Theoretical Study of the Reaction Mechanism of BO, B₂O₂, and BS with H₂

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Potential energy surfaces of various reactions in the BO/H₂, B₂O₂/H₂, and BS/H₂ systems have been studied at the G2M(MP2)/B3LYP/6-311+G(d,p) level of theory. The BO + H₂ reaction is shown to proceed by abstraction of a hydrogen atom by B to produce OBH + H with the barrier and exothermicity of 8.3 and 6.8 kcal/mol, respectively. The reaction can also occur by 1,2-insertion of BO into the H-H bond or by H abstraction by the O atom; however, the barriers for these channels are much higher, 36.4 and 42.7 kcal/mol, respectively. Via a low ~ 0.3 kcal/mol barrier, the OBH + H reaction produces the OBH₂ radical, which is the most stable compound in the BO/H₂ system and lies 15.9, 2.5, and 4.2 kcal/mol below BO + H₂, trans-HBOH, and cis-HBOH, respectively. OBH₂ can isomerize to trans-HBOH overcoming a barrier of 27.7 kcal/ mol and the latter can rearrange to the cis conformer with a barrier of 10.8 kcal/mol. BOH and H can recombine and form *cis*- or *trans*-HBOH without barriers. In the $B + H_2O$ reaction, the reactants can first form a weakly bound $B-H_2O$ complex, which then can eliminate an H atom producing BOH + H or undergo insertion of B into an O-H bond giving *trans*-HBOH with barriers of 4.7 and 6.2 kcal/mol relative to the initial reactants, respectively, and *trans*-HBOH can eventually decompose to OBH + H and a minor amount of $BO + H_2$. Singlet OBBO is shown to be much less reactive with respect to H_2 than the BO monomer. Alternatively, after two BO recombine to form a triplet OBBO molecule over a moderate 8.3 kcal/mol barrier, t-OBBO can easily react with H_2 producing either BO + OBH₂ (via a t-OBBH₂O intermediate) or OBBOH + H with barriers of 4.4 and 7.4 kcal/mol, respectively. The reactions in the BS/H_2 system are shown to be similar to those for BO/H₂, except that BS cannot insert into H₂, SBH₂ resides in a much deeper potential well (37.3 kcal/mol below BS + H_2) and can rearrange both to *trans*- and *cis*-HBSH, the B- H_2S complex is more strongly bound than $B-H_2O$, and the $B+H_2S$ reaction is expected to be significantly faster than the reaction of $B + H_2O$.

Introduction

The oxidation of boron to solid or liquid B_2O_3 is a highly exothermic process and therefore boron is of interest as a potential component of propellants.¹⁻⁷ However, significant obstacles exist for practical use of elemental boron combustion, including the formation of a protective oxide layer that hinders the ignition of boron particles, the generation of boron oxyhydride intermediates which impede the combustion process, and also a slow condensation rate to the desired liquid or solid final product. When hydrogen is present, a substantial amount of boron gets trapped as metastable species such as HBO and HOBO, with less energy release than would occur with formation of B₂O₃. Because of these problems, extensive efforts are underway to create quantitative models for the complex processes of boron ignition and combustion and to study the detailed kinetics of homogeneous gas-phase^{4-6,8} and heterogeneous boron combustion.^{5,7} These modeling studies require first of all thermodynamic and kinetic data, including heats of reactions and activation barriers.⁹⁻¹¹ Accurate ab initio and density functional calculations of potential energy surfaces (PES) for the reactions involved in boron combustion are a valuable tool to achieve these data.

In the present paper, we report the results of such calculations for several reactions related to boron combustion. These include various reactions in the BO/H₂ system, such as BO + H₂ \rightarrow HBO + H, HBO + H \rightarrow OBH₂/HOBH, and B + H₂O \rightarrow products. Some of these reactions have been studied earlier experimentally¹²⁻¹⁷ and by various theoretical methods;¹⁸⁻²² however, a complete PES for the BO/H₂ system including all possible intermediates and transition states has not been scrutinized so far at a consistently high level of theory. We also consider the reaction of the boron oxide dimer B₂O₂ with molecular hydrogen and compare its reactivity with that of the monomer. In addition, we study PES and elucidate the gasphase reaction mechanism of boron sulfide BS with H₂ and compare the BO + H_2 and BS + H_2 reactions. To our knowledge, neither $B_2O_2 + H_2$ nor BS + H₂ reactions have been studied theoretically until now. The present calculations continue systematic investigations in our group²³⁻²⁷ of the reactions of diatomic oxides MO and sulfides MS with molecular hydrogen and reverse reactions of atoms with water and H₂S and provide reliable structures of various reactants, products, intermediates, and transition states as well as their energies within chemical accuracy.

Computational Details

We investigate the lowest doublet electronic state PESs for the BO + $H_2 \rightarrow B + H_2O$ and BS + $H_2 \rightarrow B + H_2S$ reactions

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TABLE 1. Total Energies (hartree), ZPE, and Relative Energies (kcal/mol) of Various Compounds in the BO + H₂ Reaction Calculated at the B3LYP/6-311+G(d,p), MP2/6-311G(d,p), CCSD(T)/6-311G(d,p), MP2/6-311+G(3df,2p), and G2M(MP2)//B3LYP/6-311+G(d,p) Levels of Theory

	B3LYP/6-311+G(d,p)		MP2/6-311G(d,p)		CCSD(T)/6-311G(d,p)		MP2/6-311+G(3df,2p)		G2M(MP2)	
	total		rel	total	rel	total	rel	total	rel	rel
species	energy	ZPE	energy	energy	energy	energy	energy	energy	energy	energy
BO $(C_{\infty v}, {}^{2}\Sigma^{+})$	-100.05887	2.74		-99.80119		-99.81545		-99.85654		
$H_2(D_{\infty h}, {}^1\Sigma_g^+)$	-1.17957	6.34		-1.16025		-1.16834		-1.16272		
$BO + H_2$	-101.23844	9.05	0	-100.96144	0	-100.98379	0	-101.01926	0	0
TS1 ($C_{\infty v}$, ${}^{2}\Sigma^{+}$)	-101.23260	8.45	3.08	-100.94554	9.39	-100.96956	8.34	-101.00351	9.29	8.25
H (² S)	-0.50216	0		-0.49981		-0.49981		-0.49981		
OBH $(C_{\infty v}, {}^{1}\Sigma^{+})$	-100.74744	9.01		-100.47875		-100.49552		-100.53581		
OBH + H	-101.24960	9.01	-8.12	-100.97856	-11.86	-100.99533	-7.28	-101.03562	-11.38	-6.81
TS2 (C_s , ² A')	-101.24856	9.32	-6.09	-100.97851	-10.45	-100.99531	-6.96	-101.03569	-10.05	-6.56
$OBH_2(C_{2v}, {}^2B_2)$	-101.28292	12.47	-24.56	-100.97630	-5.97	-101.01571	-16.68	-101.03289	-5.20	-15.90
TS3 (C_s , ² A')	-101.22942	11.08	7.65	-100.93532	18.38	-100.96249	15.36	-100.99877	14.85	11.82
t -HOBH (C_s , ² A')	-101.27354	14.94	-16.25	-100.98777	-10.75	-101.01128	-11.47	-101.04859	-12.63	-13.36
$TS4(C_1)$	-101.11561	10.81	78.80	-100.82054	90.14	-100.85398	83.18	-100.88062	88.72	81.76
TS5 (C_s , ² A')	-101.18857	10.74	32.95	-100.90061	39.83	-100.92310	39.74	-100.96384	36.43	36.35
c -HBOH (C_s , ² A')	-101.27052	14.63	-14.66	-100.98483	-9.21	-101.00819	-9.84	-101.04559	-11.05	-11.68
TS6 (C_1)	-101.25481	13.20	-6.20	-100.96513	1.75	-100.98881	0.92	-101.02847	-1.71	-2.54
TS7 (C_s , ² A')	-101.17204	7.54	40.19	-100.88243	48.1	-100.91029	44.64	-100.94336	46.15	42.69
BOH $(C_s, {}^1A')$	-100.66957	8.29		-100.39481		-100.42105		-100.45426		
BOH + H	-101.17173	8.29	41.12	-100.89462	41.18	-100.92086	38.74	-100.95407	40.16	37.72
TS8 (C_s , ² A')	-101.12355	10.49	73.51	-100.82013	90.09	-100.85493	82.27	-100.88116	88.07	80.26
$B-H_2O(C_{2v}, {}^2B_2)$	-101.13100	14.05	72.32	-100.84153	80.15	-100.87369	73.99	-100.89924	80.22	74.06
$B + H_2O$	-101.12093	13.36	77.97	-100.83307	84.78	-100.86773	77.06	-100.89332	83.25	75.53
TS9 (C_s , ² A')	-101.22901	9.60	6.46	-100.93688	15.95	-100.96050	15.15	-100.99657	14.78	13.98

