# Ab Initio Calculations and Modeling of Three-Dimensional Adiabatic and Diabatic Potential Energy Surfaces of $\operatorname{Br}\left({ }^{2} \mathbf{P}\right) \cdots \mathbf{H}_{\mathbf{2}}\left(\mathbf{1}^{+}\right)$Pre-Reactive Complex 

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Received: February 25, 2002; In Final Form: May 13, 2002


#### Abstract

The three lowest diabatic potential energy surfaces for the $\mathrm{Br}\left({ }^{2} \mathrm{P}\right)+\mathrm{H}_{2}$ van der Waals complex are derived from accurate ab initio calculations of the T-shaped $\left(C_{2 v}\right)$ and collinear geometries ( $C_{\infty v}$ ), at the coupled cluster with single, double, and noniterative triple excitations ( $\operatorname{CCSD}(\mathrm{T})$ ) level of theory with a large basis set. For the intermediate geometries, the angular dependence is modeled by a simple Legendre-polynomial interpolation. The nonadiabatic coupling (off-diagonal derivative) matrix element and the fourth, off-diagonal, diabatic surface are determined by separate complete active space self-consisted field (CASSCF) calculations with a medium-sized basis set. Three adiabatic potential energy surfaces (PESs) are also obtained, by diagonalizing the total Hamiltonian in the diabatic basis. Both the nonrelativistic and relativistic (including spin-orbit coupling) PESs are evaluated. The dependence of the PESs on the $\mathrm{H}_{2}$ stretching coordinate is also incorporated and analyzed.


## I. Introduction

In recent years, there has been considerable theoretical interest in electronically nonadiabatic effects in chemical reactions, and hydrogen abstraction reaction by a halogen atom, $\mathrm{Hal}+\mathrm{H}_{2} \rightarrow$ $\mathrm{HalH}+\mathrm{H}$, has been one of the most important paradigm. ${ }^{1-8}$ Whereas the major thrust went into the investigation of $\mathrm{F}+\mathrm{H}_{2}$ and $\mathrm{Cl}+\mathrm{H}_{2}$, less is known about $\mathrm{Br}+\mathrm{H}_{2}$, especially on the experimental side. For this system, the reaction engaging the spin-orbit excited-state $\operatorname{Br}\left({ }^{2} \mathrm{P}_{1 / 2}\right)$ is very interesting because the energy difference between $\operatorname{Br}\left({ }^{2} \mathrm{P}_{1 / 2}\right)$ and $\operatorname{Br}\left({ }^{2} \mathrm{P}_{3 / 2}\right)$ is very large $(0.455 \mathrm{eV})$, unlike for related F or Cl atom. This energy splitting is close to the energy difference between $\mathrm{H}_{2}(v=0)$ and $\mathrm{H}_{2}(v$ $=1)(0.512 \mathrm{eV})$, where $v$ is the vibrational quantum number. Because the electronic-to-vibrational energy transfer occurs in the entrance channel, it seems important to have a detailed knowledge of the van der Waals forces that determine the potential energy surface in this region. The role of weak interactions at the outset of chemical reactions has been recently emphasized by several authors. ${ }^{9-11}$ In this paper, following our studies of the related $\mathrm{F}+\mathrm{H}_{2}$ and $\mathrm{Cl}+\mathrm{H}_{2}$ complexes, ${ }^{1,2}$ we present ab initio calculations and modeling of the $\mathrm{Br}+\mathrm{H}_{2}$ van der Waals complex.

Pioneering theoretical work carried out by Truhlar and coworkers ${ }^{5-7}$ focused on the reactive region and did not consider the van der Waals fragments of the potentials. The authors developed $2 \times 2$ diabatic potential energy surfaces and then carried out converged quantum reactive scattering calculations

[^0]for zero total angular momentum, using the outgoing wave variational principle. They found that the quenching of the spinorbit excited Br with the ground-state $\mathrm{H}_{2}$ mainly produces $\mathrm{H}_{2}$ with one quantum of vibrational excitation in the total energy range they studied. This means that the quenching process satisfies a near-resonance condition for the electronic-tovibrational energy transfer.

On the experimental side, Nesbitt and Leone ${ }^{12}$ reported interesting experimental results for the $\mathrm{Br}-\mathrm{H}_{2}$ system. They concluded, from their systematic laser photolysis study, that $\operatorname{Br}\left({ }^{2} \mathrm{P}_{1 / 2}\right)+\mathrm{H}_{2}(v=1)$ is efficiently quenched to $\operatorname{Br}\left({ }^{2} \mathrm{P}_{3 / 2}\right)+$ $\mathrm{H}_{2}(v=2)$ in the entrance channel, followed by a subsequent H atom abstraction from vibrationally exited $\mathrm{H}_{2}$

$$
\operatorname{Br}\left({ }^{2} \mathrm{P}_{1 / 2}\right)+\mathrm{H}_{2}(v=1) \rightarrow\left[\operatorname{Br}\left({ }^{2} \mathrm{P}_{3 / 2}\right) \mathrm{H}_{2}(v=2)\right] \rightarrow \underset{\mathrm{HBr}+\mathrm{H} .}{ } \quad
$$

Very recently, Takayanagi and Kurosaki ${ }^{13}$ have performed threedimensional quantum scattering calculations for the electronically nonadiabatic $\operatorname{Br}\left({ }^{2} \mathrm{P}_{1 / 2}\right)+\mathrm{H}_{2}$ reaction. A detailed analysis of the calculated probabilities confirmed that the electronically nonadiabatic transitions from $\operatorname{Br}\left({ }^{2} \mathrm{P}_{1 / 2}\right)+\mathrm{H}_{2}(v)$ to $\operatorname{Br}\left({ }^{2} \mathrm{P}_{3 / 2}\right)+$ $\mathrm{H}_{2}(v+1)$ effectively occur in the entrance region of the potential surface. However, the contribution of the electronically nonadiabatic chemical reaction, $\operatorname{Br}\left({ }^{2} \mathrm{P}_{3 / 2}\right)+\mathrm{H}_{2}(v) \rightarrow \mathrm{HBr}+$ H , is small.

