# Clusters of II–VI Materials: $Cd_iX_i$ , X = S, Se, Te, $i \le 16$

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Several structures of small  $Cd_iX_i$  clusters,  $i \le 16$ , have been characterized. Ringlike structures have been found to be the lowest lying structures for  $i \le 5$  clusters and three-dimensional spheroid structures for larger ones, i = 6-16. This trend has been ascribed to the stability of obtuse X–Cd–X angles in the first case and to the stability gained from higher coordination in the second case. The three-dimensional structures may be envisioned as being built from  $Cd_2X_2$  squares and  $Cd_3X_3$  hexagons, as it was the case for  $Zn_iO_i$ , X = O, S, Se, Te, and  $Cd_iO_i$  three-dimensional structures, studied previously in our group. Second-order free-energy differences reveal that the most stable spheroids are the i = 12 ones. The highest occupied molecular orbital–lowest unoccupied molecular orbital gaps are found to fit in the experimental trend observed for nanoparticles, which might be an indication of a possible reorganization of the nanoparticle surfaces. Vibrational spectra are provided for their use in experimental characterization.

### 1. Introduction

Semiconductors are materials of great importance in the development of technology. Computer revolution and other technological devices are in rapid development basically because of improved semiconductor materials. Some of these materials are the II–VI compounds, in which interest has increased notably because of their paramount technological potential. Applications such as photovoltaic solar cells,<sup>1–10</sup> optical sensitizers,<sup>11</sup> photocatalysts,<sup>12,13</sup> or quantum devices<sup>14</sup> have led to extensive investigation of their properties. To understand them it is essential to study the structure and electronic properties of these compounds, thereby providing more information for the rational design of these materials to enhance their applicability. Many theoretical studies have been reported concerning the bulk electronic structure of these compound semiconductors.<sup>15–22</sup> Studies on their clusters are more scarce.

There are properties of these compounds that have been seen to be local phenomena. That is, when they happen, they happen at a certain well-defined domain. Consequently, the study of small clusters of these compounds could give insight into these local properties, including their catalytic behavior.<sup>23</sup> Also, the fact that cluster and nanoparticle characterization is becoming technologically feasible is remarkable. This makes cluster science even more interesting, because in addition to its capability in helping rationalize some of their surface-related properties, studies of clusters of increasingly larger size can eventually fill the gap with the nanosize materials domain in a comprehensible manner.<sup>24</sup> For instance, in studying clusters of silicon of increasing size, it has be found that the driven force for the stability of Si nanoparticles of diameter d < 5 nm (up to 2500 Si atoms) is the surface energy minimization. This renders icosahedral lowest energy structures that deviate markedly form the bulklike structure. The latter is often assumed to be the preferred one until the cluster approaches the limit of a few hundred atoms. However, it has been shown<sup>25</sup> that when the bulk has a tetrahedrally coordinated structure, like Si and the materials of the present investigation, there is no a priori reason to assume a bulklike structure for the nanoparticles. As a matter of fact, experimental studies on nanoparticles of 2-6 nm in diameter are becoming routine work.<sup>26,27</sup> The case of II– VI nanoparticles is not an exception. Binary compounds such as ZnO<sup>28,29</sup> and ZnS,<sup>30,31</sup> CdS,<sup>32–37</sup> CdSe,<sup>37–42</sup> and CdTe<sup>37,43,44</sup> and ternary compounds such as CdS/ZnS,<sup>45</sup> CdSe/ZnSe,<sup>46,47</sup> CdTe/ZnTe,<sup>48</sup> and CdSe/CdTe<sup>49</sup> have recently been studied. These nanoparticles are grown in solution, where organic molecules surround the nanoparticle to stop its growth. It is assumed that the structure of these particles is a bulklike core surrounded by a reconstructed surface. The nature of this surface reconstruction is not known, but its properties are determinant in the chemistry of these nanoparticles. This growth of experimental works has led to an increased interest of complementary theoretical works on II–VI clusters.<sup>50–52</sup>

