

# Gaussian Form of Effective Core Potential and Response Function Basis Set Derived from Troullier–Martins Pseudopotential: Results for Ag and Au

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Received: November 30, 2003; In Final Form: June 9, 2004

We show that the Troullier–Martins scheme for constructing scalar-relativistic pseudopotentials on a particular density functional for plane-wave calculations can be applied in Gaussian-function based LCAO codes. As an example we consider the noble metals silver and gold and derive 11-electron relativistic effective core potentials, as well as a response function basis set generated by the method of Lippert et al. (*J. Phys. Chem.* **1996**, *100*, 6231). With several tests we demonstrate a better performance of these effective core potentials and basis sets as compared to non-DFT-based ECPs of equal quality.

## 1. Introduction

The low-energy physics and chemistry of molecules and solids is governed by valence electrons. The corresponding orbitals are nevertheless affected by core electrons to ensure orthogonality to core orbitals. Pseudopotentials or effective core potentials can represent the effect of the core electrons and decrease the computational effort by focusing on valence electrons only. Moreover, once derived from relativistic calculations, effective core potentials can include relativistic effects, which are important in heavy elements, even though nonrelativistic theory is applied to valence electrons.

It is a long-standing practice in the condensed matter community to use pseudopotentials in plane wave density functional theory (DFT) calculations with the density functional that was employed to generate them from a reference atomic state. For reviews on plane-wave based methods see refs 1 and 2, and on norm-conserving pseudopotentials in plane-wave calculations see ref 3. This is a natural and logical choice whenever one of the plane-wave DFT codes developed by different groups is used, e.g., CPMD,<sup>4</sup> ABINIT,<sup>5</sup> CASTEP,<sup>6</sup> FHI96md<sup>7</sup> (norm-conserving pseudopotentials), DaCapo,<sup>8</sup> PWscf,<sup>9</sup> VASP<sup>10</sup> (ultrasoft pseudopotentials). The LCAO based code SIESTA<sup>11</sup> employs the same numeric pseudopotentials as plane-wave based codes. An alternative approach is used in the Slater-orbital based ADF code,<sup>12</sup> where so-called core functions are introduced. They are not variational degrees of freedom and serve as fixed core charges which generate the potential experienced by valence electrons.

In quantum chemistry Gaussian-function-based LCAO computations, effective core potentials were originally derived either from a reference calculation of a single atom within the Hartree–Fock or Dirac–Fock approximations, or from some method including electron correlations. A review of these methods, as well as a general theory of ECPs is provided in ref 13. Effective core potentials are based on the frozen-core approximation and serve to represent the potential generated by core electrons, also incorporating relativistic effects. So-called shape-consistent ECPs are rather easy to derive and contain no

adjustable parameters. On the contrary, energy-consistent ECPs are used for high-quality studies of specific systems and specific quantities. The parameters of such ECPs and the underlying basis set can be adjusted in accordance with representative experimental data, not only for the ground state, but also for excited states, electron affinities, ionization potentials, and so on. Being of semiempirical origin, they can perform remarkably well for a given system, but their transferability to other environments can be poorer than that of shape-consistent ECPs.

The construction of shape-consistent ECPs is based on the original proposal of Christiansen–Lee–Pitzer<sup>14</sup> where norm-conservation was introduced. Simultaneously, norm-conserving pseudopotentials were introduced in computational condensed matter physics by Hamann et al.<sup>15</sup> For transition metals, a widely used analytical form of Hartree–Fock ECPs was obtained by the Los Alamos group.<sup>16,17</sup>

In the past, a flurry of work dealing with noble and transition metals within DFT employed effective core potentials derived for mainstream quantum chemistry approaches. Both transport and ground-state electronic structure calculations followed this way. As some examples, we mention recent studies of medium-size silver clusters,<sup>18</sup> adsorption on gold and platinum clusters<sup>19–21</sup> and on platinum and silver slabs,<sup>22–24</sup> transport through a molecular wire contacted to noble metals,<sup>25–28</sup> metallo-organic complexes,<sup>29</sup> metal hydrides,<sup>30</sup> and so on. The common trend to make these potentials more flexible for density-functional theory treatment is to vary exponents and contraction coefficients of Gaussian primitives to attain an optimum description. However, when used with DFT, this simple adjustment of basis functions cannot cure the problem that most popular ECPs in quantum chemistry were not derived for DFT. We must mention at the outset that this issue is not so important whenever a small core can be assumed. The smaller the core, the less important is the method by which ECP is derived. In the limit of a bare nucleus, the potential becomes  $\sim 1/r$ , which is of course independent of the method. Our primary interest is in large systems containing heavy noble and nearly-noble metals used as substrates in adsorption studies. For these metals the  $ns$  and  $np$  atomic levels lie distinctly below the  $nd$  levels ( $n = 4$  for

