delta \mathrm{HC}_{\beta} \mathrm{C}_{\alpha}, 12 \delta \mathrm{HC}_{\mathrm{m}} \mathrm{C}_{\alpha}$, |
| 20 | $\mathrm{B}_{2 \mathrm{~g}}$ | 419.3 | $25 \tau \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 18 \tau \mathrm{C}_{\beta} \mathrm{C}_{\alpha}, 14 \pi \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 10 \pi \mathrm{NH}, 10 \pi \mathrm{C}_{\mathrm{m}} \mathrm{H}$ |  |  |  | $11 \delta \mathrm{HC}_{\beta} \mathrm{C}_{\beta}$ |
| 21 | $\mathrm{B}_{3 \mathrm{~g}}$ | 430.0 | $26 \tau \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 18 \tau \mathrm{C}_{\beta} \mathrm{C}_{\alpha}, 16 \tau \mathrm{NC}, 16 \pi \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 12 \pi \mathrm{C}_{\mathrm{m}} \mathrm{H}$ | 74 | $\mathrm{B}_{3 \mathrm{u}}$ | 1289.6 | $20 \nu \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 12 \nu \mathrm{C}_{\beta} \mathrm{C}_{\alpha}, 26 \delta \mathrm{HC}_{\beta} \mathrm{C}_{\beta}, 12 \delta \mathrm{HC}_{\beta} \mathrm{C}_{\alpha}$ |
| 22 | $\mathrm{A}_{\mathrm{u}}$ | 470.0 | $25 \tau \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 21 \tau \mathrm{C}_{\beta} \mathrm{C}_{\alpha}, 10 \tau \mathrm{NC}, 11 \pi \mathrm{C}_{\beta} \mathrm{H}, 20 \pi \mathrm{C}_{\mathrm{m}} \mathrm{H}$ | 75 | $\mathrm{B}_{1 \mathrm{~g}}$ | 1322.2 | $31 \nu \mathrm{CN}, 14 v \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 14 \delta \mathrm{HC}_{\beta} \mathrm{C}_{\beta}$ |
| 23 | $\mathrm{B}_{2 \mathrm{~g}}$ | 605.0 | $51 \pi \mathrm{NH}, 36 \tau \mathrm{NC}$ | 76 | $\mathrm{Ag}_{\mathrm{g}}$ | 1351.5 | $34 v \mathrm{C}_{\beta} \mathrm{C}_{\alpha}, 16 v \mathrm{CN}, 11 \delta \mathrm{CNC}$ |
| 24 | $\mathrm{B}_{1 \mathrm{u}}$ | 642.3 | $43 \pi \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 27 \pi \mathrm{NH}, 12 \pi \mathrm{C}_{\beta} \mathrm{H}$ | 77 | $\mathrm{B}_{1 \mathrm{~g}}$ | 1356.7 | $27 \delta \mathrm{HC}_{\beta} \mathrm{C}_{\beta}, 20 \delta \mathrm{HC}_{\beta} \mathrm{C}_{\alpha}, 20 \delta \mathrm{HC}_{\mathrm{m}} \mathrm{C}_{\alpha}$ |
| 25 | $\mathrm{B}_{2 \mathrm{~g}}$ | 665.8 | $63 \pi \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 17 \pi \mathrm{C}_{\beta} \mathrm{H}$ | 78 | $\mathrm{B}_{2 \mathrm{u}}$ | 1358.8 | $21 \nu \mathrm{CN}, 20 \nu \mathrm{C}_{\beta} \mathrm{C}_{\alpha}, 19 \delta \mathrm{HC}_{\beta} \mathrm{C}_{\beta}$ |
| 26 | $\mathrm{B}_{3 \mathrm{~g}}$ | 667.4 | $68 \pi \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 13 \tau \mathrm{NC}$ | 79 | $\mathrm{B}_{1 \mathrm{~g}}$ | 1381.0 | $28 \nu \mathrm{CN}, 25 \nu \mathrm{C}_{\beta} \mathrm{C}_{\alpha}, 13 \delta \mathrm{HC}_{\beta} \mathrm{C}_{\beta}$ |
| 27 | $\mathrm{A}_{\mathrm{u}}$ | 675.7 | $72 \pi \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 11 \tau \mathrm{C}_{\beta} \mathrm{C}_{\beta}$ | 80 | $\mathrm{A}_{\mathrm{g}}$ | 1398.9 | $28 v \mathrm{CN}, 15 v \mathrm{C}_{\beta} \mathrm{C}_{\alpha}, 16 v \mathrm{C}_{\beta} \mathrm{C}_{\beta}, 24 \delta \mathrm{HC}_{\mathrm{m}} \mathrm{C}_{\alpha}$ |
| 28 | $\mathrm{B}_{2 \mathrm{~g}}$ | 695.5 | $66 \pi \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 19 \tau \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}$ | 81 | $\mathrm{B}_{3 \mathrm{u}}$ | 1399.7 | $27 v \mathrm{C}_{\beta} \mathrm{C}_{\beta}, 22 v \mathrm{CN}, 10 \nu \mathrm{C}_{\beta} \mathrm{C}_{\alpha}, 20 \delta \mathrm{HC}_{\mathrm{m}} \mathrm{C}_{\alpha}$ |
| 29 | $\mathrm{A}_{\mathrm{u}}$ | 695.8 | $62 \pi \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 18 \tau \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}$ | 82 | $\mathrm{B}_{2 \mathrm{u}}$ | 1406.3 | $30 \nu \mathrm{CN}, 12 \nu \mathrm{C}_{\beta} \mathrm{C}_{\beta}, 24 \delta \mathrm{HC}_{\mathrm{m}} \mathrm{C}_{\alpha}$ |
| 30 | $\mathrm{B}_{1 \mathrm{u}}$ | 697.3 | $47 \pi \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 24 \pi \mathrm{C}_{\beta} \mathrm{H}$ | 83 | $\mathrm{B}_{3 \mathrm{u}}$ | 1413.0 | $35 v \mathrm{C}_{\beta} \mathrm{C}_{\alpha}, 19 v \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}$ |
| 31 | $\mathrm{B}_{3 \mathrm{~g}}$ | 700.0 | $51 \pi \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 20 \pi \mathrm{C}_{\beta} \mathrm{H}$ | 84 | $\mathrm{Ag}_{\mathrm{g}}$ | 1424.3 | $30 \nu \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 39 \nu \mathrm{C}_{\beta} \mathrm{C}_{\beta}, 15 \nu \mathrm{CN}$ |
| 32 | $\mathrm{Ag}_{\mathrm{g}}$ | 719.2 | $22 v \mathrm{CN}, 11 \nu \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 14 \delta \mathrm{NC}_{\alpha} \mathrm{C}_{\mathrm{m}}$ | 85 | $\mathrm{B}_{1 \mathrm{~g}}$ | 1495.1 | $38 v \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 13 \mathrm{CN}, 10 \mathrm{HC}_{\mathrm{m}} \mathrm{C}_{\alpha}$ |
| 33 | $\mathrm{Ag}_{\mathrm{g}}$ | 722.7 | $21 \nu \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 21 \delta \mathrm{NC}_{\alpha} \mathrm{C}_{\beta}, 18 \delta \mathrm{CNC}, 14 \delta \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha} \mathrm{C}_{\beta}$ | 86 | $\mathrm{B}_{2 \mathrm{u}}$ | 1497.1 | $21 \nu \mathrm{C}_{\beta} \mathrm{C}_{\beta}, 17 \nu \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 12 \nu \mathrm{CN}, 12 \delta \mathrm{HNC}$ |
| 34 | $\mathrm{B}_{3 \mathrm{u}}$ | 731.8 | $30 \pi \mathrm{C}_{\beta} \mathrm{H}, 11 \pi \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}$ | 87 | $\mathrm{Ag}_{\mathrm{g}}$ | 1508.5 | $48 \nu \mathrm{C}_{\beta} \mathrm{C}_{\beta}, 15 \delta \mathrm{HC}_{\beta} \mathrm{C}_{\alpha}$ |
| 35 | $\mathrm{B}_{3 \mathrm{u}}$ | 734.0 | $20 \nu \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 11 \nu \mathrm{CN}, 12 \delta \mathrm{NC}_{\alpha} \mathrm{C}_{\beta}, 12 \delta \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha} \mathrm{C}_{\beta}$ | 88 | $\mathrm{B}_{3 \mathrm{u}}$ | 1516.8 | $53 v \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}$ |
| 36 | $\mathrm{B}_{2 \mathrm{u}}$ | 744.0 | $14 v \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 9 v \mathrm{CN}, 14 \delta \mathrm{NC}_{\alpha} \mathrm{C}_{\beta}, 13 \delta \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha} \mathrm{C}_{\beta}, 9 \delta \mathrm{CNC}$ | 89 | $\mathrm{B}_{3 \mathrm{u}}$ | 1528.4 | $29 v \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 27 v \mathrm{C}_{\beta} \mathrm{C}_{\beta}, 16 \delta \mathrm{HC}_{\mathrm{m}} \mathrm{C}_{\alpha}$ |
| 37 | $\mathrm{B}_{3 \mathrm{~g}}$ | 764.3 | $56 \pi \mathrm{C}_{\beta} \mathrm{H}, 21 \pi \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}$ | 90 | $\mathrm{B}_{2} \mathrm{u}$ | 1548.5 | $28 \nu \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 28 \nu \mathrm{C}_{\beta} \mathrm{C}_{\beta}, 10 \delta \mathrm{HC}_{\beta} \mathrm{C}_{\alpha}$ |
| 38 | $\mathrm{B}_{2 \mathrm{~g}}$ | 771.5 | $51 \pi \mathrm{C}_{\beta} \mathrm{H}, 20 \pi \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}$ | 91 | $\mathrm{Ag}_{\mathrm{g}}$ | 1559.7 | $35 v \mathrm{C}_{\beta} \mathrm{C}_{\beta}, 18 \nu \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 12 \delta \mathrm{HC}_{\beta} \mathrm{C}_{\alpha}$ |
| 39 | $\mathrm{B}_{1 \mathrm{u}}$ | 772.1 | $61 \pi \mathrm{C}_{\beta} \mathrm{H}, 8 \pi \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}$ | 92 | $\mathrm{B}_{1 \mathrm{~g}}$ | 1592.0 | $57 \nu \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 9 \delta \mathrm{HC}_{\mathrm{m}} \mathrm{C}_{\alpha}$ |
| 40 | $\mathrm{B}_{1 \mathrm{~g}}$ | 780.9 | $25 \delta \mathrm{C}_{\alpha} \mathrm{C}_{\beta} \mathrm{C}_{\beta}, 13 \delta \mathrm{C}_{\alpha} \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 12 \delta \mathrm{NC}_{\alpha} \mathrm{C}_{\beta}, 11 \delta \mathrm{NC}_{\alpha} \mathrm{C}_{\mathrm{m}}$ | 93 | $\mathrm{B}_{2 \mathrm{u}}$ | 1596.4 | $57 \nu \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 9 \delta \mathrm{HC}_{\mathrm{m}} \mathrm{C}_{\alpha}$ |
| 41 | $\mathrm{B}_{2 \mathrm{u}}$ | 784.2 | $10 \nu \mathrm{C}_{\beta} \mathrm{C}_{\alpha}, 25 \delta \mathrm{C}_{\alpha} \mathrm{C}_{\beta} \mathrm{C}_{\beta}, 18 \delta \mathrm{NC}_{\alpha} \mathrm{C}_{\beta}$ | 94 | $\mathrm{Ag}_{\mathrm{g}}$ | 1600.8 | $74 \nu \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 12 \delta \mathrm{HC}_{\mathrm{m}} \mathrm{C}_{\alpha}$ |
| 42 | $\mathrm{B}_{1 \mathrm{u}}$ | 785.4 | $42 \pi \mathrm{C}_{\beta} \mathrm{H}, 24 \pi \mathrm{NH}$ | 95 | $\mathrm{B}_{1 \mathrm{~g}}$ | 3056.3 | $98 \nu \mathrm{C}_{\mathrm{m}} \mathrm{H}$ |
| 43 | $\mathrm{B}_{3 \mathrm{u}}$ | 787.9 | $16 \nu \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 26 \delta \mathrm{C}_{\alpha} \mathrm{C}_{\beta} \mathrm{C}_{\beta}, 12 \delta \mathrm{C}_{\alpha} \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 10 \delta \mathrm{NC}_{\alpha} \mathrm{C}_{\beta}$ | 96 | $\mathrm{Ag}_{\mathrm{g}}$ | 3057.7 | $99 \nu \mathrm{C}_{\mathrm{m}} \mathrm{H}$ |
| 44 | $\mathrm{B}_{1 \mathrm{~g}}$ | 806.2 | $28 \delta \mathrm{C}_{\alpha} \mathrm{C}_{\beta} \mathrm{C}_{\beta}, 12 \delta \mathrm{C}_{\alpha} \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, 10 \delta \mathrm{NC}_{\alpha} \mathrm{C}_{\beta}, 12 \delta \mathrm{NC}_{\alpha} \mathrm{C}_{\mathrm{m}}$ | 97 | $\mathrm{B}_{3 \mathrm{u}}$ | 3057.8 | $98 \nu \mathrm{C}_{\mathrm{m}} \mathrm{H}$ |
| 45 | $\mathrm{B}_{3 \mathrm{~g}}$ | 839.0 | $63 \pi \mathrm{C}_{\mathrm{m}} \mathrm{H}, 18 \tau \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}$ | 98 | $\mathrm{B}_{2 \mathrm{u}}$ | 3058.7 | $99 \nu \mathrm{C}_{\mathrm{m}} \mathrm{H}$ |
| 46 | $\mathrm{A}_{\mathrm{u}}$ | 840.0 | $64 \pi \mathrm{C}_{\mathrm{m}} \mathrm{H}, 17 \tau \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}$ | 99 | $\mathrm{B}_{1 \mathrm{~g}}$ | 3090.5 | $98 \nu \mathrm{C}_{\mathrm{m}} \mathrm{H}$ |
| 47 | $\mathrm{B}_{2 \mathrm{~g}}$ | 845.0 | $62 \pi \mathrm{C}_{\mathrm{m}} \mathrm{H}, 17 \tau \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}$ | 100 | $\mathrm{B}_{3 \mathrm{u}}$ | 3090.7 | $98 \nu \mathrm{C}_{\beta} \mathrm{H}$ |
| 48 | $\mathrm{B}_{1 \mathrm{u}}$ | 845.6 | $61 \pi \mathrm{C}_{\mathrm{m}} \mathrm{H}, 16 \tau \mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}$ | 101 | $\mathrm{B}_{2 \mathrm{u}}$ | 3106.8 | $98 v \mathrm{C}_{\beta} \mathrm{H}$ |
| 49 | $\mathrm{A}_{\mathrm{u}}$ | 882.4 | $54 \pi \mathrm{C}_{\beta} \mathrm{H}, 27 \pi \mathrm{C}_{\beta} \mathrm{C}_{\beta}$ | 102 | $\mathrm{B}_{1 \mathrm{~g}}$ | 3107.2 | $98 v \mathrm{C}_{\beta} \mathrm{H}$ |
| 50 | $\mathrm{B}_{2 \mathrm{~g}}$ | 883.7 | $60 \pi \mathrm{C}_{\beta} \mathrm{H}, 26 \pi \mathrm{C}_{\beta} \mathrm{C}_{\beta}$ | 103 | $\mathrm{B}_{2 \mathrm{u}}$ | 3107.4 | $98 v \mathrm{C}_{\beta} \mathrm{H}$ |
| 51 | $\mathrm{B}_{3 \mathrm{~g}}$ | 890.1 | $44 \pi \mathrm{C}_{\beta} \mathrm{H}, 26 \pi \mathrm{C}_{\beta} \mathrm{C}_{\beta}, 18 \pi \mathrm{C}_{\mathrm{m}} \mathrm{H}$ | 104 | $\mathrm{Ag}_{\mathrm{g}}$ | 3109.2 | $98 \nu \mathrm{C}_{\beta} \mathrm{H}$ |
| 52 | $\mathrm{A}_{\mathrm{u}}$ | 891.1 | $45 \pi \mathrm{C}_{\beta} \mathrm{H}, 24 \pi \mathrm{C}_{\beta} \mathrm{C}_{\beta}, 18 \pi \mathrm{C}_{\mathrm{m}} \mathrm{H}$ | 105 | $\mathrm{B}_{3 \mathrm{u}}$ | 3116.7 | $98 \nu \mathrm{C}_{\beta} \mathrm{H}$ |
| 53 | $\mathrm{A}_{\mathrm{g}}$ | 947.7 | $52 \nu \mathrm{C}_{\beta} \mathrm{C}_{\alpha}, 16 \nu \mathrm{CN}$ | 106 | $\mathrm{Ag}_{\mathrm{g}}$ | 3123.6 | $98 \nu \mathrm{C}_{\beta} \mathrm{H}$ |
| 54 | $\mathrm{B}_{2 \mathrm{u}}$ | 948.7 | $45 \nu \mathrm{C}_{\beta} \mathrm{C}_{\alpha}, 15 \nu \mathrm{CN}$ | 107 | $\mathrm{B}_{3 \mathrm{u}}$ | 3328.7 | $100 \nu \mathrm{NH}$ |
| 55 | $\mathrm{B}_{1 \mathrm{~g}}$ | 969.5 | $32 \nu \mathrm{CN}, 11 \nu \mathrm{C}_{\beta} \mathrm{C}_{\alpha}, 22 \delta \mathrm{HNC}, 13 \delta \mathrm{HC}_{\beta} \mathrm{C}_{\alpha}$ | 108 | $\mathrm{Ag}_{\mathrm{g}}$ | 3367.3 | $100 \nu \mathrm{NH}$ |
| 56 | $\mathrm{B}_{3 \mathrm{u}}$ | 971.2 | $46 v \mathrm{C}_{\beta} \mathrm{C}_{\alpha}, 18 v \mathrm{CN}$ |  |  |  |  |

