

# Structures and Stabilities of Endo- and Exohedral Dodecahedrane Complexes ( $X@C_{20}H_{20}$ and $XC_{20}H_{20}$ , $X = H^+, H, N, P, C^-, Si^-, O^+, S^+$ )

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B3LYP/6-31G\* computations predict the relative energies and stabilities of the endohedral ( $X@C_{20}H_{20}$ ) and exohedral ( $XC_{20}H_{20}$ ) dodecahedrane complexes ( $X = H^+, H, N, P, C^-, Si^-, O^+, S^+$ ).  $H^+$  does not bind endohedrally but bridges a C–C bond exohedrally; the proton affinity is 185.3 kcal/mol. Except for  $O^+$ , all other guest species ( $H, N, P, C^-, Si^-, S^+$ ) are minima at the cage center. The H-atom inclusion energy is similar to that of helium (36.3 vs 38.0 kcal/mol), whereas the other endohedral complexes have much higher inclusion energies (125–305 kcal/mol). In all cases, the endohedral complexes are energetically less favorable than their exohedral isomers.  $C_{20}H_{21}$  has a cage-ruptured structure, whereas N, P, and their isoelectronic analogues have exohedral structures and bind as doublet states to broken cage C–C bonds. Endohedral H, N,  $C^-, O^+$ , and  $S^+$  preserve their unencapsulated ground states, whereas P and  $Si^-$  interact strongly with the cage and lose their atomic ground-state character.

## Introduction

Dodecahedrane (**1**,  $C_{20}H_{20}$ ),<sup>1</sup> a fascinating molecule with unusually high symmetry ( $I_h$ ), has been studied at various levels of theory with regard to the energy,<sup>2,3</sup> vibrational frequencies,<sup>4</sup> inelastic neutron-scattering spectrum,<sup>5</sup> substituent effects,<sup>6</sup> and charge density.<sup>7</sup> The synthesis of **1**, a difficult challenge, was first achieved by Paquette<sup>8</sup> and later by Prinzbach<sup>9</sup> using improved routes. The availability of **1** enabled chemical and physical studies on its thermochemistry, strain energy,<sup>10</sup> and C–H bond dissociation energy.<sup>11</sup> Dodecahedranes' "outside chemistry" has been investigated intensively,<sup>12</sup> with its high-voltage dehydrogenation into  $C_{20}$ ,<sup>13</sup> the smallest fullerene, the most dramatic experiment reported to date. The "inside chemistry" of **1** exploits its cage structure, and the possible encapsulation of various guest atoms and ions has been investigated.<sup>3a,b,14,15</sup> A helium atom has been "shot" into **1** to obtain stable  $He@C_{20}H_{20}$ <sup>16</sup> by using an experimental procedure developed for fullerenes.<sup>17</sup> This encapsulated species is fascinating because the steric compression within the cavity is severe and the barrier to penetrating intact **1** must be very high. Following earlier theoretical investigations, Schleyer et al.<sup>15c</sup> recently computed the structures and stabilities of 14 different endohedral dodecahedrane complexes ( $X@C_{20}H_{20}$ ,  $X = H, He, Ne, Ar, Li^{0/+}, Be^{0/+2+}, Na^{0/+}, Mg^{0/+2+}$ ). Helium encapsulation

(37.9 kcal/mol) was  $\sim 2$  kcal/mol less favorable than hydrogen encapsulation (35.8 kcal/mol) but  $> 12$  kcal/mol better than the next most stable endohedral dodecahedrane complex,  $Li@C_{20}H_{20}$  (50.6 kcal/mol).

Recently, endohedral fullerenes whose dopant atoms retain their isolated atomic states received attention, partly because of newly proposed solid-state quantum computers based on such materials.<sup>18</sup> Experimentally,  $C_{60}$ -encapsulated tritium,<sup>19</sup> nitrogen,<sup>20</sup> and phosphorus<sup>21</sup> have already been successfully prepared. Similarly, atomic hydrogen encapsulated in fully deuterated **1** ( $C_{20}D_{20}$ ) also has been proposed for use as single quantum bits (qubits) in solid-state quantum computers.<sup>18d</sup> Theoretical calculations have predicted that it may be possible to implant H atoms within the surface layer of fullerene molecules.<sup>22</sup>

The previous investigations into endohedral complexes of **1** have left many questions unanswered. As a cage hydrocarbon, to what extent does **1** bind a proton? Can neutral atoms such as H, N, P, and their isoelectronic charged analogues ( $C^-, Si^-, O^+, S^+$ ) also reside at the center of **1**? What are their electronic states when encapsulated in **1**? Is it possible to use these endohedrally doped dodecahedrane complexes as solid-state quantum bits? This paper addresses these questions by computing the structures and stabilities of endohedral  $X@C_{20}H_{20}$  ( $X = H^+, H, N, P, C^-, S^-, O^+, S^+$ ) complexes and their exohedral isomers.

