

B3LYP Investigation of  $\text{HPO}_2$ , *trans*-HOPO, *cis*-HOPO, and Their Radical Anions

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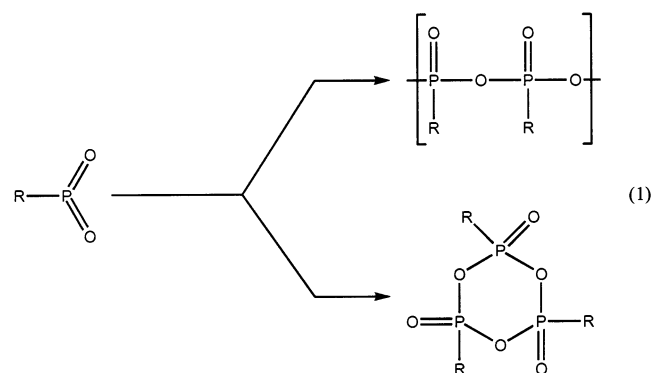
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The B3LYP density functional method was used to determine the optimized geometries, harmonic vibrational frequencies, and anharmonic vibrational frequencies of  $\text{HPO}_2$  and the *trans*- and *cis*-isomers of HOPO. Additionally, the isotropic hyperfine splitting (hfs) constants and the vibrationally averaged hfs were determined for the radical anions of each species. *cis*-HOPO is predicted to be the lowest energy isomer of the neutral systems, with *trans*-HOPO lying 3.0 kcal mol<sup>-1</sup> higher and  $\text{HPO}_2$  lying 11.9 kcal mol<sup>-1</sup> higher than that. The pyramidal  $\text{HPO}_2^-$  radical is the lowest energy anion, and the *cis*- and *trans*-isomers lie ~5 and ~8 kcal mol<sup>-1</sup>, respectively, above  $\text{HPO}_2^-$ . Higher lying  $\sigma$  radicals of HOPO<sup>-</sup> resemble  $\text{PO}_2^-$  and free H. The B3LYP/6-311+G(2d,2p) values of  $A_{\text{iso}}(^1\text{H}) = 1211.98$  MHz (*trans*) and 1199.90 MHz (*cis*) confirm that the  $^2\text{A}'$  HOPO anion dissociates to  $\text{PO}_2^- + \text{H}$ .  $\text{H}_2\text{PO}$  was also investigated because of its similarity to  $\text{HPO}_2^-$ . The computed hfs constant for  $^1\text{H}$  (109.64 MHz) is fortuitously in excellent agreement with the experimental value, while that for  $^{31}\text{P}$  (950.29 MHz) differs significantly from experiment, and this deviation is attributed to the lack of a basis set for P that provides a good description of the P 1s core. Vibrational averaging affects the computed hfs in  $\text{H}_2\text{PO}$  by 5–6 MHz for  $A_{\text{iso}}(^{31}\text{P})$  but only by ~2 MHz in  $\text{HPO}_2^-$ . The effect of vibrational averaging is small (1–2 MHz) for  $A_{\text{iso}}(^1\text{H})$  but more significant (8–20 MHz) in  $\text{HPO}_2^-$ .  $A_{\text{iso}}(^{17}\text{O})$  is relatively unaffected by vibrational averaging in both  $\text{H}_2\text{PO}$  and  $\text{HPO}_2^-$ . Solvent effects were evaluated using the conductor-like polarizable continuum model (CPCM), and these hfs values for  $\text{HPO}_2^-$  [ $A_{\text{iso}}(^{31}\text{P}) = 1123.42$  MHz,  $A_{\text{iso}}(^1\text{H}) = 243.51$  MHz] and  $\text{H}_2\text{PO}$  [ $A_{\text{iso}}(^{31}\text{P}) = 1003.54$  MHz,  $A_{\text{iso}}(^1\text{H}) = 109.27$  MHz] are in closer agreement with experiment. Convergence of the Fermi contact terms for  $^{31}\text{P}$  computed using B3LYP with the aug-cc-pCVXZ and aug-cc-pV(X+d)Z families of basis sets is erratic and slow. On the other hand, with the same basis sets, CCSD(T) produces hfs constants for the P atom that are in close agreement with experiment.

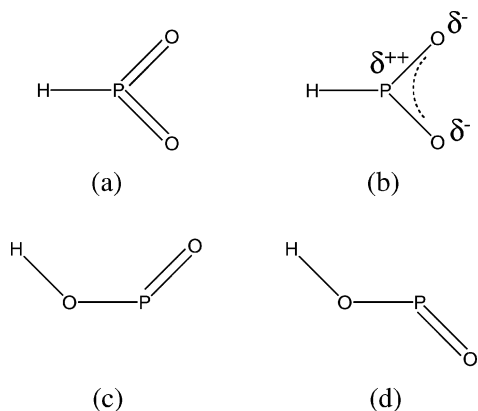
## I. Introduction

Dioxophosphoranes (three-coordinate phosphoryl derivatives,  $\text{RPO}_2$ ) have long been considered as transient species or reaction intermediates. Some dioxophosphoranes are important intermediates in combustion chemistry,<sup>1</sup> while others have a key role in biological phosphorylation.<sup>2</sup> Dioxophosphoranes can even be strong enough phosphorylating agents to react with OH groups on the surface of some solids.<sup>3</sup> In 1991, Bodalski and Quin<sup>4</sup> reported that some dioxophosphoranes attack epoxides, first forming a Lewis salt and then rearranging to form five-membered cyclic phosphates. As a result of the strong electrophilic character of phosphorus in these systems, dioxophosphoranes can undergo self-reaction, polymerizing to form linear chains or cyclic systems (eq 1). Although the interest in low-



coordination P-containing systems has grown and many have been successfully synthesized, dioxophosphoranes have remained elusive.<sup>5</sup>

Despite such interest in phosphoranes and molecules containing group 15 atoms with low coordination numbers, very few possible  $\text{RPX}_2$  isomers (where R = H or Cl and X = O, S, or Se) have been experimentally isolated. In particular, the tricoordinated planar phosphorane and the *cis*- and *trans*-phosphorane conformers (Figure 1) of  $\text{HPO}_2$  have garnered both theoretical<sup>6–9</sup> and experimental<sup>10–14</sup> interest. In 1986, Schoeller and Lerch<sup>7</sup> reported SCF/DZP results showing that metaphosphorus acid ( $\text{HPO}_2$ ) exhibits allylic-type bonding (consistent with having strong dipolar character) as opposed to having multiple bond character at the phosphorus center (Figure 1a,b). Miller and Stevens-Miller<sup>15</sup> derived the gas phase acidity of  $\text{HPO}_2$  as  $1376 \pm 17$  kJ mol<sup>-1</sup> by studying the endothermic reaction  $\text{PO}_2^- + \text{HCl} \rightarrow \text{Cl}^- + \text{HPO}_2$  in a flow-drift tube. The most recent experimental work on metaphosphorus acid was in 1994 when Hildenbrand and Lau<sup>12</sup> reacted  $\text{H}_2\text{O}(\text{g})$  with  $\text{Ca}_2\text{P}_2\text{O}_7(\text{s})$  and identified  $\text{HPO}_2$  by mass spectroscopy.  $\text{HPO}_2$  was then thermochemically characterized from several reaction equilibria, and the standard enthalpy of formation was reported as  $-110.6 \pm 3$  kcal mol<sup>-1</sup>.<sup>12</sup> The radical anion  $\text{HPO}_2^-$  was first identified in 1962 by Morton;<sup>16</sup> there has been little experimental information about this molecular system available since then. Behar and Fessenden<sup>17</sup> produced  $\text{HPO}_2^-$  from radiolysis of an aqueous solution of  $\text{OH} + \text{H}_2\text{PO}_2^-$ , and their electron para-



**Figure 1.** (a)  $C_{2v}$  isomer of  $\text{HPO}_2$  with multiple bonding at the P center versus (b) allylic-type bonding in  $\text{HPO}_2$ ; (c) *cis*- and (d) *trans*-isomers of HOPO.

magnetic resonance (EPR) results were similar to those obtained by the crystal experiments of Morton.

At the CI/TZP level of theory, Mathieu, Navech, and Barthelat<sup>9</sup> reported an energetic ordering of *cis*-HOPO < *trans*-HOPO <  $\text{HPO}_2$ , with the *trans*-isomer and  $\text{HPO}_2$  lying 3.9 and 15.0 kcal mol<sup>-1</sup>, respectively, higher than *cis*-HOPO. It is generally accepted that the *cis*-conformer is the most stable, and it has been studied experimentally more thoroughly than the other isomers. *cis*-HOPO is a final product in the combustion of organophosphorus compounds,<sup>18</sup> it is the main product in the destruction of trimethyl phosphate and dimethyl methyl phosphate,<sup>19</sup> and it is a catalyst for the reaction  $\text{OH} + \text{H}_2 \rightarrow \text{H}_2\text{O} + \text{H}$ .<sup>13</sup> *cis*-HOPO has also been identified as a primary depolymerization product of phosphorus oxides<sup>11</sup> and as a hydrolysis intermediate in the depolymerization of orthorhombic  $\text{P}_4\text{O}_{10}$ .<sup>11</sup> In 1988, Withnall and Andrews<sup>10</sup> measured the IR spectroscopy of the  $\text{O} + \text{PH}_3$  reaction products (including *cis*-HOPO) trapped in solid Ar, and in 2000, Bell and co-workers<sup>20</sup> detected the transient HOPO in the gas phase using high-resolution IR laser absorption spectroscopy.