as well as singlet and triplet PESs of the $B_2O_2 + H_2$ reaction. On these surfaces, full geometry optimizations were run to locate all local minima and transition states at the B3LYP/6-311+G-(d,p) level of theory.^{28,29} Harmonic vibrational frequencies were obtained at the same level to characterize the stationary points as minima or first-order saddle points, to obtain zero-point vibrational energy corrections (ZPE), and to generate force constant data needed in the intrinsic reaction coordinate (IRC) calculation. To predict more reliable ZPE, the raw calculated B3LYP/6-311+G(d,p) ZPE values were scaled 0.9806 to account for their average overestimation.³⁰ The IRC method³¹ was used to track minimal energy paths from transition structures to corresponding minima. A step size of 0.1 amu1/2 bohr or larger was used in the IRC procedure. The relative energies have been refined by using the modified Gaussian-2 G2M(MP2) theory³² with B3LYP/6-311+G(d,p) optimized geometries. All the ab initio calculations described here were performed employing the Gaussian 98 programs.33

Results and Discussion

BO + $H_2 \rightarrow B$ + H_2O Reaction. Total energies and ZPE corrected relative energies of various compounds in the BO + $H_2 \rightarrow B + H_2O$ reaction calculated at the B3LYP/6-311+G(d,p), MP2/6-311G(d,p), MP2/6-311+G(3df,2p), and CCSD-(T)/6-311G(d,p) levels of theory and their G2M(MP2) relative energies are listed in Table 1. Table 2 presents calculated vibrational frequencies. The BO + H_2 potential energy diagram along the reaction path computed at the G2M(MP2) level and the optimized geometries of various compounds along the predicted reaction pathway are shown in Figure 1.

Three mechanisms are possible in the reaction of boron oxide with molecular hydrogen, including abstraction of an H atom of H₂ by B and O atoms of BO and insertion of boron oxide into the H-H bond. The most favorable mechanism is the abstraction of H by the B atom, BO + H₂ \rightarrow OBH + H, proceeding via transition state TS1. The barrier for this process is calculated to be 8.3 kcal/mol. The transition state has a linear $C_{\infty v}$ -symmetric geometry that ensures the most efficient inter-

TABLE 2. Vibrational Frequencies (cm⁻¹) of Various Compounds in the BO + H₂ Reaction Calculated at the B3LYP/6-311+G(d,p) Level

species	frequencies
BO	1916
TS1 (B3LYP)	591 <i>i</i> , 10, 10, 886, 886, 1885, 2240
TS1 $(MP2)^a$	1230 <i>i</i> , 116, 116, 982, 982, 1758, 2128
OBH	768, 768, 1865, 2902
TS2	375i, 268, 762, 784, 1832, 2877
OBH ₂	548, 907, 980, 1408, 2425, 2459
TS3	1818 <i>i</i> , 637, 904, 1419, 2162, 2629
trans-HBOH	748, 870, 1090, 1330, 2574, 3837
TS4	1344 <i>i</i> , 302, 649, 1084, 2091, 3433
TS5	1681 <i>i</i> , 868, 985, 1560, 1971, 2130
cis-HBOH	739, 845, 1079, 1341, 2531, 3701
TS6	979i, 571, 968, 1301, 2467, 3929
TS7	635 <i>i</i> , 192, 697, 815, 1468, 2103
BOH	570, 1411, 3816
TS8	1671 <i>i</i> , 359, 773, 1030, 1384, 3789
$B-H_2O$	138, 215, 508, 1567, 3660, 3745
TS9	1554 <i>i</i> , 601, 776, 857, 1666, 2818

^{*a*} Calculated at the MP2/6-311G(d,p) level with the MP2/6-311G(d,p) optimized geometry.

action between the singly occupied σ orbital of BO ($^{2}\Sigma^{+}$) composed mostly of the p_z orbital of the boron atom and $\sigma_{\rm g}$ and σ_u orbitals of H₂. The resulting OBH molecule is also linear and the BO + $H_2 \rightarrow OBH + H$ reaction is 6.8 kcal/mol exothermic. In TS1, the breaking H-H bond is stretched by 14% as compared to that in an isolated H₂ molecule, while the forming B-H bond is 35% longer than that in the OBH product. This indicates an early character of the transition state, in line with the finding that the reaction is exothermic. The $BO + H_2$ \rightarrow OBH + H reaction has been carefully investigated earlier. The reaction exothermicity was computed to be 6.4, 7.8, and 7.1 kcal/mol at the MRCI/TZ2P,²¹ G2,³⁴ and CBS-Q³⁵ levels, respectively, all in close agreement with our present value. The reaction barrier obtained by Page using the MRCI/TZ2P method is 9.5 kcal/mol,²¹ about 1.2 kcal/mol higher than the G2M(MP2) result.



Figure 1. Potential energy diagram for various reactions in the BO/H_2 system calculated at the G2(MP2) level. Relative energies are given in kcal/mol. Geometric structures (bond lengths in Å and bond angles in deg) of various intermediates and transition states optimized at the B3LYP/ 6-311+G(d,p) level of theory are also shown.

In a secondary OBH + H reaction, the OBH molecule can recombine with H and addition of the latter to the middle B atom is more favorable than the addition to the terminal oxygen. Indeed, the barrier at TS2 for the OBH + H \rightarrow OBH₂ reaction is only ~ 0.25 kcal/mol, while that at TS9 for the OBH + H \rightarrow cis-HBOH reaction is 20.5 kcal/mol higher. TS2 has a very early and loose character with the forming B-H bond as long as 2.180 Å. Alternatively, TS9 is a much tighter and later transition state, where the forming O-H bond is only 16% longer than the O-H bond in the *cis*-HBOH product. The $C_{2\nu}$ -symmetric OBH₂ (²B₂) radical is the global minimum in the BO/H₂ system, which resides 15.9 kcal/mol lower in energy than the initial $BO + H_2$ reactants. The planar cis-HBOH (2A') isomer is 4.2 kcal/mol less stable than OBH_2 and lies 11.7 kcal/mol below $BO + H_2$. This value is somewhat lower than the G2 result by Duan et al., 14.0 kcal/mol.³⁴ The third isomer is planar trans-HBOH (²A'), 2.6 kcal/mol less stable than OBH₂ (²B₂) but 1.7 kcal/ mol more favorable than *cis*-HBOH (²A'). The energy difference between the trans- and cis-HBOH conformers computed at the G2 level is very similar, 1.8 kcal/mol.34 trans-HBOH lies 13.4 (G2M(MP2)), 15.8 (G2), 34 and 15.3 (CBS-Q)35 kcal/mol lower in energy than $BO + H_2$. It should be noted that we were not able to find a transition state leading directly from OBH + H to trans-HBOH; a search of a first-order single point starting from a trans conformation of TS9 converged back to TS9, which connects OBH + H with *cis*-HBOH.