Theoretical calculations have previously been performed in our group for  $Zn_iX_i$ , i = 1-9, X = O, S, Se, Te, clusters<sup>53–55</sup> and  $Cd_iO_i$ , i = 1-9, 12, 15, clusters.<sup>56</sup> In ref 57 we predicted the existence of fullerene-like spheroids of  $Zn_iO_i$ . Recently, experimentally synthesized<sup>58</sup>  $Zn_iO_i$  clusters, i = 9, 11, 15, have been related to the spheroid structures predicted theoretically, which could be the confirmation of the existence of this type of structure. In this paper we focus on  $Cd_iX_i$ ,  $i \le 16$ , X = S, Se, Te, clusters. We have been able to characterize spheroid structures with diameters of 0.96, 0.99, and 1.06 nm for  $Cd_iS_i$ ,  $Cd_iSe_i$ , and  $Cd_iTe_i$ , respectively, which lie close to the experimentally smallest detected II–VI nanoparticles, namely, 1.8 and 3 nm in diameter for CdSe and CdTe, respectively. This means that available theoretical and experimental data on small nanoparticles are actually merging.

### 2. Method

Characterized structures have been found by using local minimization procedures. The starting structures were chosen according to previous studies of other II–VI clusters and chemical intuition. All the tried structures converged to the ones presented in this study or to some others that are not presented because they are very high in energy. Some bulklike structures were attempted but converged to spheroids.

All geometries were fully optimized using the hybrid<sup>59</sup> Becke 3 Lee–Yang–Parr (B3) gradient-corrected approximate density-

TABLE 1: SKBJ(d/2df) and SKBJ(expan) Exponents for Cd, S, Se, and Te Atoms<sup>a</sup>

Cd	C					SKBJ(expan)				
	3	Se	Te	Cd	S	Se	Те			
α	α	α	α	α	α	α	α			
				0.261 148	1.231 541	0.750 763	0.535 452			
				0.182 01	0.373 393	0.375 285	0.180 824			
0.23	0.7	0.537 83	0.349 496	1.350 188	0.896 605	0.691 855	0.408 953			
		0.208 111	0.155 952	0.23	0.288 732	0.463 247	0.237 585			
				0.097 397		0.177 490	0.084 947			
		0.396 026	0.306 353	1.451	0.593 345	1.048 712	0.594 100			
				0.326 695		0.366 780	0.228 881			
(			0.23 0.7 0.537 83 0.208 111	0.23 0.7 0.537 83 0.349 496 0.208 111 0.155 952	0.23 0.7 0.537 83 0.349 496 0.182 01 0.208 111 0.155 952 0.23 0.396 026 0.306 353 1.451	0.23 0.7 0.537 83 0.349 496 1.350 188 0.896 605 0.208 111 0.155 952 0.23 0.288 732 0.396 026 0.306 353 1.451 0.593 345	0.23 0.7 0.537 83 0.349 496 1.350 188 0.896 605 0.691 855 0.208 111 0.155 952 0.23 0.288 732 0.463 247 0.396 026 0.306 353 1.451 0.593 345 1.048 712			

<sup>a</sup> All the coefficients are 1.