## Computational Details

All calculations were carried out at the (U)B3LYP/6-31G\* density functional level of theory using Gaussian 98.<sup>23</sup> Guest atoms or ions were placed at the cage centers ( $I_h$ ) of endohedral

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**TABLE 1: B3LYP/6-31G\* Optimized Endohedral Complex ( $I_h$ ) Absolute Energies (au), Zero-Point Energies (ZPE; kcal/mol, unscaled), Lowest Vibrational Frequencies ( $\omega_1$ ;  $\text{cm}^{-1}$ ) (or Imaginary Frequencies) and Optimized Bond Lengths (Å)**

	energy	ZPE	$\omega_1$	$R_{C-X}$	$R_{C-C}$	$R_{C-H}$
$C_{20}H_{20}$	-774.18503	225.59	479.1	2.181	1.557	1.095
$H^+@C_{20}H_{20}$	-774.29342	213.82	-1251.6i(12) <sup>a</sup>	2.191	1.564	1.093
$^2H@C_{20}H_{20}$	-774.63243	228.77	490.4	2.189	1.562	1.096
$^4N@C_{20}H_{20}$	-828.56724	223.89	480.2	2.218	1.583	1.097
$^4P@C_{20}H_{20}$	-1114.94712	214.40	349.3	2.253	1.608	1.105
$^4C^-@C_{20}H_{20}$	-811.83448	219.15	511.7	2.211	1.578	1.110
$^4Si^-@C_{20}H_{20}$	-1063.07519	206.44	313.6	2.238	1.597	1.122
$^4O^+@C_{20}H_{20}$	-848.75284	217.80	-282.7i(3) <sup>a</sup>	2.216	1.582	1.094
$^4S^+@C_{20}H_{20}$	-1171.60325	218.32	347.6	2.261	1.614	1.095

<sup>a</sup> Higher-order saddle point, with the number of imaginary frequencies given in parentheses.

**TABLE 2: B3LYP/6-31G\* Endohedral Complex Inclusion Energies ( $E_{inc}$ ; kcal/mol), Natural Charges ( $q$ ), and Spin Densities ( $S$ )**

	$E_{inc}$	$q_X$	$q_C$	$q_H$	$S_X$	$S_{Cn}^a$	$S_H$
empty $C_{20}H_{20}$			-0.25	0.25			
$H^+@C_{20}H_{20}$	-79.6	0.79	-0.29	0.30			
$^2H@C_{20}H_{20}$	36.3	0.08	-0.25	0.25	0.91	0.00	0.01
$^4N@C_{20}H_{20}$	125.3	-0.05	-0.25	0.25	2.57	0.00	0.02
$^4P@C_{20}H_{20}$	300.3	1.07	-0.29	0.24	1.73	0.01	0.06
$^4C^-@C_{20}H_{20}$	115.9	-0.36	-0.24	0.21	2.12	0.00	0.05
$^4Si^-@C_{20}H_{20}$	305.2	1.52	-0.31	0.19	0.93	0.02	0.09
$^4O^+@C_{20}H_{20}$	-21.0	0.46	-0.26	0.29	2.23	0.02	0.02
$^4S^+@C_{20}H_{20}$	182.22	0.88	-0.28	0.29	2.06	0.01	0.03

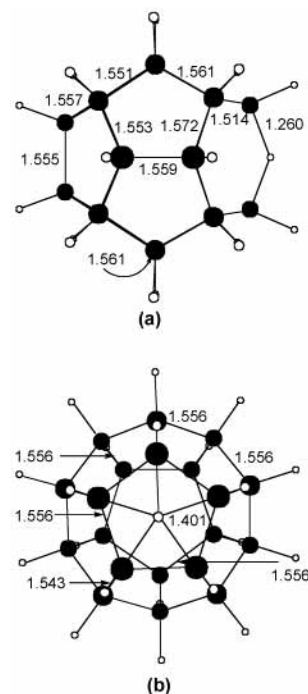
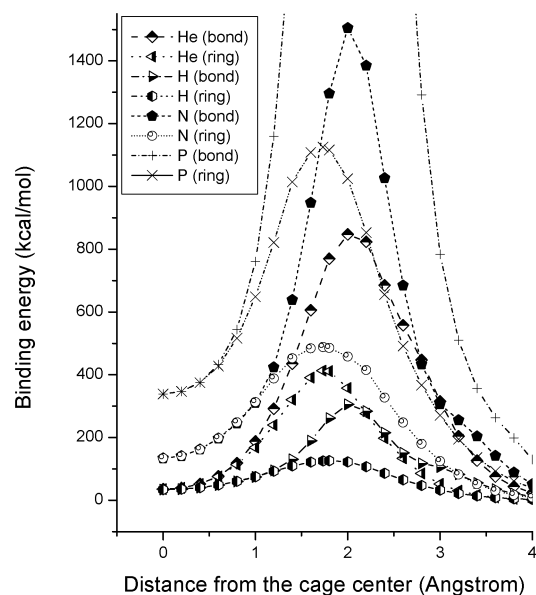
<sup>a</sup> The spin density of the carbon neighboring X (as shown in Figure 2).

complexes, and skeletally bonded  $C_{2v}$  and  $C_s$  symmetries were used for their exohedral isomers. Optimized structures were characterized by frequency calculations as energy minima (zero imaginary frequencies;  $N_{imag} = 0$ ) or saddle points ( $\geq 1$  imaginary frequency;  $N_{imag} \geq 1$ ). Mode following and optimization were used to locate the corresponding minima when imaginary frequencies were encountered. Zero-point energies (ZPE), derived from the vibrational frequency analysis of equilibrium geometries, were scaled by 0.9804. Atomic charges were evaluated using natural bond orbital (NBO) analysis.<sup>24</sup>

The inclusion energies ( $E_{inc}$ ) of endohedral complexes were evaluated by comparing the energy of  $X@C_{20}H_{20}$  with the sum of the energies of the isolated components,  $C_{20}H_{20}$  and X. For comparison, the corresponding exohedral binding energies ( $E_{bind}$ ) also were computed. The ZPE-corrected energy difference between the most stable exohedral structures and their endohedral isomers was defined as the isomerization energy ( $E_{isom}$ ). Optimized bond lengths and lowest real (or imaginary) frequencies for  $I_h$  dodecahedrane and  $X@C_{20}H_{20}$  derivatives are summarized in Table 1, and their inclusion energies ( $E_{inc}$ ) as well as the natural charge ( $q$ ) and spin densities ( $S$ ) are shown in Table 2. The optimized geometries of exohedral complexes are given in Figure 3 and Table 3, and their exohedral binding energies ( $E_{bind}$ ) and endo-exo isomerization energies ( $E_{isom}$ ) are summarized in Table 4.