While information on  $\text{HPO}_2$  and HOPO is rather limited, even less is known about the radical anions of these systems. Thus, we undertook a quantum chemical investigation of  $\text{HPO}_2^-$  and *cis*- and *trans*-HOPO and  $\text{HOPO}^-$ . A brief comment is also made on the pyramidal radical  $\text{H}_2\text{PO}$  in comparison to the pyramidal  $\text{HPO}_2^-$ . Contrasts are also drawn with results from recent work on some nitrogen-based isoelectronic species.

## II. Methods

All quantum chemical computations were performed on  $\text{HPO}_2$ , *cis*- and *trans*-HOPO, and their respective anions using the Gaussian 98<sup>21</sup> and Gaussian 03<sup>22</sup> program packages. The gradient-corrected functional, denoted B3LYP, was used to compute the geometries, energies, harmonic vibrational frequencies, anharmonic vibrational fundamentals, the hyperfine splitting constants at the equilibrium structures and at the vibrationally averaged structures, and the *g*-factors of the vibrationally averaged structures. Energies were converged to at least  $10^{-6}$  hartrees in the self-consistent field procedures, although the absolute accuracy may be somewhat lower due to numerical integration procedures. The anharmonic vibrational fundamentals reported using Gaussian 03 are computed via a perturbational approach. B3LYP is a hybrid Hartree–Fock and density functional theory (HF/DFT) method that uses Becke’s three-parameter exchange functional (B3)<sup>23</sup> with the Lee, Yang, and Parr correlation functional (LYP).<sup>24</sup> The coupled cluster with

single and double excitations and with perturbatively applied triple excitations [CCSD(T)]<sup>25–27</sup> theory was used to compute the hyperfine splitting constants of the P atom. An unrestricted Hartree–Fock reference was used for all correlated procedures. To compute the *g*-factor in solution, the conductor-like polarizable continuum model (CPCM)<sup>28,29</sup> was used.

A 6-31+G\* basis set was used in the preliminary geometry optimizations. This basis set was formed from the 6-31 basis set of Hehre et al.<sup>30</sup> and Francl et al.<sup>31</sup> combined with the polarization and diffuse functions of Frisch et al.<sup>32</sup> and Clark et al.<sup>33</sup> These basis sets have contraction schemes of H(4s/2s), O(11s5p1d/4s3p1d), and P(16s10p1d/4s3p1d). The larger 6-311+G(2d,2p) basis set was subsequently used to compute the anharmonic fundamental vibrational frequencies of *cis*-HOPO for which experimental fundamental frequencies are known. This basis set is obtained for H and O from the 6-311 basis of Hehre et al.<sup>34</sup> by adding diffuse functions and two sets of d functions on oxygen atoms and two sets of p functions on hydrogen. The 6-311+G(2d,2p) basis set for P is based on the McLean–Chandler<sup>35</sup> basis set with diffuse functions and two sets of d functions on phosphorus. The EPR-II basis set of Barone<sup>36</sup> was used for H and O for computing the Fermi contact terms of the radicals. This basis set is a double- $\zeta$  basis set with a single set of polarization functions and an enhanced s part. The contraction schemes for this basis set are H(6s1p/4s1p) and O(10s5p1d/6s2p1d).

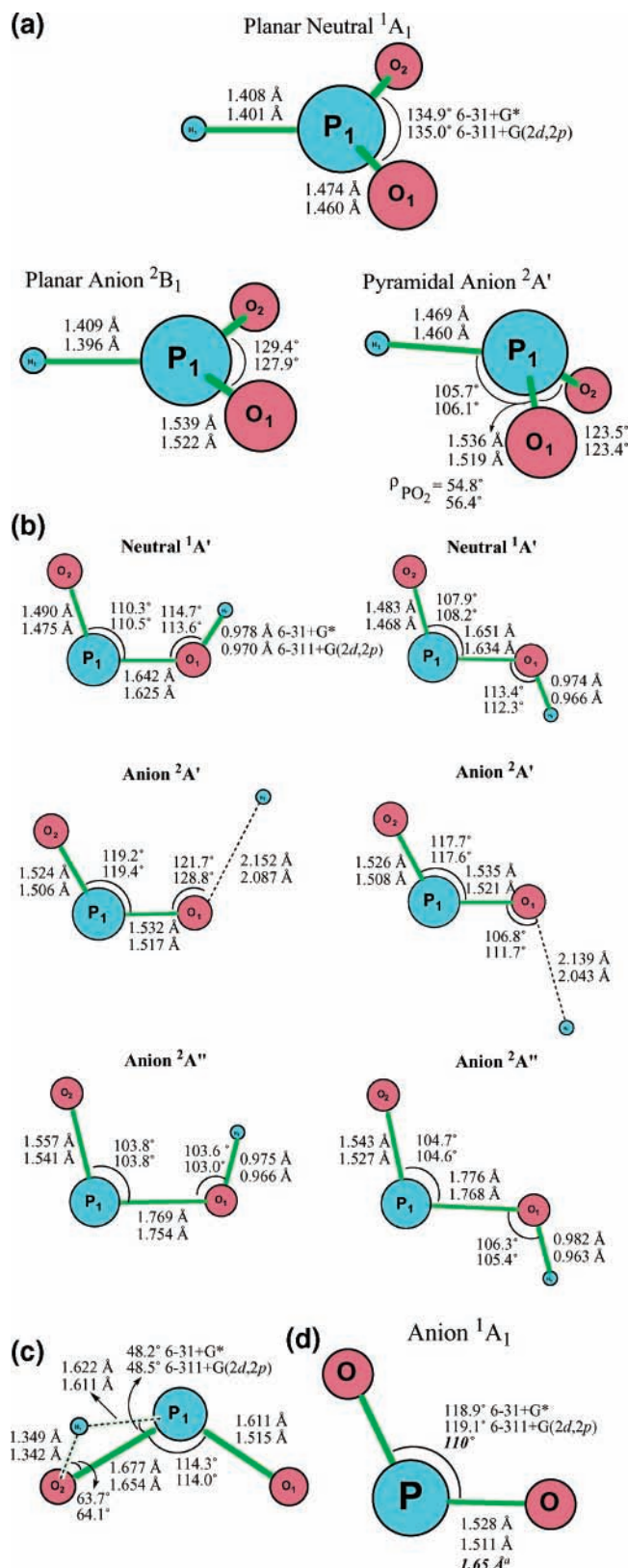
The correlation-consistent polarized core–valence family of basis sets of Woon and Dunning<sup>37</sup> augmented with diffuse functions following Kendall et al.<sup>38</sup> (aug-cc-pCVXZ) and the newer family of correlation-consistent basis sets of Dunning, Peterson, and Wilson<sup>39</sup> which include tight d functions and a systematic expansion of the higher angular moment functions [aug-cc-pV(X+d)Z] were used to systematically investigate the Fermi contact terms of the  $\text{HPO}_2^-$  and  $\text{H}_2\text{PO}$  radicals and the P atom. For  $\text{HPO}_2^-$ , The aug-cc-pCVXZ basis sets range in size from 99 contracted Gaussian basis functions (aug-cc-pCVDZ) to 398 (aug-cc-pCVQZ). For  $\text{HPO}_2$ , this range is 88–335. The valence “plus d” sets range from 87 [aug-cc-pV(D+d)Z] to 470 functions [aug-cc-pV(Z+d)Z] for  $\text{HPO}_2^-$  and from 73 to 423, respectively, for  $\text{HPO}_2$ .

Geometries were optimized for each molecular system with the B3LYP functional using analytic gradient techniques. Residual Cartesian gradients were  $<1.5 \times 10^{-5}$  hartrees/b. Stationary points found in optimizations were confirmed as minima by computing the harmonic vibrational frequencies using analytic second derivatives.

## III. Results and Discussion

**A. Structures and Relative Energies.** The B3LYP optimized structures of the neutral and anionic tricoordinated phosphorane  $\text{HPO}_2$  are given in Figure 2a. The neutral species is a planar  ${}^1A_1$   $C_{2v}$  structure. The planar  ${}^2B_1$  anion is a transition state with one imaginary frequency leading to the pyramidal  ${}^2A'$  state in  $C_s$  symmetry which is the minimum on the potential energy surface of the anion. The harmonic vibrational frequencies and the theoretical anharmonic fundamental vibrational frequencies of  $\text{HPO}_2$  and both the planar and pyramidal anions are given in Table 1. The P–H and P–O bond distances are  $\sim 0.06$  Å longer in the anion (1.460 Å; 1.519 Å) than in the neutral species (1.401 Å; 1.460 Å). With the 6-311+G(2d,2p) basis set, the O atoms are bent  $56.4^\circ$  out of the plane of the  $C_{2v}$  structure.