TABLE 2: Cd-X Bond Lengths and X-Cd-X and Cd-X-Cd Angles of Ring Structures

	R (Cd-X)			$\alpha$ (X-Cd-X)			$\alpha$ (Cd-X-Cd)		
	X = S	X = Se	X = Te	X = S	X = Se	X = Te	X = S	X = Se	X = Te
$^{(1)}Cd_2X_2^{R(I)}$	2.49	2.60	2.79	110.8	113.2	116.9	69.2	66.8	63.1
${}^{(1)}Cd_2X_2^{\tilde{R}(II)}$	2.59	2.68	2.87						
$Cd_3X_3^{R(\tilde{l})}$	2.42	2.52	2.72	155.9	159.1	161.5	84.1	81.6	78.5
$Cd_3X_3^{R(II)}$	2.42 - 2.48	2.53 - 2.57	2.53 - 2.57	126.6-135.2	132.1-140.3	132.1-140.3			
$Cd_4X_4^{\dot{R}}$	2.39	2.50	2.70	176.0	178.1	177.7	93.9	91.5	87.3
$Cd_5X_5^{R}$	2.38	2.49 - 2.50	2.69 - 2.70	175.1-177.9	173.4-179.1	171.9-178.3	97.8	94.5	90.5
$Cd_5X_5^{\dot{R}}$ $Cd_6X_6^{R}$	2.38	2.49	2.70	178.0	178.2	178.4	99.2	95.0	90.5
$Cd_7X_7^{R}$	2.38	2.49	2.70	174.9-178.9	174.6-179.0	174.6-178.4	99.6-101.2	94.7-97.0	89.6-92.0
$Cd_8X_8^R$	2.38	2.49	2.70	178.3	177.8	177.5	99.9	95.5	90.9
$Cd_9X_9^{\check{R}}$	2.38	2.49	2.70	174.7-179.2	175.4-179.5	176.5-179.6	99.9-100.6	95.0-96.1	90.3-91.4
$Cd_{10}X_{10}^R$	2.38	2.49	2.70	177.8	177.6	177.6	100.5	95.7	90.9
$Cd_{11}X_{11}^{\tilde{R}}$	2.38	2.49	2.70	173.0-179.5			100.0-101.6		
$Cd_{12}X_{12}^{R}$	2.38	2.49	2.70	178.0	177.3-179.3	177.9-179.7	100.6	95.6	90.8

functional procedure.<sup>60–62</sup> Harmonic vibrational frequencies were determined by analytical differentiation of gradients.

The relativistic compact effective core potentials and sharedexponent basis set63 of Stevens, Krauss, Basch, and Jasien (SKBJ) were used as the basic basis set in this study. The 4d electrons of Cd were included in the valence. To perform the geometry optimizations and harmonic frequency calculations an extra d functions set was added on Cd and on S, and two additional d and one f set for Se and Te, due to their importance for the proper description of the high coordination of the atoms in the three-dimensional cluster structures. This basis set is denoted as SKBJ(d/2df), and the exponents are shown in Table 1. However, the energy calculations were performed with an even more expanded basis set, denoted as SKBJ(expan), to obtain accurate relative energies. The exponents of all of these added functions were energy optimized using the GAMESS<sup>64</sup> package. Note that pure angular momentum functions were used throughout this study.

All the geometry optimizations and frequency calculations were carried out with the Gaussian 98<sup>65</sup> package.

### 3. Results

**3.1. Structures of Characterized Minima of Cd**<sub>*i*</sub>X<sub>*i*</sub>, X = **S**, Se, Te,  $i \le 16$ . In this section the calculated structures are described. Different types of families have been characterized, which are rings (R), chains (C), spheroids (S), distorted spheroids (D), and cluster tubes (CT). The difference between spheroids and distorted spheroids will be made clear below. Structures are labeled according to the following scheme: <sup>(s)</sup>Cd<sub>*i*</sub>X<sup>*a*</sup>, where (*s*) denotes the multiplicity and *i* the number of CdX units and the superscript *a* stands for the structure family. A representative structure of each family is shown in Figure 1. Molecular geometries such as the bond length and bond angles

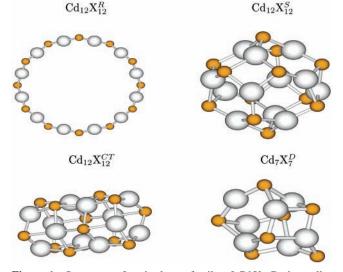


Figure 1. Structures of each cluster family of  $Cd_iX_i$ . Dark smaller atoms are those of X.

are given in Tables 2 (rings), 3 (spheroids), and 4 (chains, distorted spheroids, and cluster tubes). Note that triplet states have been considered only for small clusters, i = 1, 2, because they stand high in energy for larger clusters. Hence, for  $i \ge 3$  spin multiplicity will not be shown. X may be S, Se, or Te. Hereafter, when using Cd<sub>i</sub>X<sub>i</sub>, it will be to all Cd<sub>i</sub>S<sub>i</sub>, Cd<sub>i</sub>Se<sub>i</sub>, and Cd<sub>i</sub>Te<sub>i</sub> that we will be referring.