## Results and Discussion

**$H^+@C_{20}H_{20}$ .** Is an endohedral proton complex possible? To alleviate its extreme electron deficiency,  $H^+$  tends to attach itself to lone pairs or to bonds. Disch and Schulman<sup>14a</sup> postulated that the exterior of **1** might be protonated more favorably than the interior. Indeed,  $I_h$  geometry-optimized  $H^+@C_{20}H_{20}$  has  $N_{imag} = 12$  and represents a high-order saddle point. Mode

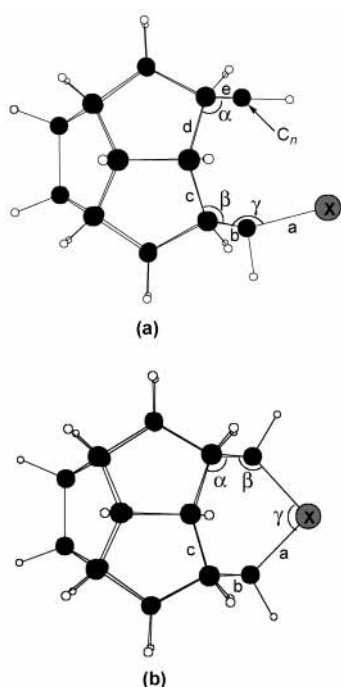
**Figure 1.** (a)  $C_{2v}$  bond- and (b)  $C_{s_v}$  face-protonated dodecahedranes.**Figure 2.** Energy of  $X@C_{20}H_{20}$  ( $X = He, H, N, P$ ) versus X distance from the cage center along bond-crossing and ring-crossing routes. For  $X = P$ , the maximum is reached at 4330 kcal/mol (not shown).

following reveals that the proton migrates out of the cage without barrier during optimization. This results in an exterior-protonated isomer ( $C_{2v}$ , Figure 1a),  $C_{20}H_{21}^+$ , in which the proton bridges two carbon atoms symmetrically and separates them by 2.345 Å. The  $C_{20}H_{21}^+$  B3LYP/6-31G\* proton affinity (PA) is 185.3 kcal/mol (Table 4). Protonated ethane also has a proton-bridged C-C bond but with a lower PA (142.5 kcal/mol).<sup>25</sup> The larger PA of **1** is a size effect because the charge is better dispersed than in ethane. For comparison, we have also calculated a face-protonated exohedral  $C_{s_v}$   $C_{20}H_{21}^+$  form, with the proton over the midpoint of a five-membered ring (Figure 1b). However, this is not a minimum ( $N_{imag} = 2$ ) and is 31.6 kcal/mol higher in energy than the  $C_{2v}$   $C_{20}H_{21}^+$  geometry.

**$X@C_{20}H_{20}$  ( $X = H, N, P$ ).** The cage-centered H, N, and P endohedral complexes are local minima. The hydrogen atom

**TABLE 3: Selected B3LYP/6-31G\* Optimized  $X\text{C}_{20}\text{H}_{20}$  (Figure 3) Bond Angles ( $\alpha$ - $\gamma$ ; degrees) and Bond Lengths (a-e; Å)**