The three isomers of the H₂BO species can rearrange to each other. For instance, migration of a hydrogen atom from B to O in OBH₂ gives *trans*-HBOH via a planar transition state TS3. The barrier at TS3 is significant, 27.7 and 25.2 kcal/mol relative to OBH₂ and *trans*-HBOH, respectively. In turn, *trans*-HBOH can undergo rotation around the B–O bond to produce *cis*-

HBOH via an asymmetric transition state TS6. The barrier in this case is much lower, 10.8 and 9.1 kcal/mol relative to transand cis-HBOH, respectively. The B-O bond in HBOH seems to have a single character and the bond elongates only by ~ 0.01 Å in the transition state. Nevertheless, the barrier at TS6 is rather large for a rotation about an ordinary single bond. Natural bond population analysis for HBOH indicates an additional dative character of the B–O bond with $\sim 0.2 e$ transferred from the p_z lone pair of the oxygen atom to the p_z empty orbital of boron. This dative interaction is upset when the planarity of the molecule is violated, which causes the increase of the barrier. The trans-HBOH molecule can eventually dissociate to the B + H₂O products although this reaction is highly endothermic. This process involves two steps, hydrogen transfer from B to O leading to formation of a B-H2O complex via transition state TS4 and dissociation of the complex occurring without an exit barrier. The barrier at the asymmetric TS4 is 95.1 kcal/mol and the complex resides 87.4 and 74.1 kcal/mol above trans-HBOH and BO + H₂, respectively. B-H₂O has a planar $C_{2\nu}$ -symmetric geometry and ${}^{2}B_{2}$ electronic state and is stabilized only by 1.5 kcal/mol with respect to the boron atom and water molecule. The overall endothermicity of the BO + $H_2 \rightarrow B + H_2O$ reaction is computed to be 75.5 kcal/mol, close to the experimental value of 76.7 kcal/mol³⁷ and to the CBS-Q result by Politzer et al., 76.0 kcal/mol.35

The second channel of the BO + H₂ reaction proceeds by the 1,2-insertion of BO into the H–H bond of the molecular hydrogen producing the *cis*-HBOH isomer. The reaction barrier at a transition state TS5 is rather high, 36.4 kcal/mol. TS5 has a planar rhomb-shaped structure and ²A' electronic state. Such an arrangement provides an overlap between the singly occupied σ orbital of BO (p_{σ} on the B atom) and the antibonding vacant $\sigma_{\rm u}$ orbital of H₂ and makes possible the electron density transfer from the former to the latter, which leads to the H–H bond cleavage. Alternatively, we were not able to find a transition state for the 1,1-insertion of the boron atom of BO into H₂ producing OBH₂. If the hydrogen molecule approaches BO within C_{2v} symmetry perpendicularly to the B–O line, the BO $(^{2}\Sigma^{+}) + H_2 (^{1}\Sigma_g^{+}) \rightarrow OBH_2 (^{2}B_2)$ reaction is symmetry forbidden, as the overall wave function of the reactants is $^{2}A_1$ within the C_{2v} point group. Once symmetry is released, the transition state search converges to the hydrogen abstraction transition state TS1. One can also see that the insertion mechanism leading to *cis*-HBOH is much less favorable than the H-abstraction channel producing OBH + H because the barrier at TS5 is 28.1 kcal/mol higher than that at TS1.

The third, least favorable channel of the $BO + H_2$ reaction is H-abstraction from H₂ by the oxygen atom of the boron oxide leading to the BOH + H products. The barrier at the corresponding TS7 is computed to be 42.7 kcal/mol and BOH + H lie 37.7 kcal/mol higher in energy than the reactants. The reaction heats computed earlier at the G2 and CBS-Q levels of theory are similar, 37.4 and 38.6 kcal/mol, respectively. In accord with the fact that the reaction is endothermic, TS7 exhibits a late character, with the breaking H-H bond stretched to 1.280 Å, 72% longer than the H–H distance in free H_2 , and the forming O-H bond is only 5% longer than that in the BOH product. The BOH angle in TS7 (129.7°) is also rather similar to that in BOH (124.7°), while the OHH fragment is nearly linear. TS7 has a planar geometry and ²A' electronic state. If secondary collisions are possible under the reaction conditions, BOH can easily recombine with H to produce cis- or trans-HBOH without a barrier. The transition state search for the H atom elimination from B in the two HBOH conformers converged to the BOH + H products thus confirming that the highly exothermic BOH + H \rightarrow cis-HBOH (-49.4 kcal/mol) and BOH + H \rightarrow trans-HBOH (-51.1 kcal/mol) reactions are barrier-free. Finally, the hydrogen atom can also add to the oxygen of BOH to produce the B-H₂O complex. This reaction is 36.3 kcal/mol endothermic and proceeds via a late transition state TS8 over a barrier of 42.5 kcal/mol. Evidently, the BOH $+ H \rightarrow B - H_2O \rightarrow B + H_2O$ reaction channel is not expected to be competitive with the barrierless H additions forming cisand trans-HBOH and with the reverse H abstraction reaction BOH + H \rightarrow BO + H₂ occurring via a 5.0 kcal/mol barrier.

 $\mathbf{B} + \mathbf{H}_2\mathbf{O}$ Reaction. As seen in Figure 1, the B + H₂O reaction can proceed by two different mechanisms following the formation of the weak B-H₂O complex. The first channel leads to trans-HBOH over a barrier of 6.2 kcal/mol at TS4. Then, the trans-HBOH molecule can isomerize to cis-HBOH and the latter would decompose to either OBH + H or BO + H₂. Alternatively, trans-HBOH can rearrange to OBH₂ and then dissociate to OBH + H. After TS4 is cleared, all intermediates and transition states lie significantly lower in energy than the $B + H_2O$ reactants. The second channel of the $B + H_2O$ reaction involves elimination of a hydrogen atom via TS8 via a lower 4.7 kcal/mol barrier leading to the BOH + H products. Secondary recombination of BOH and H is most likely to produce chemically activated cis- or trans-HBOH, which eventually decompose to OBH + H or less probably to BO + H₂. We can expect that the B + H₂O \rightarrow B-H₂O \rightarrow TS8 \rightarrow BOH + H reaction channel is slightly more preferable than B + H₂O \rightarrow B-H₂O \rightarrow TS4 \rightarrow trans-HBOH \rightarrow products (OBH + H or BO + H₂), as the barrier at TS8 is 1.5 kcal/mol lower than that at TS4. Summarizing, we conclude that BOH + Hand OBH + H should be major reaction products and a minor amount of $BO + H_2$ also can be formed. This conclusion qualitatively agrees with that made by Alberti et al. on the basis of their quasiclassical trajectory calculation.²² If the trans- and cis-HBOH and OBH₂ intermediates can be stabilized by collisions or in an inert matrix, they can be observed too. In matrix isolation experiments, Jeong et al.¹⁶ identified the HBOH product of the $B + H_2O$ reaction based on the observation of a 1408-cm⁻¹ IR band and two weak bands at 2536 and 2571 cm⁻¹. On the other hand, Andrews and Burkholder¹⁷ assigned the major reaction products as HBO and BO. They also observed several absorption peaks between 1408 and 1450 cm⁻¹, but those were assigned to the BOB and OBOB species rather than to HBOH. As seen in Table 2, the 1408-cm⁻¹ peak could additionally belong to the IR spectra of BOH or OBH₂, while the bands at 2536 and 2571 cm⁻¹ indeed can be due to *cis*- and trans-HBOH, respectively. Possibly all of the above-mentioned products were formed in some amounts in the experiments.