Rings are planar for small clusters ( $i \le 5$  for Cd<sub>i</sub>S<sub>i</sub>,  $i \le 4$  for Cd<sub>i</sub>Se<sub>i</sub> and Cd<sub>i</sub>Te<sub>i</sub>) and near planar for larger ones. The main reason to break the planarity in these ring structures is the observed strong tendency to form linear X–Cd–X angles and Cd–X–Cd angles between 100 and 90°. Thus, the X–Cd–X bond angles lie within 170–180° for these rings, and Cd–X–

TABLE 3: Cd-X Bond Lengths and X-Cd-X Angles of Spheroids

		R (Cd $-X$ )			$\alpha$ (X-Cd-X)	
	X = S	X = Se	X = Te	X = S	X = Se	X = Te
$Cd_4X_4^S$	2.61	2.72	2.90	103.0	104.8	107.1
$Cd_6X_6^{S}$	2.50 - 2.75	2.62 - 2.84	2.82 - 3.02	98.3-143.3	100.3-143.8	102.7-143.3
$Cd_8X_8^{S}$	2.49 - 2.68	2.60 - 2.79	2.81-2.97	96.9-138.8	98.6-140.2	101.0-140.2
$Cd_8X_8^{S}$ $Cd_9X_9^{S}$ $Cd_{10}X_{10}^{S}$ $Cd_{11}X_{11}^{S}$	2.49 - 2.62	2.60 - 2.73	2.80 - 2.92	97.5-132.7	99.6-140.9	101.3-140.7
$Cd_{10}X_{10}^{S}$	2.47-2.63	2.58 - 2.75	2.78 - 2.93	95.3-137.8	96.8-139.8	98.6-139.7
$Cd_{11}X_{11}^{S}$	2.48 - 2.63	2.58 - 2.74	2.79-2.93	91.7-138.3	92.4-140.3	94.5-140.3
$\begin{array}{c} Cd_{12}X_{12}^{S}\\ Cd_{13}X_{13}^{S}\end{array}$	2.47 - 2.58	2.58 - 2.69	2.79 - 2.88	94.5-131.1	95.8-131.3	98.0-130.7
$Cd_{13}X_{13}^{5}$	2.48 - 2.64	2.59 - 2.75	2.78-2.93	93.0-137.8	93.8-139.6	95.3-139.7
$Cd_{14}X_{14}^{S}$	2.47-2.61	2.58 - 2.71	2.78 - 2.94	92.1-136.4	93.4-138.3	95.6-138.1
$Cd_{15}X_{15}^{13}$	2.47-2.58	2.58 - 2.69	2.78 - 2.88	94.5-132.3	95.9-132.6	98.0-132.3
$Cd_{16}X_{16}^{S}$	2.51-2.55	2.62-2.66	2.82 - 2.86	94.6-131.7	95.9-131.7	97.5-131.1

TABLE 4:	Cd-X Bond	Lengths and X-	-Cd-X Angles of	Chains, Distorted S	Spheroids, and Cluster Tubes

	<i>R</i> (Cd-X)			$\alpha$ (X-Cd-X)			
	X = S	X = Se	X = Te	X = S	X = Se	X = Te	
$Cd_1X_1^C$	2.29	2.40	2.61				
$^{(3)}Cd_2X_2^C$	2.31-2.44	2.42 - 2.56	2.62 - 2.79	177.8	177.5	177.5	
$Cd_5X_5^D$	2.37-2.64	2.48 - 2.75	2.60 - 2.74	98.3-152.4	97.1-154.8	97.1-154.8	
$Cd_7X_7^{D(I)}$	2.38-2.65	2.49 - 2.75	2.69-3.13	94.2-177.3	96.5-176.3	98.9-177.8	
$Cd_7X_7^{D(II)}$	2.43-2.82	2.48 - 2.90	2.68 - 3.07	91.3-154.9	92.6-157.7	95.1-138.6	
$Cd_8X_8^{CT}$	2.49-2.69	2.59-2.91	2.80-3.05	94.3-155.3	98.0-160.4	101.2-155.8	
$Cd_9X_9^{CT}$	2.50 - 2.74	2.61-2.89	2.79-3.17	92.4-168.4	93.0-149.6	93.5-159.0	
$Cd_{12}X_{12}^{CT}$	2.50 - 2.75	2.60 - 2.89	2.80-3.32	92.1-164.9	84.6-159.4	90.0-154.8	
$Cd_{15}X_{15}^{CT}$	2.50 - 2.75	2.60-2.91	2.80-3.27	93.3-165.3	92.1-160.4	91.2-156.4	