$X\text{C}_{20}\text{H}_{20}$	sym	$\alpha$	$\beta$	$\gamma$	a	b	c	d	e	$C_x$	$S_x$	$S_c$
$^1\text{H}^+\text{C}_{20}\text{H}_{20}$	$C_{2v}$	116.1	107.4	136.9	1.261	1.514	1.572			0.26		
$^2\text{HC}_{20}\text{H}_{20}$	$C_{2v}$	116.9	103.5	144.8	1.325	1.526	1.577			0.26	-0.09	0.55
$^2\text{HC}_{20}\text{H}_{20}$	$C_s$	119.1	121.3	114.5	1.090	1.545	1.572	1.590	1.491	0.44	0.00	0.98
$^4\text{NC}_{20}\text{H}_{20}$	$C_{2v}$	115.9	110.0	123.2	1.381	1.582	1.547			0.03	1.31	0.0
$^2\text{NC}_{20}\text{H}_{20}$	$C_{2v}$	116.1	114.1	111.1	1.44x	1.567	1.557			-0.28	0.88	-0.06
$^4\text{PC}_{20}\text{H}_{20}$	$C_{2v}$	123.3	100.6	114.8	2.035	1.543	1.613			0.52	1.97	0.41
$^4\text{PC}_{20}\text{H}_{20}$	$C_s$	118.1	125.1	122.5	1.871	1.561	1.575	1.587	1.485	0.33	1.95	1.00
$^2\text{PC}_{20}\text{H}_{20}$	$C_{2v}$	119.2	114.5	93.2	1.862	1.557	1.566			0.64	0.98	-0.04
$^4\text{C}^-\text{C}_{20}\text{H}_{20}$	$C_{2v}$	116.8	111.1	117.6	1.468	1.570	1.559			0.16	1.80	-0.08
$^2\text{C}^-\text{C}_{20}\text{H}_{20}$	$C_{2v}$	116.3	116.0	104.2	1.525	1.575	1.561			-0.40	0.90	-0.05
$^4\text{Si}^-\text{C}_{20}\text{H}_{20}$	$C_{2v}$	120.9	110.9	98.7	1.902	1.556	1.566			0.78	1.735	0.07
$^2\text{Si}^-\text{C}_{20}\text{H}_{20}$	$C_{2v}$	119.6	115.8	87.6	1.987	1.552	1.571			0.20	1.00	-0.03
$^4\text{O}^+\text{C}_{20}\text{H}_{20}$	$C_{2v}$	122.5	99.7	126.2	1.747	1.534	1.590			0.09	1.37	0.54
$^4\text{O}^+\text{C}_{20}\text{H}_{20}$	$C_s$	117.5	122.7	120.5	1.269	1.670	1.545	1.601	1.485	-0.112	1.04	0.99
$^2\text{O}^+\text{C}_{20}\text{H}_{20}$	$C_{2v}$	114.5	113.5	116.9	1.390	1.558	1.549			-0.33	0.36	0.04
$^4\text{S}^+\text{C}_{20}\text{H}_{20}$	$C_{2v}$	124.5	98.7	116.8	2.021	1.542	1.609			0.71	1.61	0.47
$^4\text{S}^+\text{C}_{20}\text{H}_{20}$	$C_s$	117.1	125.0	120.3	1.748	1.592	1.565	1.592	1.483	0.68	1.53	1.01
$^2\text{S}^+\text{C}_{20}\text{H}_{20}$	$C_{2v}$	119.1	113.1	97.7	1.791	1.570	1.560			0.84	0.76	-0.01

**Figure 3.** General structure of (a)  $C_s$ - and (b)  $C_{2v}$ -symmetric exohedral complexes. Optimized bond lengths and angles are summarized in Table 3.

and helium have nearly the same inclusion energy (36.3 vs 38.0 kcal/mol), but the inclusion energies of N and P are much higher (125.3 and 300.3 kcal/mol, respectively). Thus, H, N, and P encapsulations are unfavorable energetically. The inclusion energies of H and He at the B3LYP/6-31G\* + ZPE level are in good agreement with our previously reported B3LYP/6-311+G(d,p) + ZPE results.<sup>15c</sup>

To determine whether the cage-centered configurations are the global minima for the endohedral complexes, the potential energy surfaces (PES) have been studied by moving the guest atoms in the fixed-cage host (Figure 2). Two extreme conditions for the guest to penetrate the cage have been investigated: one is ring crossing, which is simulated by displacing the guest atoms along the 5-fold axis from the cage center though a pentagonal surface to the exterior of the molecule, and the other is bond crossing, which is simulated by displacing the guest from the cage center to the C-C bond center and further to the exterior. The PES shown in Figure 2 indicates that the configurations with the guest at the cage center have the lowest energy and

**TABLE 4: B3LYP/6-31G\* Optimized  $X@C_{20}H_{20}$  Absolute Energies (au), Zero-Point Energies (ZPE; kcal/mol, unscaled), Lowest Vibrational Frequencies ( $\omega_1$ ;  $\text{cm}^{-1}$ ) (or Imaginary Frequencies), Exohedral Binding Energies ( $E_{\text{bind}}$ ; kcal/mol), and Exohedral Endohedral Isomerization Energies ( $E_{\text{isom}}$ ; kcal/mol) for Exohedral Isomers**

	energy	ZPE	$\omega_1$	$E_{\text{bind}}$	$E_{\text{isom}}$
$^1\text{H}^+\text{C}_{20}\text{H}_{20}$	$C_{2v}$	-774.48924	231.29	377.6	185.3
$^2\text{HC}_{20}\text{H}_{20}$	$C_{2v}$	-774.68622	227.94	-1476.3i (1) <sup>a</sup>	1.7
$^2\text{HC}_{20}\text{H}_{20}$	$C_s$	-774.70592	230.69	240.6	-7.9 44.2
$^4\text{NC}_{20}\text{H}_{20}$	$C_{2v}$	-828.65739	221.72	344.7	66.6
$^2\text{NC}_{20}\text{H}_{20}$	$C_{2v}$	-828.86928	228.80	250.3	-125.7 191.7
$^4\text{PC}_{20}\text{H}_{20}$	$C_{2v}$	-1115.28700	222.65	-729.7i(1) <sup>a</sup>	95.1
$^4\text{PC}_{20}\text{H}_{20}$	$C_s$	-1115.37763	223.90	102.8	39.4
$^2\text{PC}_{20}\text{H}_{20}$	$C_{2v}$	-1115.49135	226.75	192.4	-69.3 329.4
$^4\text{C}^-\text{C}_{20}\text{H}_{20}$	$C_{2v}$	-812.07143	222.21	862.8	-29.8
$^2\text{C}^-\text{C}_{20}\text{H}_{20}$	$C_{2v}$	-812.14252	225.41	225.2	-118.5 187.2
$^4\text{Si}^-\text{C}_{20}\text{H}_{20}$	$C_{2v}$	-1063.48822	219.79	233.2	59.1
$^2\text{Si}^-\text{C}_{20}\text{H}_{20}$	$C_{2v}$	-1063.62338	224.29	179.6	-50.2 326.5
$^4\text{O}^+\text{C}_{20}\text{H}_{20}$	$C_{2v}$	-848.84593	218.58	-1339.9(3) <sup>a</sup>	-78.6
$^4\text{O}^+\text{C}_{20}\text{H}_{20}$	$C_s$	-848.95550	221.75	162.6	-144.2
$^2\text{O}^+\text{C}_{20}\text{H}_{20}$	$C_{2v}$	-849.10212	226.82	215.4	-321.6 210.3
$^4\text{S}^+\text{C}_{20}\text{H}_{20}$	$C_{2v}$	-1171.88432	221.87	-811.1i(1) <sup>a</sup>	9.3
$^4\text{S}^+\text{C}_{20}\text{H}_{20}$	$C_s$	-1171.95646	222.03	104.8	-35.8
$^2\text{S}^+\text{C}_{20}\text{H}_{20}$	$C_{2v}$	-1172.09019	226.75	178.8	-167.5 297.3

