# Ab Initio Study on Phenylacetylene in S<sub>1</sub> and S<sub>2</sub>

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The electronic structures of phenylacetylene (PA) in S<sub>0</sub>, S<sub>1</sub>, and S<sub>2</sub> have been examined by means of ab initio complete active space self-consistent field (CASSCF) and the second-order multi-reference Möller–Plesset (MRMP2) calculations. The stable structures of PA in both S<sub>0</sub> and S<sub>1</sub> are optimized to be  $C_{2\nu}$ . The stable structure in S<sub>1</sub> is characterized as an enlarged benzene ring, which is caused by local  $\pi - \pi^*$  excitation within the benzene ring. On the other hand, the S<sub>2</sub> geometry is optimized to be a quinoid structure where the aromaticity of the benzene ring is completely lost. To discuss the internal conversion from S<sub>2</sub> into S<sub>1</sub>, the conical intersection between S<sub>2</sub> and S<sub>1</sub> (S<sub>2</sub>/S<sub>1</sub>-CIX) has been also determined. The S<sub>2</sub>/S<sub>1</sub>-CIX is characterized as a quinoid structure in the benzene part and allene-like in the acetylene part. The present computational result well reproduces the experimental findings, such as the rotational constant and the feature of the absorption spectrum.

#### I. Introduction

The photochemical behaviors of aryl alkenes and alkynes have been of great interest in the basic science of laser spectroscopy as well as in the applied material science. As to a prototype of aryl alkenes, i.e., styrene (STY), we recently proposed a new picture of the photochemical behavior.<sup>1–3</sup> In the present study, we theoretically examine the photochemical behavior of a prototype of aryl alkynes, phenylacetylene (PA), and compare it with that of STY previously reported. In the following paragraphs, we make a brief review on the previous studies on PA.

The stable geometry in  $S_0$  was of main interest in the early days of the research. It is found that the stable PA in  $S_0$  is  $C_{2\nu}$ geometry by means of microwave and electron diffraction experiments.<sup>4,5</sup> The force field analysis of the infrared and Raman spectra also support the validity of the  $C_{2\nu}$  structure.<sup>6,7</sup> This experimental finding was confirmed by means of ab initio calculations.<sup>5,8–10</sup>

The study on the low-lying excited states of PA stemmed from the work by King and So.<sup>11</sup> They measured the absorption spectrum and found three absorption bands (279-270, 239-220, and 194-190 nm), whose intensities increase in energy. The first weak absorption band is rich in a rotational structure to be analyzed. The second absorption band is diffuse with prominent twin peaks. They made comment that the second absorption band with a peculiar intensity distribution is unlikely to correspond to separate electronic transition and tentatively pointed out that this is due to the predissociation of the system of PA. The third absorption, which is not our present interest, is also structureless and is supposed to be in relation to the decomposition process of PA.<sup>12</sup>

The seminal works by King and So about the first and second absorption bands were developed by the following works. Swiderek et al. performed low-energy electron energy loss spectroscopy so as to assign the weak peak at 4.41 eV and the intense absorption around 5.05-5.30 eV to the  $S_0-S_1 0-0$  and the  $S_0-S_2$  transitions, respectively.<sup>13</sup> Smalley and co-workers

measured a dispersed fluorescence spectrum so that the S<sub>1</sub> with B<sub>2</sub> symmetry under the  $C_{2\nu}$  point group is the locally excited  $\pi - \pi^*$  within the benzene ring.<sup>14</sup> Several authors confirmed their assignment of S<sub>1</sub> by means of vibrational force field analyses.<sup>15–18</sup> Tzseng and co-workers performed the resonant two-photon ionization studies to discuss the electronic and geometrical structures in S<sub>1</sub>. By combining ab initio single excitation calculations (CIS) with their experimental results, they concluded that S<sub>1</sub> has a quinoid structure where the aromaticity of the benzene ring is lost.<sup>10</sup> Pratt and co-workers measured the rotationally resolved fluorescence spectra so as to find out PA in S<sub>1</sub> is polarized along the *b* axis and pointed out that a CIS calculation gives a result of the *a* axis being polarized.<sup>19</sup>

Contrary to the richness of the information on the  $S_1$  state, the discussion on the second absorption band with a peculiar shape is very limited. Vaida et al. examined it by means of the direct absorption spectroscopy.<sup>20</sup> They found the characteristic  $1846 \pm 15$  cm<sup>-1</sup> interval of the vibrational mode and tentatively assigned it the stretching vibration relating to the triple bond.

