# Theoretical Study of the Interaction of $NO_2$ Molecule with a Metal-Zeolite Model (Metal = Cu, Ag, Au)

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Theoretical calculations of the NO<sub>2</sub> adsorption on transition metal–exchanged zeolite (metal = Cu, Ag, Au) were carried out using density functional theory and MP2 approaches. A tritetrahedral model (T3) was used to represent a fragment of a zeolite. The density functional calculations predict that the NO<sub>2</sub> adsorption energy follows the order: Cu-T3 > Au-T3 > Ag-T3. The analysis of the electronic properties shows that the d<sup>10</sup>– $s^1d^9$  promotion favors the interaction between the NO<sub>2</sub> molecule and the metallic center. The results show that there is a charge transfer from the metallic ion to the NO<sub>2</sub> molecule, which produces a weakening of the N–O bond. The topology of the laplacian of the density correctly predicts the existence of the two stable isomers found in this work, but not the adsorption order.

#### Introduction

It is well known that nitrogen oxides, NO<sub>x</sub>, are air pollutants that cause photochemical smog and acid rain. Therefore, the reduction of NO<sub>x</sub> to N<sub>2</sub> is a very important process in the field of environmental catalysis. Currently, the selective catalytic reduction (SCR) of NO<sub>x</sub> with ammonia is the commercial catalytic process for NO<sub>x</sub> emission control.<sup>1–4</sup> The reduction is done with NH<sub>3</sub> using titania-supported vanadia in the presence of O<sub>2</sub>.<sup>1–4</sup> The main drawback of this process is the handling of ammonia that must be well controlled to avoid the corrosive and toxic effects. Other less aggressive processes such as SCR using hydrocarbons and metal–zeolite exchange, in which ammonia is not used, have been investigated.

From the pioneering works of Iwamoto<sup>5-11</sup> and Held et al.<sup>12</sup> on the reduction of  $NO_x$  by hydrocarbons using copper-zeolite catalysts until now, a huge number of works on this topic have been published. The Cu ion-exchanged zeolite catalysts have shown to have good catalytic activities,<sup>13</sup> and some studies have pointed out that the  $Cu^{1+}$ ,  $^{14-18,19}$  or  $Cu^{1+}$  -  $Cu^{2+1-2,20-22}$  are the active sites of these catalysts. Beside Cu, other systems have been studied too, such as Fe-ZMS-5,<sup>23-29</sup> Co-ZMS-5,<sup>2,9,29-34</sup> Au-MFI,<sup>35,36</sup> or Zn and ZnO.<sup>29,37</sup> Despite all these studies it is not clear yet, for example, which is the oxidation state or the structure of the active site of Fe-ZSM525,28 or Cu-zeolite systems.<sup>2,20,22</sup> It is clear that in real catalytic systems there are several cluster species that differ in size and in oxidation state and that are difficult to determine experimentally. Therefore, theoretical studies on adsorption modes, interaction energies, and charge distributions are useful to help to understand the molecular mechanisms of catalytic reduction of  $NO_x$  by transition metal-zeolites.

Sauer et al.<sup>18</sup> and Trout<sup>19</sup> have shown that the active site for NO<sub>2</sub> adsorption is a  $Cu^{1+}$  species in the Cu–zeolite catalysts.

Sodupe and collaborators<sup>38</sup> showed that in gas phase the NO<sub>2</sub> molecule is capable to form stable complexes with silver.  $Xu^{39}$  reported that at least three stable complexes are possible with gold. Until now, to our knowledge, no theoretical calculations have been performed yet for NO<sub>2</sub> adsorption on silver and gold ion-exchanged zeolites.

In the present work, the bonding of  $NO_2$  on metal-exchanged zeolite (metal = Cu, Ag, and Au) has been investigated by means of quantum chemical calculations. It presents the analysis of the electronic interaction as well as the analysis of the topology of the charge density for the interaction of the  $NO_2$  molecule with a model of metal ion—exchanged zeolite using ab initio density functional theory and MP2 calculations.