The above nonadiabatic process of electronic-to-vibration energy transfer is possible because of the weak interaction with the $\mathrm{H}_{2}$ molecule. The latter lifts the symmetry ban for the intramultiplet transition, and accepts the released energy. The intramultiplet mixing dynamics that is triggered by the van der Waals interaction is still a virgin area, despite recent theoretical progress achieved for the collisions of rare gas atoms with $\mathrm{Cl},{ }^{14}$ O, ${ }^{15}$ and S. ${ }^{16}$

The goal of this paper is to provide accurate nonrelativistic and relativistic ab initio potential energy surfaces (PESs) for the first three states of $\mathrm{Br}+\mathrm{H}_{2}$ in the entrance channel fragment. These three states arise from the interaction of $\mathrm{H}_{2}$ with the triply degenerate ${ }^{2} \mathrm{P} \mathrm{Br}$ atom. The electron configuration of Br gives rise to ${ }^{2} \Sigma^{+}$and ${ }^{2} \Pi$ states in the $C_{\infty v}$ configuration, to ${ }^{2} \mathrm{~A}_{1},{ }^{2} \mathrm{~B}_{1}$, ${ }^{2} \mathrm{~B}_{2}$ states in the triangular $C_{2 v}$ geometry, and to $1^{2} \mathrm{~A}^{\prime}, 2^{2} \mathrm{~A}^{\prime}$, and ${ }^{2} \mathrm{~A}^{\prime \prime}$ states in $C_{s}$ geometries. The PESs are derived within the recently proposed combined ab initio coupled-cluster and model treatment, termed coupled-cluster-model (CC-M). ${ }^{1,2}$

The essence of the CC-model approach is to calculate accurate coupled cluster with the single, double, and noniterative triple excitations ( $\operatorname{CCSD}(\mathrm{T})$ ) interaction energies only for two highly symmetrical configurations, the $C_{2 v}$ and $\mathrm{C}_{\infty v}$ geometries, and then model the three lowest diabatic surfaces of the $C_{s}$ symmetry by means of a simple angular interpolation. The method proved successful for the $\mathrm{F}+\mathrm{H}_{2}{ }^{1}$ and $\mathrm{Cl}+\mathrm{H}_{2}{ }^{2}$ systems. The approach takes advantage of the oblate shape of the $\mathrm{H}_{2}$ molecule, causing a relatively simple anisotropy of the interaction. To obtain the nonadiabatic coupling element of the Hamiltonian matrix (related to the fourth diabatic surface), separate complete active space self-consistent field (CASSCF) calculations are performed over the complete range of geometries.

To obtain the three lowest nonrelativistic adiabatic PESs, the Hamiltonian in the diabatic basis is diagonalized. The relativistic spin-orbit coupling effects are included by using the formalism recently developed by Alexander, Manolopoulos, and Werner, ${ }^{3}$ assuming the empirical value of the splitting parameters. The dependence of the PESs on the $\mathrm{H}_{2}$ stretching coordinate is also incorporated and analyzed.

## II. Computational Methods and Results

A. Geometries and Basis Sets. The $\mathrm{Br}-\mathrm{H}_{2}$ complex is described in Jacobi coordinates ( $R, r, \theta$ ). The $R$ variable denotes the distance between the center of the $\mathrm{H}_{2}$ monomer and the Br atom, and $\theta$ denotes the angle between the $\vec{R}$ vector and the $\mathrm{H}_{2}$ bond axis. $\theta=0^{\circ}$ corresponds to the $\mathrm{Br} \cdots \mathrm{H}-\mathrm{H}$ collinear arrangement. The $\mathrm{H}_{2}$ monomer stretch is described by the $r$ coordinate. Calculations were done for eight values of $r$ ranging from 0.4 to $1.16 \AA$ (the equilibrium distance $r_{\mathrm{e}}=0.7408 \AA$ included). Distance $R$ ranged from 1.5 to $10.0 \AA$. The origin of the system of coordinates was placed at the center of the $\mathrm{H}_{2}$ molecule. In the calculations of the diabatic energies, the $\mathrm{H}_{2}$ molecule was located along the $x$ axis, and the $z$ axis was perpendicular to the triatomic plane. Calculations employed the augmented correlation-consistent polarized basis sets of qua-druple- $\zeta$ quality (aug-cc-pvqz) basis function set of Dunning et al. ${ }^{17-19} \operatorname{CCSD}(\mathrm{~T})$ calculations (but not CASSCF ones) also included bond functions, with the exponents: $s p 0.9,0.3,0.1 ; d$ $0.6,0.2,{ }^{20}$ in the form of a set: [ $3 s 3 p 2 d$ ], denoted as (332). Bond functions were centered in the middle of the $\vec{R}$ vector. Bond functions have been shown ${ }^{21}$ to be both effective and economical for a number of van der Waals complexes including those with an open-shell moiety. ${ }^{22-25}$
B. Ab Initio Adiabatic and Diabatic Potential Energy Surfaces. The CC-M potentials are built in three steps:

1. Accurate $\operatorname{CCSD}(\mathrm{T})$ calculations are performed for the $C_{2 v}$ and $C_{\infty v}$ geometries, with a large basis set, to obtain benchmark interaction energies, see section 2.3. The model diabats for the $C_{s}$-symmetry geometries are obtained by a simple Legendrepolynomial interpolation between the $C_{2 v}$ and $C_{\infty v}$ geometries.
2. CASSCF calculations are carried out to obtain a nonadiabatic coupling (off-diagonal derivative) matrix element, mixing


Figure 1. Contour plot of the $\gamma_{\mathrm{R}}$ mixing angle calculated in aug-ccpvqz basis set, $r=r_{\mathrm{e}}$.
angle (Figure 1), and the fourth diabatic (off-diagonal) surface, see section 2.4.
3. The adiabatic PESs are obtained by diagonalizing the Hamiltonian matrix in terms of the diabatic basis set. See section 2.5.