Despite much effort to elucidate the photochemistry of PA in  $S_1$  and  $S_2$ , it is still controversial or unclear. So our present purpose is to examine both electronic and geometrical structures in  $S_1$  and  $S_2$  by means of a reliable ab initio method.

The present paper is organized as follows. In the next section, we describe the method of calculations based on preliminary configuration interaction (CI) results. In section III, we mention the electronic and geometrical structures of PA in  $S_1$  and  $S_2$  as well as  $S_0$ . Then we discuss the mechanism of the internal conversion from  $S_2$  into  $S_1$ . We also compare the photochemistry of PA with that of STY. Finally, we give a summary on the present computational results.

### **II. Method of Calculations**

The global potential energy surfaces of PA by means of complete active space self-consistent field (CASSCF) and the second-order multi-reference Möller—Plesset (MRMP2) calculations are desirable to do a reliable discussion on the photochemical behavior of PA. To obtain the global potential energy surfaces, however, we have to perform the calculations at many geometrical points, which include not only the Franck—Condon

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(FC) region but also the region far away from the FC region such as a conical intersection (CIX). Therefore, how to reduce the computational labor is important. Our strategy for the calculation of a global potential energy surface of PA is as follows. In the first step, we did CI calculations at various geometries which covered the conformations possible to contribute to the photochemical process of PA. In the preliminary CI calculations, it was found that at all of the conformations sampled here, the low-lying excited states are well described by the CSFs (configuration state functions) arising from the highest four  $\pi$  to the lowest four unoccupied  $\pi^*$  orbitals. This implies that the 8 electrons in 8 orbitals CASSCF ((m,n) CASSCF in general) and its MRMP2 are enough to discuss the photochemistry of PA. However, the nature of the set of highest four orbitals in active space is dependent on the conformation. In other words, the remaining fifth  $\pi$  occupied orbital (i.e., the lowest occupied  $\pi$  orbital) which is out of the active space at a conformation slips in a set of the active orbitals at another conformation. Generally speaking, the active space which is dependent on the conformation leads to unphysical discontinuity of the potential energy surfaces. To avoid it, the additional fifth occupied  $\pi$  orbital is included in the active space. That is, we adopted (10,9)CASSCF and MRMP2 for the scanning of the global potential energy surfaces.

First, we optimized the equilibrium geometry of  $S_0$  ( $S_0$ geometry) of PA by means of a state-specific (10,9)CASSCF method. Then we examined the electronic structures at the S<sub>0</sub>geometry by means of a state specific (10,9)CASSCF and its MRMP2. To discuss the photochemical behavior of PA, we optimized the geometries of  $S_1$  (S<sub>1</sub>-geometry) and  $S_2$ . The optimization of the S2 geometry was done under constraint of the planar structure (S<sub>2</sub>-planar). We additionally optimized the conical intersection between  $S_2$  and  $S_1$  ( $S_2/S_1$ -CIX) to discuss the internal conversion from  $S_2$  into  $S_1$ . Because of the limitation of our computer facility, the S<sub>2</sub>/S<sub>1</sub>-CIX was determined by (8,8)CASSCF method. However, this approach is reasonable because the low-lying excited states (especially  $S_2$  and  $S_1$ ) in the region around the  $S_2/S_1$ -CIX is well described by the CSFs arising from the highest four occupied into the lowest unoccupied orbitals, as mentioned above. We, of course, checked the validity of the truncation of the active space, as mentioned in the next section. In the scanning of the potential energy surfaces for the internal conversion from  $S_2$  into  $S_1$ , the molecular orbitals (MOs) were determined by means of a statespecific CASSCF. The basis set used in the present calculations is the Huzinage–Dunning double- $\zeta$  (DZ) basis set augmented by polarization ( $\alpha_d = 0.75$ ) on carbon atoms. In the present ab initio calculations, we used the GAMESS program,<sup>21</sup> except for the determination of the  $S_2/S_1$ -CIX by Gaussian 98.<sup>22</sup>

#### **III. Results and Discussions**

We begin with mentioning the electronic structures of PA at S<sub>0</sub>-geometry. S<sub>0</sub>-geometry was optimized to be  $C_{2\nu}$  symmetry. In Table 1, we listed the excitation energies, the oscillator strengths, and the main CSFs of each electronic state by means of MRMP2 as well as other methods. The S<sub>1</sub> state with B<sub>2</sub> symmetry under  $C_{2\nu}$  point group can be assigned to the local  $\pi - \pi^*$  excitations within the benzene ring, which is well described by a linear combination of the single excitation CSFs of (HOMO-1)-LUMO and HOMO–(LUMO+1) (HOMO, highest occupied MO; LUMO, lowest unoccupied MO). The S<sub>2</sub> state with A<sub>1</sub> symmetry can be assigned to the  $\pi - \pi^*$  excitation originated from the HOMO–LUMO single excitation. In Figure

