# Effect of Diffusional Film on Formation of Hydrogen Peroxide in Photocatalytic Reactions

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We recently found that photocatalytic reactions produce  $H_2O_2$  at a concentration level of ppm (parts per million) from water. For some reason, however, other researchers have paid little attention to the formation of  $H_2O_2$  in this reaction. Of course, one of the reasons is due to low sensitivities of the conventional methods employed to measure the  $H_2O_2$  concentration. However, we suppose that there is another reason which makes it difficult to measure it. To elucidate this reason, therefore, an effect of linear liquid velocity on the photocatalytic formation of  $H_2O_2$  from water is experimentally investigated, and an explanation for the experimental result is made using a mathematical model that takes into consideration the formation and decomposition of  $H_2O_2$  and its diffusion through a film in the neighborhood of the photocatalyst surface into a bulk liquid. This effect is also discussed on the formation of  $H_2O_2$  from an aqueous solution of formic acid. As a result, it is concluded that the diffusion film is responsible for the reduction in the  $H_2O_2$  concentration.

### 1. Introduction

A photocatalytic reaction is constituted by the formation of several kinds of radicals.<sup>1–3,4</sup> The mechanism of this reaction includes the formation of hydrogen peroxide,  $H_2O_2$ .<sup>5–7</sup> In fact, it is known that the photocatalytic reactions using TiO<sub>2</sub>,<sup>8,9</sup> TiO<sub>2</sub>– Co<sup>II</sup>TSP,<sup>9</sup> ZnO,<sup>8</sup> and so forth produce  $H_2O_2$ . We also have recently found that the photocatalytic reactions using TiO<sub>2</sub> and Pd–TiO<sub>2</sub> produce  $H_2O_2$  at a concentration level of ppm (parts per million) from water,<sup>10</sup> and the initial rates of formation of H<sub>2</sub>O<sub>2</sub> are in proportion to the initial rates of decomposition of formaldehyde (HCHO) and formic acid (HCOOH), i.e., the photocatalytic activities. For example, Pd–TiO<sub>2</sub> decomposed several organic compounds and produced H<sub>2</sub>O<sub>2</sub> more quickly than did TiO<sub>2</sub>.<sup>11</sup> Thus, it is clear that the photocatalytic activity is closely related to the formation of H<sub>2</sub>O<sub>2</sub>.

For some reason, however, other researchers have paid little attention to the formation of  $H_2O_2$  in the photocatalytic reaction. Of course, this is first due to the fact that the conventional methods employed to measure the concentration of a trace of  $H_2O_2$  formed during the photocatalytic reaction were insensitive. Fortunately, we could successfully measure the time course of the  $H_2O_2$  concentration by use of the enzyme *peroxidase* that catalyzes a coloring reaction.<sup>10</sup> On the other hand, we suppose that there is another reason which makes it difficult to measure the  $H_2O_2$  concentration in the photocatalytic reaction.

In the present work, therefore, we first investigate experimentally an effect of linear flow velocity on the photocatalytic formation of  $H_2O_2$  from water and then attempt to explain the experimental result using a mathematical model that takes into consideration the formation and decomposition of  $H_2O_2$  and its diffusion through a film formed in the neighborhood of the photocatalyst surface into a bulk liquid. Similarly, a formation of  $H_2O_2$  from an aqueous solution of HCOOH is investigated.

#### 2. Theory

**2.1. Photocatalytic Formation of H\_2O\_2 from H\_2O.** A masstransfer limitation to the photocatalytic reaction has first been invoked experimentally by Matthews<sup>12</sup> and then commented by Turchi and Ollis<sup>13</sup> from the standpoint of photocatalytic reactor design. However, no detailed procedure for mathematical analysis is available so far.

Let us consider the following reaction that produces  $H_2O_2$  from  $H_2O$  on the photocatalyst surface:

$$H_2O + \frac{1}{2}O_2 \xrightarrow{k_1} H_2O_2 \tag{1}$$

Assuming that the dissolved oxygen concentration in the water is sufficiently high and kept constant because of continuous supply from the air in a batch-recirculation reactor, the rate of formation of H<sub>2</sub>O<sub>2</sub> on the photocatalyst surface,  $r_{\text{H}_2\text{O}_2,i}$  (mol m<sup>-2</sup>surface min<sup>-1</sup>), is expressed as

$$r_{\rm H_2O_2,i} = \frac{k_1 K_{\rm H} C_{\rm H_2O,i}}{1 + K_{\rm H} C_{\rm H,O,i}}$$
(2)

where  $k_1$  (mol m<sup>-3</sup> min<sup>-1</sup>) is the kinetic constant,  $K_{\rm H}$  is the adsorption equilibrium constant (mol<sup>-1</sup> m<sup>3</sup>), and  $C_{\rm H_2O,i}$  is the concentration of H<sub>2</sub>O at the photocatalyst surface (mol m<sup>-3</sup>). For convenience, we will express the concentration of a given chemical substance at the photocatalyst surface in units of moles per volume. Since the concentration of H<sub>2</sub>O is extremely high, eq 2 is simplified to

$$r_{\mathrm{H}_{2}\mathrm{O}_{2},\mathrm{i}} \simeq k_{1} \tag{3}$$

which means that the formation of  $H_2O_2$  proceeds with zerothorder kinetics.