There still has been a controversy in the literature of what is the barrier for the B + H_2O reaction. Early MP2/6-31G* calculations by Sakai and Jordan¹⁸ gave the value of \sim 12 kcal/ mol for the barrier of insertion of B into an O-H bond of H₂O corresponding to our TS4. Alberti et al.²² used a value of about 20 kcal/mol in their analytical PES employed for the quasiclassical trajectory calculations. On the other hand, more recent B3LYP calculations by Wang and Huang³⁸ indicated that the insertion barrier is in the range of 0.0 kcal/mol with respect to the initial reactants and the reaction first proceeds via a rather stable B-OH₂ complex, 5.1 kcal/mol below $B + H_2O$ at their best B3LYP/6-311++G(3df,2p) level. Our higher level CCSD-(T)/6-311G(d,p) and G2M(MP2) results show that the B + H₂O reaction does have a significant insertion barrier, 6.1-6.2 kcal/ mol. Moreover, we demonstrate for the first time that the B + H_2O reaction can directly produce BOH + H through elimination of an H atom from the B-H₂O complex and the H loss barrier is somewhat lower than the insertion barrier.

Rate Constants of the Reactions in the BO/H₂ System. We carried out transition state theory (TST) calculations with Wigner's tunneling corrections³⁶ of the rate constants for various reactions in the 300-3000 K temperature range:

$$k = \left(\frac{RT}{p^{\phi}}\right)^{-\Delta n^{*}} \frac{k_{\rm B}T}{h} e^{-\Delta G_{0}^{*}/RT}$$
$$Q_{\rm tun} = 1 - \frac{1}{24} \left(\frac{hv_{\rm S}}{k_{\rm B}T}\right)^{2} (1 + k_{\rm B}T/E_{0})$$

where *R* is the Rydberg constant, k_B is the Boltzmann constant, *h* is the Planck constant, *T* and p^{ϕ} are the temperature and the standard pressure, respectively, Δn^{\dagger} is the change of the number of moles from reactants to the transition state, ΔG_0^{\dagger} is the change of the Gibbs free energy from reactants to the transition state, v_S is the transition state imaginary frequency, and E_0 is the barrier height including ZPE correction. The resultant fitted three-parameter AT^Bexp(-C/T) expressions for the rate constants are collected in Table 3. For the reactions which have a unimolecular character in the forward or reverse direction, the TST rates correspond to the high-pressure limit, while their pressure dependence can be evaluated by using RRKM theory, which is beyond the scope of this paper.

For the BO + H₂ reaction, we compared the calculated rates with those predicted by Page²¹ and with available experimental data.^{12,13} It should be noted that the B3LYP/6-311+G(d,p) calculations gave a very low value of 10 cm⁻¹ for the lowest degenerate vibrational frequency of TS1 (see Table 2). This is

TABLE 3. Fitted Three-Parameter Expressions for Rate Constants of Various Reactions in the BO/H₂ System in the Temperature Range of 300–3000 K

reaction	expression	units		
$BO + H_2 \rightarrow TS1 \rightarrow OBH + H$	$2.94 \times 10^{-19} T^{2.57} \exp(-2903/T)$	cm^3 molecule ⁻¹ s ⁻¹		
	$7.49 \times 10^{-23} T^{3.53} \exp(-1590/T)^a$			
$OBH + H \rightarrow TS1 \rightarrow BO + H_2$	$7.01 \times 10^{-16} T^{1.77} \exp(-6921/T)$	cm^3 molecule ⁻¹ s ⁻¹		
$OBH + H \rightarrow TS2 \rightarrow OBH_2$	$2.78 \times 10^{-13} T^{1.002} \exp(+159.3/T)$	cm^3 molecule ⁻¹ s ⁻¹		
$OBH + H \rightarrow TS9 \rightarrow cis$ -HBOH	$2.78 \times 10^{-14} T^{1.10} \exp(-9659/T)$	cm ³ molecule ⁻¹ s ⁻¹		
$OBH_2 \rightarrow TS2 \rightarrow OBH + H$	$2.43 \times 10^{12} T^{0.60} \exp(-5014.5/T)$	s^{-1}		
$OBH_2 \rightarrow TS3 \rightarrow trans-HBOH$	$2.41 \times 10^{12} T^{0.33} \exp(-13652/T)$	s^{-1}		
cis -HBOH \rightarrow TS9 \rightarrow OBH + H	$3.32 \times 10^{10} T^{0.93} \exp(-12590/T)$	s^{-1}		
cis -HBOH \rightarrow TS6 \rightarrow trans-HBOH	$1.46 \times 10^{12} T^{0.37} \exp(-4610/T)$	s^{-1}		
$trans$ -HBOH \rightarrow TS3 \rightarrow OBH ₂	$2.39 \times 10^{11} T^{0.62} \exp(-12303/T)$	s^{-1}		
$trans$ -HBOH \rightarrow TS6 \rightarrow cis -HBOH	$1.22 \times 10^{12} T^{0.41} \exp(-5448/T)$	s^{-1}		
<i>trans</i> -HBOH \rightarrow TS4 \rightarrow B + H ₂ O	$2.17 \times 10^{11} T^{0.80} \exp(-47784/T)$	s ⁻¹		
$B + H_2O \rightarrow TS4 \rightarrow trans-HBOH$	$1.92 \times 10^{-17} T^{2.00} \exp(-2069/T)$	cm ³ molecule ⁻¹ s ⁻¹		
$B + H_2O \rightarrow TS8 \rightarrow BOH + H$	$7.22 \times 10^{-18} T^{2.10} \exp(-1159/T)$	cm^3 molecule ⁻¹ s ⁻¹		
$BOH + H \rightarrow TS7 \rightarrow BO + H_2$	$4.34 \times 10^{-16} T^{1.62} \exp(-1791/T)$	cm^3 molecule ⁻¹ s ⁻¹		

^a Recommended expression from ref 12.



Figure 2. Arrhenius plot of experimental and calculated rate constants for the BO + $H_2 \rightarrow OBH + H$ reaction. The plain curve marked with open circles shows recommended values from ref 13. The bold line depicts experimental rates from ref 12. The long-dashed (marked with open squares) and short-dashed (marked with "×") curves show theoretical rate constants calculated in ref 21 and in the present work, respectively.

apparently an artifact of the method because TST calculations with this value give an unphysically fast growth of the rate constant with temperature. Hence, we reoptimized the structure and recalculated frequencies of TS1 at the MP2/6-311G(d,p) level. The changes in the optimized bond lengths are small and their effect on the G2M(MP2) energy of TS2 is negligible. As seen in Table 2, the frequency changes are also not very large, except for the lowest degenerate frequency, 116 cm⁻¹ at the MP2 level. This seems to be a more reasonable result, although it is somewhat lower than the 173 cm^{-1} obtained by Page at a lower CASSCF(3,3)/DZP level.²¹ Therefore, we used the MP2/ 6-311G(d,p) vibrational frequencies scaled by 0.949630 (except for the lowest 116-cm⁻¹ frequency which was scaled by 1.0127³⁰) to compute the TST rate constants. The results are shown in Figure 2. As one can see, the calculated rates closely agree with recommended rate constants for the 500-3000 K temperature range¹³ and with the rates measured experimentally between 690 and 1030 K.12 The deviation from experiment at low temperatures may be due to small curvature tunneling effects, which are not taken into account in our simple treatment of the tunneling correction. Direct dynamics calculations would



Figure 3. Arrhenius plot of calculated rate constants for the B + H2O \rightarrow TS8 \rightarrow BOH + H (marked with solid squares) and B + H2O \rightarrow TS4 \rightarrow *trans*-HBOH (marked with solid circles) reactions.

be able to provide more accurate rate constants for the lowtemperature range. The rates obtained by Page using TST calculations based on his MRCI/TZ2P//CASSCF/DZP PES²¹ significantly underestimate experimental and our values, indicating that the reaction barrier is overestimated at that level of theory. Indeed, lowering the calculated barrier from 9.5 to 8.5 kcal/mol and adjustment of the lowest degenerate frequency of the transition state from 173 to 134 cm⁻¹ led¹² to excellent agreement between experimental and TST rate constants. Our present higher level calculations confirm this result.

For the B + H2O reaction (see Figure 3), the calculated rate constants indicate that the BOH + H reaction channel occurring via TS8 is faster than the formation of *trans*-HBOH via TS4 for the entire 300-3000 K temperature range. However, the BOH + H/*trans*-HBOH branching ratio decreases from 93/7 at 300 K to 51.6/48.4 at 3000 K.