${ }^{a}$ Abreviations used: $v$, stretching; $\delta$, in-plane bending; $\pi$, out-of-plane bending; $\tau$, torsion.

If one gives a value of 10 to the most intense band, one can calculate the other relative resonance Raman intensities for a particular electronic transition. It can be shown from the above simplified equations that the most intense enhancements will be given by the normal modes that contain bonds which are specifically affected by the electronic transition under consideration. A force field leading to erroneous enhancements would have to be rejected because the potential energy distribution would contain wrong combinations of the internal coordinates.

Results. Several resonance Raman spectra on the free base porphine (FBP) and of some of its substitued analogues have been reported ${ }^{1,2}$ for the first electronic transitions. The understanding of the composition of the excited states of the free base porphine would be essential to study the electronic changes
occurring under photoexcitation or interactions with external electrons particularly in the case of biological reactions. Among recent studies on the electronic properties of the free base porphine, Nakatsuji et al. ${ }^{24}$ reported a SAC-CI study on the ground, excited, and ionized states of free base porphine The infrared, Raman, resonance Raman, fluorescence, and phosphorescence properties have been also investigated in an extensive way and compared to theoretical vibrational analyses via a scaled quantum mechanical study. ${ }^{4,5}$

FBP has a $D_{2 h}$ symmetry which can was correlated to the $D_{4 h}$ of the metalloporphyrins. Nakatsuji et al. ${ }^{24}$ using SAC-CI treatments have shown that Gouterman's four orbital model ${ }^{25}$ perfectly explains the ground-state electronic state of the FBP and that these orbitals are all of the $\pi$ type, i.e., Homo -1 ,

TABLE 6: Experimental and Calculated Wavenumbers (in $\mathrm{cm}^{-1}$ ) for the $d_{0}, d_{2}, d_{4}, d_{8}$, and $d_{12}$ Isotopomers