### **Catalyst Model**

Three different metal–zeolite (metal = Cu, Ag, and Au) systems were studied in order to analyze the binding energies and electronic properties of the NO<sub>2</sub> adsorbed on a metallic center supported over a zeolite framework. The tritetrahedral structure  $[H_3SiOAl(OH)_2OSiH_3]^-$  was chosen to model a T3 site of a zeolite, where the metallic atom, M, was set on bridge between two oxygen atoms (see Figure 1a). Similar models have been used successfully by us<sup>29</sup> and others authors<sup>18,40,41</sup> to represent one of the possible sites of the localization of the metallic ion inside the zeolite framework.

# **Computational Details**

All calculations and geometry optimizations were performed with the Gaussian 94 program<sup>42</sup> at DFT and MP2 level. For DFT, the Becke's three-parameter hybrid functional<sup>43</sup> with Lee, Yang, and Parr correlation functionals were employed.<sup>44</sup> In all cases, the unrestricted formalism (UB3LYP and UMP2) was used. The basis sets and the relativistic compact effective potentials that include explicitly the  $(n-1)s^2$ , (n-1)p,<sup>6</sup> (n-1)-

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Figure 1. Schematic representation of the molecular structures used in this work. The O1 atoms are localized along the y axis. The Al and M atoms are in the z axis. (a) M-T3 site (M = Cu, Ag, Au). (b)  $NO_2M$ -T3 structure.

 $d_x$ , and  $(n)s_y$  electrons from Stevens et al.<sup>45</sup> were used for Cu, Ag, and Au atoms. For N and O, the all-electron 6-311G(d, p) basis set was employed. The 6-31G(d, p) basis set was applied to Al, Si, and H atoms. The electronic charge distribution of the catalyst models was analyzed using the natural bond orbital (NBO) partition scheme,<sup>46,47</sup> and the topological properties of the electronic density laplacian was analyzed using the Bubble program. The T3 model (Figure 1a) has a  $C_{2v}$  symmetry and the NO<sub>2</sub>M–T3 complexes  $C_2$  symmetries (Figure 1b). Only neutral complexes were considered in this work.

## **Theoretical Background**

In the topological theory of Bader "Atoms in a Molecule" (AIM),<sup>48-50</sup> the chemical bonds and molecular reactivity is interpreted in terms of the total molecular electronic density,  $\rho(r)$ , and its corresponding laplacian,  $\nabla^2 \rho(r)$ . The values of  $\rho(r)$  and the  $\nabla^2 \rho(r)$  at the bond critical point (bcp) allow the characterization of the chemical bonds of the atoms in the molecules. According to the AIM theory,  $\nabla^2 \rho(r)$  provides information concerning electronic charge.  $\nabla^2 \rho(r) > 0$  (or  $-\nabla^2 \rho$ -(r) < 0 implies locally depleted charge while, on the contrary,  $\nabla^2 \rho(r) < 0$  (or  $-\nabla^2 \rho(r) > 0$ ) signifies locally concentrated charge.48-49 Thus, classical covalent bonds or shared interactions have values at the bcp of  $\nabla^2 \rho_{bcp} < 0$  and  $\rho_{bcp}$  large, while classical ionic bonds (closed-shell interactions) have  $\nabla^2 \rho_{\rm bcp} >$ 0 and  $\rho_{\rm bcp}$  low. Intermediate bonds are associated with  $\nabla^2 \rho_{\rm bcp}$ > 0 and  $\rho_{bcp}$  medium or large, i.e.; values between shared and closed-shell. On the other hand, Cremer and Kraka<sup>51,52</sup> have shown that for covalent and intermediate bonds the energy density  $H_{bcp}$  has negative values. Another parameter used to describe a bond is the ellipticity  $(\epsilon)$  that shows if the electronic charge is preferentially accumulated in a given direction between two bonded atoms. Sigma bonds have  $\epsilon = 0$ , while double or  $\pi$  bonds, in general, have  $\epsilon > 0$ . Beside the bcp there is another type of critical point (cp) called the ring cp, which is present in ring structures such as benzene, thiophene, etc. It has been proposed<sup>53</sup> that there is a correlation between the interaction energies of some compounds and either  $\rho(r)$  or  $\nabla^2 \rho(r)$  at the ring cp.