All ab initio calculations reported in this paper were performed using the MOLPRO package. ${ }^{26}$ The supermolecular method is used to calculate the interaction energies for the $C_{2 v}$ and $C_{\infty v}$ arrangements. This method derives the interaction energy as the difference between the energies of the dimer AB and the monomers A and B

$$
\begin{equation*}
\Delta E^{(n)}=E_{\mathrm{AB}}^{(n)}-E_{\mathrm{A}}^{(n)}-E_{\mathrm{B}}^{(n)} \tag{1}
\end{equation*}
$$

The superscript ( $n$ ) denotes the level of ab initio theory. In the $\operatorname{CCSD}(\mathrm{T})$ calculations, the use of the above equation is straightforward and free from arbitrary choices, as long as the dimer and monomer energies are calculated with the same dimer centered basis set to counterpoise the basis set extension effect. ${ }^{27}$ The $\operatorname{CCSD}(\mathrm{T})$ method is well-known to be very effective in recovering electron correlation effects in van der Waals complexes ${ }^{28,29}$ and is preferred as long as the single-reference approach is valid. The variant of $\operatorname{CCSD}(\mathrm{T}), \mathrm{R}-\mathrm{UCCSD}(\mathrm{T})$, is used, based on restricted open-shell Hartree-Fock (ROHF) orbitals, but with spin contamination allowed in the linear terms of the wave function. ${ }^{30-32}$ Only valence electrons are correlated.

To calculate the off-diagonal matrix element of the Hamiltonian matrix, the CASSCF method is used (see section 2.4).
C. Model Diabatic PESs. The $\operatorname{CCSD}(\mathrm{T})$ approach can provide us with very accurate results, close to saturation with respect to basis set and correlation effects. Not only can this method be used with confidence for the lowest state of a given symmetry but also for excited states that are adequately represented by a single Slater determinant, e.g., when the excited state is related to a single-electron promotion from one p orbital to another, orthogonal p orbital. The latter feature was exploited in our recent study of the $\mathrm{HCl}-\mathrm{Cl}$ van der Waals complex, ${ }^{33}$ where two $\mathrm{A}^{\prime}$ states in the van der Waals region were well separated in a wide range of geometries. However, whereas formally the situation in the $\mathrm{H}_{2}-\mathrm{Br}\left({ }^{2} \mathrm{P}\right)$ case is identical, the $\mathrm{H}_{2}$ molecule produces a much smaller splitting of the ${ }^{2} \mathrm{P}$ state of Br , and related hypersurfaces of the complex, and a significant nonadiabatic mixing of two adiabatic $\mathrm{A}^{\prime}$ states takes place, which



Figure 2. Contour plots of the modeled diabats and adiabats: (a) $H_{11}^{C C}$ Values in $\mathrm{cm}^{-1}, r=r_{\mathrm{e}}$.
culminates in the conical intersection for the collinear arrangement. This fact precludes the application of the $\operatorname{CCSD}(\mathrm{T})$ ansatz.

In previous work on $\mathrm{Cl}-\mathrm{H}_{2}{ }^{2,4}$ and $\mathrm{F}-\mathrm{H}_{2},{ }^{1,3,34}$ the diabatic surfaces revealed a simple and regular shape. For a given $R$, the $\theta$ dependence was smooth and monotonic between the $C_{2 v}$ and $C_{\infty \nu}$ geometries. On this basis, we proposed the CC-M method which assumed the $\operatorname{CCSD}(\mathrm{T})$ interaction energies for the $C_{2 v}$ and $C_{\infty v}$ geometries and derived the interaction energies for the $C_{s}$ geometries from the Legendre expansion truncated at $L=2$, which is equivalent to the following angular dependence:

$$
\begin{gather*}
H_{11}^{\mathrm{CC}-\mathrm{M}}(R, r, \theta)=V_{\mathrm{A}_{1}}^{\mathrm{CCSD(T})}(R, r) \sin ^{2} \theta+ \\
V_{\Sigma}^{\mathrm{CCSD}(\mathrm{~T})}(R, r) \cos ^{2} \theta  \tag{2}\\
H_{22}^{\mathrm{CC-M}}(R, r, \theta)=V_{\mathrm{B}_{2}}^{\mathrm{CCSD}(\mathrm{~T})}(R, r) \sin ^{2} \theta+ \\
V_{\Pi}^{\mathrm{CCSD}(\mathrm{~T})}(R, r) \cos ^{2} \theta \tag{3}
\end{gather*}
$$

$H_{33}^{\mathrm{CC}-\mathrm{M}}(R, r, \theta)=V_{\mathrm{B}_{1}}^{\mathrm{CCSD}(\mathrm{T})}(R, r) \sin ^{2} \theta+$

$$
\begin{equation*}
V_{\Pi}^{\operatorname{CCSD(T)}}(R, r) \cos ^{2} \theta \tag{4}
\end{equation*}
$$