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Ag and 5 for Au), whereas the  $(n + 1)s$  and  $(n + 1)p$  levels are relatively close to the  $nd$  levels so that states derived from all three levels overlap and significantly contribute to bonding in the bulk and at surfaces. Treating  $ns$  and  $np$  states together with lower-lying ones as belonging to the core is therefore a reasonable choice that leads to 11 electron ECPs. Including  $nd$  states in the core would require a large core radius and would ignore  $sp-d$  hybridization effects that are known to be important near the Fermi level of noble metals. On the other hand, treating  $ns$  and  $np$  states as valence pseudo-orbitals, leading to 19 electron ECPs, while ensuring a small core radius, increases computing time and storage at a cost that is not justified for most properties, except those significantly affected by the polarization of the states in question. For our purposes, 11 electron ECPs represent the best compromise.

There have already been reports by the Bonacic–Koutecky group<sup>31,32</sup> about BLYP single-electron ECPs for silver and gold that were successfully applied to silver and mixed silver–gold clusters. These ECPs are energy-consistent, hence difficult to construct, and are intended for high-quality studies of specific properties.

For the sake of completeness, let us briefly mention existing ECPs for silver and gold:

1. Los Alamos 11-electron ECPs<sup>16</sup> and 19-electron ECPs,<sup>17</sup> designated as Lan11DZ and Lan12DZ. These ECPs are shape-consistent and are derived from reference calculations on an isolated atom within scalar-relativistic Dirac–Fock theory, which includes mass–velocity and Darwin terms.

2. Bonacic–Koutecky 1-electron ECP for silver to be used with the BLYP functional.<sup>31,32</sup> The parameters are fitted to reproduce experimental observables of small systems.

3. Bonacic–Koutecky 11-electron ECP<sup>33</sup> for silver, intended for usage at a correlated level of theory (MRD-CI, CCSD) and supplied with a large basis set (6s5p5d/5s3p2d). The initial parameters were taken from the Los Alamos group and then re-optimized in accordance with experimental data.

4. Stuttgart–Dresden 1-electron and 19-electron ECPs,<sup>34,35</sup> designated as SDD. These energy-consistent ECPs are constructed to reproduce experimental observables of a single atom, like ionization potentials and excitation energies, within relativistic Dirac–Fock theory.

5. Basch ECP for silver.<sup>36</sup> Like Lan11DZ, it is derived from relativistic Dirac–Fock calculations and replaces the [Kr] core.

6. Steven–Basch–Krauss 19-electron ECPs,<sup>37</sup> named CEP. Like Lan12DZ, they are shape-consistent and derived from Dirac–Fock theory.

To the best of our knowledge, there are currently no 11-electron ECP for silver and gold derived for DFT-based methods to be used in Gaussian codes. Motivated by our current interests, namely the study of adsorbed molecules on silver and gold surfaces or clusters within density-functional theory, we found the present situation unsatisfactory. Our primary goal is not to construct ECPs that would rival the best existing ECPs for these metals, but rather to construct computationally effective ECPs consistent with pseudopotentials extensively used with plane waves together with a suitable Gaussian basis set that would yield a LCAO description at the same level of DFT. To derive a basis set consistent with a given ECP and a given density functional, we follow the systematic procedure of Lippert et al.<sup>38</sup> Their construction is based on response functions of a given atom that describe the linear, quadratic, cubic, etc. response to an external perturbation. Linear response functions are closely connected to the so-called chemical hardness,<sup>39</sup> a useful concept for molecular systems when interactions between

subsystems is weak. In the work presented here we included only linear response functions, which yield a basis set of double- $\zeta$  quality. Computations on small test systems demonstrate that results obtained with our 11-electron ECPs are superior to those obtained with Lan11DZ, and slightly less accurate than those using 19-electron ECPs.