The B3LYP optimized structures of *cis*- and *trans*-HOPO and the corresponding radical anions are shown in Figure 2b. These systems are all planar. The lowest unoccupied molecular orbital



**Figure 2.** B3LYP/6-31+G\* optimized structures of (a)  $\text{HPO}_2$  and  $\text{HPO}_2^-$ , (b) the *cis*- and *trans*-isomers of  $\text{HOPO}$  and  $\text{HOPO}^-$ , (c) the transition state between  $\text{HPO}_2^-$  and *cis*- $\text{HOPO}^-$ , and (d)  $\text{PO}_2^-$ .

of  $\text{HOPO}$  is  $A''$ , and the next lowest is  $A'$ . Correspondingly, for both isomers of  $\text{HOPO}^-$ , a  $\pi$  radical ( ${}^2A''$ ) and a higher lying  $\sigma$  radical ( ${}^2A'$ ) are found. A transition state for the hydrogen shift between  $\text{HPO}_2^-$  and *cis*- $\text{HOPO}^-$  was located and is shown in Figure 2c. The  $\pi$  radicals show a slightly long central O–P bond (1.754 Å, *cis*; 1.768 Å, *trans*). This is similar

**TABLE 1: Harmonic Vibrational Frequencies ( $\text{cm}^{-1}$ ) and Anharmonic Fundamental Vibrational Frequencies ( $\text{cm}^{-1}$ ) for  $\text{HPO}_2$  and  $\text{HPO}_2^-$ <sup>a</sup>**

		$\text{HPO}_2$ ( ${}^1A_1$ )	$\text{HPO}_2^-$ ( ${}^2B_1$ )	$\text{HPO}_2^-$ ( ${}^2A'$ )
$\omega_1$	6-31+G*	$A_1$	$A_1$	$A'$
$\nu_1$		2504	2458	1987
$\nu_1$		2384	2246	1853
$\omega_1$	6-311+G(2d,dp)	2461	2476	1950
$\nu_1$		2351	2249	1813
$\omega_2$	6-31+G*	1124	936	1150
$\nu_2$		1110	926	1130
$\omega_2$	6-311+G(2d,dp)	1136	958	1169
$\nu_2$		1123	945	1149
$\omega_3$	6-31+G*	453	389	976
$\nu_3$		449	382	961
$\omega_3$	6-311+G(2d,dp)	456	402	991
$\nu_3$		453	394	977
		$B_1$	$B_1$	
$\omega_4$	6-31+G*	603	[1526]	761
$\nu_4$		608	[1804]	740
$\omega_4$	6-311+G(2d,dp)	612	[1579]	760
$\nu_4$		615	[1899]	739
		$B_2$	$B_2$	
$\omega_5$	6-31+G*	1436	1181	410
$\nu_5$		1415	1164	407
$\omega_5$	6-311+G(2d,dp)	1448	1192	418
$\nu_5$		1428	1176	415
				$A''$
$\omega_6$	6-31+G*	1013	943	918
$\nu_6$		1003	917	888
$\omega_6$	6-311+G(2d,dp)	986	937	904
$\nu_6$		978	905	872

<sup>a</sup> Imaginary frequencies are in brackets.

to the findings of van Doren et al.<sup>40</sup> for the radical anions from *cis*- and *trans*-nitrous acid, where elongated central O–N bonds foreshadow dissociation into  $\text{OH}^-$  and  $\text{NO}$ . The association energy of  $\text{OH}^- + \text{PO}$  is 25.92 kcal mol<sup>-1</sup> (*cis*) and 22.39 kcal mol<sup>-1</sup> (*trans*). A counterpoise correction changes these by 3.07 and 3.03 kcal mol<sup>-1</sup>, respectively. In contrast, the  $\sigma$  radicals of both isomers show an elongated O–H bond (2.087 Å, *cis*; 2.043 Å, *trans*), indicating dissociation of free H, leaving the  $\text{PO}_2^-$  anion. The association energy of  $\text{H} + \text{PO}_2^-$  is 1.65 kcal mol<sup>-1</sup>, and a counterpoise correction makes a difference of 0.60 kcal mol<sup>-1</sup>. The B3LYP optimized structure of  $\text{PO}_2^-$  is given in Figure 2d for comparison.

The harmonic vibrational frequencies and computed anharmonic fundamental vibrational frequencies of  $\text{HOPO}$  and  $\text{HOPO}^-$  are given in Table 2; the computed harmonic frequencies and anharmonic fundamental vibrational frequencies for  $\text{PO}_2^-$  are included for comparison. Available experimental fundamental frequencies for *cis*- $\text{HOPO}$  and  $\text{PO}_2^-$  are also given. With the 6-311+G(2d,2p) basis set, there is close agreement between the theoretical anharmonic frequencies and the experimental fundamentals. The comparison of  $\nu_1$  (1156 cm<sup>-1</sup>, *trans*; 1165 cm<sup>-1</sup>, *cis*; 1170 cm<sup>-1</sup>,  $\text{PO}_2^-$ ),  $\nu_2$  (1021 cm<sup>-1</sup>, *trans*; 1023 cm<sup>-1</sup>, *cis*; 1030 cm<sup>-1</sup>,  $\text{PO}_2^-$ ), and  $\nu_3$  (420 cm<sup>-1</sup>, *trans*; 442 cm<sup>-1</sup>, *cis*; 446 cm<sup>-1</sup>,  $\text{PO}_2^-$ ) confirms the dissociation of H from  $\text{PO}_2^-$  in the  $\sigma$  radicals of the *trans*- and *cis*- $\text{HOPO}^-$  isomers. The frequencies of the  $\pi$  radicals are consistent with the notion that the unpaired electron in the  ${}^2A''$  anions is in an orbital perpendicular to the plane of the molecule. Interestingly, the  $A''$  mode of  ${}^2A''$  *trans*- $\text{HOPO}^-$  is imaginary when computed with the 6-31+G\* basis set. When computed with the larger 6-311+G(2d,2p) basis set, the harmonic vibrational frequency is predicted to be imaginary as well; however, the computed

**TABLE 2: Harmonic Vibrational Frequencies (cm<sup>-1</sup>) and Anharmonic Fundamental Vibrational Frequencies (cm<sup>-1</sup>) for *trans*-HOPO, *cis*-HOPO, the Corresponding Anions, and PO<sub>2</sub><sup>-a</sup>**

	HOPO ( <sup>1</sup> A')		<i>trans</i> - HOPO <sup>-</sup>		<i>cis</i> - HOPO <sup>-</sup>		PO <sub>2</sub> <sup>-</sup>
	trans	cis	( <sup>2</sup> A')	( <sup>2</sup> A'')	( <sup>2</sup> A')	( <sup>2</sup> A'')	( <sup>1</sup> A <sub>1</sub> )
$\omega_1$	3718	3663	1157	3718	1168	3692	1172
$\nu_1$	3529	2472	1144	3515	1151	3499	1155
$\omega_1$	3796	3742	1170	3809	1181	3775	1187
$\nu_1$	3608	3549	1156	3613	1165	3595	1170
		3551 <sup>b</sup>					1207 <sup>c</sup>
$\omega_2$	1265	1242	1023	1066	1026	1042	1031
$\nu_2$	1251	1227	1012	1045	1013	1023	1018
$\omega_2$	1279	1241	1031	1078	1034	1057	1043
$\nu_2$	1265	1241	1021	1055	1023	1042	1030
		1253 <sup>b</sup>					1097 <sup>c</sup>
$\omega_3$	925	942	466	939	448	950	445
$\nu_3$	851	900	423	850	436	930	442
$\omega_3$	964	919	489	962	452	969	449
$\nu_3$	937	919	420	848	442	963	446
							501 <sup>c</sup>
$\omega_4$	799	818	345	580	374	607	
$\nu_4$	785	803	271	565	272	592	
$\omega_4$	804	820	374	570	408	594	
$\nu_4$	788	804	310	552	366	578	
		842 <sup>b</sup>					
$\omega_5$	396	377	158	333	141	325	
$\nu_5$	395	374	101	329	120	305	
$\omega_5$	407	389	168	342	121	333	
$\nu_5$	404	386	105	332	143	307	
	A''	A''	A''	A''	A''	A''	
$\omega_6$	485	565	77	[78]	[33]	243	
$\nu_6$	485	565	12	[157]	[252]	177	
$\omega_6$	481	561	83	[95]	50	222	
$\nu_6$	450	541	164	465	189	417	
		524 <sup>b</sup>					

<sup>a</sup> Imaginary frequencies are in brackets. Available experimental fundamental frequencies are included. <sup>b</sup> Reference 20. <sup>c</sup> References 10 and 62.

fundamental vibrational frequency is real and similar in magnitude to that computed for *cis*-HOPO<sup>-</sup>.

The total electronic energies of the neutral molecules and the anions at the B3LYP/6-31+G\* and B3LYP/6-311+G(2d,2p) levels are given in Table 3. Relative energies are listed in kcal mol<sup>-1</sup>. In the neutral systems, *cis*-HOPO is the most stable conformation, with the *trans*-isomer lying 3.0 kcal mol<sup>-1</sup> higher and HPO<sub>2</sub> lying 11.9 kcal mol<sup>-1</sup> above that. The pyramidal, tricoordinated HPO<sub>2</sub><sup>-</sup> is the most stable anion, with <sup>2</sup>A'' *cis*-HOPO<sup>-</sup> ~5 kcal mol<sup>-1</sup> higher and <sup>2</sup>A' *trans*-HOPO<sup>-</sup> another 3 kcal mol<sup>-1</sup> higher. PO<sub>2</sub><sup>-</sup> + H (<sup>2</sup>A' *cis*- and *trans*-HOPO<sup>-</sup>) lies ~33 kcal mol<sup>-1</sup> above HPO<sub>2</sub><sup>-</sup>. The adiabatic electron affinity (AEA) was determined as the difference in the total electronic energy of the optimized neutral system minus that of the optimized anion. The  $\pi$  radical anions of *cis*- and *trans*-HOPO are bound [AEA(*cis*) = 0.46 eV and AEA(*trans*) = 0.46 eV]. The AEA of HPO<sub>2</sub> is 1.33 eV. With zero-point correction, these values are 0.51 eV (*cis*), 0.52 eV (*trans*), and 1.38 eV (HPO<sub>2</sub>). The vertical electron affinity (VEA) was determined as the difference in the total electronic energy of the optimized neutral system minus that of the anion at the geometry of the optimized neutral system, and this value for *cis*- and *trans*-HOPO is 0.16 and 0.20 eV, respectively. The VEA of HPO<sub>2</sub> is 0.30 eV.