The molecular reactivity in the AIM theory is related to the topology of  $-\nabla^2 \rho(r)$  at the outer valence shell of charge concentration (OVSCC), i.e, with the type and number of critical points of  $-\nabla^2 \rho(r)$ . In the OVSCC,  $\rho(r)$  is maximally concentrated and the distribution of  $-\nabla^2 \rho(r)$  over this surface is, in general, uniform for free atoms. In a molecule, the formation

TABLE 1: Geometry, Charges, Electronic Configuration, and Energy Difference for M-T3(X) Systems (M = Cu, Ag, Au; X = S Singlet, T = Triplet)

method	molecular system	M–O1 Å	angle O1-M-O1	Q <sub>M</sub>	total spd configuration	$rac{\Delta E^a}{\mathrm{eV}}$
B3LYP	Cu-T3(S) <sup>b</sup>	2.00	83.2	+0.88	sp <sup>0.18</sup> d <sup>9.94</sup>	
B3LYP	Cu-T3(T)	1.98	78.7	+0.74	sp <sup>1.09</sup> d <sup>9.17</sup>	+1.71 (+ 2.42)
B3LYP	Ag-T3(S)	2.27	73.0	+0.87	sp <sup>0.16</sup> d <sup>9.97</sup>	,
B3LYP	Ag-T3(T)	2.24	71.4	+0.46	sp <sup>1.06</sup> d <sup>9.48</sup>	+2.88 (+4.84)
<b>B3LYP</b>	Au-T3(S)	2.27	72.4	+0.78	sp <sup>0.30</sup> d <sup>9.92</sup>	
B3LYP	Au-T3(T)	2.25	71.0	+0.51	sp <sup>1.16</sup> d <sup>9.33</sup>	+1.34 (+2.40)
MP2	Cu-T3(S)	1.99	82.6	+0.90	sp <sup>0.28</sup> d <sup>9.82</sup>	
MP2	Cu-T3(T)	1.96	79.7	+0.86	sp <sup>1.16</sup> d <sup>8.98</sup>	+2.70 (+4.08)
MP2	Ag-T3(S)	2.27	72.3	+0.96	sp <sup>0.12</sup> d <sup>9.92</sup>	
MP2	Ag-T3(T)	2.12	73.7	+0.70	sp <sup>1.12</sup> d <sup>9.18</sup>	+3.69 (+5.39)
MP2	Au-T3(S)	2.25	72.3	+0.90	sp <sup>0.24</sup> d <sup>9.86</sup>	. ,
MP2	Au-T3(T)	2.17	72.2	+0.68	sp <sup>1.22</sup> d <sup>9.10</sup>	$^{+1.52}_{(+2.64)}$

<sup>*a*</sup> Values in parentheses correspond to the transition:  $M^{+1}(\text{singlet}) \rightarrow M^{+1}(\text{triplet})$  for a single atom. Experimental values: Cu 2.72 eV [64], Ag 4.85 eV [65], Au 1.86 eV [65]. <sup>*b*</sup> Data from ref 29.

of bonds produces change in the atomic  $-\nabla^2 \rho(r)$ , and local maxima, minima, and saddle points appear. There are two important types of critical points of  $-\nabla^2 \rho(r)$  at the OVSCC: maxima or charge concentrations (cc) and saddle points or electronic holes. The saddle points represent local charge depletions (cd) that are associated with electrophilic sites susceptible to nucleophile attack, while the maxima or cc are associated with the nucleophilic sites susceptible to attack by electrophiles. Thus, the acid—base reaction corresponds to the alignment of a charge concentration in the OVSCC of the base with a charge depletion, or hole, on the acid.<sup>48,49,54</sup>

#### **Results and Discussion**

Table 1 shows the geometrical properties and the electronic configuration of the M–T3 structures (M= Cu, Ag, and Au) for two spin states (singlet and triplet). In general both methodologies, UB3LYP and UMP2, produce qualitatively the same results. The distance M–O (M–O1, Figure 1a) is shorter for the triplet state than for the singlet, and the positive charge on the metal is greater for the singlet than for the triplet, indicating that one electronic transfer from the metal to the T3 site occurs. The analysis of the electronic configuration of the