All calculations have been performed with the Gaussian03 package.<sup>40</sup>

## 2. Procedure

Our starting point is to select a well-defined and well-tested pseudopotential scheme. Among several possibilities, we choose the popular and relatively simple Troullier–Martins scheme.<sup>41</sup> For the details of constructing numerical Troullier–Martins pseudopotentials for the different  $l$ -channels we refer to the original article. Briefly, a pseudo-orbital of angular momentum  $l$  is written in the core region as  $r^l \exp[p_6(r)]$  with  $p_6(r)$  being a sixth-order polynomial with seven fitting constants. The latter are adjusted to ensure norm-conservation, continuity of the pseudo-orbital, and its first and second derivatives at a chosen core radius  $r_c$ , as well as other specific requirements. Then, screened pseudopotentials are derived by inverting the Schrodinger equation (using the all-electron energy eigenvalue) and transferable ionic pseudopotentials are finally obtained by subtracting from those  $l$ -dependent pseudopotentials Hartree and exchange-correlation potentials produced by pseudo valence electrons. Atomic pseudo-orbitals are therefore solutions to the single-particle radial Schrodinger equation for a screened pseudopotential, as well as solutions of the self-consistent Kohn–Sham equations for the corresponding ionic pseudopotentials. The required all-electron calculations are performed in the spin-restricted formalism (with half occupancies allowed) and scalar-relativistic mass-velocity and Darwin terms are included in the radial Kohn–Sham equation:

$$\left[ \frac{1}{2M(r)} \left( -\frac{d^2}{dr^2} - \frac{1}{2M(r)c^2} \frac{dV_{\text{eff}}(r)}{dr} r \frac{d}{dr} \frac{1}{r} + \frac{l(l+1)}{r^2} \right) + V_{\text{eff}}(r) - \epsilon_i \right] u_{nl}(r) = 0 \quad (1)$$

where  $V_{\text{eff}}(r)$  is the effective Kohn–Sham potential and  $M(r) = 1 + (\epsilon_i - V_{\text{eff}}(r))/2c^2$ .

**2.1. Effective Core Potentials.** To perform all-electron calculations and construct a numerical Troullier–Martins DFT pseudopotential, we use the well-tested and widely used fhi98PP code.<sup>42</sup> In this article we present results obtained with the BLYP generalized-gradient functional.<sup>43,44</sup>

We choose the  $f(l = 3)$  component to be local and equal to the bare core potential:

$$V_{l=3}(r) = -\frac{Z}{r} \quad (2)$$

In our case  $Z = 11$ ; the  $l$ -dependent components for lower angular momentum channels are defined as

$$V_{l<3}(r) = V_l^{\text{TM}}(r) + \frac{Z}{r} \quad (3)$$

where  $l = 0, 1, 2$  (s, p, d) and TM stands for Troullier–Martins. Because the latter pseudopotentials are finite at the origin,  $V_{l<3}(r)$  behave like  $r^{-1}$  as  $r \rightarrow 0$  in contrast to Stuttgart–Dresden or Los Alamos ECPs, which diverge like  $r^{-2}$ . In a manner similar to those ECPs we expand these projections as a finite

sum of weighted Gaussians multiplied by the Jacobian weighting factor  $r^2$ :

$$U_{l-L}(r) = V_{l-L}(r)r^2 = \sum_k b_k r^{n_k} e^{-\zeta_k r^2} \quad (4)$$

where  $n_k = 1$  for  $k = 1$  and  $n_k = 2$  otherwise. The expansion coefficients  $b_k$ 's and exponents  $\zeta_k$ 's are to be determined by a suitable fitting procedure. Of course, the parameters are different for different  $l$ -components.

**2.2. Basis Set.** Troullier–Martins, as well as all norm-conserving pseudopotentials, share the property that logarithmic derivatives of pseudo-orbitals and all-electron orbitals for a given  $l$  are equal at the appropriate core radius and reference energy (atomic eigenvalue). This property strictly applies in the limit of a full basis set. In practice, one can make use of norm-conservation if a rather good basis set is chosen.

There are many ways to generate a suitable and compact basis set for a given problem (see, e.g., refs 45–47 and references therein). Assuming that an atom is subject to an external perturbation parametrized by  $t$ , Kohn–Sham orbitals can be expanded in a Taylor series with respect to the perturbation:

$$\psi(t) = \psi(0) + t \frac{\partial \psi}{\partial t} + \frac{t^2}{2} \frac{\partial^2 \psi}{\partial t^2} + \dots \quad (5)$$

Lippert et al.<sup>38</sup> showed that the local atomic basis set

$$\psi, \frac{\partial \psi}{\partial t}, \frac{\partial^2 \psi}{\partial t^2} \dots \quad (6)$$

provides a rapidly convergent description of the atom embedded in a molecule or a solid. Here we apply this procedure for a pseudoatom keeping only linear terms. A similar procedure was applied for pseudoatom calculations to generate basis functions for  $O(N)$  calculations in ref 48. As the perturbation, we consider the change in partial occupancies of atomic s and p states, the total charge being conserved.