 TABLE 1: Excitation Energies, Oscillator Strengths and the

 Main CSFs of PA Excitation Energy (in eV) Oscillator

 Strength Main CSFs<sup>a</sup>

	excitation energy (eV)	oscillator strength	main CSFs <sup>a</sup>
MRMP2 <sup>b</sup>			
$S_0(1^1A_1)^c$	0.0		0.936(closed shell)
$S_1(1^1B_2)$	4.232	0.001	0.645(2-1') + 0.576(1-2')
$S_2(2^1A_1)$	5.502	0.234	0.791(1-1')+0.361(3-1')
SDT-CI			
$S_0(1^1A_1)$	0.0		0.953(closed shell)
$S_1(1^1B_2)$	5.193	0.002	0.650(2-1') + 0.612(1-2')
$S_2(2^1A_1)$	6.629	0.230	0.842(1-1')-0.314(2-2')
SCI			
$S_0(1^1A_1)$	0.0		1.0(closed shell)
$S_1(1^1B_2)$	6.047	0.002	0.709(2-1') + 0.669(1-2')
$S_2(2^1A_1)$	6.122	0.126	0.835(1-1')+0.316(3-3')
/			-0.364(2-2')

<sup>*a*</sup> The CSFs of which absolute values of CI coefficients are greater than 0.3 are listed. Five occupied  $\pi$  orbitals and the lowest four unoccupied  $\pi^*$  ones in the order of energy are designated by 5,4,3,2,1(HOMO),1'(LUMO),2',3',4', respectively. 1–1' in the parenthesis, for instance, indicates the CSF of single excitation from orbital 1 to 1'. <sup>*b*</sup> The excitation energies are obtained by means of MRMP2 with (10,9)CASSCF wave function. The oscillator strengths are obtained by means of (10,9)CASSCF. <sup>*c*</sup> The symmetry label of each electronic state is under  $C_{2\nu}$  geometry.



**Figure 1.** Molecular orbitals relevant to  $S_1$  and  $S_2$  states at  $S_0$ -geometry.

1, the relevant MOs are shown to see what type of MOs contribute to  $S_1$  and  $S_2$ . The calculated excitation energies and the oscillator strengths are in agreement with the experimental absorption spectrum.<sup>11</sup> That is, the first absorption (279 nm, i.e., 4.444 eV) is weak, whereas the second one (239 nm, i.e., 5.188 eV) is strong.

Next we mention the optimized geometry of each state in Table 2. The numberings of atoms are shown in Figure 2. The S<sub>0</sub>-geometry is optimized to have  $C_{2\nu}$  symmetry. The bond distance of  $C^{\alpha} \equiv C^{\beta}$  (1.216 Å) is calculated to be very similar to that of a normal  $C \equiv C$  triple bond. On the other hand, the linkage bond of  $C^1-C^{\alpha}$  (1.448 Å) is slightly shorter than a normal C-Csingle bond, which is ascribed to somewhat resonance between the phenyl group and the triple bond of  $C^{\alpha} \equiv C^{\beta}$ . Furthermore, the C–C bond distances of the phenyl group (ca.  $1.40\text{\AA}$ ) take intermediate values between normal single and double bond distances, which are close to that of aromatic benzene. These features are in good agreement with the experimental value as well as the previous computational ones at restricted Hartree-Fock (HF) level.<sup>5,8-10</sup> The S<sub>1</sub>-geometry is also optimized to be  $C_{2\nu}$  symmetry. The most characteristic point of the S<sub>1</sub> geometry (see Table 1) is that the benzene rings enlarges. This can be

**TABLE 2:** Characteristic Optimized Parameters of PA

	$S_0$	$\mathbf{S}_1$	S <sub>2</sub> -planar	S <sub>2</sub> /S <sub>1</sub> -CIX	
Bond Distances (in Å)					
$R(C^{\alpha}-C^{\beta})$	1.216	1.210	$1.281(1.260)^{a}$	1.338	
$R(C^1-C^{\alpha})$	1.448	1.417	1.358 (1.373)	1.358	
$R(C^1-C^2)$	1.395	1.446	1.456 (1.446)	1.482	
$R(C^2-C^3)$	1.395	1.438	1.372 (1.372)	1.370	
$R(C^{3}-C^{4})$	1.398	1.432	1.445 (1.405)	1.411	
$R(C^4 - C^5)$	1.398	1.432	1.445 (1.405)	1.411	
$R(C^5 - C^6)$	1.395	1.438	1.372 (1.372)	1.370	
$R(C^{\beta}-H^{\beta})$	1.059	1.059	1.058 (1.054)	1.080	
bond Angles (in Degree)					
$\alpha (\langle C^1 C^\alpha C^\beta)$	180.0	180.0	180.0	179.7	
$\alpha(< C^{\alpha}C^{\beta}H^{\beta})$	180.0	180.0	180.0	121.3	
Dihedral Angles (in Degree)					
$< C^1 C^\alpha C^\beta H^\beta$		0		180.0	