TABLE 2: Geometries, Binding Energies ( $\Delta E$ ), and NBO Electronic Populations for NO<sub>2</sub> Metal-T3 Systems [Normal Mode (NO<sub>2</sub>MT3||)]

molecular	M-O1	angle	N-O3	ang	le	O3-M	$\Delta E$ (kcal/mol)
system	(Å)	O1-M-O1	(Å)	O3–N	-O3	(Å)	
$\begin{array}{c} NO_{2}Cu-T3^{a}\\ NO_{2}Ag-T3\\ NO_{2}Au-T3\\ NO_{2}\\ NO_{2}^{(-1)}\\ \end{array}$	1.94 2.17 2.19	80.6 73.2 72.0	1.26 1.26 1.26 1.19 1.26	110 111 112 134 116	.9 .7 .5 .2 .8	2.02 2.23 2.25	-43.2 -7.2 -27.0
	Q <sub>NO2</sub>	Q <sub>metal</sub>	d <sub>xy</sub>	$d_{xz}$	d <sub>yz</sub>	$d_{x^2-y^2}$	$d_{z^2}$
NO <sub>2</sub> Cu-T3 <sup>a</sup>	-0.60	+1.33	2.00	1.99	1.31	1.98	1.98
NO <sub>2</sub> Ag-T3	-0.50	+1.12	2.00	1.99	1.55	1.99	1.97
NO <sub>2</sub> Au-T3	-0.47	+1.06	2.00	1.99	1.44	1.98	1.93

<sup>a</sup> Data from ref 29.

TABLE 3: Geometries, Binding Energies ( $\Delta E$ ), and NBO Electronic Populations for NO<sub>2</sub>Metal-T3 Systems [Perpendicular Mode (NO<sub>2</sub>MT3 $\perp$ )

molecular system	M-O1 (Å)	angle O1-M-O1	N-O3 (Å)	ang O3-N	gle I-O3	O3-M (Å)	$\Delta E$ (kcal/mol)
$NO_2Cu - T3^a$	2.00	79.5	1.26	109	).9	2.00	-27.9
$NO_2Ag-T3$	2.26	71.5	1.26	109	9.4	2.25	+7.8
$NO_2Au - T3$	2.27	69.7	1.26	110	).1	2.23	-7.0
	Q <sub>NO2</sub>	Q <sub>metal</sub>	d <sub>xy</sub>	$\mathbf{d}_{xz}$	$d_{yz}$	$d_{x^2-y^2}$	$d_{z^2}$
$NO_2Cu - T3^a$	-0.55	+1.34	2.00	1.30	1.98	2.00	1.98
NO <sub>2</sub> Ag-T3	-0.35	+1.07	2.00	1.65	1.98	2.00	1.97
NO <sub>2</sub> Au-T3	-0.38	+1.07	2.00	1.49	1.96	1.99	1.93

<sup>a</sup> Data from ref 29.

metal shows that in the singlet state the metal has an  $nd^{10}$  configuration, while for the triplet, one d electron is promoted to the empty (n+1)s orbital. This promotion reduces the electron–electron repulsion between the electrons of the metal and the electrons of the support reducing therefore, the M–O1 distance.

For the cases presented in Table 1, the transition or promotion energy  $nd^{10} \rightarrow nd^9(n+1)s^1$  (singlet to triplet) is lower for the metallic atom anchored on the zeolite than for a single M<sup>+</sup> gasphase ion. According to the values reported in Table 1, the B3LYP methodology reproduces better the experimental values of the transition energy  $M^{+1}(nd^{10}) \rightarrow M^{+1}((n+1)s^{1}nd^{9})$  than does the MP2 approach. This result agrees with the well-known fact that for some transition metals the energies calculated at MPn level are often no reliable.55,56 For example, for Fe-Cu the Møller-Plesset perturbation energy does not converge and shows large oscillations.<sup>56,57</sup> Our value of 1.7 eV for Cu-T3 is in good agreement with the value reported by Sauer et al.18 The stabilization of the triplet state by the zeolitic framework is due, in part, to the fact that the  $nd^{9}(n+1)s^{1}$  promotion reduces the electron-electron repulsion between the metal d electrons and the electrons of the oxygens. Therefore, the electrostatic attraction between the M<sup>+</sup> ion and the T3 site increases, stabilizing the triplet sate and reducing the energy gap.