The CC-M method was carefully verified by comparison with the scaled multireference configuration interaction results. ${ }^{1,2} \mathrm{Ab}$ initio $\operatorname{CCSD}(\mathrm{T})$ results for the $\mathrm{A}_{1}, \mathrm{~B}_{1}$, and $\mathrm{B}_{2}$ representations of the $C_{2 v}$ symmetry and $\Sigma^{+}$and $\Pi$ representations for the $C_{\infty v}$

diabat, (b) $\mathrm{H}_{22}^{\mathrm{CC}-\mathrm{M}}$ diabat, (c) $1 \mathrm{~A}_{\mathrm{CC}-\mathrm{m}}^{\prime}$ adiabat and (d) $2 \mathrm{~A}_{\mathrm{CC}-\mathrm{m}}^{\prime}$ adiabat.
symmetry have been fitted to analytic expressions to represent $V_{X}^{C C S D(T)}(R, r)$ in eqs $2-4$. We use the analytic expression based on the Taylor expansion in the $r$ coordinate with additional exponential $r$-dependent terms and the $R$ dependence is of the Esposti-Werner ${ }^{35}$ type:

$$
\begin{equation*}
V(R, r)=\left[G(R) e^{-a_{1}\left(R-a_{2}\right)-b_{1} \xi-b_{2} \xi^{2}}-T(R) \sum_{i=5}^{9} \frac{C_{i}}{R^{i}}\right] H(\xi) \tag{5}
\end{equation*}
$$

where

$$
\begin{gather*}
G(R)=\sum_{j=0}^{8} g_{j} R^{j}  \tag{6}\\
H(\xi)=\sum_{m=0}^{2} h_{m} \xi^{m}, \quad \xi=\frac{r-r_{\mathrm{e}}}{r_{\mathrm{e}}} \tag{7}
\end{gather*}
$$

and damping function

$$
\begin{equation*}
T(R)=\frac{1}{2}\left(1+\tanh \left(t_{1}+t_{2} R\right)\right) \tag{8}
\end{equation*}
$$

FORTRAN codes generating PES are available on request from J. Kłos.

The contour plots of $\mathrm{H}_{11}^{\mathrm{CC}-\mathrm{M}}$ and $\mathrm{H}_{22}^{\mathrm{CC}-\mathrm{M}}$ for $r=0.7408 \AA$ are shown in Figure 2 parts a and b, respectively. The contour
plot of the $\mathrm{H}_{33}^{\mathrm{CC}-\mathrm{M}}$ diabat is very similar to that in Figure 2b. In Figures 2 parts a and $b$, the bold line indicates the crossing of diabats, $\mathrm{H}_{11}^{\mathrm{CC}-\mathrm{M}}=\mathrm{H}_{22}^{\mathrm{CC}-\mathrm{M}}$. It originates at the region of $\Sigma^{+}-\Pi$ conical intersection, at $\theta=0^{\circ}$ ).
D. CASSCF Calculations and Fitting of Fourth Diabatic Potential. 1. CASSCF Calculations. The state averaged CASSCF orbitals are allowed for all three states, $1 \mathrm{~A}^{\prime}, 2 \mathrm{~A}^{\prime}$, and $1 A^{\prime \prime} .{ }^{36,37}$ The Br-moiety-related 1 s orbital was kept frozen, the $2 \mathrm{~s}, 2 \mathrm{p}, 3 \mathrm{~s}$ and 3 p orbitals were doubly occupied, and the 4 s and 4 p orbitals were active. The $\sigma_{g}$ and $\sigma_{u}^{*}$ molecular orbitals of hydrogen were also included in the active space.

Calculations were performed for several values of interhydrogen distance $r$ and in a wide range of $R$ and $\theta$ variables. These calculations require neither the self-consistency corrections nor the counterpoise correction. The basis set has been a bare aug-cc-pvqz set (without bond functions).
2. Diabatic Transformation. Diabatic surfaces provide more convenient representations for simulations of the van der Waals spectra of the system. These potentials contain information about couplings between the adiabatic wave functions of the same symmetry. The adiabatic-diabatic transformation yields diabatic states for which the nonadiabatic coupling matrix elements approximately vanish. The diabatic states are related to adiabatic states by a orthogonal transformation ${ }^{38,39}$

$$
\left[\begin{array}{l}
\Psi_{1}^{d}  \tag{9}\\
\Psi_{2}^{d} \\
\Psi_{3}^{d}
\end{array}\right]=\left[\begin{array}{lll}
\cos \gamma & \sin \gamma & 0 \\
-\sin \gamma & \cos \gamma & 0 \\
0 & 0 & 1
\end{array}\right]\left[\begin{array}{c}
\Psi_{2}^{a} \\
\Psi_{2}^{a} \\
\Psi_{3}^{a}
\end{array}\right]
$$

where the transformation angle $\gamma$ depends on the nuclear coordinates. The resulting diabatic wave functions are no longer eigenstates of the electronic Hamiltonian. The Hamiltonian in the diabatic $\left(\mathrm{p}_{x}, \mathrm{p}_{y}, \mathrm{p}_{z}\right)$ basis is not diagonal, and the matrix elements are modeled as

$$
\begin{gather*}
H_{11}=H_{11}^{\mathrm{CC}-\mathrm{M}} \\
H_{22}=H_{22}^{\mathrm{CC}-\mathrm{M}} \\
H_{33}=H_{33}^{\mathrm{CC}-\mathrm{M}} \\
H_{12}=\sqrt{2}\left(E_{1 A^{\prime}}^{\mathrm{CAS}}-E_{2 A^{\prime}}^{\mathrm{CAS}}\right) \cos \gamma \sin \gamma \tag{10}
\end{gather*}
$$

The transformation angle $\gamma$, the so-called "mixing angle", is defined as the angle between the vector of the singly occupied $p$ orbital and the $\vec{R}$ vector. It is a function of the Jacobi coordinates of the system. Within a two-state model, the mixing angle can, in principle, be obtained by the numerical integration of the nonadiabatic coupling matrix elements (NACMEs). To calculate the mixing angle, we used the method which maximizes the overlap with orbitals of the reference geometry. ${ }^{40}$ The reference geometry is taken to be a collinear one for large intermolecular distances. This choice of reference geometry ensures that diabatic states coincide with adiabatic ones. This method calculates NACME in an approximate way using two slightly displaced geometries and the method of finite differences. Because it is convenient to perform a diabatic transformation in a system of coordinates with one axis along the $\vec{R}$ vector, the actual $\gamma$ is redefined as

$$
\begin{equation*}
\gamma_{\mathrm{R}}=\gamma+\theta-\frac{\pi}{2} \tag{11}
\end{equation*}
$$