To be specific, s and d basis functions are derived by a least-squares fit of a finite sum of primitive Gaussians to numerical Troullier–Martins pseudoorbitals, that is

$$\psi_l(r) = \sum_i c_{il} g_l(\alpha_{il}, r) \quad (7)$$

where  $l = 0, 2$  and  $g_l$  stand for normalized primitive Gaussians with exponents  $\alpha_{il}$ . Linear response s and d functions, which we call  $s^+$  and  $d^+$ , are derived by performing a spin-restricted calculations of an atom with occupancy of d set to 10.0, but occupancies of s and p set to 0.95 and 0.05, respectively. From the resulting numerical pseudoorbitals  $\psi'$ , linear response functions are obtained by a least-squares fit of the difference:

$$\psi_l^+(r) = N(\psi_l(r) - \psi_l'(r)) = \sum_i d_{il} g_l(\beta_{il}, r) \quad (8)$$

$N$  being a normalization factor. Polarization functions p and  $p^+$  are derived by making use of the known result that the partial occupancy of the valence p atomic state in solid silver and gold is approximately 0.3.<sup>49</sup> Therefore, we performed atomic calculations with occupancies of s and p states set to 0.7, 0.3 as well as 0.65, 0.35, respectively, and derived pseudo-orbital and linear response functions p and  $p^+$  by a similar fitting procedure. Choosing three primitive Gaussians we obtain compact basis sets (6s6p6d/2s2p2d) for silver and (6s6p5d/2s2p2d) for gold.

Numerical TM pseudopotentials for Ag

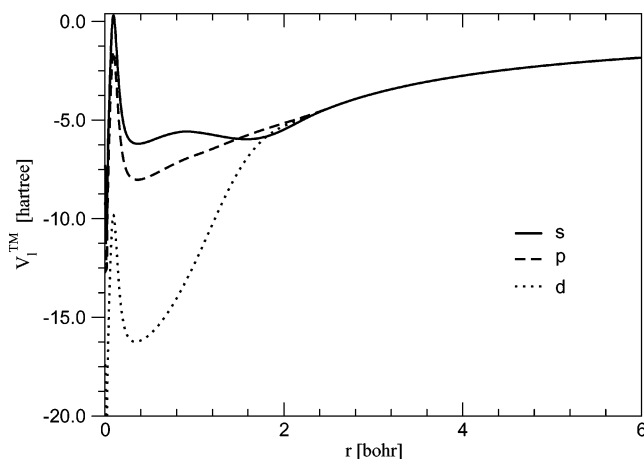


Figure 1. Numerical Troullier–Martins pseudopotentials for silver.

Effective core potentials

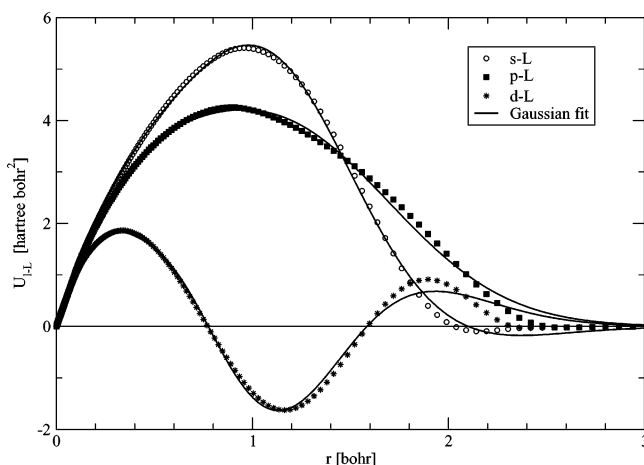


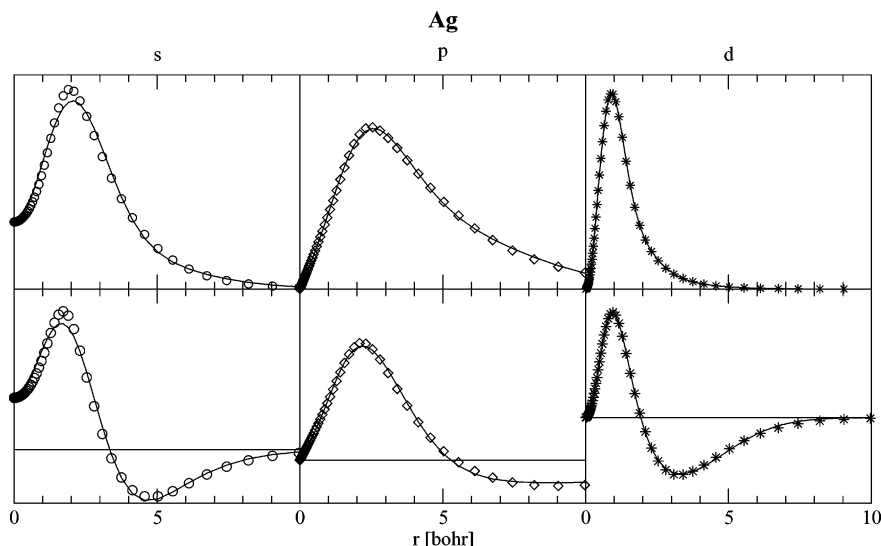
Figure 2. Effective core potentials for silver. Symbols show numerical values, and solid lines represent analytical fits.