In both methodologies, DFT and MP2, the highest and the lowest energy gap correspond to the Ag and Au atoms, respectively. Nachtigall, Nachtigallová, and Sauer<sup>41</sup> showed that the values of vertical  $T_1 \leftarrow S_0$  excitation energy as well as the vertical  $S_0 \leftarrow T_1$  emission energy for Cu<sup>+</sup>-zeolite systems depend on the size of the cluster model. Nevertheless, the spread of the values does not exceed the amount of 0.2 eV. Then we expect that the error in our calculations due to the cluster size used be small. Therefore, we can conclude, according to our results, that is easier to produce an electronic excitation on Auexchanged zeolites than in Cu- or Ag-exchanged zeolites.

Table 2 shows the geometrical properties as well as the

calculated binding energy for the normal (NO<sub>2</sub>M-T3||) adsorption mode of the NO<sub>2</sub> on M-T3 systems (M = Cu, Ag, Au), and Figure 1b displays a schematic representation of the structure of these complexes. In these structures the NO<sub>2</sub> molecule is parallel to the plane O1-Al-O1. All values reported herein for the NO<sub>2</sub>M-T3 complexes were obtained using the B3LYP approach.

From the analysis of Table 2 it is clear that the interaction of NO<sub>2</sub> with the metallic atom produces an enlargement of the N-O distance (N-O3) from 1.19 to 1.26 Å and a reduction of the natural angle (O3-N-O3) of the NO2 molecule. The geometrical parameters of the adsorbed NO<sub>2</sub> are closer to the free ion  $NO_2^-$  than to the  $NO_2$  free molecule, which is an indication of a charge transfer from the metal to the NO<sub>2</sub> molecule. The charges and NBO population analysis show that after the interaction of the NO<sub>2</sub> molecule with the M-T3 system, the metallic atom has a d<sup>9</sup> configuration with a high positive charge (+1.33e, +1.12e, +1.06e for M = Cu, Ag, andAu, respectively) with the unpaired electron localized in the  $nd_{yz}$  orbital; while the NO<sub>2</sub> is negatively charged. This charge transfer increases the electrostatic interactions of the metal with the negatively charged zeolite, reducing the M-O1 distance and stabilizing the ion. Although there is a charge transfer from the M-T3 system to the NO<sub>2</sub> molecule, calculations with diffuse functions were not performed because previous work<sup>29</sup> showed that neither geometry nor calculated binding energies change significantly when these functions are used.

Table 3 shows the geometrical properties as well as the calculated binding energy for the perpendicular adsorption mode (NO<sub>2</sub>M-T3 $\perp$ ). In these structures the NO<sub>2</sub> molecule is perpendicular to the plane O1-Al-O1 and parallel to the plane O2-Al-O2. Again, there is a charge transfer from the metal to the NO<sub>2</sub> molecule and an enlargement of the N-O3 distance and the NBO analysis show that the metal unpaired electron is localized in the *nd*<sub>xz</sub> orbital.

TABLE 4: Topological Properties of the Electronic Density<sup>*a*</sup> of M-T3 and NO<sub>2</sub>M-T3 Complexes (M = Cu, Ag, Au)