 $B_2O_2 + H_2$ Reaction. Density functional calculations of PES for the B + H₂O and B₂ + H₂O reactions by Wang and Huang³⁸ showed that the boron dimer has a higher reactivity than B in inserting into water. In this view, we considered the reaction of the boron oxide dimer with H₂ and compared the reactivity of B₂O₂ with respect to molecular hydrogen with that of BO. The most stable isomer of the boron dimer is linear OBBO, which is 72.3 kcal/mol more stable than a cyclic form at the B3PW91 level.³⁵ Therefore, we have studied PES of the OBBO

TABLE 4. Total Energies (hartree), ZPE, and Relative Energies (kcal/mol) of Various Compounds in the $B_2O_2 + H_2$ Reaction Calculated at the B3LYP/6-311+G(d,p), MP2/6-311G(d,p), CCSD(T)/6-311G(d,p), MP2/6-311+G(3df,2p), and G2M(MP2)//B3LYP/6-311+G(d,p) Levels of Theory

	B3LYP/6-311+G(d,p)			MP2/6-311G(d,p)		CCSD(T)/6-311G(d,p)		MP2/6-311+G(3df,2p)		G2M(MP2)
	total		rel	total	rel	total	rel	total	rel	rel
species	energy	ZPE	energy	energy	energy	energy	energy	energy	energy	energy
$s-B_2O_2(D_{\infty h}, {}^1\Sigma_g^+)$	-200.30435	8.48		-199.79106		-199.81486		-199.90064		
$s-B_2O_2 + H_2$	-201.48392	14.79	0	-200.95131	0	-200.98320	0	-201.06336	0	0
s-TS1 (C_1)	-201.40964	17.29	49.06	-200.86884	54.19	-200.90120	53.90	-200.98695	50.40	50.10
s-cis-OBB(H)OH	-201.50763	21.77	-8.03	-200.96575	-2.22	-201.00225	-5.12	-201.08262	-5.25	-8.14
$(C_s, {}^1\mathrm{A'})$										
s-TS2 (C_1)	-201.48372	20.04	5.27	-200.93747	13.83	-200.97375	11.07	-201.05789	8.58	5.82
s-trans-OBB(H)OH	-201.50657	21.80	-7.34	-200.96451	-1.41	-201.00094	-4.27	-201.08198	-4.81	-7.67
$(C_{s}, {}^{1}A')$										
s-TS3 (C_s , ¹ A')	-201.40259	17.00	53.21	-200.86153	58.51	-200.89484	57.61	-200.97981	54.60	53.70
s-TS4 (C_s , ¹ A')	-201.37208	17.46	72.80	-200.82704	80.60	-200.86060	79.54	-200.94449	77.21	76.15
OBH + OBH	-201.49487	15.82	-5.86	-200.95749	-2.87	-200.99105	-3.92	-201.07161	-4.17	-5.22
$t-B_2O_2(C_s, {}^{3}A')$	-200.12818	6.73		-199.59124		-199.63275		-199.70010		
$t-B_2O_2 + H_2$	-201.30775	13.06	108.85	-200.7515	123.69	-200.80109	112.58	-200.86283	124.13	113.03
t-TS1 (C_1)	-201.30623	14.35	111.07	-200.74460	129.28	-200.79474	117.83	-200.85735	128.84	117.39
t-OBBH ₂ O (C_s , ³ A ^{$\prime\prime$})	-201.36582	16.12	75.41	-200.79069	102.09	-200.84953	85.18	-200.90026	103.65	86.74
$t-TS2 (C_s, {}^{3}A'')$	-201.34143	15.74	90.34	-200.77661	110.55	-200.83053	96.73	-200.88861	110.58	96.76
$BO + OBH_2$	-201.34180	15.21	90.23	-200.77749	109.49	-200.83117	95.81	-200.88943	109.56	95.88
t-TS3 (C_s , ³ A')	-201.30376	14.40	112.67	-200.74128	131.41	-200.79061	120.46	-200.85340	131.36	120.42
OBBOH $(C_s, {}^2A') + H$	-201.33840	15.18	91.70	-200.79933	95.75	-200.83219	95.14	-200.91489	93.55	92.94
t-TS4 (C_s , ³ A')	-200.10815	5.83	120.27^{a}	-199.58531	126.46 ^a	-199.61661	121.75^{a}	-199.69763	124.74^{a}	120.03^{a}

^{*a*} Relative energy is given with respect to s-B₂O₂.

TABLE 5. Vibrational Frequencies (cm⁻¹) of Various Compounds in the B₂O₂ + H₂ Reaction Calculated at the B3LYP/ 6-311+G(d,p) Level

species	frequencies				
s-B ₂ O ₂	216, 498, 503, 616, 1961, 2135				
s-TS1	1816 <i>i</i> , 193, 240, 495, 518, 675, 979, 1100, 1614, 1982, 2029, 2267				
s-cis-OBB(H)OH	190, 284, 489, 656, 702, 913, 1005, 1187, 1363, 2010, 2597, 3832				
s-TS2	880 <i>i</i> , 177, 280, 487, 512, 711, 849, 1121, 1315, 1999, 2573, 3993				
s-trans-OBB(H)OH	175, 285, 503, 671, 701, 891, 1022, 1175, 1346, 2005, 2639, 3836				
s-TS3	1887 <i>i</i> , 184, 187, 374, 473, 692, 790, 992, 1546, 1956, 1976, 2715				
s-TS4	1723 <i>i</i> , 171, 265, 349, 582, 706, 897, 1135, 1605, 1985, 2037, 2481				
$t-B_2O_2$	150, 282, 380, 666, 1289, 1946				
t-TS1	301i, 140, 156, 229, 306, 389, 494, 627, 671, 1277, 1956				
t-OBBH ₂ O	145, 240, 379, 474, 572, 590, 643, 783, 1248, 1983, 2087, 2129				
t-TS2	87 <i>i</i> , 44, 47, 139, 213, 544, 885, 970, 1379, 1913, 2419, 2454				
t-TS3	471 <i>i</i> , 168, 188, 300, 362, 441, 442, 575, 671, 1322, 1967, 3637				
OBBOH	176, 206, 279, 458, 611, 988, 1456, 1971, 3677				
t-TS4	322 <i>i</i> , 60, 106, 332, 1683, 1900				

+ H_2 reaction. The dimer has the ${}^{1}\Sigma_{g}{}^{+}$ ground electronic state and is bound by 111.7 kcal/mol (at the G2M(MP2) level) with respect to two monomers.

Total energies and ZPE corrected relative energies of various compounds in the OBBO + H₂ reaction in the ground singlet and lowest triplet electronic states calculated at the B3LYP/6-311+G(d,p), MP2/6-311G(d,p), MP2/6-311+G(3df,2p), and CCSD(T)/6-311G(d,p) levels of theory and their G2M(MP2) relative energies are listed in Table 4, while Table 5 shows calculated vibrational frequencies. The OBBO + H₂ potential energy diagram along the reaction path computed at the G2M-(MP2) level and the optimized geometries of various compounds along the predicted reaction pathways are shown in Figure 4. In accord with its higher stability as compared to BO, OBBO exhibits a lower reactivity. We found two channels for the $OBBO + H_2$ reaction. The first mechanism is 1,2-insertion of a BO fragment into the H-H bond proceeding via transition state s-TS1 via a barrier of 50.1 kcal/mol. This process leads to a cis-OBB(H)OH intermediate residing 8.1 kcal/mol below the reactants. As one can see, the 1,2-insertion barrier for OBBO is 13.8 kcal/mol higher than that for the BO monomer. Next, cis-OBB(H)OH can isomerize to a trans conformer by rotation around the B-O bond. The calculated barrier is 14.0 kcal/mol and it occurs at s-TS2. The *trans*-OBB(H)OH isomer lies 0.5 kcal/mol higher in energy than the cis form. *trans*-OBB(H)OH can dissociate to two OBH molecules through 1,2-hydrogen migration from one boron atom to the other accompanied by a cleavage of the B–B bond. The corresponding transition state s-TS3 lies 53.7 and 61.4 kcal/mol above OBBO + H₂ and *trans*-OBB(H)OH, respectively. The overall exothermicity of the OBBO + H₂ \rightarrow 20BH is calculated to be 5.2 kcal/mol at the G2M(MP2) level, somewhat higher than the CBS-Q value of 2.3 kcal/mol.³⁵ Otherwise, *cis*- and *trans*-OBB(H)OH can decompose to OBBOH + H or BO + OBH₂ by the cleavage of the B–H or B–B single bonds, respectively. However, these processes are highly endothermic, as the products reside 92.9 (OBBOH + H) and 95.9 kcal/mol (BO + OBH₂) higher in energy than OBBO + H₂.