If necessary, more basis functions can be generated, and polarization f functions can be added by slightly modifying the procedure.

### 3. Results

**3.1. ECPs.** Numerical Troullier–Martins pseudopotentials for silver are plotted in Figure 1. There is still freedom in constructing a pseudopotential given a well-defined scheme, namely, choosing the core radii at which all-electron and pseudoatom Kohn–Sham orbitals are matched. Usually, the bigger the radius, the smoother the pseudopotentials, and hence the lower the cutoff for plane-wave calculations. On the contrary, the smaller the core radius, the harder the pseudopotentials, but the better their transferability. In plane-wave codes, constructing a pseudopotential is therefore a tradeoff between those two extremes. In the LCAO formulation wave functions need not be smooth, and therefore transferability can be better. Nevertheless, for a meaningful comparison we choose core radii to be the same as used in plane-wave calculations, namely 2.40 bohr for s and d, and 2.60 bohr for p states.

The different  $l$ -components as well as Gaussian fits in the case of silver are depicted in Figure 2. In the course of our work, we found that fitting a numerical ECP to a sum of Gaussians is by far the most delicate task. It appeared easier to



**Figure 3.** Ag pseudoorbitals (top) and linear response orbitals (bottom). Symbols show numerical values, and solid lines represent analytical fits.

**TABLE 1: ECP Parameters for Silver**

<i>k</i>	s - L			p - L			d - L		
	<i>n<sub>k</sub></i>	$\zeta_k$	<i>b<sub>k</sub></i>	<i>n<sub>k</sub></i>	$\zeta_k$	<i>b<sub>k</sub></i>	<i>n<sub>k</sub></i>	$\zeta_k$	<i>b<sub>k</sub></i>
1	1	1.712	11.074	1	0.897	11.074	1	12.668	9.524
2	2	1.391	-166.201	2	1.2260	-22.6472	2	1.662	227.659
3	2	1.194	255.676	2	0.9789	16.8557	2	1.400	-363.576
4	2	1.033	-91.757				2	1.205	150.286

**TABLE 2: ECP Parameters for Gold**

<i>k</i>	s - L			p - L			d - L		
	<i>n<sub>k</sub></i>	$\zeta_k$	<i>b<sub>k</sub></i>	<i>n<sub>k</sub></i>	$\zeta_k$	<i>b<sub>k</sub></i>	<i>n<sub>k</sub></i>	$\zeta_k$	<i>b<sub>k</sub></i>
1	1	2.286	10.881	1	1.380	10.721	1	11.000	9.383
2	2	1.088	-97.386	2	1.111	-63.222	2	1.660	225.822
3	2	1.267	270.134	2	0.987	60.634	2	1.342	286.233
4	2	1.499	-171.733				2	1.437	-497.561

fit the wave functions than ECPs. Nonlinear fits were performed with the help of Grace package,<sup>50</sup> using the Levenberg–Marquardt algorithm without weighting function. It is also more important to get accurate fits for the pseudopotentials, because SCF calculations are variational in orbital space, but not in pseudopotentials. As a result, the performance of a given ECP will largely depend on the care devoted to the fitting procedure, for which sophisticated algorithms might improve the quality of the fit.

Parameters of our ECP for silver are presented in Table 1 and those for gold in Table 2. The coefficients  $b_1$  of eq 4 are close to 11.0 because  $n_1 = 1$ , whereas  $n_k = 2$  for  $k > 1$ . Instead of imposing  $b_1 = Z$ , we treat all  $b_k$ 's and  $\zeta_k$ 's as adjustable parameters to obtain the best possible agreement in the range where each of the  $U_{l-L}$  is large.

**3.2. Basis Set.** The pseudoorbitals and linear response orbitals of silver are plotted in Figure 3. The p function is the most diffuse, showing the fact that it is weakly bound, whereas the d function is highly localized. The node of the  $s^+$  function occurs at approximately 3.2 bohr, that of the  $p^+$  function at 5.1 bohr, and of the  $d^+$  function at 2.0 bohr, which is almost the extent of the pseudoorbitals themselves. Parameters of the response function basis set of double- $\zeta$  quality are presented in Tables 3 and 4.