<sup>*a*</sup> The values in the parentheses are those in  $S_1$  taken from ref 10.



Figure 2. Numbering of atoms in phenylacetylene.

 TABLE 3: Relative Energies (in eV) at the Important Conformations

	S <sub>0</sub> -geometry	S <sub>1</sub> -geometry	S <sub>2</sub> (planar)	$S_2/S_1$ -CIX
$egin{array}{c} \mathbf{S}_0 \ \mathbf{S}_1 \ \mathbf{S}_2 \end{array}$	0.0 4.232 5.503	3.980	4.265 5.230	5.218 5.022

TABLE 4: Rotational Constants (in MHz) of PA in  $S_0$ ,  $S_1$ , and  $S_2$ 

state	constant	ab initio	experiment <sup>a</sup>
$\mathbf{S}_0$	А	5670.70(5763.51) <sup>b</sup>	5681.5
	В	1512.88 (1602.99)	1529.8
	С	1194.26 (1214.76)	1204.9
$S_1$	А	5419.84	5459.6
	В	1479.73	1505.1
	С	1162.37	1179.9
S <sub>2</sub> (planar)	А	5241.01 (5567.44)	
-	В	1511.98 (1528.94)	
	С	1173.45	

<sup>*a*</sup> The values are taken from ref 19. <sup>*b*</sup> The values in parentheses are those in  $S_1$  taken from ref 10.

ascribed to the local  $\pi - \pi^*$  excitation within the benzene ring. That is, the occupied  $\pi$  electrons in the benzene ring are excited into unoccupied  $\pi^*$  orbitals, which leads to a weakening and lengthening of the relevant C-C bonds in the benzene ring. This feature is found in that of styrene in  $S_1$ .<sup>2</sup> As seen in Table 3, the energy at the  $S_1$ -geometry (3.980 eV) is lower than that at the  $S_0$ -geometry (4.232 eV). This implies that the  $S_1$  state characterized above is stable in the FC region with a long lifetime. Actually, PA in S1 has a long fluorescence lifetime of 43 ns. We justify the feature of the enlargement of the benzene ring by comparing the calculated rotational constants with the experimental ones.<sup>19</sup> In Table 4, we listed the computational and experimental rotational constants in  $S_0$  and  $S_1$ . It can be seen that they are in good agreement with each other. The remarkable decrease of  $\Delta A$  in  $S_1$  can be interpreted as the enlargement of the benzene ring.

We turn to discuss the geometrical feature of  $S_2$  in relation to the electronic structure.  $S_2$ -planar which is optimized under constraint of the planar is characterized as a quinoid structure with  $C_{2v}$  symmetry. The aromaticity of the benzene ring is completely lost. The bond distances of  $C^2-C^3$  and  $C^5-C^6$ becomes shorter than a normal C-C bond distance of aromatic benzene ring and closer to a normal C=C double bond, whereas the other becomes closer to a normal C-C single bond. The linkage bond distance of  $C^1-C^{\alpha}$  more shrinks to a normal C= C double bond, whereas the bond distance of  $C^{\alpha}-C^{\beta}$  elongates from a  $C \equiv C$  triple bond to a C = C double bond. In other words, the part of  $C^1C^{\alpha}C^{\beta}$  prefers to take an allene-like ( $C^1=C^{\alpha}=C^{\beta}$ ) structure in S<sub>2</sub> rather than the structure of  $C^1-C^{\alpha} \equiv C^{\beta}$ . This geometrical change of the  $C^1C^{\alpha}C^{\beta}$  part can be explained in terms of the nature of HOMO and LUMO, considering S2 is well described by HOMO-LUMO single excitation (refer to Figure 1). Upon electronic excitation into  $S_2$ , the out-of-plane  $\pi$  bonding orbital around the  $C^{\alpha}-C^{\beta}$  bond changes into the antibonding orbital and the  $\pi$  orbital in the linkage bond region changes from antibonding into bonding character. This is an explanation why the part of  $C^1C^{\alpha}C^{\beta}$  takes an allene-like structure in S<sub>2</sub>. Additionally, the drastic change of this part is suggestive to discuss the shape of the  $S_2$  potential energy surface around the S<sub>2</sub>-planar. That is, the electronic excitation into S<sub>2</sub> causes the change of the hybridizations of the carbon atom  $C^{\beta}$  from sp into sp<sup>2</sup>. As a consequence,  $H^{\beta}$  is preferable to be located out of the plane spanned by the remaining part. In other words, S<sub>2</sub>-planar is expected to be unstable with respect to the  $\langle H^{\beta}C^{\beta}C^{\alpha}$ out-of-plane bending motion, which will be mentioned in detail later