Cd tend to 100° for CdS, to 95° for CdSe, and to 90° for CdTe. The bond lengths decrease as the size of the ring increases from 2.54 to 2.38 Å for Cd<sub>i</sub>S<sub>i</sub>, 2.66 to 2.49 Å for Cd<sub>i</sub>Se<sub>i</sub>, and 2.89 to 2.69 Å for Cd<sub>i</sub>Te<sub>i</sub>. Spheroids can be depicted as being built from  $Cd_2X_2^R$  (squares)- and  $Cd_3X_3^R$  (hexagons)-like structures. The number of squares remains constant, six, while the number of hexagons increases by one when adding a new CdX unit. A similar structural tendency is observed in  $Zn_iX_i$  clusters.<sup>53–55,57</sup> In fullerenes there are pentagons instead of squares, but similarly the number of pentagons remains constant, 12, and the number of hexagons increases by one adding two carbon atoms. Spheroids that do not follow this trend are labeled as distorted spheroids.  $Cd_7X_7^{D(II)}$  and  $Cd_5X_5^{D}$  are built by squares and hexagons, while  $Cd_7X_7^{D(I)}$  has also octagons. Finally, cluster tubes are built by rings located parallel to each other, forming short tubes. All these structures have been described in detail elsewhere.56

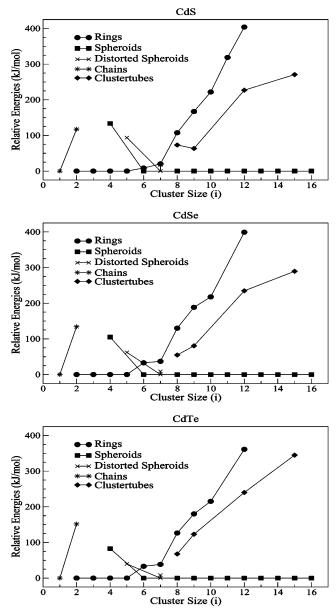
In Figure 2 the relative energies for all shown Cd<sub>i</sub>X<sub>i</sub> clusters are plotted versus the number of CdX units, *i*. In the region of small clusters,  $i \leq 5$ , rings are found to be the most stable structures. Chains are stable only for small sizes, i = 1, 2. Spheroids become more stable as the cluster size increases, and as it can be observed in the region of  $6 \le i \le 16$ , they are the most stable structures. In the case of i = 7 distorted spheroids are the most stable ones, but while for  $Cd_iS_i$  and  $Cd_iSe_i$   $Cd_7$  $X_7^{D(I)}$  is the most stable one, for  $Cd_iTe_i$  this structure lies above the other distorted spheroid,  $Cd_7X_7^{D(II)}$ . Results for  $i \le 7$  are in agreement with previous theoretical calculations. Finally, we observe that, as the cluster size increases, the relative energy between spheroids and rings and cluster tubes increases, the spheroids being the dominant ones. Although similar plots are obtained for all  $Cd_iX_i$ , the most salient feature is that as X goes down in the periodic table from S to Te, the relative energies decrease as well. This is consistent with the relative energies found for  $Cd_iO_i$  clusters<sup>56</sup> and  $Zn_iX_i$ , X = O, S, Se, Te,