**B. Hyperfine Splitting Constants.** From his EPR investigation,<sup>16</sup> Morton reported that the HPO<sub>2</sub><sup>-</sup> radical is pyramidal, with the unpaired electron localized on the phosphorus atom in a hybrid  $\sigma$  orbital. The computed isotropic hyperfine splitting (hfs) constants for the planar <sup>2</sup>B<sub>1</sub> and pyramidal <sup>2</sup>A' HPO<sub>2</sub><sup>-</sup> are given in Tables 4 and 5, respectively. The 6-31+G\* and 6-311+G(2d,2p) values of  $A_{\text{iso}}(^1\text{H}) = 230.53$  and 229.07 MHz for <sup>2</sup>A' HPO<sub>2</sub><sup>-</sup> are in close agreement with Morton's average experimental value of 230 MHz, but this agreement may be fortuitous, since the EPR-II/6-311+G(2d,2p) value of 257 MHz deviates from experiment by almost 30 MHz. In solution, the Fermi contact term for <sup>1</sup>H is 270.98 MHz (6-31+G\*), 247.91 MHz [6-311+G(2d,2p)], and 243.51 MHz [EPR-II/6-311+G(2d,2p)], all of which are in close accord with the experimental solution phase value of 252 MHz.<sup>17</sup> However, the computed hfs constant for <sup>31</sup>P (880.29 MHz) compares poorly with the experimental value of 1385 MHz. The larger basis sets improve the computed value to 1063.76 MHz [6-311+G(2d,2p)] and 1065.32 MHz [EPR-II/6-311+G(2d,2p)], but these values are still ~300 MHz different from experiment. In solution, the computed values of  $A_{\text{iso}}(^{31}\text{P})$  all move toward experiment [1108.73 MHz, 6-31+G\*; 953.60 MHz, 6-311+G(2d,2p); 1123.42 MHz, EPR-II/6-311+G(2d,2p)]. The remaining deviation is most likely a consequence of the deficiencies in the available basis sets for adequately describing the 1s core of the phosphorus atom.

Deficiencies in structural predictions were observed by Wesolowski et al.<sup>41</sup> in a high-level theoretical investigation of H<sub>3</sub>PO and H<sub>2</sub>POH. It was noted that the conventional Dunning correlation-consistent polarized valence (cc-pVXZ)<sup>42-45</sup> basis sets fail to provide correct results for these P-containing systems even when used with a high level of theory such as coupled-cluster singles and doubles with perturbatively applied triple excitations. Results were improved with the inclusion of tight d functions by using Dunning's core-valence (cc-pCVXZ)<sup>37</sup> or the plus d [cc-pV(X+d)Z]<sup>39</sup> basis sets. In subsequent work, Tackett and Clouthier<sup>46</sup> reported difficulties in obtaining reliable excitation energies for HPO with all but very large basis sets and high levels of theoretical methods. With this in mind, the aug-cc-pCVXZ and aug-cc-pV(X+d) basis sets were used to compute the Fermi contact terms of HPO<sub>2</sub><sup>-</sup> using the optimized geometry obtained at the B3LYP/6-311+G(2d,2p) level. These values are also given in Table 5. Graphs of these data are shown in Figures 3 and 4.

The trends in the values of  $A_{\text{iso}}(^{17}\text{O})$  computed with the two families of basis sets are given in Figures 3a and 4a, and with the aug-cc-pCVXZ basis sets, it appears that this value is converging to about -20 MHz. With the aug-cc-pV(X+d)Z basis sets, the aug-cc-pV(D+d)Z through aug-cc-pV(Q+d)Z values also appear to be converging to about -12 MHz, although from the opposite direction as that with the aug-cc-pCVXZ basis sets. However, the (5+d)Z value drops back down to -16.54 MHz, and it is suspected that if the aug-cc-pCV5Z basis set were available, this value would drop to -18 or -19 MHz, leaving convergence still somewhat nebulous. Figures 3b and 4b show even more troubling trends for  $A_{\text{iso}}(^{31}\text{P})$  computed with these basis sets. With the aug-cc-pCVXZ basis set, there is a large jump between the aug-cc-pCVTZ value (987.46 MHz) and the aug-cc-pCVQZ value (1011.42 MHz). The aug-cc-pV(X+d)Z values do not show a convergence trend. However, the values do appear to be "sandwiched" between the aug-cc-pV(D+d)Z value of 922.89 MHz and the aug-cc-pV(5+d)Z value of 968.52 MHz. Graphs of  $A_{\text{iso}}(^1\text{H})$  computed with both

**TABLE 3: B3LYP Total Electronic Energies ( $E_h$  Values) for  $\text{HPO}_2$ , *trans*-HOPO, *cis*-HOPO, and the Corresponding Anions<sup>a</sup>**

		neutral	anion	
		$\text{HPO}_2$		
AEA = 1.43 eV (1.04 eV)	6-31+G*	-492.412 187 [16.0]	-492.464 620 [0.0]	
1.33 eV (1.38 eV)	6-311+G(2d,2p)	-492.504 705 [14.9]	-492.553 454 [0.0]	
VEA = 0.13 eV 0.30 eV	6-31+G* 6-311+G(2d,2p)			
		<i>trans</i> -HOPO		
AEA = 0.57 eV (0.63 eV)	6-31+G*	-492.431 926 [3.6]	<sup>2</sup> A' -492.412 430 [32.8]	<sup>2</sup> A'' -492.452 946 [7.3]
0.46 eV (0.52 eV)	6-311+G(2d,2p)	-492.523 586 [3.0]	-492.500 985 [32.9]	-492.540 636 [8.04]
VEA = 0.31 eV 0.20 eV	6-31+G* 6-311+G(2d,2p)			
		<i>cis</i> -HOPO		
AEA = 0.58 eV (0.62 eV)	6-31+G*	-492.437 633 [0.0]	<sup>2</sup> A' -492.412 562 [32.7]	<sup>2</sup> A'' -492.458 764 [3.7]
0.46 eV (0.51 eV)	6-311+G(2d,2p)	-492.528 402 [0.0]	-492.501 448 [32.6]	-492.545 333 [5.1]
VEA = 0.27 eV 0.16 eV	6-31+G* 6-311+G(2d,2p)			

<sup>a</sup> Relative energies (kcal mol<sup>-1</sup>) are listed in brackets. Adiabatic and vertical electron affinities (AEAs and VEAs, respectively) are given in eV. Zero-point corrected values are in parentheses. The EAs for the *trans*- and *cis*-isomers are to the lower energy <sup>2</sup>A'' state.

**TABLE 4: Isotropic Fermi Contact Couplings (MHz) for the <sup>2</sup>B<sub>1</sub> State of  $\text{HPO}_2^-$  Using B3LYP<sup>a</sup>**

<sup>2</sup> B <sub>1</sub> $\text{HPO}_2^-$	<sup>17</sup> O <sub>1</sub>	<sup>17</sup> O <sub>2</sub>	<sup>31</sup> P	<sup>1</sup> H
6-31+G*	-27.21	-27.21	163.93	-27.21
0 K	-29.66	-29.66	260.62	-63.03
298 K	-29.71	-29.71	261.81	-51.13
6-311+G(2d,2p)	-19.95	-19.95	205.75	-68.03
0 K	-22.71	-22.71	235.98	-53.17
298 K	-22.78	-22.78	236.98	52.84
EPR-II [H,O], 6-311+G(2d,2p) [P]	-25.95	-25.95	214.64	-73.52
0 K	-29.63	-29.63	291.25	-54.97
298 K	-29.71	-29.71	292.87	-54.97

<sup>a</sup> Vibrationally averaged values were computed at 0 and 298 K and are in italics.

families of basis sets [Figure 3c, aug-cc-pCVXZ; Figure 4c, aug-cc-pV(X+d)Z] show that these values are not converging.

While there are observed problems with the convergence of the Fermi contact terms for each nuclear center in  $\text{HPO}_2^-$ , these are most likely all consequences of the basis sets available for P. The B3LYP and CCSD(T) computed hfs constants for the <sup>4</sup>S P atom are given in Table 6, and graphs of the values with the aug-cc-pCVXZ and aug-cc-pV(X+d)Z basis sets are respectively shown in parts a and b of Figures 5 (B3LYP) and 6 [CCSD(T)]. The graphs of the B3LYP data show that the values of  $A_{\text{iso}}(^{31}\text{P})$  do not appear to converge smoothly, although the magnitude of the aug-cc-pCVQZ value of -51.13 MHz [which is similar to the 6-311+G(2d,2p) value of -51.79 MHz] is in reasonable agreement (in magnitude) with the experimental value of 55.1 MHz.<sup>47</sup> The aug-cc-pV(6+d)Z value is -68.79 MHz, which is ~14 MHz greater than experiment.