Here it may be worthwhile making comment on the difference between previous computational results and ours. Tzeng and co-workers performed the geometry optimization of S1 by means of single excitation CI (SCI or CIS in the terminology of the Gaussinan package) so as to obtain a quinoid stable structure in S<sub>1</sub>, which is similar to our S<sub>2</sub>-planar.<sup>10</sup> They mentioned that their S1 geometry well reproduces the rotational constants in S1, though our result at S1-geometry characterized as an enlarged benzene ring is much better (see Table 4). To check the difference, we performed two types of CI calculations at S<sub>0</sub>geometry, i.e., SCI and SDT-CI, where the CSFs up to triple excitations from the closed-shell HF configuration are included. The results are also listed in Table 1. The SDT-CI results are in qualitative agreement with the present MRMP2 results. That is, the main CSFs, oscillator strengths and the energy difference between S<sub>2</sub> and S<sub>1</sub> are similar to those by the more sophisticated method of MRMP2. In the SCI results, on the other hand, the electronic states of S1 and S2 are very close to each other around the FC region. So the excited state of which stable geometry is a quinoid stable structure may be  $S_1$  at their geometry optimization step by means of SCI. Furthermore, SCI results cannot explain the experimental absorption spectrum. Even in our SCI calculation, S<sub>1</sub>, whose absorption intensity is weak, is not well separated by S2 with strong intensity. This is not in agreement with the experimental findings.<sup>11</sup> Pratt et al. also pointed out the difference between SCI result and their experimental finding.<sup>19</sup> They found that  $S_1$  is *b*-axis polarized, whereas  $S_1$ by SCI is a-axis polarized because of the HOMO-LUMO single excitation. Therefore, we conclude that the SCI calculation is possible to give a wrong order among the excited states and the multiple excitations, inherently neglected in SCI calculations, are important to properly describe the local  $\pi - \pi^*$  excited state within the benzene ring.

Again we are back to discuss the photochemistry of PA based on our present calculations. The next concern is the internal conversion from  $S_2$  into  $S_1$ . So we did an optimization of the  $S_2/S_1$ -CIX. The characteristic optimized parameters are also listed in Table 2. Most of the parameters are similar to those of

# <u>detour pathway</u> A



direct pathway B



S<sub>2</sub>/S<sub>1</sub>-CIX

S<sub>0</sub>-geometry **Figure 3.** Schematic representation of possible internal conversion from  $S_2$  into  $S_1$ .



Figure 4. Potential energy curves with respect to the  $C^{\beta}-H^{\beta}$  out-of-plane mode ( $\beta$ ) by MRMP2 with (10,9)CASSCF wave function. Glossary of A-S<sub>1</sub>, for instance, means the potential energy curve of S<sub>1</sub> at a given  $\sigma_A$ .

TABLE 5: Relative Energies and the Main CSFs at  $S_2/S_1$ -CIX

	relative energy $(in eV)^a$	main CSFs <sup>b</sup>
$S_1$	5.218	0.610(2-1') +0.581(1-2')
$S_2$	5.022	0.884(1-1')

<sup>a</sup> The values are obtained by means of MRMP2 with the (10,9)CASS-CF wave function.<sup>b</sup> The CSFs of which absolute values of CI coefficients are greater than 0.3 are listed. Five occupied  $\pi$ -orbitals and the lowest four unoccupied  $\pi^*$ -ones in the order of energy are designated by 5,4,3,2,1(HOMO),1'(LUMO),2',3',4', respectively. 1-1' in the parenthesis, for instance, indicates the CSF of single excitation from orbital 1 to 1'.