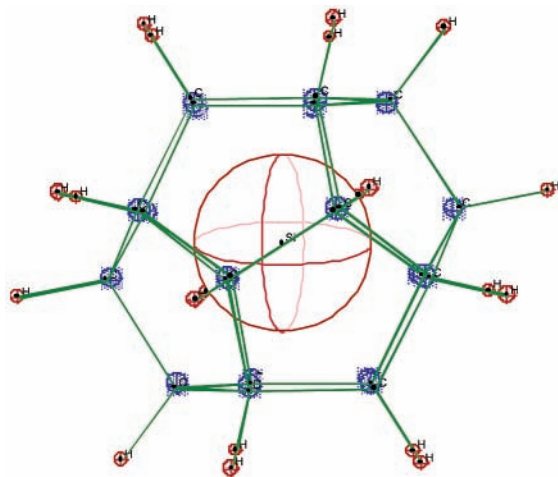
<sup>a</sup> Transition state or higher saddle point, with the number of the imaginary frequencies are given in parentheses.

that the energy increases monotonically along both ring-crossing and bond-crossing routes to the exterior. The PES for off-center displacements confirms that H/N/P atoms are located at the cage center.

The net charges and spin densities of  $X@C_{20}H_{20}$  ( $X = \text{H}, \text{N}, \text{P}$ ) are listed in Table 2. There is negligible electron transfer between hydrogen and the cage framework. With a spin density of 0.91e, hydrogen nearly maintains its unencapsulated atomic electron configuration. N and P are much larger than H, and their host-guest interactions are greater. The encapsulated nitrogen atom accepts 0.05e from the cage and has a spin density of 2.57e, thus it still can be considered to preserve its atomic quartet ground-state approximately. Phosphorus, however, donates 1.07e to the cage and has a spin density of 1.73, indicating heavy orbital mixing with the framework of **1**.

As expected, all of the exohedral isomers are much more stable than their endohedral analogues. (See Table 4.) The most stable  $\text{HC}_{20}\text{H}_{20}$  structure has a -7.9 kcal/mol hydrogen binding energy and is  $C_s$ -symmetric, with a  $\text{CH}_2$  group and a ruptured C-C bond (Figure 3a). The increase in  $\text{C}_{20}\text{H}_{20}$  strain energy when the cage is smaller than the bond energy of the new C-H bond, hence a ruptured cage structure is preferred.





**Figure 4.** HOMO of B3LYP/6-31G\*-optimized and  $I_h$ -symmetric  ${}^4\text{Si}^-$ @ $\text{C}_{20}\text{H}_{20}$ . The  ${}^4\text{Si}^-$  encapsulating cage ( $\text{C}-\text{C} = 1.597 \text{ \AA}$ ) is more compact than  ${}^4\text{Si}^+$ @ $\text{C}_{20}\text{H}_{20}$  ( $\text{C}-\text{C} = 1.614 \text{ \AA}$ ) because of electron donation from the anion center into the  $\text{C}-\text{C}$  bonding HOMO as shown. This is opposite to the ionic radii of their respective endohedral species (i.e.,  ${}^4\text{Si}^- > {}^4\text{Si}^+$ ).

The  $C_{2v}$  structure (Figure 3b) with hydrogen symmetrically inserted into a  $\text{C}-\text{C}$  bond is a transition state and only slightly higher in energy (by 1.7 kcal/mol) than its infinitely separated components. This very low dissociation energy is also due to the smaller strain energy in  $\text{C}_{20}\text{H}_{20}$  than in the ruptured cage.

Both doublet and quartet states of  $C_{2v}$   $\text{NC}_{20}\text{H}_{20}$  are local minima (Figure 3b). The exohedral doublet complex is 125.7 kcal/mol more stable than the infinitely separated components, and the exohedral quartet is unstable by 66.6 kcal/mol toward dissociation into  $\text{C}_{20}\text{H}_{20}$  and  ${}^4\text{N}$ . The 192.3 kcal/mol energy difference between the doublet and quartet exohedral binding energies is much larger than the doublet–quartet separation of atomic nitrogen (66.2 kcal/mol). Similarly, exohedral doublet  $\text{PC}_{20}\text{H}_{20}$  has a  $C_{2v}$  minimum with phosphorus binding to a  $\text{C}-\text{C}$  bond (Figure 3b) and is energetically more favorable by 69.3 kcal/mol than its independent components. In contrast, the  $C_{2v}$  structure is a transition state toward dissociation for exohedral quartet  ${}^4\text{PC}_{20}\text{H}_{20}$ ; the  $C_s$ -symmetric structure with a CHP group and a ruptured  $\text{C}-\text{C}$  bond (Figure 3a) is a local minimum but is much higher in energy than the doublet state.  $E_{\text{isom}}$  is the smallest for encapsulated H (44.2 kcal/mol), whereas the endo  $\rightarrow$  exo isomerization energies for N and P are very exothermic, approximately 192 and 329 kcal/mol, respectively.