The alternative reaction channel is 1,2-insertion of the B-B fragment of OBBO into the H_2 molecule. This leads directly to the OBH + OBH products; two new B-H bonds are formed, while the H-H and B-B bonds are cleaved during this process occurring via transition state s-TS4. The barrier is very high, 76.1 kcal/mol, so that this reaction mechanism is not likely. As was described in a previous section, the most favorable mechanism of the BO + H_2 reaction is H abstraction leading



Figure 4. Potential energy diagram for the $B_2O_2 + H_2$ reactions in the lowest singlet and triplet electronic states calculated at the G2(MP2) level. Relative energies are given in kcal/mol. Geometric structures (bond lengths in Å and bond angles in deg) of various intermediates and transition states optimized at the B3LYP/6-311+G(d,p) level of theory are also shown.

to OBH + H. In the case of OBBO, the hydrogen abstraction would lead from two closed-shell species to two radicals, OBBOH + H. Therefore, the reaction energy, 92.9 kcal/mol, is too high and this channel is not probable. As a consequence of its greater stability, the singlet OBBO is not expected to be reactive with molecular hydrogen, except at high temperatures when the 50.1 and 53.7 kcal/mol at s-TS1 and s-TS3 can be overcome and two OBH molecules can be produced.

Alternatively, electronically excited triplet OBBO, which lies 113.0 kcal/mol above the ground state minimum and 1.7 kcal/mol higher in energy than two BO monomers, can easily react with H_2 . The most favorable reaction mechanism is 1,1-insertion of a B atom into the H–H bond proceeding via transition state t-TS1 with a barrier of 4.4 kcal/mol. The transition state has an asymmetric geometry and a very early character (see Figure 4). A t-OBBH₂O molecule residing 26.3 kcal/mol below t-B₂O₂

+ H₂ is formed as a result of the insertion. This molecule can decompose to the $BO + OBH_2$ products via a barrier of 10.0 kcal/mol at t-TS2. The transition state lies 16.3 kcal/mol lower in energy than the initial triplet state reactants, so that the decomposition of the chemically activated t-OBBH2O species is expected to be fast. The t-B₂O₂ + H₂ \rightarrow BO + OBH₂ reaction is thus 17.2 kcal/mol exothermic and the initial step with the 4.4 kcal/mol barrier is rate determining. The second channel of the $t-B_2O_2 + H_2$ reaction involves abstraction of a hydrogen atom by a terminal oxygen. In this case, the products are OBBOH + H and the reaction is more exothermic, by 20.1 kcal/mol. However, the abstraction barrier located at t-TS3, 7.4 kcal/mol, is 3.0 kcal/mol higher than the insertion barrier at t-TS1. Therefore, the production of $BO + OBH_2$ in the reaction of the triplet boron dimer with molecular hydrogen is expected to be more probable than the production of OBBOH + H.

TABLE 6. Total Energies (hartree), ZPE, and Relative Energies (kcal/mol) of Various Compounds in the BS + H₂ Reaction Calculated at the B3LYP/6-311+G(d,p), MP2/6-311G(d,p), CCSD(T)/6-311G(d,p), MP2/6-311+G(3df,2p), and G2M(MP2)//B3LYP/6-311+G(d,p) Levels of Theory

	B3LYP/6-311+G(d,p)		MP2/6-311G(d,p)		CCSD(T)/6-311G(d,p)		MP2/6-311+G(3df,2p)		G2M(MP2)	
	total		rel	total	rel	total	rel	total	rel	rel
species	energy	ZPE	energy	energy	energy	energy	energy	energy	energy	energy
BS $(C_{\infty v}, {}^{2}\Sigma^{+})$	-423.00362	1.68		-422.35806		-422.38860		-422.41142		
$BS + H_2$	-424.18319	8.00	0	-423.51831	0	-423.55694	0	-423.57414	0	0
TS1 ($C_{\infty v}$, $^{2}\Sigma^{+}$)	-424.17527	7.12	4.11	-423.50101	10.00	-423.54029	9.59	-423.55800	9.27	8.86
SBH $(C_{\infty v}, {}^{1}\Sigma^{+})$	-423.68919	7.82		-423.03345		-423.06494		-423.09019		
SBH + H	-424.19135	7.82	-5.29	-423.53326	-9.56	-423.56475	-5.08	-423.59000	-10.13	-5.65
TS2 (C_s , ² A')	-424.19138	8.00	-5.14	-423.53174	-8.43	-423.56352	-4.13	-423.58897	-9.31	-5.01
$SBH_2(C_{2\nu}, {}^2B_2)$	-424.25794	12.23	-42.77	-423.58283	-36.34	-423.62329	-37.49	-423.63829	-36.12	-37.26
TS3 (C_s , ² A')	-424.19026	9.72	-2.75	-423.51799	1.89	-423.55607	2.24	-423.57761	-0.49	-0.14
trans-HBSH (C_s , ² A')	-424.21860	11.76	-18.53	-423.55051	-16.52	-423.58820	-15.95	-423.60803	-17.58	-17.00
$TS4(C_1)$	-424.08540	8.36	61.71	-423.40653	70.49	-423.45637	63.46	-423.46236	70.49	63.46
TS9 (C_s , ² A')	-424.18932	8.10	-3.75	-423.52211	-2.29	-423.55631	0.49	-423.58020	-3.71	-0.92
<i>cis</i> -HBSH (C_s , ² A')	-424.21860	11.76	-18.53	-423.54837	-15.17	-423.58618	-14.66	-423.60600	-16.30	-15.79
$TS6(C_1)$	-424.19273	10.62	-3.42	-423.52185	0.35	-423.55954	0.94	-423.57954	-0.82	-0.23
TS5 (C_s , ² A')	-424.18074	9.90	3.40	-423.50508	10.17	-423.54475	9.52	-423.56641	6.72	6.07
TS7 (C_s , ² A')	-424.08401	5.86	60.13	-423.41708	61.42	-423.46036	58.50	-423.47437	60.51	57.59
BSH $(C_s, {}^1A')$	-423.58157	5.67		-422.92110		-422.96386		-422.97749		
BSH + H	-424.08372	5.67	60.13	-423.42091	58.84	-423.46367	56.24	-423.47730	58.48	55.89
TS8 (C_1)	-424.08102	6.57	62.70	-423.40018	72.72	-423.45197	64.46	-423.45752	71.77	63.52
$B-H_2S(C_{2v}, {}^2B_2)$	-424.09464	9.75	57.28	-423.41589	65.99	-423.46486	59.50	-423.47517	63.83	57.34
$B + H_2S$	-424.08500	9.41	63.00	-423.41560	65.84	-423.46365	59.92	-423.46810	67.92	62.01

Interestingly, the presence of a second BO radical can alter the course of the $BO + H_2$ reaction. For instance, two BOradicals can recombine to form triplet OBBO via a barrier of 8.3 kcal/mol at t-TS4 (see Figure 4). The recombination on the triplet PES is certainly less favorable than the 111.7 kcal/mol exothermic and barrierless formation of s-OBBO in the singlet electronic state; however, the triplet reaction can play some role at elevated and high temperatures. Then, t-B₂O₂ can react with H_2 by the following mechanism, $t-B_2O_2 + H_2 \rightarrow t-TS1 \rightarrow$ t-OBBH₂O \rightarrow t-TS2 \rightarrow BO + OBH₂. The overall reaction is then $BO + BO + H_2 \rightarrow BO + OBH_2$ and the rate-limiting step is the initial recombination of two BO with the barrier of 8.3 kcal/mol. Without a second BO, the $BO + H_2$ reaction produces OBH + H with a similar barrier. Thus, the second boron oxide species can enhance the formation of the OBH₂ radical instead of HBO + H.