S<sub>2</sub>-planar characterized as a quinoid structure. However, the following two are different from those of S2-planar. One is the bending angle of  $\langle H^{\beta}C^{\beta}C^{\alpha}$  (121.3, not 180 of S<sub>2</sub>-planar). The other is the allene part of  $C^1 = C^{\alpha} = C^{\beta}$ . That is, at the  $S_2/S_1$ -CIX, the two bond distances ( $C^1-C^{\alpha}$  and  $C^{\alpha}-C^{\beta}$ ) are similar to each other, which is found in many allenoid molecules in S<sub>0</sub>. These support that the partial structure of  $C^1C^{\alpha}C^{\beta}H^{\beta}$  is allene-like, as rationalized above. In Table 5, we listed the energy and the main CSFs by means of MRMP2 with (10,9)-CASSCF wave function at the (8,8)CASSCF S<sub>2</sub>/S<sub>1</sub>-CIX geometry. It can be seen that both electronic structures in  $S_1$  and  $S_2$ are still similar to the characters in the FC region but the energy difference between  $S_2$  and  $S_1$  is small enough to be a CIX. This implies that the S<sub>2</sub>/S<sub>1</sub>-CIX geometry by means of MRMP2 optimization with the (10,9)CASSCF wave function, which is quite unrealistic level of calculation for the present, is not so different from that of the present (8,8)CASSCF method.

Now we discuss the mechanism of the internal conversion from S<sub>2</sub> into S<sub>1</sub>, based on the ingredients of electronic and geometrical structures mentioned in the previous paragraphs. Our concern is about how PA in S<sub>2</sub> travels from the S<sub>0</sub>-geometry into  $S_2/S_1$ -CIX. There are two promising pathways of "detour" pathway A" and "direct pathway B", as shown in Figure 3 schematically. In Figure 4, we show the  $S_1$  and  $S_2$  potential energy curves with respect to the bending angle  $\beta$  (see Figure 2). Here we define a quinoid coordinate which ensures the continuous change of the geometrical parameters from Sogeometry into  $S_2$ -planar or  $S_2/S_1$ -CIX. The quinoid coordinates of  $Q_{iA}$  and  $Q_{iB}$  are expressed by the following:

$$\begin{split} Q_{iA} &= (1 - \sigma_A)Q_i(S_0\text{-geometry}) + \sigma_AQ_i(S_2\text{-planar}), \\ 0 &\leq \sigma_A \leq 1 \\ Q_{iB} &= (1 - \sigma_B)Q_i(S_0\text{-geometry}) + \sigma_BQ_i(S_2\text{/}S_1\text{-CIX}), \\ 0 &\leq \sigma_B \leq 1 \end{split}$$

In other words, the parameters  $\sigma_A$  and  $\sigma_B$  are a good measure of the extent that the aromaticity of the benzene ring at Sogeometry is lost. The S<sub>2</sub> potential energy for  $\sigma_j = 0$  (j = A and B) (i.e, geometrical parameters are fixed to be those of  $S_0$ -geometry except for  $\beta$ ) becomes unstable as the increment of  $\beta$ . As increment of  $\sigma_i$ , the S<sub>2</sub> potential curve for  $\sigma_B$  is lower

TABLE 6: Vibrational Frequencies (in cm<sup>-1</sup>) and L-Matrix Elements of the  $v_5$  Band<sup>*a*</sup>

state	geometry	$freq^a$	L-matrix elements <sup>b</sup>
$S_0$	S <sub>0</sub> -geometry	2099	$0.772(C^{\alpha}C^{\beta} \text{ str.})-0.559(C^{1}C^{\alpha} \text{ str.})$
$S_1$	S <sub>1</sub> -geometry	2065	$0.793(C^{\alpha}C^{\beta} \text{ str.})-0.541(C^{1}C^{\alpha} \text{ str.})$
$S_2$	$S_0$ -geometry( $\sigma_B = 0.0$ )	1959	$0.758(C^{\alpha}C^{\beta} \text{ str.})-0.572(C^{1}C^{\alpha} \text{ str.})$
$S_2$	$\sigma_{\rm B} = 0.25,  \beta = 0^{\circ}$	1900	$0.776(C^{\alpha}C^{\beta} \text{ str.})-0.576(C^{1}C^{\alpha} \text{ str.})$
$S_2$	$\sigma_{\rm B} = 0.5, \beta = 20^{\circ}$	1826	$0.710(C^{\alpha}C^{\beta} \text{ str.})-0.624(C^{1}C^{\alpha} \text{ str.})$

<sup>*a*</sup> The force constants in the  $a_1$  block under  $C_{2\nu}$  symmetry are scaled down by 0.82 (relating to C–H stretches) and 0.88 (others), respectively. The absolute values of the coefficients of the L-matrix larger than 0.3 are listed.

than that for  $\sigma_A$ . This means that the direct pathway is more realistic. Incidentally, for  $\sigma_B = 0.5$ , the S<sub>2</sub> curve becomes flat with respect to  $\beta$ , and for  $\sigma_B = 1.0$ , two curves of S<sub>1</sub> and S<sub>2</sub> crosses each other at a highly bending angle  $\beta$  so as for PA to relax from S<sub>2</sub> into S<sub>1</sub>. On the basis of the above discussion, we can deduce that PA in S<sub>2</sub> travels from S<sub>0</sub>-geometry into S<sub>2</sub>/S<sub>1</sub>-CIX without passing through the S<sub>2</sub>-planar (i.e., direct pathway B).