|  |  | $d_{0}$ |  | $d_{2}$ |  | $d_{4}$ |  | $d_{8}$ |  | $d_{12}$ |  | no. | sym | $d_{0}$ |  | $d_{2}$ |  | $d_{4}$ |  | $d_{8}$ |  | $d_{12}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| no. | sym | exp | calc | exp | calc | exp | calc | exp | calc | $\exp$ | calc |  |  | exp | calc | exp | calc | exp | calc | exp | calc | exp | calc |
| 1 | $\mathrm{B}_{1 \mathrm{u}}$ |  | 51.7 |  | 51.7 |  | 52 |  | 50 |  | 50 | 55 | $B_{1 g}$ | 976 | 969.5 |  | 861 | 972 | 976 | 846 | 843 | 840 | 837 |
| 2 | $\mathrm{B}_{1 \mathrm{~g}}$ | 109 | 72.3 |  | 71.2 |  | 72 |  | 72 |  | 71 | 56 | $\mathrm{B}_{3 \mathrm{u}}$ | 971 | 971.2 | 957 | 954 | 981 | 978 | 773 | 780 | 775 | 758 |
| 3 | $\mathrm{A}_{\mathrm{u}}$ |  | 92.0 |  | 92.1 |  | 89 |  | 90 |  | 87 | 57 | $\mathrm{B}_{2 \mathrm{u}}$ | 977 | 981.7 |  | 865 | 961 | 954 | 784 | 781 |  | 767 |
| 4 | $\mathrm{B}_{1 \mathrm{u}}$ |  | 117.8 |  | 116.1 |  | 117 |  | 111 |  | 111 | 58 | $\mathrm{A}_{\mathrm{g}}$ | 988 | 984.5 | 978 | 968 |  | 956.2 | 794 | 792 | 770 | 771 |
| 5 | $\mathrm{B}_{2 \mathrm{~g}}$ |  | 135.1 |  | 131.1 |  | 135 |  | 128 |  | 128 | 59 | $B_{3 u}$ | 994 | 1002.4 |  | 1002 |  | 924 | 884 | 885 |  | 872 |
| 6 | $\mathrm{B}_{3 \mathrm{~g}}$ |  | 138.1 |  | 138.1 |  | 137 |  | 131 |  | 130 | 60 | $\mathrm{B}_{1 \mathrm{~g}}$ | 1005 | 1004.4 | 1004 | 1004 | 998 | 1001 | 908 | 910 | 896 | 897 |
| 7 | $\mathrm{Ag}_{\mathrm{g}}$ | 155 | 160.9 | 155 | 160.3 | 155 | 160.8 | 153 | 158.3 | 152 | 158.3 | 61 | $\mathrm{B}_{2 \mathrm{u}}$ | 1054 | 1052.1 | 1053 | 1051 | 996 | 992 | 881 | 879 | 870 | 868 |
| 8 | $\mathrm{B}_{2 \mathrm{~g}}$ |  | 192.4 |  | 191.4 |  | 186 |  | 188 |  | 182 | 62 | $\mathrm{B}_{3 \mathrm{u}}$ | 1043 | 1053.5 | 1043 | 1053 | 1044 | 1055 | 959 | 958 | 920 | 926 |
| 9 | $\mathrm{B}_{3 \mathrm{~g}}$ |  | 212.6 |  | 211.7 |  | 212 |  | 207 |  | 207 | 63 | $\mathrm{A}_{\mathrm{g}}$ | 1063 | 1054.9 | 1056 | 1055 | 1015 | 1007 | 944 | 937 | 923 | 921 |
| 10 | $\mathrm{B}_{1 \mathrm{u}}$ | 219 | 213.5 |  | 213.5 |  | 208 |  | 208 |  | 203 | 64 | $\mathrm{A}_{\mathrm{g}}$ | 1064 | 1063.7 | 1062 | 1063 | 1072 | 1061 | 978 | 967.6 | 957 | 947 |
| 11 | $\mathrm{B}_{2 \mathrm{u}}$ |  | 290.2 |  | 282.2 |  | 290 |  | 282 |  | 279 | 65 | $\mathrm{B}_{1 \mathrm{~g}}$ | 1138 | 1132.6 | 1182 | 1186 | 918 | 924 | 1095 | 1094 | 928 | 922 |
| 12 | $\mathrm{A}_{\mathrm{u}}$ |  | 296.0 |  | 296 |  | 296 |  | 277 |  | 277 | 66 | $\mathrm{B}_{3 \mathrm{u}}$ | 1134 | 1136.0 | 1134 | 1135 | 990 | 1002 | 1092 | 1087 | 969 | 967 |
| 13 | $\mathrm{Ag}_{\mathrm{g}}$ | 309 | 301.3 | 308 | 300 | 308 | 300.8 | 303 | 295.3 | 302 | 294.8 | 67 | $\mathrm{B}_{2 \mathrm{u}}$ | 1156 | 1155.1 | 1098 | 1095 | 1062 | 1058 |  | 1063 | 952 | 950 |
| 14 | $\mathrm{B}_{3 \mathrm{u}}$ | 310 | 310.5 |  | 309.5 |  | 306 |  | 303 |  | 299 | 68 | $\mathrm{Ag}_{\mathrm{g}}$ | 1172 | 1177.7 | 1175 | 1175 | 1072 | 1071.4 | 1171 | 1173 | 1019 | 1008.5 |
| 15 | $\mathrm{B}_{1 \mathrm{u}}$ | 335 | 331.8 |  | 332 |  | 304 |  | 328 |  | 301 | 69 | $\mathrm{B}_{1 \mathrm{~g}}$ | 1182 | 1183.9 |  | 1157 | 1170 | 1159 | 1045 | 1042 | 1043 | 1040 |
| 16 | $\mathrm{B}_{3 \mathrm{u}}$ | 357 | 344.0 |  | 343.3 |  | 343 |  | 324 |  | 323 | 70 | $\mathrm{B}_{1 \mathrm{~g}}$ | 1226 | 1225.9 |  | 1094 | 1218 | 1212 | 1218 | 1217 | 1149 | 1151 |
| 17 | $\mathrm{B}_{2 \mathrm{u}}$ | 357 | 347.8 |  | 347.3 | 357 | 346 |  | 330 |  | 329 | 71 | $\mathrm{B}_{3 \mathrm{u}}$ | 1177 | 1226.6 | 1172 | 1166 | 1161 | 1199 | 1162 | 1209 | 1114 | 1132 |
| 18 | $\mathrm{B}_{1 \mathrm{~g}}$ | 389 | 389.9 | 389 | 383 | 384 | 383 | 372 | 371 | 363 | 365 | 72 | $\mathrm{B}_{2 \mathrm{u}}$ | 1228 | 1226.9 |  | 1223 | 1203 | 1208 | 1204 | 1204 |  | 1111 |
| 19 | $\mathrm{B}_{1 \mathrm{~g}}$ | 418 | 407.8 | 418 | 407.7 | 419 | 408 | 389 | 376 | 385 | 376 | 73 | $\mathrm{B}_{2 \mathrm{u}}$ | 1255 | 1254.6 | 1255 | 1252 | 1241 | 1239 | 1225 | 1229 | 1211 | 1212 |
| 20 | $\mathrm{B}_{2 \mathrm{~g}}$ |  | 419.3 |  | 418.7 |  | 402 |  | 395 |  | 379 | 74 | $\mathrm{B}_{3 \mathrm{u}}$ | 1287 | 1289.6 |  | 1289 | 1264 | 1275 | 1210 | 1218 | 1173 | 1228 |
| 21 | $\mathrm{B}_{3 \mathrm{~g}}$ |  | 430.0 |  | 430 |  | 410 |  | 408 |  | 388 | 75 | $\mathrm{B}_{1 \mathrm{~g}}$ | 1313 | 1322.2 | 1316 | 1322 | 1290 | 1294 | 1238 | 1240 | 1282 | 1290 |
| 22 | $\mathrm{A}_{\mathrm{u}}$ |  | 470.0 |  | 470 |  | 454 |  | 434 |  | 422 | 76 | $\mathrm{Ag}_{\mathrm{g}}$ | 1352 | 1351.5 |  | 1349 | 1318 | 1316.0 | 1349 | 1341 | 1316 | 1319 |
| 23 | $\mathrm{B}_{2 \mathrm{~g}}$ |  | 605.0 |  | 454.4 |  | 618 |  | 543 |  | 542 | 77 | $\mathrm{B}_{1 \mathrm{~g}}$ | 1350 | 1356.7 | 1362 | 1355 | 1331 | 1334 | 1315 | 1321 | 1230 | 1213 |
| 24 | $\mathrm{B}_{1 \mathrm{u}}$ | 639 | 642.3 |  | 651 |  | 626 |  | 541 |  | 541 | 78 | $\mathrm{B}_{2 \mathrm{u}}$ | 1357 | 1358.8 | 1352 | 1356 | 1339 | 1341 | 1324 | 1320 | 1310 | 1313 |
| 25 | $\mathrm{B}_{2 \mathrm{~g}}$ |  | 665.8 |  | 665.8 |  | 677 |  | 549 |  | 549 | 79 | $\mathrm{B}_{1 \mathrm{~g}}$ | 1400 | 1381.0 | 1385 | 1379 | 1388 | 1377 | 1364 | 1363 | 1355 | 1341 |
| 26 | $\mathrm{B}_{3 \mathrm{~g}}$ |  | 667.4 |  | 538 |  | 669 |  | 643 |  | 632 | 80 | $\mathrm{Ag}_{\mathrm{g}}$ | 1384 | 1398.9 |  | 1393 | 1364 | 1368.2 | 1401 | 1399 | 1359 | 1356 |
| 27 | $\mathrm{A}_{\mathrm{u}}$ |  | 675.7 |  | 675.7 |  | 678 |  | 610 |  | 611 | 81 | $\mathrm{B}_{3 \mathrm{u}}$ | 1396 | 1399.7 | 1394 | 1394 | 1352 | 1377 | 1359 | 1354 | 1350 | 1347 |