#### 4. Test Results

In this section we discuss test results for several simple silver and gold systems. Results obtained with different ECPs are

**TABLE 3: Parameters of the Response Function Basis Set for Silver**

<i>i</i>	s		p		d	
	$\alpha_{i0}$	<i>c<sub>i0</sub></i>	$\alpha_{i1}$	<i>c<sub>i1</sub></i>	$\alpha_{i2}$	<i>c<sub>i2</sub></i>
1	0.2453	-2.8644	0.4583	-0.0478	1.3546	0.6361
2	0.2023	3.29386	0.1198	0.4529	0.4226	0.4217
3	0.0365	0.49972	0.0274	0.6994	0.1271	0.1444

<i>i</i>	$s^+$		$p^+$		$d^+$	
	$\beta_{i0}$	<i>d<sub>i0</sub></i>	$\beta_{i1}$	<i>d<sub>i1</sub></i>	$\beta_{i2}$	<i>d<sub>i2</sub></i>
1	0.2725	-2.4880	0.5756	-0.0417	1.1744	0.2168
2	0.1765	4.4625	0.1224	0.59572	0.6084	0.1877
3	0.0570	-2.0099	0.0067	-0.8984	0.0982	-1.0009

**TABLE 4: Parameters of the Response Function Basis Set for Gold**

<i>i</i>	s		p		d	
	$\alpha_{i0}$	<i>c<sub>i0</sub></i>	$\alpha_{i1}$	<i>c<sub>i1</sub></i>	$\alpha_{i2}$	<i>c<sub>i2</sub></i>
1	0.2668	-2.9011	0.3837	-0.0770	1.2109	0.5513
2	0.2137	3.4494	0.1268	0.4872	0.4059	0.4709
3	0.0354	0.3681	0.0290	0.6863	0.1257	0.1801

<i>i</i>	$s^+$		$p^+$		$d^+$	
	$\beta_{i0}$	<i>d<sub>i0</sub></i>	$\beta_{i1}$	<i>d<sub>i1</sub></i>	$\beta_{i2}$	<i>d<sub>i2</sub></i>
1	0.2870	-2.9512	0.4947	-0.0700	0.8854	0.4146
2	0.1870	5.5399	0.1306	0.6590	0.08670	-0.9702
3	0.0750	-2.6642	0.0084	-0.8922		

compared. In the following table the present ECPs are denoted as TM (Troullier–Martins) and SZ (single- $\zeta$ ) or DZ (double- $\zeta$ ). For atoms, a very big basis set including twelve Gaussians (for each of *s* and *d* functions) was also tested in the case of TM and Lanl1 ECPs.

**4.1. Atomic Tests.** Results for the silver atom are presented in Table 5. We did not include numerical ionization potentials (IPs) and electron affinities (EAs) mainly because neutral atom calculations were performed in the spin-restricted formalism (spin-singlet state with half occupancies). This raises the energy of an isolated atom and therefore decreases the IP value and increases the EA value. Numerical Kohn–Sham eigenenergies are close to those of TMSZ and TMDZ; SDD also shows very good agreement, whereas Lanl2DZ slightly overbinds d-states. Lanl1DZ performs very poorly, over-binding d-states and under-binding the s-state, thus giving rise to a *s* - *d* difference of 5.88 eV, which can lead to a poor description of *s*-*d*

**TABLE 5: Comparison of Kohn–Sham Eigenenergies, Ionization Potentials, and Electron Affinities of the Ag Atom**

	$\epsilon_{4d}$ (eV)	$\epsilon_{4d}$ (eV)	$\epsilon_{5s}$ (eV)	$E_{\text{tot}}$ (au)	IP (eV)	EA (eV)
numerical value		-7.34	-4.45	-35.9900		
Lan11DZ	-9.80	-9.67	-3.92	-38.9551	6.97	0.39
Lan12DZ	-7.46	-7.32	-4.60	-145.6558	7.80	1.10
Lan11-12Z	-9.75	-9.62	-3.94	-38.9621	7.05	0.97
SDD	-7.30	-7.13	-4.73	-146.9080	8.08	1.43
CEP	-7.13	-6.97	-4.53	-146.1825	7.88	1.06
TMSZ	-7.42	-7.20	-4.67	-35.9650	8.14	0.63
TMDZ	-7.34	-7.16	-4.66	-35.9652	7.92	1.18
TM-12Z	-7.23	-7.05	-4.72	-35.9797	8.03	1.42
exp					7.58	1.30