molecular						
system	bond	cp type <sup>b</sup>	$ ho_{ m cp}$	$H_{\rm cp}$	$ abla^2  ho_{ m cp}$	$\epsilon$
Cu-T3 <sup>c</sup>	Cu-01	bcp	0.0758	-0.0168	0.3865	0.0164
	Cu-O1	bcp	0.0859	-0.0184	0.4313	0.0271
NO <sub>2</sub> CuT3	Cu-O3	bcp	0.0752	-0.0158	0.3266	0.1021
	N-03	bcp	0.4578	-0.5708	-1.012	0.0841
		ring	0.0441		0.2741	
	Cu-01	bcp	0.0760	-0.0164	0.3741	0.0544
NO₂CuT3⊥	Cu-O3	bcp	0.0791	-0.0168	0.3492	0.1477
	N-03	bcp	0.4566	-0.5694	-1.012	0.0886
		ring	0.0455		0.2929	
Ag-T3	Ag-O1	bcp	0.0572	-0.0036	0.2790	0.0389
	Ag-01	bcp	0.0696	-0.0057	0.3284	0.0276
NO <sub>2</sub> Ag T3	Ag-03	bcp	0.0640	-0.0045	0.2764	0.1124
	N-03	bcp	0.4603	-0.5782	-1.025	0.0859
		ring	0.0372		0.2088	
	Ag-O1	bcp	0.0585	-0.0036	0.2902	0.0208
NO₂AgT3⊥	Ag-O3	bcp	0.0613	-0.0035	0.2673	0.1420
	N-03	bcp	0.4600	-0.5799	-1.033	0.0921
		ring	0.0367		0.1954	
Au-T3	Au-O1	bcp	0.0647	-0.0055	0.2981	0.0433
	Au-O1	bcp	0.0780	-0.0108	0.3345	0.0292
NO <sub>2</sub> AuT3	Au-O3	bcp	0.0712	-0.0076	0.2835	0.1355
	N-03	bcp	0.4653	-0.5916	-1.055	0.0872
		ring	0.0397		0.2387	
	Au-O1	bcp	0.0655	-0.0057	0.3034	0.0139
NO <sub>2</sub> AuT3⊥	Au-O3	bcp	0.0737	-0.0079	0.2979	0.1844
	N-03	bcp	0.4629	-0.5884	-1.055	0.0961
		ring	0.0410		0.2451	

<sup>*a*</sup> Values in atomic units. $\rho_{cp}$  electronic density at the cp;  $H_{cp}$  energy density at the cp;  $\nabla^2 \rho_{cp}$  laplacian of  $\rho(r)$  at the cp.  $\epsilon$  bond ellipticity. <sup>*b*</sup> bcp correspond to a (3, -1) cp; ring type to a (3, +1) cp. <sup>*c*</sup> Data from ref 29.

The proposed mechanisms<sup>18</sup> to explain the interaction of NO<sub>2</sub> with the metal indicate that the promotion  $nd^{10} \rightarrow nd^9(n+1)s^1$ is necessary. In the excited state, d9s1, the interaction is done using the s electron of the metal, therefore the unpaired electron must be localized in the d orbitals. For the NO<sub>2</sub>M-T3|| complexes, the unpaired electron is localized in the  $nd_{yz}$  orbital (see Table 2), while for the NO<sub>2</sub>M $-T3\perp$  the electron is in the  $nd_{rr}$  orbital (see Table 3). These results indicate that the promotion must occur in the d orbital that diminishes the electron-electron repulsion between the d electrons of the metallic center and the electrons of the oxygen atoms that belong to the  $NO_2$  molecule. As a matter of fact, the adsorption energy correlates with the electronic population in the  $nd_{yz}$  orbital for the NO<sub>2</sub>M-T3|| complexes while for NO<sub>2</sub>M-T3 $\perp$  the correlation is with the  $nd_{xz}$  electronic population, i.e., greater  $nd_{yz}$  or nd<sub>xz</sub> population lowers adsorption energy. Since in the perpendicular mode the  $nd_{yz}$  orbital is doubly occupied (see Figure 1b), there is a strong electronic repulsion between the  $nd_{yz}$  and the oxygen electrons of the zeolite (atoms O1). This repulsion destabilizes the absorption. Therefore, the binding energies for the NO<sub>2</sub>M $-T3\perp$  are lower than the corresponding to the NO<sub>2</sub>M-T3||. The second factor related to the adsorption process is the charge transfer from the metal to the NO<sub>2</sub> molecule. The easier this charge transfer is, the more favored the adsorption process will be. This explains the fact that the binding energy order correlates with the inverse ionization potential order of the M<sup>+</sup> cation; i.e., the binding energy follows the sequence Cu-T3 (IP = 20.3 ev)<sup>58</sup> > Au-T3 (IP = 20.5 ev)<sup>59</sup> >  $Ag-T3(IP = 21.5 \text{ ev}).^{59}$ 

The topological properties of the molecular electronic density  $\rho$  at the bcp, (see Table 4 and Figure 2) show that the interaction between the transition metal (Cu, Ag, and Au) and the oxygen