| 28 | $\mathrm{B}_{2 \mathrm{~g}}$ |  | 695.5 |  | 695.6 |  | 646 |  | 559 |  | 559 | 82 | $\mathrm{B}_{2 \mathrm{u}}$ | 1406 | 1406.3 |  | 1398 | 1347 | 1359 | 1402 | 1400 | 1352 | 1360 |
| 29 | $\mathrm{A}_{\mathrm{u}}$ |  | 695.8 |  | 695.7 |  | 594 |  | 656 |  | 587 | 83 | $\mathrm{B}_{3 \mathrm{u}}$ | 1412 | 1413.0 | 1406 | 1412 | 1409 | 1412 | 1406 | 1395 | 1369 | 1374 |
| 30 | $\mathrm{B}_{1 \mathrm{u}}$ | 691 | 697.3 | 693 | 697.3 | 647 | 731 | 566 | 622 | 563 | 594 | 84 | $\mathrm{Ag}_{\mathrm{g}}$ | 1424 | 1424.3 | 1428 | 1424 | 1428 | 1417.1 | 1405 | 1404 | 1398 | 1396.0 |
| 31 | $\mathrm{B}_{3 \mathrm{~g}}$ |  | 700.0 |  | 700 |  | 714 |  | 622 |  | 600 | 85 | $\mathrm{B}_{1 \mathrm{~g}}$ | 1493 | 1495.1 | 1493 | 1484 | 1480 | 1480 | 1478 | 1484 | 1466 | 1468 |
| 32 | $\mathrm{Ag}_{\mathrm{g}}$ | 723 | 719.2 | 721 | 719 | 663 | 662 | 701 | 697.2 | 665 | 653 | 86 | $\mathrm{B}_{2 \mathrm{u}}$ | 1490 | 1497.1 | 1479 | 1480 | 1479 | 1487 | 1447 | 1463 | 1447 | 1452 |
| 33 | $\mathrm{Ag}_{\mathrm{g}}$ | 736 | 722.7 | 726 | 721.1 | 702 | 697 | 722 | 715 | 699 | 695 | 87 | $\mathrm{A}_{\mathrm{g}}$ | 1492 | 1508.5 | 1496 | 1508 | 1485 | 1497 | 1450 | 1463 | 1451 | 1455 |
| 34 | $\mathrm{B}_{1 \mathrm{u}}$ | 731 | 731.8 |  | 657 | 699 | 701 |  | 703 | 635 | 629 | 88 | $\mathrm{B}_{3 \mathrm{u}}$ | 1507 | 1516.8 |  | 1517 | 1498 | 1503 |  | 1493 | 1471 | 1477 |
| 35 | $\mathrm{B}_{3 \mathrm{u}}$ | 723 | 734.0 | 723 | 733 | 680 | 687 | 700 | 704 | 667 | 672 | 89 | $\mathrm{B}_{3 \mathrm{u}}$ | 1522 | 1528.4 |  | 1527 | 1505 | 1517 | 1515 | 1518 | 1500 | 1497 |
| 36 | $\mathrm{B}_{2 \mathrm{u}}$ | 745 | 744.0 | 744 | 731 | 694 | 693 |  | 761 | 677 | 676 | 90 | $\mathrm{B}_{2 \mathrm{u}}$ | 1540 | 1548.5 |  | 1548 | 1542 | 1545 | 1521 | 1525 | 1522 | 1519 |
| 37 | $\mathrm{B}_{3 \mathrm{~g}}$ |  | 764.3 |  | 758 |  | 776 |  | 731 |  | 733 | 91 | $\mathrm{A}_{\mathrm{g}}$ | 1544 | 1559.7 | 1555 | 1559 | 1554 | 1555.7 | 1524 | 1528.3 | 1518 | 1522.1 |
| 38 | $\mathrm{B}_{2 \mathrm{~g}}$ |  | 771.5 |  | 764 |  | 788 |  | 707 |  | 652 | 92 | $\mathrm{B}_{1 \mathrm{~g}}$ |  | 1592.0 | 1590 | 1582 | 1587 | 1581 | 1594 | 1587 | 1579 | 1575 |
| 39 | $\mathrm{B}_{1 \mathrm{u}}$ | 773 | 772.1 | 762 | 769 | 745 | 752 | 722 | 721 | 709 | 706 | 93 | $\mathrm{B}_{2 \mathrm{u}}$ |  | 1596.4 |  | 1586 |  | 1587 |  | 1590 |  | 1580 |
| 40 | $\mathrm{B}_{1 \mathrm{~g}}$ | 786 | 780.9 |  | 746 | 763 | 761 | 758 | 755 | 747 | 743 | 94 | $\mathrm{Ag}_{\mathrm{g}}$ | 1609 | 1600.8 | 1614 | 1601 | 1601 | 1587.2 | 1615 | 1598.6 | 1598 | 1585 |
| 41 | $\mathrm{B}_{2 \mathrm{u}}$ |  | 784.2 |  | 740 |  | 768 | 710 | 709 | 752 | 751 | 95 | $\mathrm{B}_{1 \mathrm{~g}}$ |  | 3056.3 | 3041 | 3056 | 2263 | 2256.9 |  | 3057 | 2258 | 2256.4 |
| 42 | $\mathrm{B}_{1 \mathrm{u}}$ | 785 | 785.4 |  | 776 | 779 | 774 | 753 | 759 | 745 | 742 | 96 | $\mathrm{Ag}_{\mathrm{g}}$ |  | 3057.7 | 3059 | 3058 |  | 2257.6 |  | 3058 |  | 2257.1 |
| 43 | $\mathrm{B}_{3 \mathrm{u}}$ | 780 | 787.9 |  | 787 | 770 | 776 | 760 | 760 | 741 | 749 | 97 | $\mathrm{B}_{3 \mathrm{u}}$ | 3042 | 3057.8 | 3042 | 3058 | 2266 | 2257.7 | 3040 | 3058 | 2260 | 2257.6 |
| 44 | $\mathrm{B}_{1 \mathrm{~g}}$ | 805 | 806.2 | 805 | 800 | 796 | 793 | 776 | 773 | 762 | 760 | 98 | $\mathrm{B}_{2 \mathrm{u}}$ | 3045 | 3058.7 | 3045 | 3059 | 2258 | 2257.7 | 3046 | 3059 | 2258 | 2257.6 |
| 45 | $\mathrm{B}_{3 \mathrm{~g}}$ |  | 839.0 |  | 839 |  | 744 |  | 849 |  | 679 | 99 | $\mathrm{B}_{1 \mathrm{~g}}$ |  | 3090.5 |  | 3090 |  | 3090.2 |  | 2280.2 |  | 2280.6 |
| 46 | $\mathrm{A}_{\mathrm{u}}$ |  | 840.0 |  | 840 |  | 619 |  | 846 |  | 653 | 100 | $\mathrm{B}_{3 \mathrm{u}}$ | 3088 | 3090.7 | 3118 | 3091 |  | 3090.4 |  | 2280.4 | 2269 | 2280.8 |
| 47 | $\mathrm{B}_{2 \mathrm{~g}}$ |  | 845.0 |  | 845 |  | 598 |  | 842 |  | 723 | 101 | $\mathrm{B}_{2 \mathrm{u}}$ | 3112 | 3106.8 | 3112 | 3107 | 3110 | 3107.0 |  | 2296.5 | 2263 | 2296.6 |
| 48 | $\mathrm{B}_{1 \mathrm{u}}$ | 852 | 845.6 | 853 | 846 | 799 | 794 | 847 | 839 | 764 | 759 | 102 | $\mathrm{B}_{1 \mathrm{~g}}$ |  | 3107.2 |  | 3107 |  | 3107.2 |  | 2296.6 |  | 2296.7 |
| 49 | $\mathrm{A}_{\mathrm{u}}$ |  | 882.4 |  | 882 |  | 882 |  | 742 |  | 747 | 103 | $\mathrm{B}_{2 \mathrm{u}}$ | 3124 | 3107.4 | 3124 | 3108 | 3122 | 3107.4 | 2338 | 2321.4 | 2324 | 2321.4 |
| 50 | $\mathrm{B}_{2 \mathrm{~g}}$ |  | 883.7 |  | 884 |  | 882 |  | 732 |  | 761 | 104 | $\mathrm{Ag}_{\mathrm{g}}$ |  | 3109.2 |  | 3109 |  | 3109.2 |  | 2322.6 |  | 2322.6 |
| 51 | $\mathrm{B}_{3 \mathrm{~g}}$ |  | 890.1 |  | 890 |  | 888 |  | 738 |  | 760 | 105 | $\mathrm{B}_{3 \mathrm{u}}$ | 3128 | 3116.7 | 3128 | 3117 | 3117 | 3116.9 | 2336 | 2323.5 | 2334 | 2323.5 |
| 52 | $\mathrm{A}_{\mathrm{u}}$ |  | 891.1 |  | 891 |  | 888 |  | 729 |  | 767 | 106 | $\mathrm{Ag}_{\mathrm{g}}$ | 3158 | 3123.6 |  | 3124 |  | 3123.6 |  | 2328.8 |  | 2328.5 |
| 53 | $\mathrm{Ag}_{\mathrm{g}}$ | 952 | 947.7 | 950 | 946 | 920 | 914.0 | 776 | 767 | 773 | 762 | 107 | $\mathrm{B}_{3 \mathrm{u}}$ | 3324 | 3328.7 | 2475 | 2449 | 3324 | 3328.7 | 3324 | 3328.7 |  | 3328.7 |
| 54 | $\mathrm{B}_{2 \mathrm{u}}$ | 951 | 948.7 | 950 | 948 | 923 | 923 | 938 | 935 | 918 | 920 | 108 | $\mathrm{Ag}_{\mathrm{g}}$ |  | 3367.3 |  | 2474 |  | 3367.3 |  | 3367.3 |  | 3367.3 |