In a study of the theoretical spin densities and hyperfine coupling in the atoms B-F,<sup>48</sup> it was reported that the B3LYP functional used with the aug-cc-pCVXZ basis sets produces limiting values for the N atom that are fortuitously close to experiment. While similar results might be expected for the isoelectronic P atom, the magnitude of the computed  $A_{\text{iso}}(^{31}\text{P})$  value is close to experiment, but the sign is opposite. The CCSD(T) data, however, converge to values of 52.00 MHz (aug-cc-

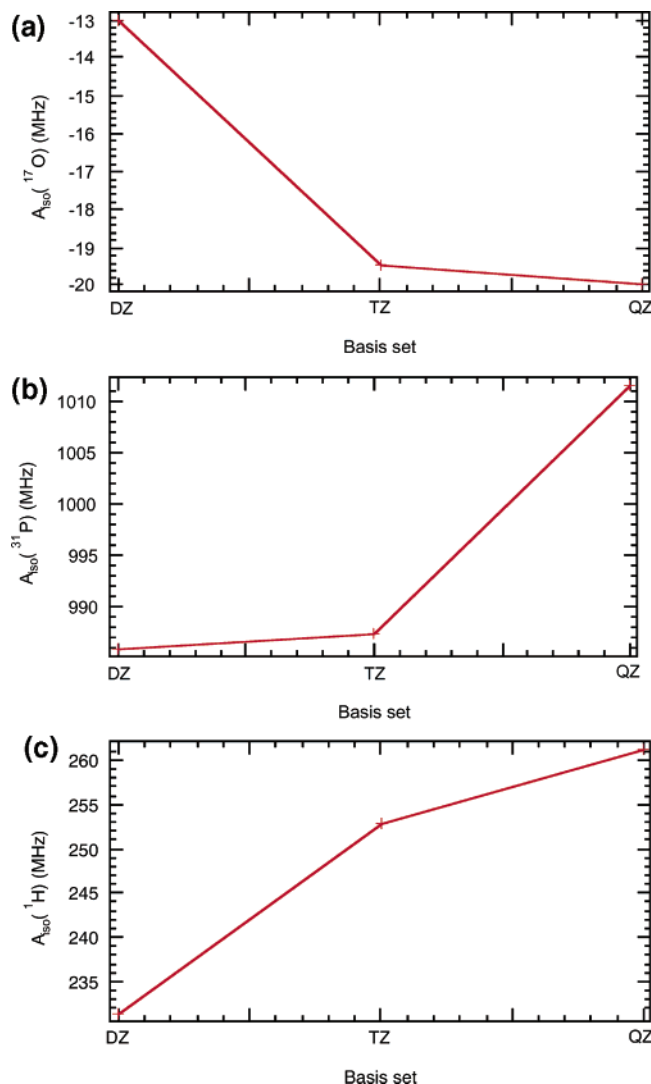
**TABLE 5: Isotropic Fermi Contact Couplings (MHz) for the <sup>2</sup>A' State of  $\text{HPO}_2^-$  Using B3LYP<sup>a</sup>**

<sup>2</sup> A' $\text{HPO}_2^-$	<sup>17</sup> O	<sup>31</sup> P	<sup>1</sup> H
6-31+G*	-29.39	880.29	230.53
0 K	-29.48	880.30	250.92
298 K	-29.29	878.52	237.67
CPCM	-31.66	953.60	247.91
6-311+G(2d,2p)	-23.54	1063.76	229.07
0 K	-23.47	1061.29	235.98
298 K	-23.47	1061.23	236.14
CPCM	-26.34	1123.42	243.51
EPR-II [H,O], 6-311+G(2d,2p) [P]	-28.11	1065.32	257.44
0 K	-28.04	1063.40	265.28
298 K	-28.04	1063.35	265.46
CPCM	-30.44	1108.73	270.98
aug-cc-pV(D+d)Z	-30.28	922.89	233.07
aug-cc-pV(T+d)Z	-12.72	964.74	252.60
aug-cc-pV(Q+d)Z	-12.29	933.67	261.32
aug-cc-pV(5+d)Z	-16.54	968.52	271.21
aug-cc-pCVDZ	-13.04	985.91	231.31
aug-cc-pCVTZ	-19.48	987.46	252.77
aug-cc-pCVQZ	-19.96	1011.42	261.14
aug-cc-pCVDZ+1s	-13.05	964.28	231.22
aug-cc-pCVTZ+1s	-19.48	1003.83	252.77
aug-cc-pCVQZ+1s	-19.96	1003.80	261.14
TZVP	-25.95	1027.41	235.01
expt		1385 <sup>b</sup>	230 <sup>b</sup>
		1346 <sup>c</sup>	252 <sup>c</sup>

<sup>a</sup> Vibrationally averaged values were computed at 0 and 298 K and are in italics. Solution phase values were estimated using CPCM. Available experimental values are given. <sup>b</sup> Reference 16. <sup>c</sup> Reference 17.

pCVQZ) and 57.06 MHz [aug-cc-pV(5+d)], which are in good agreement with both the magnitude and sign of the experimental value.

Further attempts to increase the basis set flexibility in the core region by including energy optimized, high-exponent s functions with the aug-cc-pCVXZ basis sets led to little change in the predicted coupling constants computed for the P atom. However, when these modified basis sets were used for  $\text{HPO}_2^-$ ,  $A_{\text{iso}}(^{31}\text{P})$  shows a nice convergence trend: 964.28 MHz (aug-

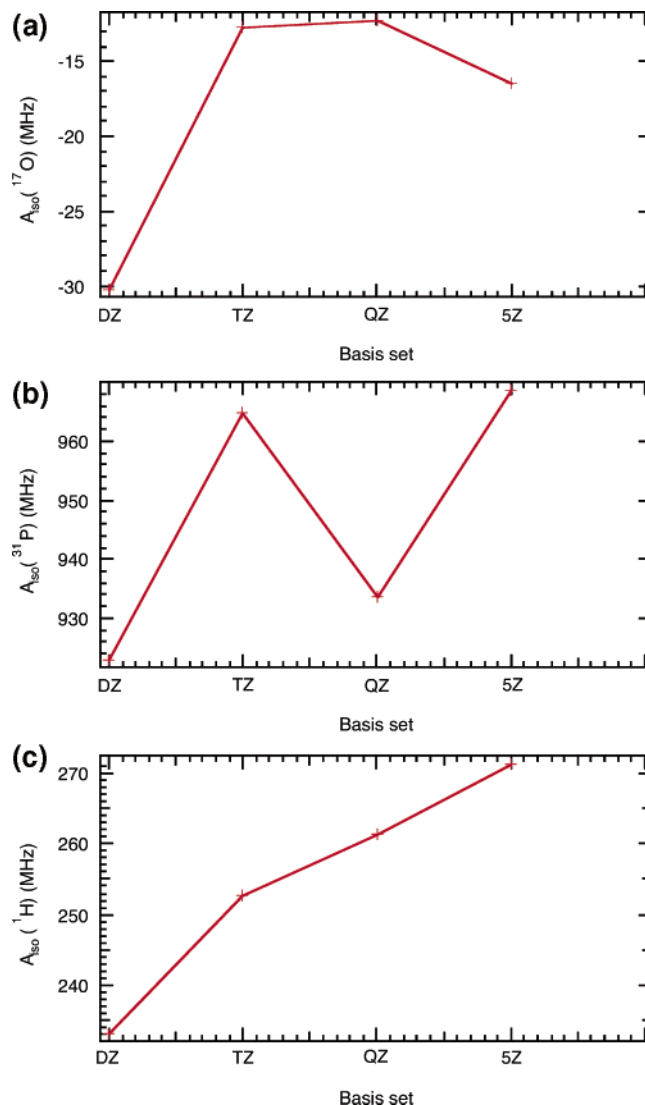


**Figure 3.** Isotropic hyperfine splitting constants of (a)  $^{17}\text{O}$ , (b)  $^{31}\text{P}$ , and (c)  $^1\text{H}$  with the aug-cc-pCVXZ family of basis sets.

cc-pCVDZ+1s), 1003.83 MHz (aug-cc-pCVTZ+1s), and 1003.80 MHz (aug-cc-pCVQZ+1s). While this value is still 350–400 MHz different from experiment, the convergence of this value is good.

In a study of P-containing radicals, Nguyen et al.<sup>49</sup> reported that the TZVP basis set of Godbout and co-workers<sup>50</sup> used with the B3LYP functional produces computed hfs constants that are in better agreement with experiment than the other basis sets included in their study. Thus, the Fermi contact terms for  $\text{HPO}_2^-$  were computed here at the B3LYP/TZVP level of theory, and these values are included in Table 5. The value of  $A_{\text{iso}}(^{31}\text{P}) = 1027.41$  MHz is found to be in worse agreement with experiment than that computed with the 6-311+G(2d,2p) or EPR-II/6-311+G(2d,2p) basis sets, while  $A_{\text{iso}}(^1\text{H}) = 235.01$  MHz is comparable to the 6-311+G(2d,2p) value and to experiment.

**C. Vibrational Averaging and Solution Effects.** It should also be noted that the static Fermi contact terms for  $^1\text{H}$  vary from  $-27.21$ ,  $-68.03$ , and  $-73.52$  MHz [6-31+G\*, 6-311+G(2d,2p), EPR-II/6-311+G(2d,2p), respectively] in the planar structure to 230.53, 229.07, and 257.44 MHz [6-31+G\*, 6-311+G(2d,2p), EPR-II/6-311+G(2d,2p), respectively] in the pyramidal minimum. It is known that EPR parameters are strongly influenced by inversion motion at the radical center. Barone and co-workers<sup>51–54</sup> developed a numerical procedure



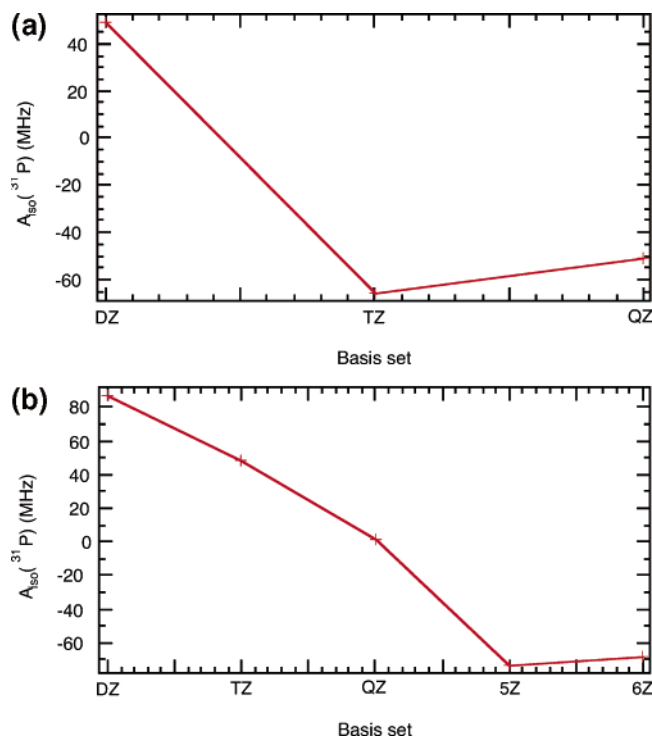
**Figure 4.** Isotropic hyperfine splitting constants of (a)  $^{17}\text{O}$ , (b)  $^{31}\text{P}$ , and (c)  $^1\text{H}$  with the aug-cc-pV(X+d)Z family of basis sets.