The plot of $\gamma_{\mathrm{R}}$ values is shown in Figure 1. This figure distinctly

TABLE 1: Stationary Points of Modeled Diabatic Surfaces for $r=r_{e}=0.7408 \AA$

| diabat | $D_{\mathrm{e}} / \mathrm{cm}^{-1}$ | $R_{\mathrm{e}} / \AA$ | $\theta_{\mathrm{e}}$ | type |
| :--- | :---: | :---: | :---: | :--- |
| $\mathrm{H}_{11}^{\mathrm{CC}-\mathrm{M}}$ | 165.1 | 3.15 | 90 | minimum |
|  | 28.2 | 3.70 | 0 | saddle point |
| $\mathrm{H}_{22}^{\mathrm{CC}-\mathrm{M}}$ | 83.1 | 3.85 | 0 | minimum |
|  | 27 | 4.15 | 90 | saddle point |
| $\mathrm{H}_{33}^{\mathrm{CC}-\mathrm{M}}$ | 83.1 | 3.85 | 0 | minimum |
|  | 38.2 | 4.00 | 90 | saddle point |

exhibits the region where the $\mathrm{A}^{\prime}$ states avoid crossing each other and the point where the $\Sigma^{+}$and $\Pi$ states cross. This is the region where the mixing is the strongest and the angle in eq 9 reaches $45^{\circ}$. The conical intersection occurs at $\mathrm{Br} \cdots \mathrm{H}-\mathrm{H}, \theta=0^{\circ}, R \approx$ $3.4 \AA$. The intersection is related to the crossing of the $\Sigma^{+}$and $\Pi$ states.
3. 3-D Fitting. To fit the three-dimensional set of ab initio data for $\mathrm{H}_{12}$ we used an analytical expression based on the expansion in associated Legendre functions $\mathrm{P}_{l}^{1}$ and the Taylor expansion around $r=r_{\mathrm{e}}$ interhydrogen distance

$$
\begin{equation*}
H_{12}(r, R, \theta)=V_{\mathrm{sh}}(r, R, \theta)+V_{\mathrm{as}}(r, R, \theta) \tag{12}
\end{equation*}
$$

where

$$
\begin{align*}
& V_{\mathrm{sh}}(r, R, \theta)= \\
& \sum_{l=1}^{6} \sum_{i=0}^{3} \sum_{j=0}^{3} g_{l j} c_{i} R^{j} \xi^{i} e^{\sqrt{1 / 2}(a-b R)-c \xi-d \xi^{2}} \sqrt{\frac{4 l+1}{2}} P_{2 l}^{1}(\cos \theta) \tag{13}
\end{align*}
$$

and
$V_{\mathrm{as}}(r, R, \theta)=$
$\sum_{n=5}^{7} \sum_{i=0}^{3} c_{i} \xi^{\frac{C_{n}}{R^{\mathrm{n}}}} \sqrt{\frac{2(n-4)+1}{2}} P_{2(n-4)}^{1}(\cos \theta), \quad \xi=\frac{r-r_{\mathrm{e}}}{r_{\mathrm{e}}}$
The fit contains 35 optimized parameters. Its quality can be expressed in terms of the root-mean-square value of $3.7 \mathrm{~cm}^{-1}$. The biggest relative error equals approximately $20 \%$, but for small values of energy, it is on the order of $1 \mathrm{~cm}^{-1}$. Most of the relative errors are within the range of $2-8 \%$.
E. Model Nonrelativistic Adiabatic PESs. To obtain the adiabatic counterparts of the diabatic surfaces, the diabatic matrix

$$
\mathbf{H}^{\mathrm{el}}=\left[\begin{array}{lll}
H_{11} & H_{12} & 0  \tag{15}\\
H_{12} & H_{22} & 0 \\
0 & 0 & H_{33}
\end{array}\right]
$$

is diagonalized. The global minima and stationary points of the modeled diabatic and adiabatic surfaces are shown in Table 1. The contour plots of $1 \mathrm{~A}^{\prime}$ and $2 \mathrm{~A}^{\prime}$ adiabatic surfaces for $r=r_{\mathrm{e}}$ are shown in Figure 2 parts c and d, respectively.

## III. Effect of $\mathbf{H}_{\mathbf{2}}$ Stretch

In Figures 3 and 4, we show $R$ - and $r$-dependent contour plots of $V(R, r)$ for the $C_{\infty v}$ symmetry (the $\Sigma^{+}$and $\Pi$ states, Figure 3 parts a and b , respectively) and for the $C_{2 v}$ symmetry (the $A_{1}, B_{1}$, and $B_{2}$ states, Figure 4 parts $a-c$, respectively). One can see that the $\mathrm{A}_{1}$ and $\Sigma^{+}$potentials, which define the ground adiabatic state, are the most sensitive functions of $r$, whereas the other $V(R, r)$ potentials only weakly depend on $r$. The $V_{\Sigma}$ potential reveals a shallow van der Waals minimum for large


Figure 3. ( $R, r$ ) dependence of interaction energies of (a) $\Sigma$ and (b) $\Pi$ symmetry. Values in $\mathrm{cm}^{-1}$.
values of $R$, with $r$ close to $r_{\mathrm{e}}$ and shorter, and has a large well for small values of $R$ and large values of $r$, where the reaction region is reached. The $\mathrm{V}_{\mathrm{A} 1}$ potential for large $R$ is everywhere attractive and fairly wide and flat with respect to $r$. On decreasing $R$ and for small $r$, a repulsive bank emerges, whereas the attractive region is narrowed to larger $r$ only, where the potential falls steeply into the reactive region.