Homo, Lumo, and Lumo +1 . They have shown that these molecular orbitals (MO) display $\pi$ conjugation over the whole molecule and noted that an another MO of the $\pi$ type could strongly perturbe this model.

The lowest energetic electronic transitions are given by two pairs of degenerate states the Q bands $\left(\mathrm{Q}_{x}, \mathrm{Q}_{y}\right)$ and the $\mathrm{B}_{x}(\mathrm{~B}$ Soret band) and N states lying respectively at 480 and 380 nm in the electronic spectrum of the FBP. The components of each pair are polarized perpendicularly to the components of the other pair.

In the resonance Raman spectra, the totally symmetric $\mathrm{A}_{\mathrm{g}}$ modes (for FBP with $D_{2 h}$ symmetry) will be enhanced via two kinds of mechanisms: (i) the Frank-Condon (FC) mechanism (which originates in the difference between the equilibrium geometries of the ground and excited electronic states; (ii) the Herzberg-Teller (HT) mechanism (vibronic coupling between
electronic states). The relative enhancements observed for the electronic transition centered on the Q band have been given in ref 2 .

The FC mechanism will lead to polarized Raman bands with a polarization ratio lying in the 0.125 and 0.75 range. The Raman bands originating from the HT coupling generally give depolarized bands $(\rho=0.75)$, but in the case of two excited states belonging to the same representation their direct product containing the totally symmetric representation can lead to the appearance of a nonzero (resonance) Raman activity.

In the present work, we tried to use a DFT description of the frontier orbitals to give a crude description of the resonance activity for the lowest electronic transitions.