$\text{X}@C_{20}\text{H}_{20}$  ( $\text{X} = \text{C}^-, \text{Si}^-, \text{O}^+, \text{S}^+$ ). Quartet N and P are minima in the cage center because of their half-filled valence shells and spherically distributed wave functions. What is the nature of their isoelectronic charged analogues  $\text{C}^-$ ,  $\text{Si}^-$ ,  $\text{O}^+$ , and  $\text{S}^+$  with half-filled shells? Except for  $\text{O}^+@C_{20}\text{H}_{20}$ , which is a third-order saddle point, all of the other ionic species are local  $I_h$  minima but are highly unstable (by 116–305 kcal/mol) toward dissociation. The exohedral low-spin complexes have significant binding energies ranging from  $-50$  to  $-322$  kcal/mol. The relative isomerization energies favoring exohedral over endohedral complexes are very high, in the 187–327 kcal/mol range (Table 4).

Both low- and high-spin  $C_{2v}$   $\text{XC}_{20}\text{H}_{20}$  ( $\text{X} = \text{C}^-, \text{Si}^-$ ) species are minima. The high-spin complexes,  $\text{O}^+@C_{20}\text{H}_{20}$  and  $\text{S}^+@C_{20}\text{H}_{20}$ , favor  $C_s$  structures, and their  $C_{2v}$  forms are transition states with very weak  $\text{C}-\text{X}$  bonds. In high-spin  $I_h$  endohedral complexes,  $\text{C}^-$ ,  $\text{O}^+$ , and  $\text{S}^+$  have spin densities of 2.12e, 2.23e, and 2.06e, respectively, and their quartet ground states are preserved

approximately. However, with a spin density of 0.93e,  $\text{Si}^-$  loses its atomic ground-state character at the cage center.

The endohedral-complex cage bond lengths in the optimized geometries reveal subtle trends. Previously,<sup>15c</sup> we showed that cage  $\text{C}-\text{C}$  bonds shortened ( $<0.01 \text{ \AA}$ ) and  $\text{C}-\text{H}$  bonds lengthened ( $\leq 0.02 \text{ \AA}$ ) in response to electron donation into the  $\text{C}-\text{C}$  bonding and  $\text{C}-\text{H}$  antibonding HOMOs of endohedral complexes. The same trend is apparent in the quartet state  $\text{X}@C_{20}\text{H}_{20}$  bond lengths, as shown in Table 1. The trend in atomic radii is  $\text{Si}^- > \text{P} > \text{S}^+$ , yet the  $\text{C}-\text{C}$  bond lengths decrease over the series  ${}^4\text{S}^+@C_{20}\text{H}_{20}$  (1.614  $\text{ \AA}$ )  $>$   ${}^4\text{P}@C_{20}\text{H}_{20}$  (1.608  $\text{ \AA}$ )  $>$   ${}^4\text{Si}^-@C_{20}\text{H}_{20}$  (1.597  $\text{ \AA}$ ). That is, the cage shrinks when encapsulating large species, whereas the  $\text{C}-\text{H}$  bonds lengthen slightly. Similarly, the radius of  $\text{C}^-$  is larger than that of N, but the cage  $\text{C}-\text{C}$  bonds lengthen and  $\text{C}-\text{H}$  bonds shorten when going from  ${}^4\text{C}^-@C_{20}\text{H}_{20}$  to  ${}^4\text{N}@C_{20}\text{H}_{20}$ . These bond-length alternations are explained qualitatively by the  $\text{X}@C_{20}\text{H}_{20}$  HOMO, which resembles the  $\text{C}-\text{C}$  bonding and  $\text{C}-\text{H}$  antibonding  $\text{C}_{20}\text{H}_{20}$  LUMOs in compact cages such as  ${}^4\text{Si}^-@C_{20}\text{H}_{20}$  (Figure 4).

## Conclusions

In summary, B3LYP density functional studies have located endohedral dodecahedrane minima and predict their stability toward dissociation. A proton ( $\text{H}^+$ ) is not endohedrally encapsulated but prefers attachment to the external dodecahedrane surface. The  $\text{C}_{20}\text{H}_{21}^+$  minimum is an exohedral complex whose proton bridges two carbons with a 2.35  $\text{ \AA}$   $\text{C}-\text{C}$  distance. H, N, P, and their isoelectronic species ( $\text{C}^-$ ,  $\text{Si}^-$ ,  $\text{S}^+$ ) have local minima at the cage center, but  $\text{O}^+$  does not. H has an endothermic inclusion energy (36.3 kcal/mol) similar to that of helium (38.0 kcal/mol), whereas the larger species (N, P,  $\text{C}^-$ ,  $\text{Si}^-$ ,  $\text{O}^+$ , and  $\text{S}^+$ ) have much higher inclusion energies (ca. 125–305 kcal/mol). The exohedral complexes are favorable for all species.  $\text{C}_{20}\text{H}_{21}$  prefers a structure with a  $\text{CH}_2$  group and a ruptured  $\text{C}-\text{C}$  bond. N, P, and their isoelectronic analogues favor doublet exohedral complexes with symmetrical skeletally bound atoms. A low-energy ion beam colliding with  $\text{C}_{20}\text{H}_{20}$  should result in exohedral complexes for all of these species, whereas a high-energy beam might result in the endohedral species for endohedral complexes between dodecahedrane and H, N, and P and their isoelectronic species ( $\text{C}^-$ ,  $\text{Si}^-$ ,  $\text{S}^+$ ). Encapsulated H, N,  $\text{C}^-$ ,  $\text{O}^+$ , and  $\text{S}^+$  preserve their atomic ground states and thus are promising electron spin quantum-computing nanodevices, whereas P and  $\text{Si}^-$  interact with the cage strongly and their electronic states mix.