The behavior of $V(R, r)$ determines the behavior of the diabats and adiabats according to eqs $2-4$. The changes of $r$ have the most significant impact on the $\mathrm{H}_{11}$ diabatic surface and only a mild effect on the other two, $\mathrm{H}_{22}$ and $\mathrm{H}_{33}$. Compared with the plot for $r=r_{\mathrm{e}}$ (Figure 2a) upon compressing $\mathrm{H}_{2}$ to $r=0.5292$ $\AA$ (Figure 5a), the T-shaped geometry minimum rises from - 165 up to $-97 \mathrm{~cm}^{-1}$, whereas the collinear stationary point is slightly lowered (by a few $\mathrm{cm}^{-1}$ ). In other words, the minimum energy path around Br is now shallower and flatter. By contrast, stretching $\mathrm{H}_{2}$ to $r=0.8466 \AA$ (Figure 5b) makes the T-shaped minimum deeper, from -165 down to $-203 \mathrm{~cm}^{-1}$.

The effect of stretching and compressing $\mathrm{H}_{2}$ on the $\mathrm{H}_{22}$ and $\mathrm{H}_{33}$ diabats is minor, so we do not show it in the figures.

## IV. Spin-Orbit Coupling and Model Relativistic Adiabatic PESs

Upon allowing for the spin-orbit coupling of the halogen atom, one obtains two atomic terms: ${ }^{2} \mathrm{P}_{3 / 2}$ and ${ }^{2} \mathrm{P}_{1 / 2}$, separated by $\Delta_{\mathrm{SO}}=3669.8 \mathrm{~cm}^{-1}$. The interaction with $\mathrm{H}_{2}$ further splits the ${ }^{2} \mathrm{P}_{3 / 2}$ state into two states. To evaluate the resulting adiabatic


Figure 4. ( $R, r$ ) dependence of interaction energies of (a) $\mathrm{A}_{1}$, (b) $\mathrm{B}_{1}$, and (c) $\mathrm{B}_{2}$ symmetries. Values in $\mathrm{cm}^{-1}$.
potential energy surfaces, we use the procedure described by Alexander, Manolopoulos, and Werner. ${ }^{3}$ The matrix of the electrostatic interaction plus the spin-orbit Hamiltonian is expressed in the basis set invariant to time reversal (see ref 3 for details). Then the total matrix decouples

$$
\mathbf{H}^{\mathrm{el}}+\mathbf{H}^{\mathrm{SO}}=\left[\begin{array}{ll}
\mathbf{H} & 0  \tag{16}\\
0 & \mathbf{H}^{\dagger}
\end{array}\right]
$$

where $\mathbf{H}$ is the $3 \times 3$ Hermitian matrix



Figure 5. Contour plots of the modeled $\mathrm{H}_{11}^{\mathrm{CC}-\mathrm{M}}$ diabat for (a) $r=$ $0.529177 \AA$ and (b) $r=0.846683 \AA$. Values in $\mathrm{cm}^{-1}$.

$$
\mathbf{H}=\left[\begin{array}{cc}
H_{11}-V_{1}-i \sqrt{2} B & V_{1}  \tag{17}\\
V_{\Pi}+A & V_{2} \\
& V_{\Pi}-A
\end{array}\right]
$$

where $\mathrm{V}_{1}=H_{12}, \mathrm{~V}_{\Pi}=\left(H_{33}+H_{22}\right) / 2$, and $\mathrm{V}_{2}=\left(H_{33}-H_{22}\right) /$ 2. $A$ and $B$ are spin-orbit matrix elements:

$$
\begin{equation*}
A \equiv i\left\langle\Pi_{y}\right| H^{\mathrm{SO}}\left|\Pi_{x}\right\rangle \tag{18}
\end{equation*}
$$

and

$$
\begin{equation*}
B \equiv\left\langle\bar{\Pi}_{x}\right| H^{\mathrm{SO}}|\Sigma\rangle \tag{19}
\end{equation*}
$$

where, after Alexander et al., ${ }^{3}$ we used the compact Cartesian notation for diabatic states: $\left|\Pi_{x}\right\rangle,\left|\Pi_{y}\right\rangle$, and $|\Sigma\rangle$, related to the projections of the electronic orbital and spin momenta along the vector $\vec{R}$. The bar above the $\left|\Pi_{x}\right\rangle$ state in Eq. 19 denotes $\beta$ spin. On diagonalizing the matrix in eq 17, three adiabatic potential energy surfaces are obtained, shown in Figure 6 parts $a-c$. They are numbered in the order of increasing energy. In the limit of large $R$, the first two adiabatic PESs correlate with the ${ }^{2} \mathrm{P}_{3 / 2}$ state of Br , with the projection of $j$ upon the $\mathrm{b} \vec{R}$ vector equal to $3 / 2$ for the ground state and $1 / 2$ the first excited state. The third adiabat (Figure 6c) correlates with the ${ }^{2} \mathrm{P}_{1 / 2}$ term of the Br atom.

One can see that the relativistic adiabatic surfaces significantly differ from nonrelativistic ones. The lowest adiabatic surface


Figure 6. Contour plots of the spin-orbit corrected adiabats. (a) adiabat 1, which correlates with $\operatorname{Br}\left({ }^{2} \mathrm{P}_{3 / 2}\right)$, (b) adiabat 2, which correlates with $\operatorname{Br}\left({ }^{2} \mathrm{P}_{3 / 2}\right)$, and (c) adiabat 3 , which correlates to $\operatorname{Br}\left({ }^{2} \mathrm{P}_{1 / 2}\right)$. Values in $\mathrm{cm}^{-1}, r=r_{\mathrm{e}}$.
is now half as deep at the T-shaped minimum ( $D_{\mathrm{e}}=87 \mathrm{~cm}^{-1}$ ), and considerably flattened with a $17 \mathrm{~cm}^{-1}$ barrier for the $\mathrm{H}_{2}$ rotation, around $40^{\circ}$, and another local minimum for the collinear arrangement ( $D_{\mathrm{e}}=83 \mathrm{~cm}^{-1}$ ). The other adiabatic surface related to the same ${ }^{2} \mathrm{P}_{3 / 2}$ asymptotic limit is shallower, with a maximum at $90^{\circ}$ and a minimum at $0^{\circ}$ with the well depth of $46 \mathrm{~cm}^{-1}$. The third state, asymptotically separated by the $3669.8 \mathrm{~cm}^{-1}$ SO coupling, resembles the second in shape but is slightly deeper.