**Figure 2.** Schematic representation of the position of the critical points (cp) of the electronic density of the NO<sub>2</sub>M-T3 structures (M = Cu, Ag, Au). NO<sub>2</sub> is in the plane of the Al and the O1 atoms.

atoms can be classified as closed-shell or intermediate interaction. The molecular electronic density at the bcp ( $\rho_{bcp}$ ) is low, the lapacian  $(\nabla^2 \rho_{bcp})$  is positive, but the energy density  $H_{bcp}$ has a negative value. Published results<sup>58–61</sup> show that, in general, the metal-oxygen interaction is characterized by positive values of  $\nabla^2 \rho_{bcp}$  and  $\epsilon$ . The high  $\epsilon$  values for M–O3 bonds suggest a strong  $\pi$  contribution in this bond. The values of  $\nabla^2 \rho$  and  $\rho$  at the ring cp predict that for NO<sub>2</sub>M-T3|| and NO<sub>2</sub>M-T3 $\perp$ complexes the order of the interaction energy is  $NO_2Cu-T3$  $> NO_2Au-T3|| > NO_2Ag-T3||$  and  $NO_2Cu-T3\perp > NO_2-T3$ Au-T3 $\perp$  >NO<sub>2</sub>Ag-T3 $\perp$ . This is the same order obtained from the calculated binding energies reported in Tables 2 and 3. The trend given by the  $\nabla^2 \rho$  values or  $\rho$  at the ring cp is valid only for the same type of complex; as a matter of fact, the  $\nabla^2 \rho$  and  $\rho$  for NO<sub>2</sub>Cu-T3 $\perp$  are greater than for NO<sub>2</sub>Cu-T3|| ( $\nabla^2 \rho$  = 0.2929 au and  $\nabla^2 \rho = 0.2741$  au;  $\rho = 0.0455$  au and  $\rho = 0.0441$ au, respectively) but the binding energy is greater for NO<sub>2</sub>Cu-T3|| than for NO<sub>2</sub>Cu-T3 $\perp$ .

For the M–O3 bonds in the NO<sub>2</sub>M–T3 structures (see Table 4), the electronic density  $\rho_{bcp}$  correlates with the binding energies only if the same type of complex is used, i.e., greater  $\rho_{bcp}$  values correspond to greater binding energies. However, there is not correlation if the values of NO<sub>2</sub>M–T3|| and NO<sub>2</sub>M–T3 $\perp$  are used in conjunction. For example, for M = Cu and Au,  $\rho_{bcp}$ (NO<sub>2</sub>M–T3 $\perp$ ) >  $\rho_{bcp}$ (NO<sub>2</sub>M–T3||) but the binding energy  $\Delta E$ (NO<sub>2</sub>M–T3 $\perp$ ) <  $\Delta E$ (NO<sub>2</sub>M–T3||). This shows that there is not a general correlation between  $\rho_{bcp}$  and  $\Delta E$ .

In the case of the NO<sub>2</sub> and NO<sub>2</sub><sup>-</sup> free molecules (see Figure 3), the topological properties of the N–O bond correspond to a shared interaction. The positive values of  $\epsilon$  can be rationalized considering that the HOMO orbital of these molecules has a strong contribution of the  $p_z$  atomic orbital of the N and the O atoms and therefore some  $\pi$  character is present in the N–O bond. Due to the charge transfer from the metal to the NO<sub>2</sub> molecule, the topological properties of the N–O3 bond in the NO<sub>2</sub>M–T3 complexes are similar to the properties of the NO<sub>2</sub> free molecule. The increasing of the N–O bond length in the final complexes NO<sub>2</sub>M–T3 (see Tables 2 and 3) results in the electronic density as well as the degree of local charge concentration ( $\nabla^2 \rho$  <sub>bcp</sub>) being lower than in the NO<sub>2</sub> free molecule and closer to the NO<sub>2</sub><sup>-</sup> free molecule.



**Figure 3.** Schematic representation of the position of the critical points of the electronic density and the values of the topological parameter of the  $NO_2^-$  ion (top) and the  $NO_2$  neutral molecule (bottom).