For the free base porphine with $D_{2 h}$ symmetry, Table 7 gives the eigenvalues and symmetries of the molecular orbitals together with values obtained from other studies. ${ }^{24,26,27}$ In the

TABLE 7: Eigenvalues (in eV) and Symmetries of the Frontier Orbitals As Obtained from Different Quantum Mechanical Studies

| molecular orbital | DFT/B3-LYP (this work) |  | $\mathrm{LDA}^{26}$ |  | CAS-SCF ${ }^{27}$ |  | SAC-CI ${ }^{24}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | energy | sym | energy | sym | energy | sym | energy | sym |
| Lumo +2 |  |  | -0.58 | $\mathrm{A}_{\mathrm{u}}(\pi)$ |  |  |  |  |
| Lumo + 1 | -2.23 | $\mathrm{B}_{2 \mathrm{~g}}(\pi)$ | -1.92 | $\mathrm{B}_{3 \mathrm{~g}}(\pi)$ | 3.06 | $\mathrm{B}_{2 \mathrm{~g}}(\pi)$ | 0.141 | $4 \mathrm{~b}_{3 \mathrm{~g}}$ |
| Lumo | -2.24 | $\mathrm{B}_{3 \mathrm{~g}}(\pi)$ | -1.94 | $\mathrm{B}_{2 \mathrm{~g}}(\pi)$ | 2.88 | $\mathrm{B}_{3 \mathrm{~g}}(\pi)$ | -0.069 | $4 \mathrm{~b}_{2 \mathrm{~g}}$ |
| Homo | -5.16 | $\mathrm{B}_{1 \mathrm{u}}(\pi)$ | -3.90 | $\mathrm{B}_{1 \mathrm{u}}(\pi)$ | -4.18 | $\mathrm{A}_{\mathrm{u}}(\pi)$ | -6.52 | 2 au |
| Homo - 1 | -5.30 | $\mathrm{A}_{\mathrm{u}}(\pi)$ | -4.15 | $\mathrm{A}_{\mathrm{u}}(\pi)$ | -4.24 | $\mathrm{B}_{1 \mathrm{u}}(\pi)$ | -6.68 | $5 b_{1 u}$ |
| Homo - 2 |  |  | -4.71 | $\mathrm{B}_{2 \mathrm{~g}}(\pi)$ | -7.10 |  |  |  |
| Homo - 3 |  |  | -4.84 | $\mathrm{B}_{1 \mathrm{u}}(\pi)$ |  |  |  |  |
| Homo - 4 |  |  | -5.17 | $\operatorname{Ag}(\sigma)$ |  |  |  |  |
| Homo - 5 |  |  | -5.19 | $\mathrm{B}_{3 \mathrm{u}}(\sigma)$ |  |  |  |  |

TABLE 8: Molecular Orbital Coefficients Occurring in the Frontier Orbitals of FBP As Estimated from the Ground State ${ }^{a}$

| atom numbering | basis function | $\begin{gathered} \text { Homo }-1 \\ \left(-0.194819 E_{\mathrm{h}}\right. \text {, } \\ \text { OCC } \left.1, \operatorname{sym} \mathrm{~A}_{\mathrm{u}}\right) \end{gathered}$ | $\begin{gathered} \text { Homo } \\ \left(-0.189607 E_{\mathrm{h}},\right. \\ \text { OCC } \left.1, \operatorname{sym} \mathrm{~B}_{1 \mathrm{u}}\right) \end{gathered}$ | $\begin{gathered} \text { Lumo } \\ \left(-0.082385 E_{\mathrm{h}}\right. \text {, } \\ \text { OCC } \left.0, \operatorname{sym} \mathrm{~B}_{3 \mathrm{~g}}\right) \end{gathered}$ | $\begin{gathered} \text { Lumo }+1 \\ \left(-0.081991 E_{\mathrm{h}}\right. \text {, } \\ \text { OCC } \left.0, \operatorname{sym} \mathrm{~B}_{2 \mathrm{~g}}\right) \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| N1 | 3 s |  | 0.212 | -0.175 |  |
|  | $2 \mathrm{p}_{x}$ |  | 0.176 | -0.170 |  |
| N3 | 3 s |  | 0.212 | 0.175 |  |
|  | $2 \mathrm{p}_{x}$ |  | 0.176 | 0.170 |  |
| N6 | 3 s | 0.146 |  |  | 0.157 |
|  | $2 \mathrm{p}_{x}$ | 0.138 |  |  | 0.172 |
| N7 | 3 s | 0.146 |  |  | -0.157 |
|  | $2 \mathrm{p}_{x}$ | 0.138 |  |  | -0.172 |
| C8 | 3 s | 0.191 | -0.065 | 0.138 | 0.113 |
|  | $2 \mathrm{p}_{x}$ | 0.142 | -0.041 | 0.127 | 0.110 |
| C9 | 3 s | -0.191 | -0.065 | -0.138 | 0.113 |
|  | $2 \mathrm{p}_{x}$ | -0.142 | -0.041 | -0.127 | 0.110 |
| C10 | 3 s | 0.199 |  | 0.065 | -0.167 |
|  | $2 \mathrm{p}_{x}$ | 0.144 |  | 0.050 | -0.146 |
| C11 | 3 s | -0.199 |  | 0.065 | -0.167 |
|  | $2 \mathrm{p}_{x}$ | -0.144 |  | 0.050 | -0.146 |
| C12 | 3 s | 0.191 | -0.065 | -0.138 | -0.113 |
|  | $2 \mathrm{p}_{x}$ | 0.142 | -0.041 | -0.127 | -0.110 |
| C13 | 3 s | -0.191 | -0.065 | 0.138 | -0.113 |
|  | $2 \mathrm{p}_{x}$ | -0.142 | -0.041 | 0.127 | -0.110 |
| C14 | 3 s | 0.199 |  | -0.065 | 0.167 |
|  | $2 \mathrm{p}_{x}$ | 0.144 |  | -0.050 | 0.146 |
| C15 | 3 s | -0.199 |  | -0.065 | -0.167 |
|  | $2 \mathrm{p}_{x}$ | -0.144 |  | -0.050 | -0.146 |
| C17 | 3 s |  |  | 0.045 | -0.153 |
|  | $2 \mathrm{p}_{x}$ |  |  | 0.038 | -0.158 |
| C18 | 3 s |  | -0.229 | -0.193 | 0.159 |
|  | $2 \mathrm{p}_{x}$ |  | -0.199 | -0.190 | 0.145 |
| C19 | 3 s | 0.108 | 0.073 | 0.165 | 0.070 |
|  | $2 \mathrm{p}_{x}$ | 0.096 | 0.057 | 0.167 | 0.069 |
| C20 | 3 s |  | -0.229 | 0.193 | 0.159 |
|  | $2 \mathrm{p}_{x}$ |  | -0.199 | 0.190 | 0.145 |
| C21 | 3 s | 0.095 |  | 0.045 | 0.53 |
|  | $2 \mathrm{p}_{x}$ | 0.088 |  | 0.038 | 0.158 |
| C22 | 3 s |  | -0.229 | -0.165 | -0.159 |
|  | $2 \mathrm{p}_{x}$ |  | -0.199 | -0.190 | -0.145 |
| C23 | 3 s | -0.108 | 0.073 | 0.165 | 0.070 |
|  | $2 \mathrm{p}_{x}$ | -0.096 | 0.057 | 0.167 | 0.069 |
| C24 | 3 s | 0.095 |  | -0.045 | -0.153 |
|  | $2 \mathrm{p}_{x}$ | 0.088 |  | -0.038 | -0.158 |
| C26 | 3 s |  | -0.229 | 0.193 | -0.159 |
|  | $2 \mathrm{p}_{x}$ |  | -0.199 | 0.190 | -0.145 |
| C27 | 3 s | 0.108 | 0.073 | -0.165 | 0.070 |
|  | $2 \mathrm{p}_{x}$ | 0.096 | 0.057 | -0.167 | 0.069 |
| C28 | 3 s | -0.108 | 0.073 | -0.165 | -0.070 |
|  | $2 \mathrm{p}_{x}$ | -0.096 | 0.057 | -0.167 | 0.069 |
| C29 | 3 s | -0.095 |  | -0.045 | 0.153 |
|  | $2 \mathrm{p}_{x}$ | -0.088 |  | -0.038 | 0.158 |

${ }^{a}$ Molecular orbital energies are expressed in hartrees $\left(E_{\mathrm{h}}\right)$. OCC and sym are the occupancy number and symmetry type, respectively.
present work, the excitation energies for the Homo to Lumo $(\mathrm{H} \rightarrow \mathrm{L})$, Homo to Lumo $+1(\mathrm{H} \rightarrow \mathrm{L}+1)$, Homo -1 to Lumo ( $\mathrm{H}-1 \rightarrow \mathrm{~L}$ ), and $\mathrm{H}-1 \rightarrow \mathrm{~L}+1$ transitions have been calculated to correspond to the 425-405 nm range.

Nakatsuji et al. ${ }^{24}$ have shown that the Q band is composed of two bands $\left(\mathrm{Q}_{x}\right.$ and $\left.\mathrm{Q}_{y}\right)$ assigned to the $1 \mathrm{~B}_{3 \mathrm{u}}$ and $1 \mathrm{~B}_{2 \mathrm{u}}$ states, respectively, and noted an overestimation of 0.2 eV in the corresponding excitation energies. If one takes the same relative
error for the excitation energy, the electronic transition obtained from the present DFT study would be centered at about 450 nm and related to the Q electronic band.