**TABLE 6: Isotropic Fermi Contact Couplings (MHz) for  $^4\text{S}$  P Using B3LYP**

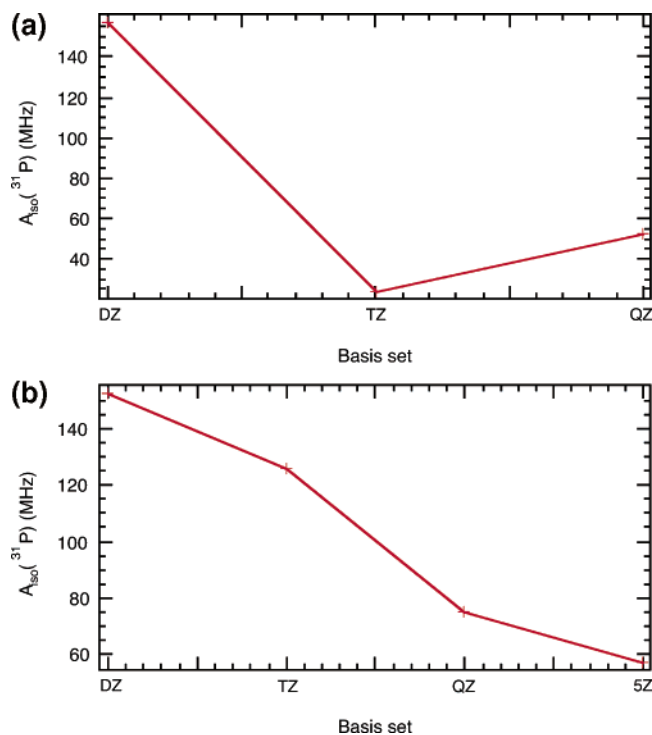
	B3LYP	CCSD(T)
6-31+G*	-12.61	
6-311+G(2d,2p)	-51.79	
aug-cc-pV(D+d)Z	86.71	152.28
aug-cc-pV(T+d)Z	47.86	125.42
aug-cc-pV(Q+d)Z	1.51	74.86
aug-cc-pV(5+d)Z	-73.36	57.06
aug-cc-pV(6+d)Z	-68.79	
aug-cc-pCVDZ	48.81	156.73
aug-cc-pCVTZ	-65.99	23.67
aug-cc-pCVQZ	-51.13	52.00
expt	55.1 <sup>a</sup>	

<sup>a</sup> Reference 47.

to treat large-amplitude nuclear motions in nonrigid radicals. This method was applied to  $\text{HPO}_2^-$  in the present work. The primary effect of pyramidalization is an increase in the s character of the singly occupied molecular orbital (SOMO) at the radical center which is reflected by an increase in the hfs constants at  $^{31}\text{P}$  and  $^1\text{H}$ . These effects computed with the 6-31+G\* basis set are shown in Figure 7. The barrier to inversion in  $\text{HPO}_2^-$  is  $\sim 24$  kcal mol<sup>-1</sup> (Figure 8a), and thus, the vibrational averaging effects are less pronounced, since high barriers imply widely spaced vibrational states and smaller



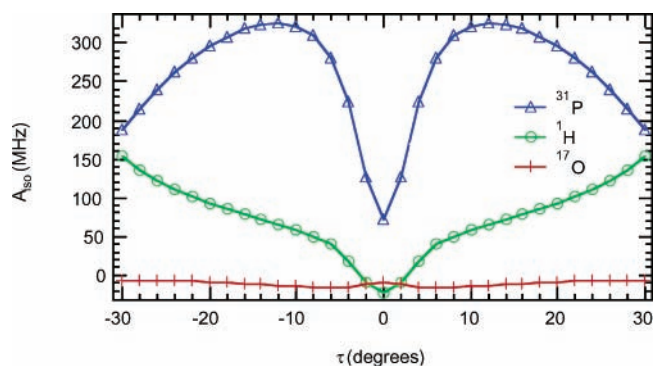
**Figure 5.** B3LYP isotropic hyperfine splitting constants of the  $^{31}\text{P}$  atom with the (a) aug-cc-pCVXZ and (b) aug-cc-pV(X+d)Z families of basis sets.



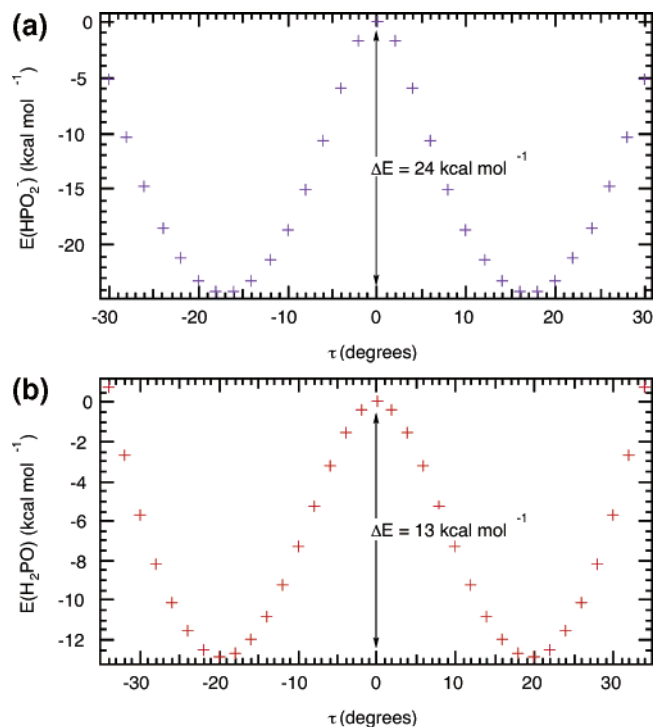
**Figure 6.** CCSD(T) isotropic hyperfine splitting constants of the  $^{31}\text{P}$  atom with the (a) aug-cc-pCVXZ and (b) aug-cc-pV(X+d)Z families of basis sets.

average displacements from the equilibrium structure. In such a case, there is better agreement between the experimental Fermi contact terms and the static computed values. By way of contrast, in  $\text{HNO}_2^-$ , a low inversion barrier leads to large-amplitude motion and consequently large vibrational effects on the computed coupling constants.<sup>55</sup>

In  $\text{HPO}_2^-$ , the inclusion of vibrational averaging at 0 K causes little change observed for  $A_{\text{iso}}(^{17}\text{O})$  [−29.39 to −29.48 MHz



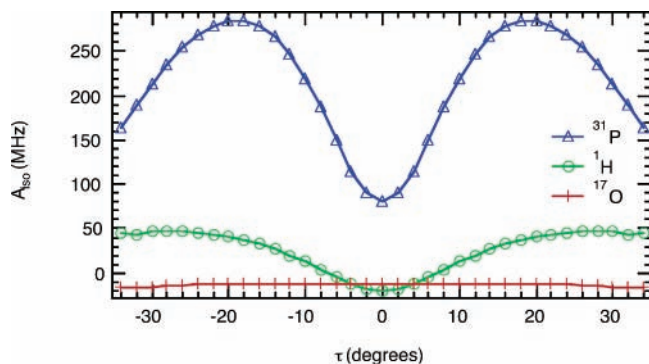
**Figure 7.** Isotropic hyperfine splitting constants of  $^{31}\text{P}$ ,  $^1\text{H}$ , and  $^{17}\text{O}$  of  $\text{HPO}_2$  as a function of the degree of pyramidalization ( $\tau$ ).



**Figure 8.** (a) Relative energy ( $\text{kcal mol}^{-1}$ ) of  $\text{HPO}_2^-$  as a function of the degree of pyramidalization ( $\tau$ ); (b) relative energy ( $\text{kcal mol}^{-1}$ ) of  $\text{H}_2\text{PO}$  as a function of the degree of pyramidalization ( $\tau$ ).

with 6-31+G\*; −23.54 to −23.47 MHz with 6-311+G(2d,2p); −28.11 to −28.04 MHz with EPR-II/6-311+G(2d,2p)] and  $A_{\text{iso}}(^{31}\text{P})$  [880.29 to 880.30 MHz with 6-31+G\*; 1063.76 to 1061.29 MHz with 6-311+G(2d,2p); 1065.32 to 1063.40 MHz with EPR-II/6-311+G(2d,2p)]. However, vibrational averaging has a more significant effect on the Fermi contact term for  $^1\text{H}$  [230.53 to 250.92 MHz with 6-31+G\*; 229.07 to 235.98 MHz with 6-311+G(2d,2p); 257.44 to 265.46 MHz with EPR-II/6-311+G(2d,2p)]. Increasing the size of the basis set also has the most significant effect on  $A_{\text{iso}}(^{31}\text{P})$ , which increases from  $\sim 880$  MHz with the 6-31+G\* basis set to 1065.32 MHz with EPR-II/6-311+G\*(2d,2p). Temperature affects are negligible for  $\text{HPO}_2^-$ . At 298 K, the hfs constants computed with the EPR-II/6-311+G(2d,2p) basis set are  $A_{\text{iso}}(^{17}\text{O}) = -28.04$  MHz,  $A_{\text{iso}}(^{31}\text{P}) = 1063.35$  MHz, and  $A_{\text{iso}}(^1\text{H}) = 265.46$  MHz.