**Figure 4.** Schematic representation of the positions of the local charge concentrations (lcc's) and the values of  $-\nabla^2 \rho$  at these points for the NO<sub>2</sub> molecule.

Figure 4 shows the geometric distribution of the local charge concentrations and the values of  $-\nabla^2 \rho$  at these points for the NO<sub>2</sub> molecule. The OVSCC of the N atom presents three lcc's, two of them in the N–O bond direction, while the oxygen atoms have two lcc's outside the bond area N–O. On the other hand, the M–T3 aggregate shows four lcd's as displayed in Figure 5 and whose values are reported in Table 5. Therefore, it is clear that the reaction of NO<sub>2</sub> with M–T3 corresponds to the alignment of the NO<sub>2</sub> lcc's with the M–T3 lcd's. The values of  $-\nabla^2 \rho$  at the lcd points of the metallic atoms  $(-\nabla^2 \rho_L, -\nabla^2 \rho_X,$  see Table 5) correctly predict the stability of the isomers, i.e.,  $-\nabla^2 \rho_L (NO_2M-T3||) > -\nabla^2 \rho_X (NO_2M-T3\perp)$  and  $\Delta E(NO_2M-T3||) > \Delta E(NO_2Au-T3||) > \Delta E(NO_2Au-T3||)$ .

### Conclusions

The geometric parameters, electronic structures, binding energies, and topological properties of the charge distribution have been determined for the M–T3 and NO<sub>2</sub>M–T3 systems (M = Cu, Ag, and Au). The results show that the strongest



**Figure 5.** Schematic representation of the position of the local charge depletions, (lcd's),  $\nabla^2 \rho_L$ , and  $\nabla^2 \rho_X$  in the M–T3 structures (M = Cu, Ag, and Au).

TABLE 5: Values<sup>*a*</sup> of  $-\nabla^2 \rho$  and  $\rho$  at the Critical Points of  $-\nabla^2 \rho$  at the Valence Shell of the Metal for the M-T3 Complexes (M= Cu, Ag, Au)

	cp type <sup>b</sup>	$ ho_{ m L}$	$-\nabla^2  ho_L$	$ ho_{\mathrm{X}}$	$-\nabla^2  ho_{\mathrm{X}}$
Cu-T3	lcd	6.809	126.748	6.624	117.669
Ag-T3	lcd	2.183	30.122	2.168	29.547
Au-T3	lcd	1.634	20.794	1.598	19.549

<sup>*a*</sup> In atomic units. <sup>*b*</sup> The lcd type corresponds to (3, +1) cps.

NO<sub>2</sub> interaction corresponds to the Cu atom, while the weakest corresponds to Ag. As a matter of fact, for the perpendicular mode there is not adsorption over the Ag-T3 system. The coordination of NO<sub>2</sub> through the two oxygen atoms to the metallic center was found to be the most stable one, while other coordination modes were found to be less stable. This agrees with previous works<sup>18,38,39,62,63</sup> which show that, in general, the  $\eta^2$ –O,O structure is the most stable one when the NO<sub>2</sub> binds to a metallic ion in a zeolite framework. The lengthening of the N-O bond of the adsorbed NO<sub>2</sub> molecule can be explained in terms of the charge transfer from the M-T3 complex to the nitrogen dioxide. After the interaction, the resulting charge transfer goes to an antibonding NO<sub>2</sub> orbital, weakening the N-O bond. As a matter of fact, the geometrical as well the topological properties of the charge density of the adsorbed NO2 are closer to the  $NO_2^-$  than to the NO<sub>2</sub> free molecule. In addition to this, the increases in the positive charge on the metal favors the electrostatic interactions between the metal and the negatively charged zeolite, therefore reducing the metal-O(ZSM-5) distance.

The bonding mechanism proposed by Sauer et al.<sup>18</sup> explains the interaction of NO<sub>2</sub> with Cu<sup>1+</sup>, Ag<sup>1+</sup>, and Au<sup>1+</sup>. The topology of the laplacian of the electronic density correctly predicts the existence of the two stable isomers found for the NO<sub>2</sub>M–T3 systems but not the trend in the binding energy. The binding energy correlates with the values of  $\nabla^2 \rho$  and  $\rho$  at the ring critical point.

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