On the other hand, when conducting the photocatalytic reaction in an aqueous solution, a diffusion film is commonly formed in the neighborhood of the photocatalyst surface, as illustrated in Figure 1. Reactant molecules must diffuse through the film to the photocatalyst surface, which lowers the rate of the photocatalytic reaction. Therefore, the overall rate of the photocatalytic reaction must be described by taking into consideration the effect of film-diffusional resistance. Moreover,

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Glass tube

Figure 1. Distribution of hydrogen peroxide concentration in neighborhood of photocatalyst surface.

the decomposition of  $H_2O_2$  proceeds in parallel with its formation in the very neighborhood of the photocatalyst surface where various kinds of radical species exist at high concentrations. Consequently, we simply describe the formation and decomposition of  $H_2O_2$  as

$$H_2O + \frac{1}{2}O_2 \stackrel{k_1}{\underset{k_2}{\longleftrightarrow}} H_2O_2 \tag{4}$$

When the system is at equilibrium, the rate of formation of  $H_2O_2$ on the photocatalyst surface,  $r_{H_2O_2,i}$  is identical to the rate of diffusion of  $H_2O_2$  through the film,  $N_{H_2O_2}$  (mol m<sup>-2</sup>-surface h<sup>-1</sup>), so that<sup>14</sup>

$$N_{\rm H_2O_2} = k_{\rm L}(C_{\rm H_2O_2,i} - C_{\rm H_2O_2,b}) = k_1 - k_2 C_{\rm H_2O_2,i} = r_{\rm H_2O_2,i}$$
(5)

where  $C_{\text{H}_2\text{O}_2,i}$  and  $C_{\text{H}_2\text{O}_2,b}$  express the concentrations of  $\text{H}_2\text{O}_2$ (mol m<sup>-3</sup>) at the photocatalyst surface and in the bulk liquid, respectively, and  $k_{\text{L}}$  is the mass-transfer coefficient (m h<sup>-1</sup>). Solving eq 5 with respect to  $C_{\text{H}_2\text{O}_2,i}$  leads to

$$C_{\rm H_2O_2,i} = \frac{C_{\rm H_2O_2,b} + k_1/k_{\rm L}}{1 + k_2/k_{\rm I}}$$
(6)

Therefore, the rate of formation of  $H_2O_2$  on the photocatalyst surface is described as a function of only  $C_{H_2O_2,b}$  by

$$r_{\rm H_2O_2,i} = \frac{k_1 - k_2 C_{\rm H_2O_2,b}}{1 + k_2/k_{\rm I}}$$
(7)

Consequently, when a reaction mixture with a liquid volume of  $V_{\rm L}$  (m<sup>3</sup>) is treated by the photocatalyst with an external surface of *S* (m<sup>2</sup>-surface) irradiated with UV light, the rate of photocatalytic reaction on a liquid volume basis,  $r_{\rm H_2O_2,L}$  (mol m<sup>-3</sup>-liquid min<sup>-1</sup>), is given as

$$r_{\rm H_2O_2,L} = \frac{dC_{\rm H_2O_2,b}}{dt} = (S/V_{\rm L})\frac{k_1 - k_2C_{\rm H_2O_2,b}}{1 + k_2/k_{\rm L}}$$
(8)

2.2. Method for Determination of Kinetic Parameters and Mass-Transfer Coefficient. Before calculating the time course of the  $H_2O_2$  concentration in the photocatalytic reaction, it is necessary to determine the kinetic parameters and mass-transfer

coefficient involved in eq 8 from the experimental data. As described later, we conducted a series of the photocatalytic reaction experiments in a batch-recirculation reactor, as described elsewhere,<sup>10,15</sup> where the reactant mixture was recirculated at a constant flow velocity between the annular-flow reactor and perfectly mixed flow vessel. In the following, therefore, we will describe the method for determination of kinetic parameters and mass-transfer coefficient on the assumption of using the experimental data obtained in the batch-recirculation reactions.