Table 8 displays the molecular orbital coefficients (MOC) calculated for the ground state of FBP ( $D_{2 h}$ symmetry). The most important contributions to the MOC are given by the Rydberg (3s) orbitals that are very poorly occupied and by the $2 \mathrm{p}_{z}$ coefficients (with $z$ being perpendicular to the molecular

TABLE 9: Changes in the Bond Orders Occurring in the Electronic Transitions Represented by the Four-Orbital Model

| internal <br> coord | $\Delta$ bo- <br> $(\mathrm{H} \rightarrow \mathrm{L})$ | $\Delta$ bo- <br> $(\mathrm{H} \rightarrow \mathrm{L}+1)$ | $\Delta$ bo- <br> $(\mathrm{H}-1 \rightarrow \mathrm{~L})$ | $\Delta$ bo- <br> $(\mathrm{H}-1 \rightarrow \mathrm{~L}+1)$ |
| :--- | ---: | :---: | :---: | :---: |
| $\mathrm{N}-\mathrm{H}$ | 0.0000 | 0.0000 | 0.0000 | 0.0000 |
| $\mathrm{C}_{\mathrm{m}}-\mathrm{C}_{\alpha}$ | -1.1791 | 2.5329 | -0.4849 | 3.1883 |
| $\left(\mathrm{C}_{\mathrm{m}}-\mathrm{C}_{\alpha}\right)^{a}$ | 1.0231 | -1.9433 | 1.4258 | -1.5034 |
| $\mathrm{C}-\mathrm{N}$ | -0.4593 | -1.9237 | -0.9042 | -2.3503 |
| $(\mathrm{C}-\mathrm{N})^{a}$ | -0.5519 | 0.1806 | -0.3568 | 0.3665 |
| $\mathrm{C}_{\beta}-\mathrm{C}_{\alpha}$ | 1.6846 | -0.8661 | 2.7476 | 0.2287 |
| $\left(\mathrm{C}_{\beta}-\mathrm{C}_{\alpha}\right)^{a}$ | -0.1734 | 2.0333 | 1.0091 | 3.1883 |
| $\mathrm{C}_{\beta}-\mathrm{C}_{\beta}{ }^{2}+2.0930$ | 0.8391 | -2.5419 | 0.3535 |  |
| $\left(\mathrm{C}_{\beta}-\mathrm{C}_{\beta}\right)^{a}$ | 0.1661 | -2.2313 | -0.5435 | -2.9111 |
| $\mathrm{C}_{\mathrm{m}}-\mathrm{H}$ | 0.0000 | 0.0000 | 0.0000 | 0.0000 |
| $\mathrm{C}_{\beta}-\mathrm{H}$ | 0.0000 | 0.0000 | 0.0000 | 0.0000 |

${ }^{a}$ For bonds belonging to the unprotonated pyrrole rings.
plane). The four orbitals are all of the $\pi$ type and correspond to the description of Gouterman. ${ }^{25}$

Table 9 gives the calculated bond order changes for the monoelectronic $\mathrm{H} \rightarrow \mathrm{L}$ transition and for the other possible transitions. As the bond order changes are opposed in sign to the changes in bond lengths, the $\pi$ bond lengths decrease while the $\sigma$ bond lengths increase and the relative changes in bond orders follow the totally symmetric representation. The most intense changes in bond orders are given for the four molecular orbitals by the $\mathrm{C}_{\beta}=\mathrm{C}_{\beta}$ and $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ bonds in the protonated pyrrole rings.

Table 10 gives the predicted resonance Raman intensities (RRI) for the normal modes belonging to the $\mathrm{A}_{\mathrm{g}}$ species. The RRI given for the $\mathrm{H} \rightarrow \mathrm{L}$ electronic transition are in a general good accordance with the enhanced bands observed in the resonance Raman spectrum recorded at the 488 nm excitation wavelength and corresponding to maximum absorption of the Q band. As a matter of comparison, the predicted RRI obtained from an equal participation of the four monoelectronic transitions ( $25 \%$ each) are also given in the table.

The general agreement between the predicted and experimental RRI gives some confidence to the force field obtained
from the DFT method as an incorrect potential energy distribution would lead to erroneous predicted resonance Raman bands. Moreover, the predicted resonance Raman intensities corresponding to the unscaled DFT-derived force field (all scaling factors being equal to 1 ) are equally reported in this table. No marked changes between predicted RRI obtained with or without a set of scaling factors could be detected. The meaning of this fact stands in the high values of the scaling factors, and consequently, the potential energy distribution gives comparable participations of the internal coordinates to the normal modes.

The predicted relative resonance Raman intensities for the normal modes with $\mathrm{A}_{\mathrm{g}}$ symmetry appearing at $1607,1490,1349$, and $1174 \mathrm{~cm}^{-1}$ correlate well with the experimental enhancements. The experimental RRI were estimated from the peak heights observed in the spectrum recorded at $488 \mathrm{~nm}^{2}$ with the most intense band being normalized to 10 . The corresponding wavenumbers were predicted at $1601,1508,1351$, and 1178 $\mathrm{cm}^{-1}$ and involve principally $\mathrm{C}_{\mathrm{m}} \mathrm{C}_{\alpha}, \mathrm{C}_{\beta} \mathrm{C}_{\beta}$, and $\mathrm{C}_{\beta} \mathrm{C}_{\alpha}$ stretching and bending $\delta \mathrm{CNC}$ in-plane motions as it can be observed from the potential energy distribution.
The very intense RRI (7.4) observed at $1314 \mathrm{~cm}^{-1}$ at the 488 nm excitation wavelength ${ }^{2}$ corresponds here to a $\mathrm{B}_{1 \mathrm{~g}}$ mode calculated at $1322 \mathrm{~cm}^{-1}$. No resonance intensity could be calculated for this mode as the method proposed here to calculate the RRI applies only to totally symmetric modes. This is an indirect way to confirm the non-totally symmetric nature of this normal mode.
In the Q -band region, the $\mathrm{A}_{g}$ and $\mathrm{B}_{3 \mathrm{~g}}$ modes give rise to resonance Raman enhancements while, in the Soret band near $380-400 \mathrm{~nm}$, only the Ag modes should undergo such enhancements. ${ }^{5}$

The small RRI (1.0) observed at $1136 \mathrm{~cm}^{-1}$ corresponds to the predicted $\mathrm{B}_{1 \mathrm{~g}}$ mode at $1133 \mathrm{~cm}^{-1}$. For the same reasons as previously, no RRI could be predicted for this mode.

Two normal modes with $\mathrm{A}_{\mathrm{g}}$ symmetry are predicted at 1064 and $1055 \mathrm{~cm}^{-1}$ with calculated RRI of 8.4 and 0.7 for the $\mathrm{H} \rightarrow$ L transition and RRI of 5.47 and 2.50 in the case of an equal

TABLE 10: Calculated Relative Resonance Raman Intensities (RRI) As Obtained from the Estimation of the Changes in Bond Orders along the Electronic Transition Corresponding to the Q Band Observed at 488 nm for the Free Base Porphine with $D_{2 h}$ Symmetry ${ }^{a}$