TABLE 2: Stationary Points of Modeled Spin-Orbit Corrected Adiabatic Surfaces for $r=r_{\mathrm{e}}=\mathbf{0 . 7 4 0 8}$ A

| adiabat | $D_{\mathrm{e}} / \mathrm{cm}^{-1}$ | $R_{\mathrm{e}} / \AA$ | $\theta_{\mathrm{e}}$ | type |
| :---: | :---: | :---: | ---: | :--- |
| adiabat 1 | 87 | 3.55 | 90 | minimum |
| adiabat 1 | 83 | 3.85 | 0 | minimum |
| adiabat 2 | 49 | 3.80 | 30 | minimum |
| adiabat 2 | 46 | 3.80 | 0 | saddle |
| adiabat 2 | 32 | 4.05 | 90 | saddle |
| adiabat 3 | 64 | 3.80 | 0 | minimum |
| adiabat 3 | 51 | 3.85 | 90 | saddle |

The $D_{\mathrm{e}}$ and $R_{\mathrm{e}}$ parameters of the three adiabatic PESs are listed in Table 2.

## V. Summary and Conclusions

The 3-D CC-M diabatic potentials for the first three states of the $\mathrm{H}_{2}-\mathrm{Br}$ complex have been derived from ab initio calculations for the T-shaped and collinear forms at the CCSD(T) level of theory with a large basis set. It has been found that the ground state is sensitive to the changes of $r$. In particular, the height of the barrier decreases by stretching the $\mathrm{H}_{2}$ molecule and increases by compressing it.

The ground state $1 \mathrm{~A}^{\prime}$ PES of $\mathrm{H}_{2}-\mathrm{Br}$ may be compared with the ground state $1 \mathrm{~A}^{\prime} \mathrm{PES}$ of $\mathrm{H}_{2}-\mathrm{Cl}$ which was derived recently by us within the same CC-M framework. ${ }^{2}$ The intermediate and long range of these surfaces are similar, with the $\mathrm{H}_{2}-\mathrm{Cl}$ van der Waals well being almost of the same well depth, and with almost the same hindrance for the $\mathrm{H}_{2}$ rotation of ca. $82 \mathrm{~cm}^{-1}$.

The characteristics of the PESs are dramatically changed upon allowing for the spin-orbit effects. The relativistic ground-state adiabatic PES is half as deep as the nonrelativistic one, 87 vs $165 \mathrm{~cm}^{-1}$, and the barrier to the rotation of $\mathrm{H}_{2}$ is shifted toward $40^{\circ}$ and lowered from 82 to $17 \mathrm{~cm}^{-1}$, whereas the collinear saddle point transforms into a minimum. The second and third adiabatic surfaces are also considerably flattened. These results qualitatively agree with the finding of Alexander, Manolopoulos, and Werner ${ }^{3}$ for $\mathrm{F}+\mathrm{H}_{2}$ in that the "spin-orbit coupling cannot be neglected in the region of the van der Waals minimum [...] and significantly alters both the depth and position of the van der Waals well".

We also checked the influence of the electronic correlation of the inner shells of the Br atom on the interaction energy of the $A_{1}$ state in the global minimum. Upon setting active space to include the $1 \mathrm{~s}, 2 \mathrm{~s}$, and 2 p orbitals frozen, the $3 \mathrm{~s}, 3 \mathrm{p}, 3 \mathrm{~d}, 4 \mathrm{~s}$, $4 \mathrm{p}_{x}$, and $4 \mathrm{p}_{y}$ doubly occupied, and $4 \mathrm{p}_{z}$ active, the interaction energy increased to $167.7 \mathrm{~cm}^{-1}$. The difference with the default $\left(1 \mathrm{~s}, 2 \mathrm{~s}, 3 \mathrm{~s}, 3 \mathrm{p}\right.$, and 3 d orbitals frozen, $4 \mathrm{~s}, 4 \mathrm{p}_{x}$ and $4 \mathrm{p}_{y}$ doubly occupied, and $4 \mathrm{p}_{z}$ active) active space is $2.7 \mathrm{~cm}^{-1}$, so it is less than $2 \%$.

Finally, it is worthwhile to stress that our CC-M approach is expected to provide reliable PESs for other atom $-\mathrm{H}_{2}$ complexes as well, which are in the entry channels of many reactions, such as $\mathrm{O}+\mathrm{H}_{2}, \mathrm{~N}+\mathrm{H}_{2}, \mathrm{~S}+\mathrm{H}_{2}$, etc. Recently, a similar approach has been successfully adapted to the van der Waals system Cl$\left({ }^{2} \mathrm{P}\right)+\mathrm{CH}_{4}{ }^{41}$ which is even more challenging. The expansion of the anisotropy of the $\mathrm{Cl}\left({ }^{2} \mathrm{P}\right)+\mathrm{CH}_{4}$ system was done in spherical harmonics adapted to the tetrahedral symmetry of the problem.

Acknowledgment. M.M.S. and G.C. thank the National Science Foundation (Grant No. CHE-0078533) for its support.

International collaboration was supported by NATO through the Linkage Grant CRG.LG 974215. J.K. and G.C. acknowledge support by the Polish Committee for Scientific Research KBN (Grant 3 T09A 112 18).