From eq 8, it is obvious that the initial rate of formation of  $H_2O_2$  from  $H_2O$  is written as

$$r_{\rm H_2O_2,L}|_{t=0} = \frac{dC_{\rm H_2O_2,b}}{dt}\Big|_{t=0} = (S/V_{\rm L})\frac{k_1 - k_2C_{\rm H_2O_2,b}}{1 + k_2/k_{\rm L}}\Big|_{t=0} = (S/V_{\rm L})\frac{k_1}{1 + k_2/k_{\rm L}}$$
(9)

Since the mass-transfer coefficient increases toward the infinity as the recirculation flow rate (or linear velocity) increases, eq 9 becomes

$$r_{\rm H_2O_2L}|_{t=0} = (S/V_{\rm L})k_1 \tag{10}$$

which indicates that the initial rates of formation of  $H_2O_2$  measured at different linear velocities become constant at a sufficiently large linear velocity. Consequently, the value of  $k_1$  can be determined from the measured values.

Similarly, when  $H_2O_2$  is added to  $H_2O$  to decompose under irradiation with UV light recirculating the solution at a sufficiently high linear velocity, eq 8 gives the rate of the decomposition as

$$-r_{\rm H_2O_2,L} = -\frac{dC_{\rm H_2O_2,b}}{dt} = (S/V_{\rm L})(k_2C_{\rm H_2O_2,b} - k_1) \quad (11)$$

which gives the following relationship between the initial rate of decomposition of  $H_2O_2$  and the initial concentration of  $H_2O_2$ .

$$-r_{\rm H_2O_2,L}|_{t=0} = -\frac{\mathrm{d}C_{\rm H_2O_2,b}}{\mathrm{d}t}\Big|_{t=0} = (S/V_{\rm L})(k_2C_{\rm H_2O_2,b0} - k_1)$$
(12)

Thus, the initial rates of photocatalytic decomposition of  $H_2O_2$  are measured at different initial concentrations of  $H_2O_2$ , and these values and the value of  $k_1$  already determined are applied to eq 12. As a result, the value of  $k_2$  is obtained.

Furthermore, solving eq 9 for  $k_{\rm L}$  leads to

$$k_{\rm L} = \frac{r_{\rm H_2O_2,L}|_{t=0}k_2}{(S/V_{\rm L})k_1 - r_{\rm H_2O_2,L}|_{t=0}}$$
(13)

Therefore, the values of  $k_1$  and  $k_2$  determined above and the values of  $r_{\text{H}_2\text{O}_2,\text{L}}|_{t=0}$  measured at different linear velocities,  $u_z$  (m h<sup>-1</sup>), are applied to eq 13. The values of  $k_{\text{L}}$  thus calculated are plotted against their respective linear velocities. In general, the relationship between  $k_{\text{L}}$  and  $u_z$  is expressed as<sup>16,17</sup>

$$k_{\rm L} = a u_{\rm z}^{\ b} \tag{14}$$

Thus, eq 14 is applied to the plotted data in order to determine the parameter values by the least-squares method.

#### **3. Experimental Section**

**3.1. Materials and Reagents.** Titanium tetraisopropozide (TIP) was purchased from Katayama Chemicals Co., Ltd.



Figure 2. Annular-flow photocatalytic reactor.

(Tokyo). Isopropyl alcohol (IPA) was obtained form Wako Pure Chemical Industries Ltd. (Osaka). A 31% (v/v) aqueous  $H_2O_2$ solution was a product of Mitsubishi Chemical Co., Ltd. (Tokyo). Glucose B test Wako (Wako Pure Chemical Industries Ltd.) was used to measure the  $H_2O_2$  concentration. Two kinds of 6 W UV lamps were used as a light source; black light blue fluorescent lamp (FL6BL-B; Matsushita Denki, Tokyo) and germicidal lamp (GL-6; Sankyo Denki, Tokyo). The wavelength distributions of UV lights emitted from these lamps are available elsewhere.<sup>18,19</sup>

**3.2. Operational Method of the Photocatalytic Reactor.** Amorphous titanium dioxide was prepared from TIP and used to coat the surface of a glass tube according to the procedure described elsewhere.<sup>20,21</sup> As illustrated in Figure 2, the photocatalytic reactor has an annular structure,<sup>21–23</sup> consisting of a light source protected by a quartz glass tube (24 mm in outer diameter and 220 mm long) centered along the main axis of a plastic cylinder and a Pyrex glass tube (28 mm in inner diameter, 140 mm long, and 1.8 mm in thickness), whose inner surface is coated with a thin film of photocatalyst (surface area 0.0123 m<sup>2</sup>), which is inserted and fixed so as to closely contact with the outer surface of the plastic cylinder. A reactant mixture was allowed to flow through the annulus of 2 mm in width between the quartz and Pyrex glass tubes. The inlet volume of the reactor was about  $7 \times 10^{-5}$  m<sup>3</sup>.