By comparison, vibrational averaging is important for accurately producing theoretical hfs constants for H in the nonrigid  $\text{H}_2\text{PO}$  radical. The Fermi contact terms of the dihydrophosphoryl radical ( $\text{H}_2\text{PO}$ ) have been the subject<sup>56–60</sup> of considerable debate and interest for at least a decade. Most recently, Wesolowski et



**Figure 9.** Isotropic hyperfine splitting constants of <sup>31</sup>P, <sup>1</sup>H, and <sup>17</sup>O of H<sub>2</sub>PO as a function of the degree of pyramidalization ( $\tau$ ).

**TABLE 7: Isotropic Fermi Contact Couplings (MHz) for the <sup>2</sup>A' State of H<sub>2</sub>PO Using B3LYP<sup>a</sup>**

<sup>2</sup> A' H <sub>2</sub> PO	<sup>17</sup> O	<sup>31</sup> P	<sup>1</sup> H
6-31+G*	-34.27	797.69	112.27
0 K	<i>-34.34</i>	<i>792.95</i>	<i>113.95</i>
298 K	<i>-34.34</i>	<i>792.77</i>	<i>114.01</i>
CPCM	-33.07	852.39	112.83
6-311+G(2d,2p)	-19.71	956.41	107.86
0 K	<i>-19.74</i>	<i>950.29</i>	<i>109.64</i>
298 K	<i>-19.74</i>	<i>950.06</i>	<i>109.70</i>
CPCM	-21.28	1003.54	108.73
EPR-II [H,O], 6-311+G(2d,2p) [P]	-23.13	951.90	120.50
0 K	<i>-23.18</i>	<i>946.12</i>	<i>122.46</i>
298 K	<i>-23.18</i>	<i>945.92</i>	<i>122.53</i>
CPCM	-24.74	993.37	121.42
aug-cc-pV(D+d)Z	-46.66	890.22	96.37
aug-cc-pV(T+d)Z	-10.41	923.68	107.37
aug-cc-pV(Q+d)Z	-9.05	893.96	111.63
aug-cc-pV(5+d)Z	-17.23	922.95	115.80
aug-cc-pCVDZ	-11.52	947.69	95.23
aug-cc-pCVTZ	-23.58	935.80	107.61
aug-cc-pCVQZ	-24.24	963.33	111.51
expt		1023.43 <sup>b</sup>	109.27 <sup>b</sup>

<sup>a</sup> Vibrationally averaged values were computed at 0 and 298 K and are in italics. Solution phase values were estimated using CPCM. Available experimental values are given. <sup>b</sup> Reference 61.

al.<sup>60</sup> used high levels of ab initio theory [CCSD(T)/TZ2P(f,d)] to investigate this radical. While reporting that “the predicted structure and properties of H<sub>2</sub>PO greatly depend on the level of theory employed”,<sup>60</sup> the authors neglected to consider the effects of vibrational averaging on the computed hfs constants. Their values of  $A_{\text{iso}}(^{31}\text{P}) = 969.4$  MHz and  $A_{\text{iso}}(^1\text{H}) = 90.7$  MHz deviated from experiment<sup>61</sup> (1023.43 and 109.27 MHz, respectively) by as much as 54 MHz. While the deviation for <sup>31</sup>P is once again likely due to a poor description of the 1s core in the phosphorus basis set, the discrepancy of almost 20 MHz for <sup>1</sup>H may, in part, be a result of neglecting the out-of-plane deviations at the radical center, which can directly affect the spin density and the hfs constant.

The barrier to inversion in H<sub>2</sub>PO is only 12.9 kcal mol<sup>-1</sup> (Figure 8b), and the hfs constants for <sup>31</sup>P and <sup>1</sup>H both increase with pyramidalization of this radical (Figure 9). The computed isotropic hfs constants for H<sub>2</sub>PO are given in Table 7. Vibrational averaging has little effect on the Fermi contact term for <sup>17</sup>O [-34.27 to -34.34 MHz, 6-31+G\*; -19.71 to -19.74 MHz, 6-311+G(2d,2p); -23.13 to -23.18 MHz, EPR-II/6-311+G(2d,2p)]. The effect on  $A_{\text{iso}}(^{31}\text{P})$  is ~5 MHz [797.69 to 792.95 MHz, 6-31+G\*; 956.41 to 950.29 MHz, 6-311+G(2d,2p); 951.90 to 946.12 MHz, EPR-II/6-311+G(2d,2p)], and the effect on  $A_{\text{iso}}(^1\text{H})$  is ~2 MHz [112.27 to 113.95 MHz, 6-31+G\*; 107.86 to 109.64 MHz, 6-311+G(2d,2p); 120.50 to

**TABLE 8: Isotropic Fermi Contact Couplings (MHz) for the <sup>2</sup>A'' State of *trans*-HOPO<sup>-</sup> Using B3LYP<sup>a</sup>**

<i>trans</i> -HOPO <sup>-</sup>	<sup>17</sup> O <sub>1</sub>	<sup>17</sup> O <sub>2</sub>	<sup>31</sup> P	<sup>1</sup> H
6-31+G*	-8.81	-28.29	59.60	-5.27
0 K	<i>-8.15</i>	<i>-28.62</i>	<i>62.81</i>	<i>-2.08</i>
298 K	<i>-5.27</i>	<i>-30.89</i>	<i>61.33</i>	<i>-12.01</i>
CPCM	-11.35	-27.00	74.03	-11.35
6-311+G(2d,2p)	-5.54	-18.30	49.75	-5.17
0 K	<i>-4.99</i>	<i>-18.38</i>	<i>49.95</i>	<i>-2.60</i>
298 K	<i>-3.08</i>	<i>-18.67</i>	<i>50.64</i>	<i>-6.34</i>
CPCM	-7.44	-17.56	59.26	-5.67
EPR-II [H,O], 6-311+G(2d,2p) [P]	-7.40	-24.58	73.74	-6.13
0 K	<i>-7.00</i>	<i>-24.66</i>	<i>73.75</i>	<i>-4.90</i>
298 K	<i>-6.54</i>	<i>-24.74</i>	<i>73.77</i>	<i>-3.49</i>
CPCM	-9.51	-23.43	73.28	-6.60

<sup>a</sup> Vibrationally averaged values were computed at 0 and 298 K and are in italics. Solution phase values were estimated using CPCM.

**TABLE 9: Isotropic Fermi Contact Couplings (MHz) for the <sup>2</sup>A'' State of *cis*-HOPO<sup>-</sup> Using B3LYP<sup>a</sup>**

<i>cis</i> -HOPO <sup>-</sup>	<sup>17</sup> O <sub>1</sub>	<sup>17</sup> O <sub>2</sub>	<sup>31</sup> P	<sup>1</sup> H
6-31+G*	-9.11	-27.63	59.55	-5.93
0 K	<i>-9.41</i>	<i>-27.68</i>	<i>59.46</i>	<i>-3.39</i>
298 K	<i>-9.68</i>	<i>-27.73</i>	<i>59.40</i>	<i>-1.09</i>
CPCM	-11.24	-26.42	73.12	-6.40
6-311+G(2d,2p)	-5.59	-17.88	52.25	-6.09
0 K	<i>-6.09</i>	<i>-17.87</i>	<i>52.16</i>	<i>-2.78</i>
298 K	<i>-6.62</i>	<i>-17.86</i>	<i>52.06</i>	<i>0.68</i>
CPCM	-7.18	-17.16	60.69	-6.58
EPR-II [H,O], 6-311+G(2d,2p) [P]	-7.96	-24.06	71.00	-6.96
0 K	<i>-7.65</i>	<i>-24.51</i>	<i>69.15</i>	<i>-4.26</i>
298 K	<i>-9.77</i>	<i>-26.84</i>	<i>59.32</i>	<i>63.54</i>
CPCM	-8.74	-23.00	75.01	-7.33

<sup>a</sup> Vibrationally averaged values were computed at 0 and 298 K and are in italics. Solution phase values were estimated using CPCM.

122.46 MHz, EPR-II/6-311+G(2d,2p)]. Again, temperature effects are minimal, changing the computed hfs constants by only a few tenths of a megahertz for <sup>31</sup>P and <sup>1</sup>H. Clearly, there are still other factors to consider than just vibrational averaging. Thus, the aug-cc-pCVXZ and aug-cc-pV(X+d)Z families of basis sets were used to compute the hfs constants of H<sub>2</sub>PO at the B3LYP/6-311+G(2d,2p) optimized geometry. Similar “convergence” trends to those that were observed for HPO<sub>2</sub><sup>-</sup> were observed for H<sub>2</sub>PO. While the aug-cc-pCVQZ value of  $A_{\text{iso}}(^{31}\text{P}) = 963.33$  MHz is still significantly different from experiment (1023.43 MHz), the hfs constant of 111.51 MHz for <sup>1</sup>H is in close agreement with the experimental value of 109.27 MHz.