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## Note Added in Proof

Following the acceptance of this paper for publication, a paper (Mascal, M. *J. Org. Chem.* **2002**, 67, 8644) appeared reporting the activation barriers and reaction coordinate energy profiles for the penetration of  $\text{H}^+$ , He,  $\text{Li}^+$ ,  $\text{Be}^+$ ,  $\text{Be}^{2+}$ , and  $\text{Mg}^{2+}$  into dodecahedrane.

## References and Notes

- (1) (a) Paquette, L. A. *Chem. Rev.* **1989**, 89, 1051. (b) Eaton, P. E. *Tetrahedron* **1979**, 35, 2189. (c) Eaton, P. E. *Top. Curr. Chem.* **1979**, 79, 41.

- (2) (a) Engler, E. M.; Andose, J. D.; Schleyer, P. v. R. *J. Am. Chem. Soc.* **1973**, *95*, 8005. (b) Allinger, N. L. *J. Am. Chem. Soc.* **1977**, *99*, 8127. (c) Allinger, N. L.; Geise, H. J.; Pyckhout, W.; Paquette, L. A.; Gallucci, J. C. *J. Am. Chem. Soc.* **1989**, *111*, 1106.
- (3) (a) Schulman, J. M.; Disch, R. L. *J. Am. Chem. Soc.* **1978**, *100*, 5677. (b) Dixon, D. A.; Deerfield, D.; Graham, G. D. *Chem. Phys. Lett.* **1981**, *78*, 161. (c) Schulman, J. M.; Disch, R. L. *J. Am. Chem. Soc.* **1984**, *106*, 1202. (d) Disch, R. L.; Schulman, J. M.; Sabio, M. L. *J. Am. Chem. Soc.* **1985**, *107*, 1904. (e) Scamehorn, C. A.; Hermiller, S. M.; Pitzer, R. M. *J. Chem. Phys.* **1986**, *84*, 833. (f) Disch, R. L.; Schulman, J. M. *J. Phys. Chem.* **1996**, *109*, 3504.
- (4) Ermer, O. *Angew. Chem., Int. Ed. Engl.* **1977**, *16*, 411.
- (5) Hudson, B. S.; Braden, D. A.; Parker, S. F.; Prinzbach, H. *Angew. Chem., Int. Ed.* **2000**, *39*, 514.
- (6) Wahl, F.; Wörth, J.; Prinzbach, H. *Angew. Chem., Int. Ed. Engl.* **1993**, *32*, 1722.
- (7) Schulman, J. M.; Venanzi, T.; Disch, R. L. *J. Am. Chem. Soc.* **1975**, *97*, 5335.
- (8) Paquette, L. A.; Ternansky, R. J.; Balogh, D. W.; Kentgen, G. J. *Am. Chem. Soc.* **1983**, *105*, 5446.
- (9) (a) Fessner, W. D.; Murty, B. A. R. C.; Wörth, J.; Hunkler, D.; Fritz, H.; Prinzbach, H.; Roth, W. D.; Schleyer, P. v. R.; McEwen, A. B.; Maier, W. F. *Angew. Chem., Int. Ed. Engl.* **1987**, *26*, 452. (b) Bertau, M.; Wahl, F.; Weiler, A.; Scheumann, K.; Worth, J.; Keller, M.; Prinzbach, H. *Tetrahedron* **1997**, *53*, 10029. (c) Bertau, M.; Leonhardt, J.; Weiler, A.; Weber, K.; Prinzbach, H. *Chem.—Eur. J.* **1996**, *2*, 570.
- (10) Beckhaus, H.-D.; Rüdhardt, C.; Lagerwall; Paquette, L. A.; Wahl, F.; Prinzbach, H. *J. Am. Chem. Soc.* **1994**, *116*, 11775.
- (11) Broadus, K. M.; Kass, S. R.; Osswald, T.; Prinzbach, H. *J. Am. Chem. Soc.* **2000**, *122*, 10964.
- (12) (a) Paquette, L. A. In *Cage Hydrocarbons*; Olah, G. A., Ed.; Wiley & Sons: New York, 1990; pp 313–352. (b) Fessner, W. D.; Prinzbach, H. In *Cage Hydrocarbons*; Olah, G. A., Ed.; Wiley & Sons: New York, 1990; pp 353–405. (c) Prinzbach, H.; Weber, K. *Angew. Chem., Int. Ed. Engl.* **1994**, *33*, 2239.
- (13) Prinzbach, H.; Weller, A.; Landenberger, P.; Wahl, F.; Worth, J.; Scott, L. T.; Gelmont, M.; Olevano, D.; v. Issendorff, B. *Nature (London)* **2000**, *407*, 60.
- (14) (a) Disch, R. L.; Schulman, J. M. *J. Am. Chem. Soc.* **1981**, *103*, 3297. (b) Jiménez-Vázquez, H. A.; Tamariz, J.; Cross, R. J. *J. Phys. Chem. A* **2001**, *105*, 1315.