BS + **H**₂ → **B** + **H**₂**S Reaction.** Total energies and ZPE corrected relative energies of various compounds in the BS + $H_2 \rightarrow B + H_2S$ reaction calculated at the B3LYP/6-311+G-(d,p), MP2/6-311G(d,p), MP2/6-311+G(3df,2p), and CCSD-(T)/6-311G(d,p) levels of theory and their G2M(MP2) relative energies are collected in Table 6. Table 7 shows calculated vibrational frequencies. The BS + H_2 potential energy diagram along the reaction path computed at the G2M(MP2) level and the optimized geometries of various compounds along the predicted reaction pathway are shown in Figure 5. The mechanism of the BS + H_2 reaction is similar to that for BO + H_2 , although the energetics and some details differ. Hence, we used the same notation for transition states in the BS/H₂ system as that for BO/H₂.

The most favorable reaction channel is abstraction of a hydrogen atom of H_2 by a B atom of BS, giving the SBH + H products. The calculated barrier at the linear transition state TS1 and the reaction exothermicity, 8.9 and 5.7 kcal/mol, respectively, are very close to the values obtained for the BO + H_2 \rightarrow OBH + H_2 reaction. As compared to BO + H_2 , the reaction exothermicity decreases by 1.1 kcal/mol and the barrier correspondingly increases by 0.6 kcal/mol. In the secondary SBH + H reaction, the hydrogen atom can easily add to the middle boron of SBH to produce the SBH₂ molecule. The barrier at TS2 is only 0.6 kcal/mol, slightly higher than the 0.3 kcal/mol

TABLE 7. Vibrational Frequencies (cm⁻¹) of Various Compounds in the BS + H₂ Reaction Calculated at the B3LYP/6-311+G(d,p) Level

species	frequencies
TS1 (B3LYP)	767 <i>i</i> , 25, 25, 925, 925, 1171, 1934
TS1 ((MP2) ^a	1331 <i>i</i> , 58, 58, 924, 924, 1177, 1913
SBH	723, 723, 1186, 2839
TS2	136 <i>i</i> , 139, 719, 720, 1176, 2840
SBH_2	564, 837, 893, 1103, 2538, 2615
TS3	1449 <i>i</i> , 444, 764, 885, 2045, 2664
trans-HBSH	597, 681, 840, 919, 2500, 2690
TS4	428 <i>i</i> , 222, 260, 945, 1746, 2670
TS9	481 <i>i</i> , 265, 680, 722, 1156, 2841
cis-HBSH	597, 681, 840, 919, 2500, 2690
TS6	1157 <i>i</i> , 602, 755, 830, 2604, 2640
TS5	1226 <i>i</i> , 604, 738, 899, 1954, 2732
TS7	263 <i>i</i> , 134, 306, 631, 751, 2276
BSH	602, 760, 2545
TS8	529 <i>i</i> , 169, 382, 673, 723, 2647

^{*a*} Calculated at the MP2/6-311G(d,p) level with the MP2/6-311G(d,p) optimized geometry.

calculated for the OBH + H \rightarrow OBH₂ process. However, SBH₂ is more stable than OBH2 because the former resides 37.3 kcal/ mol lower in energy than $BS + H_2$ as compared to only 15.9 kcal/mol for the latter. The addition of H to the sulfur end of SBH forming cis-HBSH via TS9 exhibits a somewhat higher barrier, 4.7 kcal/mol. This value is much lower than the barrier for the OBH + H \rightarrow TS9 \rightarrow cis-HBOH process, 20.8 kcal/mol. cis-HBSH lies 15.8 kcal/mol below $BS + H_2$, i.e., it is slightly more stable than *cis*-HBOH with respect to $BO + H_2$, -11.7 kcal/mol. The trans-HBSH isomer is 1.2 kcal/mol more stable than the cis conformer, but 20.3 kcal/mol less favorable than SBH₂. One can see that the SBH₂ structure lies in a deeper potential energy well with respect to the HBSH isomers as compared to OBH₂. 1,2-Hydrogen migration from B to S via TS3 leads from SBH₂ to trans-HBSH but the barrier is higher than that in the BO/H₂ system, 37.1 versus 27.7 kcal/mol. The rotational barrier at TS6 separating the trans and cis forms of HBSH is calculated to be 16.8 and 15.6 kcal/mol relative to trans- and cis-HBSH, respectively, again higher than the rotational barrier for HBOH, 10.8 and 9.1 kcal/mol. The increase of the barrier for the rotation around the B-S bond correlates



Figure 5. Potential energy diagram for various reactions in the BS/H₂ system calculated at the G2(MP2) level. Relative energies are given in kcal/mol. Geometric structures (bond lengths in Å and bond angles in deg) of various intermediates and transition states optimized at the B3LYP/ 6-311+G(d,p) level of theory are also shown.

with larger elongation of the B–S bond in TS6, 0.08-0.09 Å, as compared to only 0.01 Å in HOBH.

In addition to TS3, the transition state between SBH₂ and trans-HBSH, we also found a transition state connecting SBH₂ with the cis-HBSH isomer. We started the first-order saddle point search with a structure similar to TS5 for BO/H₂, which is a transition state for 1,2-insertion of BO into the H-H bond. However, the calculations converged to the structure TS5 shown in Figure 5, which, according to IRC calculations, connects cis-HBSH with SBH_2 but not with $BS + H_2$. This result represents the main difference between the BS/H₂ and BO/H₂ systems. Thus, on the contrary to BO, boron sulfide cannot insert into the H-H bond of H₂. As we discussed above, the 1,1-insertion is not favorable because the singly occupied p_z orbital of the boron atom cannot interact in this case both with the occupied $\sigma_{\rm g}$ and vacant $\sigma_{\rm u}$ orbitals of H₂. A first-order saddle point on the 1,2-insertion pathway disappears for BS apparently because of a larger size of the BS molecule as compared to BO. Along this pathway, the H-H bond has to be broken and S-H to be formed while the electron density is transferred from $p_z(B)$ to $\sigma_{\rm u}({\rm H_2})$. The B–S bond length is ~0.4 Å longer than B–O and the H-H bond has to be stretched more significantly before the S-H bond can start to form, which leads to an energy increase on the insertion pathway. On the other hand, in cis-HBSH two hydrogen atoms are located farther away from each other than in cis-HBOH and repulsion between them is not as large when one of them migrates from S to B, making possible the direct *cis*-HBSH \rightarrow SBH₂ rearrangement. In HBOH, two hydrogens have to be located in a trans position to allow the 1,2-H shift.

The barrier at TS5 is calculated to be 21.9 kcal/mol relative to *cis*-HBSH, 5.0 kcal/mol higher than the barrier for the *trans*-HBSH \rightarrow SBH₂ isomerization at TS3. The HBSH species can decompose to BSH + H without exit barriers and the strengths of the B-H bond are 71.7 and 72.9 kcal/mol for the cis and trans isomers, respectively. Additionally, *trans*-HBSH can dissociate to B + H₂S through a 1,2-H shift from B to S and formation of the B-H₂S complex. Note that the B-H₂S complex formation energy, 4.7 kcal/mol, is significantly larger than that for B-H₂O, 1.5 kcal/mol. The overall heat of the endothermic BS + H₂ \rightarrow B + H₂S reaction, 62.0 kcal/mol, is 13.5 kcal/mol lower than the endothermicity of the BO + H₂ \rightarrow B + H₂O reaction.