clusters.<sup>53–55</sup> This trend may be seen clearly in Figure 3, where the relative energies between rings and three-dimensional structures are shown for all Zn<sub>i</sub>X<sub>i</sub> and Cd<sub>i</sub>X<sub>i</sub> combinations. These relative energies are calculated as  $\Delta E = E_{3D} - E_{ring}$ . Thus, when  $\Delta E$  is positive, the ring structure is more stable and so on. When both the  $Cd_iX_i$  and the  $Zn_iX_i$  series are compared, it is observed that the relative energies are very similar for both cases, which means that Zn and Cd have similar behavior at least in these compounds, and the differences come mainly from X atoms. The main difference is that ring structures are more stable than spheroids for  $i \leq 7$ , in the case of  $Zn_iO_i$  and  $Cd_iO_i$ , while for i  $\leq$  5 in the case of the remaining combinations. This may be explained by the larger ability of S, Se, and Te to achieve higher coordination, due to the d orbitals which, however, are very high in energy for O. The break of ring planarity occurs at different cluster sizes for different compounds, that is, i = 4for  $Y_iSe_i$  and  $Y_iTe_i$  (Y = Zn, Cd), i = 5 for  $Y_iS_i$  and  $Cd_iO_i$ , and i = 7 for  $Zn_iO_i$ . In these compounds the break of planarity occurs at a smaller size as X goes down in the periodic table. In other words, the larger the size of X, the more difficult it is to achieve linear angles. The larger size of Cd with respect to Zn explains why for CdO rings the break occurs at a smaller size compared to ZnO clusters.

**3.2. Stability. Cohesive Energies and Second-Order Free-Energy Differences.** It has been demonstrated elsewhere<sup>66</sup> that many cluster properties, in accordance with the liquid drop model, lie within lines when plotted versus  $i^{-1/3}$ , where *i* is the number of CdX units. The cohesive energy

$$E_{\rm f} = \frac{iE_{\rm Cd} + iE_{\rm X} - E_{\rm Cd_iX_i}}{i} \tag{1}$$

is one of these properties. It has been observed both theoretically and experimentally for  $Si_i$  clusters<sup>67</sup> that clusters belonging to the same family lie within a line. The family lying above is the



**Figure 2.** Relative energies for  $Cd_iX_i$  clusters: starting from above,  $Cd_iS_i$ ,  $Cd_iSe_i$ , and  $Cd_iTe_i$  clusters, respectively.

most stable family in that cluster size range. The cohesive energies of the three families of  $Cd_iX_i$  clusters, i = 3-15, X = S, Se, Te, namely, rings, spheroids, and cluster tubes, are plotted versu  $i^{-1/3}$  in Figure 4.

The points corresponding to the ring structures lie on a line with smaller slope than that of the spheroids and cluster tubes. For small clusters the ring line lies above that of the spheroids and cluster tubes. But at i = 6 there is a crossing and the spheroids lie above, while the cluster tubes lie between the spheroids and the rings. Qualitatively all three graphs are similar, though the cohesive energies are found to decrease as X goes down in the periodic table, which is consistent with experimental data.

Fitting a line to the spheroid points and extrapolating it to  $i^{-1/3} = 0$ , the theoretical value for the cohesive energy of a hypothetical infinite-size spheroid can be obtained. The predicted cohesive energies are 469.62, 432.24, and 363.79 kJ/mol for CdS, CdSe, and CdTe, respectively. In the infinite-size region the bulk is the most stable structure. The bulk cohesive energies are calculated by eq 2,

$$E_{\rm f,exp} = |\Delta H_{\rm f}^{\circ}({\rm CdX}) - \Delta H_{\rm f}^{\circ}({\rm Cd}) - \Delta H_{\rm f}^{\circ}({\rm X})| - RT \quad (2)$$

and according to the CODATA data $^{68}$  are 550.09 and 401.0 kJ/mol for CdS and CdTe, respectively. No experimental data for CdSe have been found.

The cohesive energy is an estimator of the stability; the larger the cohesive energy, the more stable the structure is. The spheroid's extrapolated cohesive energies are close to the bulk ones, which indicates that the stability of the spheroids is large in this size region, i = 6-16. This statement has been confirmed for ZnO clusters, as we predicted, in ref 58 by Bulgakov et al.