- (15) (a) Chen, Z.; Jiao, H.; Bühl, M.; Hirsch, A.; Thiel, W. *Theor. Chem. Acc.* **2001**, *106*, 352. (b) Jimenez-Vazquez, H. A.; Tamariz, J.; Cross, R. J. *J. Phys. Chem. A* **2001**, *105*, 1315. (c) Moran, D.; Stahl, F.; Jemmis, E. D.; Schaefer, H. F., III; Schleyer, P. v. R. *J. Phys. Chem. A* **2002**, *106*, 5144.
- (16) Cross, R. J.; Saunders, M.; Prinzbach, H. *Org. Lett.* **1999**, *1*, 1479.
- (17) (a) Saunders, M.; Jiménez-Vázquez, H. A.; Cross, R. J.; Poreda, R. J. *Science (Washington, D.C.)* **1993**, *259*, 1428. (b) Saunders, M.; Cross, R. J.; Jiménez-Vázquez, H. A.; Shimshi, R.; Khong, A. *Science (Washington, D.C.)* **1996**, *271*, 1693.
- (18) (a) Harneit, W.; Waiblinger, M.; Meyer, C.; Lips, K.; Weidinger, A. *Proc. Electrochem. Soc.* **2001**, *11*, 358. (b) Meyer, C.; Harneit, W.; Waiblinger, M.; Lips, K.; Weidinger, A. *AIP Conference Proceedings* **2001**, *591*, 101. (c) Harneit, W.; Waiblinger, M.; Lips, K.; Makarov, S.; Weidinger, A. *AIP Conf. Proc.* **2000**, *544*, 207. (d) Park, S.; Srivastava, D.; Cho, K. *J. Nanosci. Nanotech.* **2001**, *1*, 1. (e) Harneit, W. *Phys. Rev. A* **2002**, *65*, 032322.
- (19) Sahoo, R. R.; Patnaik, A. *Chem. Phys. Lett.* **2001**, *349*, 201.
- (20) (a) Almeida, M. T.; Pawlik, T.; Weidinger, A.; Höhne, M.; Alcalá, R.; Spaeth, J. M. *Phys. Rev. Lett.* **1996**, *77*, 1075. (b) Knapp, C.; Dinse, K. P.; Pietzak, B.; Waiblinger, M.; Weidinger, A. *Chem. Phys. Lett.* **1997**, *272*, 433. (c) Pietzak, B.; Waiblinger, M.; Almeida, M. T.; Weidinger, A.; Höhne, M.; Dietel, E.; Hirsch, A. *Chem. Phys. Lett.* **1997**, *279*, 259.
- (21) Knapp, C.; Weiden, N.; Kass, K.; Dinse, K. P.; Pietzak, B.; Waiblinger, M.; Weidinger, A. *Mol. Phys.* **1998**, *95*, 999.
- (22) Smith, R.; Beardmore, K.; Belbruno, J. *Chem. Phys.* **1999**, *111*, 9227.
- (23) Frisch, M. J.; Trucks, G. W.; Schlegel, H. B.; Scuseria, G. E.; Robb, M. A.; Cheeseman, J. R.; Zakrzewski, V. G.; Montgomery, J. A., Jr.; Stratmann, R. E.; Burant, J. C.; Dapprich, S.; Millam, J. M.; Daniels, A. D.; Kudin, K. N.; Strain, M. C.; Farkas, O.; Tomasi, J.; Barone, V.; Cossi, M.; Cammi, R.; Mennucci, B.; Pomelli, C.; Adamo, C.; Clifford, S.; Ochterski, J.; Petersson, G. A.; Ayala, P. Y.; Cui, Q.; Morokuma, K.; Malick, D. K.; Rabuck, A. D.; Raghavachari, K.; Foresman, J. B.; Cioslowski, J.; Ortiz, J. V.; Stefanov, B. B.; Liu, G.; Liashenko, A.; Piskorz, P.; Komaromi, I.; Gomperts, R.; Martin, R. L.; Fox, D. J.; Keith, T.; Al-Laham, M. A.; Peng, C. Y.; Nanayakkara, A.; Gonzalez, C.; Challacombe, M.; Gill, P. M. W.; Johnson, B. G.; Chen, W.; Wong, M. W.; Andres, J. L.; Head-Gordon, M.; Replogle, E. S.; Pople, J. A. *Gaussian 98*, revision A.5; Gaussian, Inc.: Pittsburgh, PA, 1998.
- (24) Glendening, E. D.; Badenhoop, J. K.; Reed, A. E.; Carpenter, J. E.; Weinhold, F. *NBO*, version 4.0; University of Wisconsin: Madison, WI, 1996.
- (25) (a) Carneiro, J. W. d. M.; Schleyer, P. v. R.; Saunders, M.; Remington, R.; Schaefer, H. F., III; Rauk, A.; Sorensen, T. S. *J. Am. Chem. Soc.* **1994**, *116*, 3483. (b) Bohme, D. K.; Mackay, G. I. *J. Am. Chem. Soc.* **1981**, *103*, 2173.