Solution effects on the Fermi contact terms for HPO<sub>2</sub><sup>-</sup> and H<sub>2</sub>PO were estimated using CPCM. These data are included in Tables 5 and 7. The shifts in the Fermi contact terms for HPO<sub>2</sub><sup>-</sup> are toward experiment for both <sup>31</sup>P and <sup>1</sup>H with each basis set. With the 6-311+G(2d,2p) basis set,  $A_{\text{iso}}(^{17}\text{O}) = -26.34$  MHz,  $A_{\text{iso}}(^{31}\text{P}) = 1123.42$  MHz, and  $A_{\text{iso}}(^1\text{H}) = 243.51$  MHz. The shifts in  $A_{\text{iso}}(^{31}\text{P})$  and  $A_{\text{iso}}(^1\text{H})$  for H<sub>2</sub>PO are also toward experiment, with 6-311+G(2d,2p) values of -21.28 MHz (<sup>17</sup>O), 1003.54 MHz (<sup>31</sup>P), and 108.73 MHz (<sup>1</sup>H).

The Fermi contact terms for the  $\pi$  radicals of *trans*- and *cis*-HOPO<sup>-</sup> are given in Tables 8 and 9, respectively. At the B3LYP/6-311+G\*(2d,2p) level of theory, the hfs constants for *trans*-HOPO<sup>-</sup> are  $A_{\text{iso}}(^{17}\text{O}_1) = -5.54$  MHz,  $A_{\text{iso}}(^{17}\text{O}_2) = -18.30$  MHz,  $A_{\text{iso}}(^{31}\text{P}) = 49.75$  MHz, and  $A_{\text{iso}}(^1\text{H}) = -5.17$  MHz. For the *cis*-isomer, these values are -5.59 MHz (<sup>17</sup>O<sub>1</sub>), -17.88 MHz (<sup>17</sup>O<sub>2</sub>), 52.25 MHz (<sup>31</sup>P), and -6.09 MHz (<sup>1</sup>H). Vibrational averaging and temperature affect the computed hfs constants



**TABLE 10:  $g$ -Factors for  $\text{HPO}_2^-$ ,  $\text{trans-HOPO}^-$ , and  $\text{cis-HOPO}^-$  Using B3LYP<sup>a</sup>**

	$\text{HPO}_2^-$	$\text{HPO}_2^-$	$\text{trans-HOPO}^-$		$\text{cis-HOPO}^-$		$\text{H}_2\text{PO}$
	( <sup>2</sup> B <sub>1</sub> )	( <sup>2</sup> A')	( <sup>2</sup> A')	( <sup>2</sup> A'')	( <sup>2</sup> A')	( <sup>2</sup> A'')	
6-31+G*	2.002 52 <i>2.003 36</i>	2.002 44 <i>2.003 42</i>	2.002 33	2.001 17 <i>2.001 95</i>	2.002 27	2.001 90 <i>2.001 85</i>	2.002 70 <i>2.002 67</i>
6-311+G(2d,2p)	2.002 55 <i>2.003 66</i>	2.002 41 <i>2.003 21</i>	2.002 33	2.000 97 <i>2.001 84</i>	2.002 27	2.000 89 <i>2.001 75</i>	2.002 70 (2.002 66)
EPR-II [H,O], 6-311+G(2d,2p) [P]	2.002 46 <i>2.002 99</i>	2.002 40 <i>2.003 15</i> [2.003 03] <sup>b</sup>	2.002 33	2.000 37 <i>2.001 60</i>	2.002 27	2.000 03 <i>2.001 43</i>	2.002 69 (2.002 66)

<sup>a</sup> The experimental  $g$ -factor for  $\text{HPO}_2^-$  is in brackets. Values in solution are in italics. <sup>b</sup> Reference 16.

of <sup>17</sup>O<sub>1</sub>, <sup>17</sup>O<sub>2</sub>, <sup>31</sup>P, and <sup>1</sup>H by 2–4 MHz in the trans-isomer. In the cis-isomer, vibrational averaging and temperature have minimal effects on the Fermi contact terms of either O center. With the 6-31+G\* and 6-311+G(2d,2p) basis sets,  $A_{\text{iso}}(^{31}\text{P})$  is not significantly affected by either of these two effects. However, with the EPR-II/6-311+G(2d,2p) basis set, vibrational averaging has an effect of ~2 MHz at 0 K and ~12 MHz at 298 K. The hfs constant of <sup>1</sup>H in  $\text{cis-HOPO}^-$  is affected the most by vibrational averaging. At 0 K, there is a difference of ~3 MHz, while, at 298 K, the difference is ~5 MHz with the 6-31+G\* and 6-311+G(2d,2p) basis sets and 56.58 MHz with the EPR-II/6-31+G(2d,2p) basis set.

**D.  $g$ -Factors.** The  $g$ -factors of the  $\text{HPO}_2^-$ ,  $\text{trans-HOPO}^-$ , and  $\text{cis-HOPO}^-$  radicals are given in Table 10. The  $g$ -factor is analogous to chemical shielding in NMR. The internal magnetic fields of bound unpaired electrons can shift or split the basic resonance line into multiple components. The orbital angular momentum of the unpaired electron contributes to the total magnetic moment, producing a shift in the  $g$ -factor from the free electron value of 2.002 32. In radical ions,  $g$ -factors are generally within 1–2% of the free electron value because the orbital angular momentum may be quenched. Using the EPR-II/6-311+G(2d,2p) basis set, this is observed for the radical anions studied here. The value of  $\delta g_{\text{obs}} = 2.002 40$  for <sup>2</sup>A'  $\text{HPO}_2^-$  is in good agreement with the experimental value of 2.003 03.<sup>16</sup> Using CPCM to estimate solution effects ( $\delta g_{\text{obs}} = 2.003 15$ ), the agreement with theory is even better. For  $\text{trans-}$  and  $\text{cis-HOPO}^-$ , the  $g$ -factors are 2.000 37 and 2.000 03, respectively, and with solution effects, these values are 2.001 60 (trans) and 2.001 43 (cis). Solution effects are much less pronounced for the computed  $g$ -factor for  $\text{H}_2\text{PO}$ . With the EPR-II/6-311+G(2d,2p) basis set, the  $g$ -factor is 2.002 69, and using the CPCM, this value is 2.002 66.

#### IV. Conclusions

The energetic ordering of the isomers of  $\text{HPO}_2$  is  $\text{cis-HOPO}^- < \text{trans-HOPO}^- < \text{HPO}_2$ , while that of the anions is  $\text{HPO}_2^- < \text{cis-HOPO}^- < \text{trans-HOPO}^-$ . The relative energies of the neutral systems are 0.0 kcal mol<sup>-1</sup> (cis), 3.0 kcal mol<sup>-1</sup> (trans), and 14.9 kcal mol<sup>-1</sup> ( $\text{HPO}_2$ ). The cis- and trans-anions lie ~5 and ~8 kcal mol<sup>-1</sup>, respectively, higher than  $\text{HPO}_2^-$ . The minimum on the potential energy surface of the  $\text{HPO}_2^-$  radical is a pyramidal structure in  $C_s$  symmetry. Two radical anions are found for each cis- and trans-isomer of  $\text{HOPO}^-$ . The  $\pi$  radicals are lower in energy, while the  $\sigma$  radicals are really  $\text{PO}_2^-$  loosely associated with free H.

Vibrational averaging can be important for the theoretical prediction of Fermi contact terms for nonrigid radicals. This affects the computed hfs constants for  $\text{H}_2\text{PO}$  by 5–6 MHz for  $A_{\text{iso}}(^{31}\text{P})$  and 1–2 MHz for  $A_{\text{iso}}(^1\text{H})$ , but  $A_{\text{iso}}(^{17}\text{O})$  is relatively unaffected. The Fermi contact terms for  $\text{HPO}_2^-$  show a smaller

vibrational averaging effect for <sup>31</sup>P (~2 MHz) but a larger effect for <sup>1</sup>H (8–20 MHz).  $A_{\text{iso}}(^{17}\text{O})$  remains relatively unaffected by vibrational averaging.

It is shown here that solvent effects are important to the accurate computation of hfs constants of the  $\text{HPO}_2^-$  and  $\text{H}_2\text{PO}$  radicals. With the 6-311+G(2d,2p) basis set, the computed Fermi contact terms for <sup>31</sup>P and <sup>1</sup>H in both radicals are in close agreement with experiment. In  $\text{HPO}_2^-$ , the values of  $A_{\text{iso}}(^{31}\text{P}) = 1123.42$  MHz and  $A_{\text{iso}}(^1\text{H}) = 243.51$  MHz compare to the experimental values of 1346 and 252 MHz, respectively. In  $\text{HPO}_2$ , the computed values of  $A_{\text{iso}}(^{31}\text{P}) = 1003.54$  MHz and  $A_{\text{iso}}(^1\text{H}) = 108.73$  MHz compare to the experimental values of 1023.43 and 109.27 MHz, respectively.

The Fermi contact terms computed for  $\text{HPO}_2^-$ ,  $\text{H}_2\text{PO}$ , and P using B3LYP with the aug-cc-pCVXZ and aug-cc-pV(X+d)Z families of basis sets show that the convergence of  $A_{\text{iso}}(^{31}\text{P})$  is erratic and slow. While the more expensive CCSD(T) method produces hfs constants for the P atom that are in good agreement with the experimental value, the problems encountered using B3LYP show that using a basis set with a good description of the 1s core of P is critical for producing accurate theoretical values of  $A_{\text{iso}}(^{31}\text{P})$ . Our attempts to make the core more flexible are successful in providing a more balanced basis set, as reflected by the convergence to experiment of the CCSD(T) results. However, the B3LYP values still do not show such convergence for this property of the P atom, which reflects the deficiency of the functional, which was after all parametrized from thermochemistry. Our modified aug-cc-pCVXZ basis sets do show good convergence for the Fermi contact term of the P center in  $\text{HPO}_2^-$ , although the converged value of  $A_{\text{iso}}(^{31}\text{P}) = 1003.80$  MHz is still different from experiment by ~400 MHz.

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