The second free-energy difference is a measurement of the stability of the structures. It is also often used as a measure of local stability. We will use it as a measurement of the stability of spheroids. It can be calculated according to

$$\Delta_2 G(\mathrm{Cd}_i X_i^{\mathrm{S}}) = G(\mathrm{Cd}_{i+1} X_{i+1}^{\mathrm{S}}) + G(\mathrm{Cd}_{i-1} X_{i-1}^{\mathrm{S}}) - 2G(\mathrm{Cd}_i X_i^{\mathrm{S}})$$
(3)

and positive values of it correspond to stable structures. These stable structures are associated with electronic shell closure within the jellium model.<sup>69</sup> Gibbs free energies have been used in the calculation of the second differences. The graphs of  $\Delta_2 G$ shown in Figure 5 display maxima at i = 6, 9, 12, and 15. The peak corresponding to i = 12 is clearly the most positive one. This suggests that the Cd<sub>12</sub>X<sub>12</sub> spheroids are the most stable of the studied spheroids. In Figure 6 we provide the vibrational spectra of these most stable spheroids, to help in the characterization of these species.

**3.3. Highest Occupied Molecular Orbital–Lowest Unoccopied Molecular Orbital (HL) Gaps and Experimental Absorption Energies.** HL gaps may be used as an estimator of the excitation energies. They are an upper bound to the true excitation energy,<sup>57</sup> and as the particle size increases the gap approaches the true excitation energy. We have calculated these

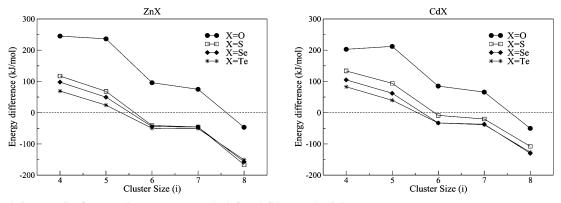


Figure 3. Relative energies for  $Y_iX_i$  clusters:  $Zn_iX_i$  on the left and  $Cd_iX_i$  on the right.

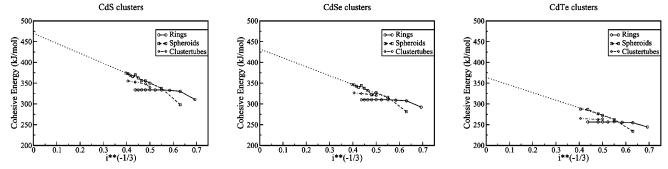


Figure 4. Cohesive energies of Cd<sub>i</sub>X<sub>i</sub> clusters: starting from the left Cd<sub>i</sub>S<sub>i</sub>, Cd<sub>i</sub>Se<sub>i</sub>, and Cd<sub>i</sub>Te<sub>i</sub> clusters, respectively.

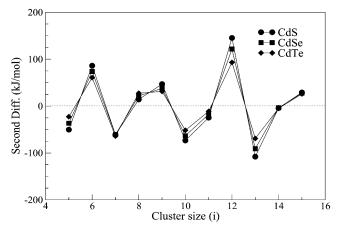


Figure 5. Second differences in energy calculated using Gibbs free energies.

gaps for the characterized spheroids, rings, and cluster tubes, and they are depicted versus the diameter of the particle in Figure 7. For all CdX the largest HL gaps correspond to rings, and the smallest ones correspond to cluster tubes. The experimentally grown nanoparticles are assumed to be spherical with a bulklike crystal structure at the core and a reconstructed surface.<sup>70,71</sup> The shape of this surface reconstruction is not well-

known yet. It is also assumed that the number of atoms of the core are much larger than those of the surface. As the particle size increases, the absorption energy decreases toward bulklike values. This can be observed in Figure 7 as well, where the values of absorption energies tend to bulk values, namely, 2.42 eV for CdS, 1.74 eV for CdSe, and 1.45 eV for CdTe.<sup>1</sup> Comparing HL gaps of clusters with experimental data of smallest nanoparticles, we observe that the HL gaps of spheroids do follow the nanoparticle trend. In the case of the smallest nanoparticles, the importance of the surface absorption is much larger than in large nanoparticles, where the surface/volume ratio is much larger. That is, the absorption energies in the smallest nanoparticles occur mainly in the surface. The similarity between the spheroid's HL gaps and the absorption energies of nanoparticles could be due to structural similarities between them; that is, the nanostructure surface resembles the square-hexagon structure of spheroids. Nevertheless, excitation energies should be calculated to confirm these similarities.