Next we make comment on the peculiar shape of the second absorption band. According to the work on PA in the low-lying excited states by King and So, the second structureless band is related to predissociation.<sup>11</sup> However, our interpretation is different from theirs. Vaida et al. found the characteristic 1846  $\pm$  15 cm<sup>-1</sup> interval of the vibrational mode.<sup>20</sup> They tentatively assigned it to the stretching vibration relating to the triple bond. In Table 6, we listed the calculated vibrational frequencies of the  $v_5$  band (a<sub>1</sub> mode under  $C_{2v}$  symmetry) with L-matrix coefficients. It is found that all of the  $\nu_5$  bands can be assigned to the coupling vibrational mode between the  $C^{\alpha}-C^{\beta}$  and  $C^{1}-C^{\beta}$  $C^{\alpha}$  stretches. The  $\nu_5$  band in S<sub>0</sub> at the S<sub>0</sub>-geometry is calculated to be 2099  $\text{cm}^{-1}$  which reproduces the experimental one (2120  $cm^{-1}$ ).<sup>6,7</sup> It is a typical triple C–C bond vibrational frequency. The  $\nu_5$  band in S<sub>1</sub> at S<sub>1</sub>-geometry is calculated to be 2065 cm<sup>-1</sup>, which is a little smaller than that in  $S_0$ . This is due to the resonance between the triple bond and the phenyl part so that the  $C^{\alpha}$ - $C^{\beta}$  part loses a bit of its triple bond character. The  $\nu_5$ band in S<sub>2</sub> around the FC region, ranging from S<sub>0</sub>-geometry at most to  $\sigma_{\rm B} = 0.5$ , is much smaller than those of S<sub>0</sub> and S<sub>1</sub> and is in agreement with the experimental one.20 So we conclude that the peculiar peaks over the broad absorption band is due to the  $C^1 = C^{\alpha} = C^{\beta}$  anti-stretch vibration characteristic in the allenoid molecules.

Finally, we point out the similarity of the photochemistry between PA and STY. As to the photochemistry of STY, we recently gave new insights of the photochemical behavior of STY to promote the experimental evidence:<sup>1-3</sup> (i) After the strong transition into S<sub>2</sub>, at the initial stage, STY in S<sub>2</sub> prefers to lose the aromaticity of the benzene ring for the photoisomerization; (ii) the S<sub>1</sub>/S<sub>0</sub>-CIX where the photoisomerization around the ethylenic double bond takes place is a crossing region between zwtterionic and covalent diradical states. The new insight (i) on STY is similar to the present picture on the initial process of PA. That is, the loss of the aromaticity of the benzene ring is essential to the internal conversion from S<sub>2</sub> into S<sub>1</sub> in both PA and STY.

#### **IV. Concluding Remarks**

In this paper, we reported on PA in  $S_1$  and  $S_2$  by means of ab initio CASSCF and MRMP2 calculations. Contrary to the

previous result by means of SCI calculations, the stable geometry in S<sub>1</sub> is characterized by the enlarged benzene ring. In S<sub>2</sub>, on the other hand, the aromaticity of the benzene ring is lost and an allenoid structure of  $C^1=C^{\alpha}=C^{\beta}$  is preferable than a structure of  $C^1-C^{\alpha}\equiv C^{\beta}$ , which is similar to optimized geometry of S<sub>1</sub> by previous SCI calculations. The experimental findings of the rotational constants, the vibrational frequencies, and the absorption spectrum can be reasonably interpreted by our present computational results of geometrical features.

Acknowledgment. The numerical calculations were partly performed in the Computer Center of Institute for Molecular Science. This work is financially supported by a Grant-in-Aid for Scientific Research (C) (No. 12640485) and Grant-in-Aid for Scientific Research on Priority Area (A) (Molecular Physical Chemistry) (No. 12042212) from the Ministry of Education, Culture, Sports, Science and Technology.