Since the insertion of BS into H-H is not possible, the only alternative channel of the BS + H₂ reaction is H abstraction by the S atom leading to BSH + H. As for BO + H₂, the BS + H₂ \rightarrow BSH + H reaction is endothermic and exhibits a high barrier at TS7. The barrier height and reaction heat, 57.6 and 55.9 kcal/ mol, respectively, both are 14.9 and 18.2 kcal/mol higher than the corresponding values for the BO + H₂ \rightarrow BOH + H reaction. BSH and H can in turn recombine producing *cis*- or *trans*-HBSH without entrance barriers. The reverse BSH + H \rightarrow BS + H₂ abstraction reaction has a 1.7-kcal/mol barrier, 3.3 kcal/mol lower than that for BOH + H \rightarrow BO + H₂. Finally, H addition to the S atom of BSH gives the B-SH₂ complex via a barrier of 7.6 kcal/mol at TS8. This barrier is much lower than the barrier calculated for the BOH + H \rightarrow TS8 \rightarrow B-OH₂ process, 42.5 kcal/mol.

The $B + H_2S$ reaction starts from the formation of the relatively strong $B-SH_2$ complex and then proceeds by elimina-

TABLE 8. Calculated and Experimental Heats of Formation $[\Delta H_f(0K), \text{ kcal/mol}]$ for Various Species in the BO/H₂, B₂O₂/H₂, and BS/H₂ Systems

species	calcd ^a	exptl	$G3^b$	CBS-Q ^b
BO	1.2	$1.6 \pm 2.6^{\circ}$	0.8	1.6
OBH	-57.2	$-50.2 \pm 6.0^{\circ}$	-57.6	-57.6
BOH	-12.7			
OBH ₂	-14.7			
trans-HBOH	-12.2			
cis-HBOH	-10.5			
B2O2	-109.3	$-109.9 \pm 2.4^{\circ}$	-112.4	-112.4
cis-OBB(H)OH	-117.4			
trans-OBB(H)OH	-117.0			
BS	67.6	57.4 ± 4.1^{d}	66.5	66.5
SBH	10.3	-4.0^{d}	10.1	10.1
BSH	71.8			
SBH ₂	30.3			
trans-HBSH	50.6			
cis-HBSH	51.8			

^{*a*} Present calculations. Based on the heats of reactions calculated in this study and experimental $\Delta H_f(0K)$ for B (133.8 kcal/mol), H₂O (-57.1), H₂S (-4.2), and H (51.6). ^{*b*} Theoretical data obtained with use of the G3 and CBS-Q methods are taken from ref 40. ^{*c*} From ref 39. ^{*d*} From ref 37.

tion of an H atom via a barrier of only 1.5 kcal/mol with respect to the initial reactants leading to the BSH + H products. On the other hand, B can insert into an S-H bond and produce trans-HBSH with a barrier of 1.45 kcal/mol relative to B + H₂S. Then, *trans*-HBSH can rearrange to SBH₂ or *cis*-HBSH via transition states lying much lower in energy than the reactants. As HBSH and SBH₂ can decompose only SBH + H (not counting highly endothermic dissociation to BSH + H, which more likely can be formed by the H elimination mechanism from the $B-SH_2$ complex), $BS + H_2$ cannot be primary products of the $B + H_2S$ reaction. This is an implication of the fact that no transition state exists for the insertion of BS into H₂. As compared to the $B + H_2O$ reaction, $B + H_2S$ is expected to be much faster because the activation barriers are as low as 1.5 kcal/mol, significantly lower than 4.7 and 6.2 kcal/mol for $B + H_2O$.

Heats of Formation for Various Species. Heats of formation of various species in the BO/H₂, B₂O₂/H₂, and BS/H₂ systems computed by using the heats of reactions calculated in the present study are collected in Table 8. They are compared with available experimental data37,39 and with the results of most accurate theoretical calculations, using the G3 and CBS-Q model chemistries.⁴⁰ As one can see, the agreement of the calculated $\Delta H_{\rm f}$ with experiment is within 1 kcal/mol for BO and B₂O₂. On the other hand, the deviations are large for OBH (7 kcal/ mol), BS (10 kcal/mol), and SBH (14 kcal/mol). However, our results for these species closely agree with the values obtained at the most accurate G3 and CBS-Q levels of theory. As the experimental $\Delta H_{\rm f}$ values for OBH, BS, and SBH were reported⁴⁰ with large error bars and are not well established, new measurements would be required to reconcile theory and experiment. For the reaction intermediates, such various isomers of OBH₂, SBH₂, and B₂O₂H₂, experimental heats of formation are not available to our knowledge, and our calculations provide these important thermodynamic quantities.

Conclusions

G2M(MP2) calculations of PES for the BO + H_2 reaction demonstrate that the reaction proceeds by abstraction of a hydrogen atom by B of the boron oxide to produce OBH + H and the barrier and exothermicity of the reaction are computed to be 8.3 and 6.8 kcal/mol, respectively. TST calculations of the reaction rate constants with the G2M(MP2) barrier and MP2/ 6-311G(d,p) vibrational frequencies of the transition state give close agreement with experiment for the rates in the 500-3000 K temperature range. The reaction can also occur by 1,2insertion of BO into the H-H bond or by H abstraction by the O atom; however, the barriers for these mechanisms are much higher, 36.4 and 42.7 kcal/mol, respectively. The OBH + H reaction produces the OBH₂ radical via a small ~0.3-kcal/mol barrier. OBH₂ is 2.5 and 4.2 kcal/mol lower in energy than transand cis-HBOH, respectively, and can isomerize to trans-HBOH by the 1,2-H shift overcoming a barrier of 27.7 kcal/mol. In turn, trans-HBOH can rearrange to the cis conformer by rotation about the B-O bond over a barrier of 10.8 kcal/mol. Dissociation of *trans*-HBOH to $B + H_2O$ is highly endothermic and is not probable. BOH and H can recombine and form cis- or trans-HBOH without barriers. In the $B + H_2O$ reaction, the reactants can first form a weakly bound B-H₂O complex, which then can eliminate an H atom producing BOH + H over a barrier of 4.7 kcal/mol with respect to the initial reactants. The second channel is insertion of B into an O-H bond giving trans-HBOH via a 6.2-kcal/mol barrier. The most probable products for this channel are OBH + H, although minor amounts of $BO + H_2$ and BOH + H also can be produced.

If two BO radicals form a stable dimer OBBO in the ground singlet electronic state, the reactivity with respect to molecular hydrogen drastically decreases because the barriers for the OBBO + $H_2 \rightarrow cis$ -OBB(H)OH $\rightarrow trans$ -OBB(H)OH \rightarrow OBH + OBH reaction are calculated to be as high as 50–54 kcal/ mol. Alternatively, two BO can recombine to form the OBBO molecule in triplet electronic state over a moderate 8.3-kcal/ mol barrier. t-OBBO can easily react with H₂ producing either BO + OBH₂ (via a t-OBBH₂O intermediate) or OBBOH + H with barriers of 4.4 and 7.4 kcal/mol, respectively. Thus, the formation of the triplet dimer can enhance the yield of OBH₂.

The reactions in the BS/H₂ system are shown to be similar to those for BO/H₂, except for some details in the energetics and mechanism. The main differences are that BS cannot insert into H₂ and SBH₂ resides in a much deeper potential well (37.3 kcal/mol below BS + H₂) and rearranges by 1,2-H migrations not only to *trans*- but also to *cis*-HBSH. B and H₂S can form a much more strongly bound complex than B and H₂O and the B + H₂S reaction is expected to be significantly faster than B + H₂O because the barriers for H elimination from the complex and for B insertion into an S–H bond are in the range of 1.5 kcal/mol. BSH + H and SBH + H are predicted to be produced in the B + H₂S reaction, while BS + H₂ are not likely to be formed as primary products.

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