**TABLE 6: Comparison of Equilibrium Distances  $r_e$ , Binding Energies  $D_e$ , and Vibrational Frequencies  $\omega_e$  for the Ag<sub>2</sub> Dimer.**

ECP	$r_e$ (Å)	$D_e$ (eV)	$\omega_e$ (cm <sup>-1</sup> )
Lan11DZ	2.75	1.26	131
Lan12DZ	2.62	1.69	174
SDD	2.60	1.66	175
CEP	2.62	1.68	172
TMSZ	2.71	1.41	157
TMDZ	2.67	1.48	164
exp	2.50	1.67	192

**TABLE 7: Comparison of Equilibrium Distances  $r_e$ , Binding Energies  $D_e$ , Vibrational Frequencies  $\omega_e$ , Dipole Moments  $\mu_e$ , and Mulliken Charges on Hydrogen Atom  $\Delta q_H$  for the AgH Molecule**

ECP	$r_e$ (Å)	$D_e$ (eV)	$\omega_e$ (cm <sup>-1</sup> )	$\mu_e$ (D)	$\Delta q_H$
Lan11DZ	1.77	2.00	1385	3.25	-0.06
Lan12DZ	1.64	2.41	1702	2.55	+0.03
SDD	1.63	2.47	1765	2.31	+0.05
CEP	1.64	2.44	1742	2.40	+0.03
TMSZ	1.69	2.26	1643	2.45	+0.01
TMDZ	1.68	2.29	1640	2.40	+0.02
exp	1.62	2.39	1760		

**TABLE 8: Comparison of Equilibrium Distances  $r_e$ , Binding Energies  $D_e$ , Vibrational Frequencies  $\omega_e$ , Dipole Moments  $\mu_e$ , and Mulliken Charges on Chlorine Atom  $\Delta q_{Cl}$  for the AgCl Molecule.**

ECP	$r_e$ (Å)	$D_e$ (eV)	$\omega_e$ (cm <sup>-1</sup> )	$\mu_e$ (D)	$\Delta q_{Cl}$
Lan11DZ	2.47	2.91	282	6.30	-0.39
Lan12DZ	2.41	2.76	308	5.29	-0.28
SDD	2.38	2.82	312	5.05	-0.25
CEP	2.39	2.83	314	5.04	-0.30
TMSZ	2.46	2.51	288	5.06	-0.35
TMDZ	2.45	2.67	292	5.15	-0.33
exp	2.28	3.24	344	5.73	

hybridization in polyatomic systems. Even when the large 12Z basis set is used in conjunction with TM and Lan11 ECPs, the trends remain the same. Compared to experimental IP and EA values, all ECPs with double- $\zeta$  basis sets (except Lan11DZ) show a good agreement. Lan11DZ, on the contrary, underestimates IP and severely underestimates EA; TMSZ, being of “minimal” nature, performs not too well either but gives some improvement over Lan11DZ. The same tendencies are apparent for the gold atom (Table 9). For the eigenvalues, SDD and TMDZ perform very well, whereas Lan12DZ slightly overbinds d-states. Lan11DZ again overbinds d-states and underbinds the s-state. For IPs and EAs, Lan12DZ, SDD, and TMDZ perform very much alike, whereas Lan11DZ fails once again. Given that SDD, CEP, and Lan12DZ are 19-electron ECPs, the good performance of 11-electron ECP TMDZ is encouraging.

**4.2. Diatomic Molecules.** Turning now to properties of dimers, for Ag<sub>2</sub> the performance of TMDZ is poorer than that of Lan12DZ and SDD if compared to experimental results.

**TABLE 9: Comparison of Kohn–Sham Eigenenergies, Ionization Potentials, and Electron Affinities of the Au Atom**

	$\epsilon_{4d}$ (eV)	$\epsilon_{4d}$ (eV)	$\epsilon_{5s}$ (eV)	$E_{\text{tot}}$ (au)	IP (eV)	EA (eV)
numerical value		-6.76	-5.77	-32.9259		
Lan11DZ	-8.88	-8.66	-4.80	-34.7921	8.24	0.86
Lan12DZ	-7.14	-6.92	-6.07	-135.3516	9.49	2.22
Lan11-12Z	-8.80	-8.58	-4.87	-34.8028	8.28	1.52
SDD	-6.93	-6.69	-5.95	-135.6906	9.53	2.29
CEP	-6.72	-5.78	-6.49	-136.0018	9.39	2.03
TMSZ	-7.00	-6.70	-5.96	-32.9691	9.82	1.54
TMDZ	-6.93	-6.65	-5.95	-32.9693	9.50	2.15
TM-12Z	-6.80	-6.53	-6.08	-32.9836	9.66	2.39
exp					9.23	2.31