#### **References and Notes**

(1) Amatatsu, Y. Chem. Phys. Lett. 2001, 344, 200-206.

(2) Amatatsu, Y. J. Compt. Chem. 2002, 23, 928–937. The review on the photochemistry of styrene is also therein.

(3) Amatatsu, Y. J. Compt. Chem. 2002, 23, 950-956.

(4) Cox, A. P.; Ewart, I. C.; Stigliani, W. M. J. Chem. Soc. Fraday Trans. 2 1975, 71, 504-514.

(5) Shultz, G.; Nagy, T.; Portalone, G.; Ramondo, F.; Hargittai, I.; Domenicano, A. Struct. Chem. **1993**, *4*, 183–190.

(6) King, G. W.; So, S. P. J. Mol. Spectrosc. 1970, 36, 468-487.

(7) Singh, K. M.; Thakur, S. N. Indian J. Phys. 1995, 69B, 407-419.

(8) Czászár, A. G.; Fogarasi, G.; Boggs, J. E. J. Phys. Chem. 1989, 93, 7644-7651.

(9) Martin, P. S.; Yates, K.; Czismadia, I. G. J. Mol. Struct. (THEOCHEM) 1989, 183, 279-290.

(10) Narayanan, K.; Chang, G. C.; Shieh, K. C.; Tung, C. C.; Tzeng,
 W. B. Spectrochim. Acta A 1996, 52, 1703–1716.

(11) King, G. W.; So, S. P. J. Mol. Spectrosc. 1970, 37, 543-570.

(12) Sorkhabi, O.; Qi, F.; Rizvi, A. H.; Suits, A. G. J. Am. Chem. Soc. 2001, 123, 671–676.

(13) Swiderek, P.; Göötz, B. Ber. Bunsen-Ges. Phys. Chem. 1998, 102, 882-893.

(14) Powers, D. E.; Hopkins, J. B.; Smalley, R. E. J. Chem. Phys. 1981, 74, 5971–5976.

(15) Singh, K. M.; Singh, R. A.; Thakur, S. N. Indian J. Pure Appl. Phys. **1997**, 35, 5–9.

(16) Singh, H.; Laposa, J. D. J. Lumin. 1972, 5, 32-46.

(17) Bacon, A. R.; Hollas, J. M. Chem. Phys. Lett. 1985, 120, 477-480.

(18) Chia L.; Goodman, L. J. Chem. Phys. 1982, 76, 4745-4750.

(19) Ribblett, J. W.; Borst, D. R.; Pratt, D. W. J. Chem. Phys. 1999, 111, 8454-8461.

(20) Leopold, D. G.; Hemley, R. J.; Vaida, V. J. Chem. Phys. 1981, 75, 4758-4769.

(21) Schmidt, M. W.; Baldridge, K. K.; Boatz, J. A.; Elbert, S. T.; Gordon, M. S.; Jensen, J.H.; Koseki, S.; Matsunaga, N.; Nguyen, K. A.; Su, S. J.; Windus, T. L.; Dupuis, M.; Montgomery, Jr., J. A. J. Comput. Chem. **1993**, *14*, 1347–1363.

(22) Frisch, M. J.; Trucks, G. W.; Schlegel, H. B.; Scuseria, G. E.; Robb, M. A.; Cheeseman, J. R.; Zakrzewski, V. G.; Montgomery, J. A., Jr.; Stratmann, R. E.; Burant, J. C.; Dapprich, S.; Millam, J. M.; Daniels, A. D.; Kudin, K. N.; Strain, M. C.; Farkas, O.; Tomasi, J.; Barone, V.; Cossi, M.; Cammi, R.; Mennucci, B.; Pomelli, C.; Adamo, C.; Clifford, S.; Ochterski, J.; Petersson, G. A.; Ayala, P. Y.; Cui, Q.; Morokuma, K.; Malick, D. K.; Rabuck, A. D.; Raghavachari, K.; Foresman, J. B.; Cioslowski, J.; Ortiz, J. V.; Stefanov, B. B.; Liu, G.; Liashenko, A.; Piskorz, P.; Komaromi, I.; Gomperts, R.; Martin, R. L.; Fox, D. J.; Keith, T.; Al-Laham, M. A.; Peng, C. Y.; Nanayakkara, A.; Gonzalez, C.; Challacombe, M.; Gill, P. M. W.; Johnson, B. G.; Chen, W.; Wong, M. W.; Andres, J. L.; Head-Gordon, M.; Replogle, E. S.; Pople, J. A. *Gaussian 98*, revision A.7; Gaussian, Inc.: Pittsburgh, PA, 1998.