Another point of interest is the fact that when the nanocrystal structures become more stable than spheroids. Experimental nanoparticles are grown in solution, while our calculations are in the gas phase, which makes it difficult to obtain a strong conclusion, but with the data available some predictions can be made. Recall that the coordination number of spheroids is

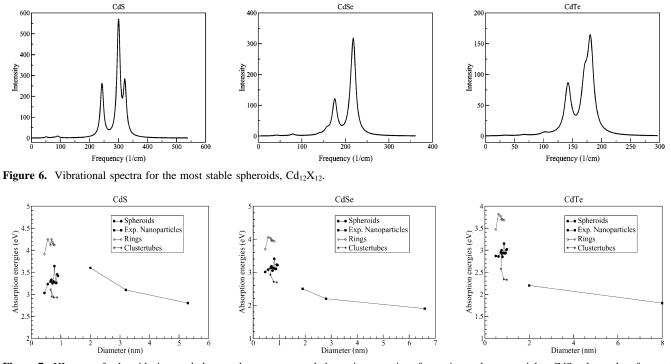


Figure 7. HL gaps of spheroid, ring, and cluster tube structures and absorption energies of experimental nanoparticles. CdS values taken from ref 39, CdSe values from ref 40, and CdTe values from ref 41.

three while that of the bulk is four. In solution, the atoms of the nanoparticle placed in the surface can achieve the fourth coordination number in the interaction with solvent molecules, which can favor bulklike nanocrystals against spheroids. We, therefore, think that spheroids could be difficult to obtain in the experiments that are carried out in solution. However, for experiments made in the gas phase, these spheroids could be characterized. These experiments have been carried out for ZnO, and spheroids have been found, as we predicted.<sup>57</sup>

#### 4. Conclusions

Several structure families of the clusters  $Cd_iX_i$ , i = 1-16, X = S, Se, Te, have been studied. They are found to undergo a ring-to-three-dimensional structural transition. This behavior parallels that of the previously investigated  $Zn_iX_i$  clusters, X =S, Se, Te, but differs markly from that of Zn<sub>i</sub>O<sub>i</sub> and Cd<sub>i</sub>O<sub>i</sub> clusters. This is due to the fact that oxygen d orbitals lie higher in energy and the ability of S, Se, and Te to achieve higher coordination is larger. The structural transition alluded to above arises from a delicate balance between two opposite tendencies. On one hand, rings are favored by the tendency to linearity of the X-Cd-X bonds, and on the other hand, three-dimensional structures are favored by the tendency to achieve higher coordination. Our calculations indicate that the former dominates when the higher coordination does not carry too much strain for the bond angles. This takes place at i = 8 for Cd<sub>i</sub>O<sub>i</sub> and  $Zn_iO_i$  and at i = 6 for  $Zn_iX_i$ ,  $Cd_iX_i$ , X = S, Se, Te. Naturally, the smaller size of the oxygen valence orbitals accounts for its transition occurring at higher cluster sizes.

The predicted structures of the lowest energy threedimensional spheroid structures of  $Cd_iX_i$  can be envisioned as being built of smaller basic building units, namely, the Cd<sub>2</sub>X<sub>2</sub> squares and Cd<sub>3</sub>X<sub>3</sub> hexagons. These structures appear to be the basic structural units for larger clusters in the same sense that C5 pentagons and C6 hexagons constitute the basic structural units of fullerenes. Second-order differences in energy points out that the most stable spheroids in all cases are  $Cd_{12}X_{12}$ . The transition to cluster structures having a larger coordination number, or bulklike structure, is predicted to happen for cluster size i > 16. The diameter of these spheroids is roughly half that of the smallest nanoparticles found experimentally. The experimental nanoparticles are assumed to have bulklike structures; however, a reorganization of the surface on these structures is seen to happen. According to the HL differences of spheroids and absorption energies of nanoparticles, these surface reconstructions could happen in a way where the surfaces resemble a spheroid. We think that these spheroids could be found in gas-phase experiments, as has recently been the case of several small  $Zn_iO_i$  spheroids, predicted previously by our group.

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