## References and Notes

(1) Kłos, J.; Chałasiński, G.; Szczȩśniak, M. M. Int. J. Quantum Chem. In press.
(2) Kłos, J.; Chałasiński, G.; Szczȩśniak, M. M. J. Chem. Phys. In press.
(3) Alexander, M. H.; Manolopoulos, D. E.; Werner, H.-J. J. Chem. Phys. 2000, 113, 11084.
(4) Bian, W.; Werner, H.-J. J. Chem. Phys. 2000, 112, 220.
(5) Mielke, S. L.; Tawa, G. J.; Truhlar, D. G.; Schwenke, D. Chem. Phys. Lett. 1995, 234, 57.
(6) Mielke, S. L.; Truhlar, D. G.; Schwenke, D. J. Phys. Chem. 1995, 99, 16210.
(7) Volobuev, Y. L.; Hack, M. D.; Truhlar, D. G. J. Phys. Chem. A 1999, 103, 6255.
(8) Aquilanti, V.; Cavalli, S.; Pirani, F.; Volpi, A.; Cappelletti, D. J. Phys. Chem. A 2001, 105, 2401.
(9) Skouteris, D.; Manolopoulos, D. E.; Bian, W.; Werner, H. J.; Lai, L.-H.; Liu, K. Science 1999, 286, 1713.
(10) Loomis, R. A.; Lester, M. I. Annu. Rev. Phys. Chem. 1997, 48, 643.
(11) Marshall, M. D.; Pond, B.; Hopman, S.; Lester, M. J. Chem. Phys. 2001, 114, 7001.
(12) Nesbitt, D. J.; Leone, S. R. J. Chem. Phys 1980, 73, 6182.
(13) Takayanagi, T.; Kurosaki, Y. J. Chem. Phys 2000, 112, 7158.
(14) Krems, R. V.; Buchachenko, A. A. J. Phys. B 2000, 33, 4551.
(15) Krems, R. V.; Buchachenko, A. A.; Szczȩśniak, M. M.; Kłos, J.; Chałasiński, G. J. Chem. Phys. 2002, 116, 1457.
(16) Kłos, J.; Chałasiński, G.; Krems, R. V.; Buchachenko, A. A.; Aquilanti, V.; Pirani, F.; Cappelletti, D. J. Chem. Phys. 2002, 116, 9269.
(17) Dunning, T. H., Jr. J. Chem. Phys. 1989, 90, 1007.
(18) Kendall, R. A.; Dunning, T. H., Jr.; Harrison, R. J. J. Chem. Phys. 1992, 96, 6796.
(19) Woon, D. E.; Dunning, T. H., Jr. J. Chem. Phys. 1993, 98, 1358.
(20) Tao, F.-M.; Pan, Y.-K. J. Chem. Phys. 1992, 97, 4989.
(21) Burcl, R.; Chałasiński, G.; Bukowski, R.; Szczę̧́niak, M. M. J. Chem. Phys. 1995, 103, 1498.
(22) Cybulski, S. M.; Kendall, R. A.; Chałasiński, G.; Severson, M. W.; Szczęśniak, M. M. J. Chem. Phys. 1997, 106, 7731.
(23) Kendall, R. A.; Chałasiński, G.; Kłos, J.; Bukowski, R.; Severson, M. W.; Szczȩśniak, M. M.; Cybulski, S. M. J. Chem. Phys. 1998, 108, 3235.
(24) Cybulski, S. M.; Burcl, R.; Chałasiński, G.; Szczȩśniak, M. M. J. Chem. Phys. 1995, 103, 10116.
(25) Cybulski, S. M.; Toczyłowski, R. J. Chem. Phys. 1999, 111, 10520.
(26) MOLPRO is a package of ab initio programs written by H.-J. Werner and P. J. Knowles, with contributions from R. D. Amos, A. Bernhardsson, A. Berning, P. Celani, D. L. Cooper, M. J. O. Deegans, A. J. Dobbyn, F. Eckert, C. Hampel, G. Hetzer, T. Korona, R. Lindh, A. W. Lloyd, S. J. McNicholas, F. R. Manby, W. Meyer, M. E. Mura.; Nicklass, A.; Pitzer, P. P. R.; Rauhut, G.; Schütz, M.; Stoll, H.; Stone, A. J.; Tarroni, R.; Thorsteinsson., T.
(27) Boys, S. F.; Bernardi, F. Mol. Phys. 1970, 19, 553.
(28) Chałasiński, G.; Szczȩśniak, M. M. Chem. Rev. 1994, 94, 1723.
(29) Chałasiński, G.; Szczȩśniak, M. M. Chem. Rev. 2000, 100, 4253.
(30) Knowles, P. J.; Hampel, C.; Werner, H.-J. J. Chem. Phys. 1993, 99, 5219.
(31) Scuseria, G. Chem. Phys. Lett. 1991, 176, 27.
(32) Rittby, M.; Bartlett, R. J. Phys. Chem. 1988, 92, 3033.
(33) Kłos, J.; Chałasiński, G.; Szczęśniak, M. M.; Werner, H.-J. J. Chem. Phys. 2001, 115, 3085.
(34) Stark, K.; Werner, H.-J. J. Chem. Phys. 1996, 104, 6515.
(35) Esposti, A. D.; Werner, H.-J. J. Chem. Phys. 1990, 93, 3351.
(36) Werner, H.-J.; Knowles, P. J. J. Chem. Phys. 1985, 82, 5053.
(37) Knowles, P. J.; Werner, H.-J. Chem. Phys. Lett. 1985, 115, 259.
(38) Werner, H.-J.; Follmeg, B.; Alexander, M. H. J. Chem. Phys. 1988, 89, 3139.
(39) Alexander, M. H. J. Chem. Phys. 1993, 99, 6014.
(40) Simah, D.; Hartke, B.; Werner, H.-J. J. Chem. Phys 1999, 111, 4523.
(41) Kłos, J. Chem. Phys. Lett. 2002, 359, 309.


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