| $\exp \left(\mathrm{cm}^{-1}\right)$ | RRI ${ }^{\text {exp }}$ | calc $\left(\mathrm{cm}^{-1}\right)$ | sym | $R R I^{\text {calc }}(\mathrm{H} \rightarrow \mathrm{L})$ | $\mathrm{calc}^{\text {b }}$ | $\mathrm{RRI}^{\text {calc }}(\mathrm{H} \rightarrow \mathrm{L})^{b}$ | $R R I^{\text {calc }}$ (all MO) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1666 | 1.2 |  |  |  |  |  |  |
| 1643 | 1.2 |  |  |  |  |  |  |
| 1607 | 10.0 | 1601 | $\mathrm{Ag}_{\mathrm{g}}$ | 10.0 | 1656 | 10.0 | 10.0 |
| 1580 | 1.6 | 1592 | $\mathrm{B}_{1 \mathrm{~g}}$ |  |  |  |  |
| 1558 | 0.8 | 1548 | $\mathrm{A}_{\mathrm{g}}$ | 0.7 | 1603 | 0.7 | 0.98 |
| 1541 | 0.8 |  |  |  |  |  |  |
| 1490 | 5.4 | 1508 | Ag | 5.4 | 1552 | 5.1 | 4.9 |
| 1446 | 1.0 |  |  |  |  |  |  |
| 1425 | 1.0 | 1424 | Ag | 4.2 | 1476 | 5.3 | 4.64 |
| 1402 | 0.0 | 1399 | $\mathrm{Ag}_{\mathrm{g}}$ | 4.0 | 1442 | 3.4 | 4.80 |
| 1384 | 0.0 | 1381 | $\mathrm{B}_{1 \mathrm{~g}}$ | 0.0 |  |  |  |
| 1349 | 2.1 | 1351 | $\mathrm{Ag}_{\mathrm{g}}$ | 3.0 | 1386 | 3.5 | 2.5 |
| 1314 | 7.4 | 1322 | $\mathrm{B}_{1 \mathrm{~g}}$ |  |  |  |  |
| $1191{ }^{\text {sh }}$ | 0.9 | 1184 | $\mathrm{B}_{1 \mathrm{~g}}$ | 0.0 |  |  |  |
| 1174 | 2.9 | 1178 | $\mathrm{A}_{\mathrm{g}}$ | 2.5 | 1208 | 2.7 | 1.60 |
| 1136 | 1.0 | 1133 | $\mathrm{B}_{1 \mathrm{~g}}$ | 0.0 |  |  |  |
| 1086 | 4.6 |  |  |  |  |  |  |
| 1062 | 3.7 | 1064 | $\mathrm{Ag}_{\mathrm{g}}$ | 8.4 | 1092 | 8.4 | 5.47 |
| 1049 | 1.6 | 1055 | $\mathrm{Ag}_{\mathrm{g}}$ | 0.7 | 1083 | 0.5 | 2.5 |
| 985 | 3.3 | 985 | $\mathrm{Ag}_{\mathrm{g}}$ | 0.8 | 1014 | 0.6 | 0.82 |
| 950 | 1.6 | 948 | $\mathrm{Ag}_{\mathrm{g}}$ | 0. | 976 | 0 | 0.75 |
| 736 | 4.9 | 723 | $\mathrm{Ag}_{\mathrm{g}}$ | 2.0 | 737 | 2.3 | 1.44 |
| 721 | 2.0 | 719 | $\mathrm{Ag}_{\mathrm{g}}$ | 1.0 | 734 | 0.7 | 0.82 |
| 558 | 3.0 |  |  |  |  |  |  |

[^1] of 1 .
participation of the four orbitals. The corresponding observed values are 3.7 and 1.6. These last calculated RRI are in better agreement with the experimental ones. The associated potential energy distribution implies $\mathrm{C}_{\alpha} \mathrm{C}_{\beta} \mathrm{H}$ and $\mathrm{C}_{\beta} \mathrm{C}_{\beta} \mathrm{H}$ in-plane bending vibrations and the frequency shifts observed in the experimental spectrum for the $d_{8}$ isotopomer ( 944 and $959 \mathrm{~cm}^{-1}$ ) are correctly predicted at 937 and $958 \mathrm{~cm}^{-1}$ leading to some confidence with the normal mode description. From this it follows that a particular linear combination of monoelectronic transitions should have better to be used than a particular one. Nakatsuji et al., ${ }^{24}$ using SAC-CI calculations, pointed out the fact that a lone pair orbital $\left(4 \mathrm{~b}_{1 \mathrm{u}}\right)$ could also pertub the four-orbital model; this could explain the differences between the values of the calculated and experimental RRI.

As a matter of discrepancy, a normal mode with $\mathrm{A}_{\mathrm{g}}$ symmetry observed at $1402 \mathrm{~cm}^{-1}$ in the normal Raman spectrum ${ }^{5}$ is calculated here at $1399 \mathrm{~cm}^{-1}$ with a surprising strong RRI (4.0). No counterpart could be observed in the resonance Raman spectra recorded for the 488 nm excitation ( Q band). As was pointed out by Kozlowski et al., ${ }^{5}$ no corresponding resonance enhancement could be observed in the Soret region for FBP. We obtained the same feature as described by these authors. They could observe a Raman band at $1400 \mathrm{~cm}^{-1}$ (calculated at $1402 \mathrm{~cm}^{-1}$ ) and found a corresponding phosphorescence line at $1405 \mathrm{~cm}^{-1}$. They calculated a much larger intensity for this particular band than for the observed one and, finally, assigned this band to an $\mathrm{A}_{1 \mathrm{~g}}$ mode and the neighboring one observed at $1384 \mathrm{~cm}^{-1}$ to a mode with $\mathrm{B}_{1 \mathrm{~g}}$ symmetry. We can confirm this assignment for the $1402 \mathrm{~cm}^{-1}$ Raman band, but the reason for which no experimental RRI could be observed is not clear and may be due to interferences between the FC and HT mechanisms. ${ }^{5}$

The $\mathrm{A}_{\mathrm{g}}$ mode observed at $985 \mathrm{~cm}^{-1}$ is calculated at the same wavelength with a lower resonance intensity ( 0.80 ) than observed (3.3), while no RRI intensity could be calculated for the $\mathrm{A}_{\mathrm{g}}$ mode observed at $950 \mathrm{~cm}^{-1}$ (predicted at $948 \mathrm{~cm}^{-1}$ ) if one takes only the $\mathrm{H} \rightarrow \mathrm{L}$ transition into account. However, a small RRI could be predicted ( 0.75 , observed 1.6 ) if the four monoelectronic transitions are taken into account. These two modes are mainly $\nu \mathrm{C}_{\alpha} \mathrm{C}_{\beta}$ and $\nu \mathrm{CN}$ in character with a larger participation of the $\delta \mathrm{CNH}$ and $\delta \mathrm{C}_{\alpha} \mathrm{C}_{\beta} \mathrm{H}$ in-plane motions for the highest frequency. The corresponding wavenumbers observed in the $d_{8}$ isotopomer at 794 and $776 \mathrm{~cm}^{-1}$ are correctly reproduced for these two modes.

The doublet at 736 and $721 \mathrm{~cm}^{-1}$ observed in the resonance Raman ${ }^{2}$ spectrum at 488 nm is well reproduced in the present work by the two predicted bands at 723 and $719 \mathrm{~cm}^{-1}$. The corresponding predicted RRI (2.0 and 1.0) are somewhat less intense than in the experimental spectrum (4.9 and 2.0), but their mutual relative intensities are in agreement with the experiment. These two bands involve $\mathrm{C}_{\alpha} \mathrm{C}_{\mathrm{m}}$ and pyrrole ring in-plane bending modes. No dependence on the hydrogen substituents was predicted, this being in agreement with the observation of only a very weak shift in the isotopomer.

## Conclusion

The accordance between the present assignments for the $d_{0}$, $d_{2}, d_{4}, d_{8}$, and $d_{12}$ isotopomers of the free base porphyrin and previous normal-mode analysis using a quantum scaled force field leads to the conclusion of two important points: (i) The use of symmetry or internal coordinates to treat the redundancy problem does not change in a large way the assigments of the normal modes. (ii) The determination of the resonance Raman intensities appears to be a good way to identify the totally
symmetric modes for a complex molecule such as the free base porphyrin. The normal Raman band with $\mathrm{A}_{\mathrm{g}}$ symmetry observed at $1402 \mathrm{~cm}^{-1}$ would have to be studied in more detail to explain its lack of experimental resonance Raman intensity and its too strong calculated Raman intensity.

The determination of the resonance Raman intensities appears as a complementary tool to the vibrational analysis and determination of Raman or infrared intensities. The knowledge of the ground electronic state is enough to explain the principal features observed along the resonance Raman enhancements. When dealing with quantum studies, this method is easy to use.

In the case of metalloporphyrins, vibrational wavenumbers will be perturbated for a certain number of bands that are involved in the interactions with the metal. The resonance Raman enhancements would also depend on such interactions, and then the determination of these changes could be related to the electronic transition of the porphine base when linked to the metal ligand.

We have shown that the determination of the RRI is a very restrictive method when dealing with various force fields and that only a force field was possible to retrieve the RRI.

The next application of the determination of the resonance Raman intensities will be done for the metalloporphyrins, and the normal modes having totally symmetric motions will be particularly studied.

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[^0]:    ${ }^{\dagger}$ E-mail: gerard.vergoten@univ-lille1.fr.

[^1]:    ${ }^{a}$ sh: shoulder. RRI are calculated for an equal participation of the four monoelectronic transitions (all MO). ${ }^{b}$ Values given for a scaling factor