**TABLE 10: Comparison of Equilibrium Distances  $r_e$ , Binding Energies  $D_e$ , and Vibrational Frequencies  $\omega_e$  for the Au<sub>2</sub> Dimer**

ECP	$r_e$ (Å)	$D_e$ (eV)	$\omega_e$ (cm <sup>-1</sup> )
Lan11DZ	2.74	1.53	138
Lan12DZ	2.58	1.99	156
SDD	2.60	2.00	158
CEP	2.59	2.06	159
TMSZ	2.65	1.74	148
TMDZ	2.62	1.85	153
exp	2.47	2.29	191

**TABLE 11: Comparison of Equilibrium Distances  $r_e$ , Binding Energies  $D_e$ , Vibrational Frequencies  $\omega_e$ , Dipole Moments  $\mu_e$ , and Mulliken Charges on Fluorine Atom  $\Delta q_F$  for the AuF Molecule**

ECP	$r_e$ (Å)	$D_e$ (eV)	$\omega_e$ (cm <sup>-1</sup> )	$\mu_e$ (D)	$\Delta q_F$
Lan11DZ	2.17	2.83	469	4.44	-0.34
Lan12DZ	2.00	2.80	497	3.38	-0.30
SDD	2.00	3.11	512	3.75	-0.26
CEP	2.00	2.98	534	3.47	-0.28
TMSZ	2.05	2.42	483	3.12	-0.30
TMDZ	2.03	2.87	510	3.58	-0.27
MP4 <sup>52</sup>	1.94	3.05	540	5.00	

Lan11DZ performs worse than TMSZ, but keeping in mind the underbinding tendency of the BLYP functional,<sup>51</sup> the larger-than-experimental values of binding energies obtained with Lan12DZ and CEP seem to indicate an intrinsic deficiency of these ECPs when used with DFT. For Au<sub>2</sub> (Table 10), all ECPs seem to perform rather well; SDD, CEP, and Lan12DZ yield a somewhat better agreement, whereas Lan11DZ fails here also. For the case of AgH (Table 7), Lan12DZ and SDD perform slightly better than TMDZ, but the latter gives significant improvement over Lan11DZ. The dipole moments predicted by all the ECPs, except Lan11DZ, are close to each other.

It is very important to test molecules, in which charge transfer is expected to be significant. Results for molecule AgCl and AuF are presented in Tables 8 and 11, respectively (6-31G basis set was used for F, and Lan12DZ for Cl). Compared to Lan12DZ, CEP and SDD, TMDZ shows the same trends as in Ag<sub>2</sub> and Au<sub>2</sub>: equilibrium distances are slightly larger, binding energies and vibrational frequencies slightly smaller, but dipole moments are similar, as well as Mulliken charges on chlorine and fluorine atoms.

We note, however, that the comparison of different ECPs should be viewed with some care. Lan12DZ, SDD, and CEP include semicore states and there is a total energy gain in the molecular system because of the semicore polarization. In contrast, no semicore states are included in the calculations employing TM and Lan11 ECPs. Nevertheless, in our opinion, the adopted method of constructing effective core potentials and basis functions for Gaussian codes has the advantage of being systematic and thus open for improvement.

## 5. Conclusions

We have shown how Troullier–Martins atomic pseudo-potentials, generated for a particular density functional, can be used to construct effective core potentials for Gaussian-based codes. Going beyond the present double- $\zeta$  level, basis sets of triple- $\zeta$  and higher quality, as well as polarization functions, can be constructed by similar means. Our 11-electron ECPs are not expected to perform better than 19-electron ECPs (both semiempirical like SDD or shape-consistent like LanL2DZ) but give significant improvement over non-DFT derived 11-electron ECPs. They can be thus used for studies of larger systems, like molecules adsorbed on noble metal clusters and slabs. Results can in principle be more meaningfully compared to plane-wave calculations based on the same density functional. In the present study we tested the performance of these ECPs (together with a double- $\zeta$  response function basis set) for small systems containing silver and gold atoms and showed them to perform well as opposed to 11-electron ECP derived from Dirac–Fock calculation (LanL1DZ). This clearly demonstrates that the derivation of ECPs and their application should be based on the same model chemistry.

**Acknowledgment.** We acknowledge financial support from the Swiss National Science Foundation through its NCCR for Nanoscale Science, and the Computing Center of the University of Basel for computational resources. We thank S. Goedecker for discussions and in particular for pointing out ref 38.

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