The photocatalytic reactor was circularly connected with a mixed-flow vessel and a peristaltic pump (RP-1000; EYELA, Tokyo), as shown in Figure 3. Distilled water of  $3.0 \times 10^{-4}$  m<sup>3</sup> with or without formic acid was poured into the mixed-flow vessel and circulated at a constant flow rate. The light source was switched on to start the photocatalytic reaction and a small amount of reaction mixture was withdrawn at appropriate intervals from the mixed-flow vessel. All the experiments were conducted by placing the experimental apparatus in a constant-temperature chamber to keep the liquid temperature constant (21 °C) and to shut out all unnecessary light.

**3.3. Measurement of H<sub>2</sub>O<sub>2</sub> Concentration.** Glucose B Test Wako  $(3.0 \times 10^{-6} \text{ m}^3)$  was added to the reaction mixture (2.0  $\times 10^{-6} \text{ m}^3)$  withdrawn from the mixed-flow vessel to cause a coloring reaction. After 20 min, the absorbance of the solution



Figure 3. Batch-recirculation reactor system.

was measured at 505 nm with a spectrophotometer (UV-240; Shimazu, Tokyo) to determine the  $H_2O_2$  concentration.

## 4. Results and Discussion

**4.1.** H<sub>2</sub>O System. 4.1.1. Relationship between the Initial Rate of Formation of  $H_2O_2$  and Linear Velocity. Table 1 summarizes the kinetic scheme of the photocatalytic reaction described in a number of papers.<sup>5–7</sup> There exist two elementary reactions that produce  $H_2O_2$ . We experimentally elucidated that the photocatalyst can produce  $H_2O_2$  from distilled water. However, the rate of its formation sconer or later slowed and became constant, suggesting that the decomposition of  $H_2O_2$  takes place in parallel with its decomposition.

It is considered that this decomposition is caused by the highly active radicals formed during the photocatalytic reaction as well

 TABLE 1: Formation of Radicals in a Photocatalytic Reaction

$_{2} \bullet \rightarrow \mathrm{HO}_{2}^{-} + \mathrm{O}_{2}$
$\rightarrow$ H <sub>2</sub> O <sub>2</sub>
$\rightarrow \mathrm{HO} \bullet + \mathrm{OH}^-$
$\bullet \rightarrow \mathrm{HO} \bullet + \mathrm{OH}^- + \mathrm{O}_2$
→2HO•

as the UV light, which terminates increasing concentration of H<sub>2</sub>O<sub>2</sub> at a certain low level. As a result, it becomes difficult to monitor the time course of the H2O2 concentration in the photocatalytic reaction. According to our measurement,<sup>21</sup> the concentration of  $H_2O_2$  formed is on the order of  $10^{-4}-10^{-3}$ mol m<sup>-3</sup> at the maximum. We were able to accurately measure the concentration of H<sub>2</sub>O<sub>2</sub> at such a low level by introducing an enzymatic method. Another advantage of using this enzymatic method is the substrate specificity of the enzyme, in which the enzyme acts on only H<sub>2</sub>O<sub>2</sub>. Thus, the true concentration can be measured. However, would the low sensitivities of the measurement methods be only a reason for the fact that little measurement of H<sub>2</sub>O<sub>2</sub> has been done in the past photocatalytic reaction studies? A comparison shows that most of the photocatalytic reaction experiments reported by other researchers have been performed at low linear velocities compared with our experiment, so that we suppose that this experimental condition may cause a difficulty in the measurement of H<sub>2</sub>O<sub>2</sub> concentration in the photocatalytic reaction. In the following, therefore, the effect of linear velocity on the photocatalytic reaction will be investigated both experimentally and theoretically.



Figure 4. Effect of linear velocity on initial rate of formation of hydrogen peroxide.

Figure 4 shows the relationship between the initial rate of formation of  $H_2O_2$  and the linear velocity when the surface of the photocatalyst immersed in the distilled water was irradiated with the UV light from a black light fluorescent lamp and

germicidal lamp. The initial rate of formation of  $H_2O_2$  initially increases linearly with the linear velocity and then plateaus. The Reynolds number <sup>24</sup> in the present system lies in the range of 66.7–233 for the linear velocity of 2–7 m min<sup>-1</sup>, indicating that the liquid flow in the photocatalytic reactor is a laminar flow. A comparison at the same linear velocity indicates that the germicidal lamp, emitting more powerful UV light with a shorter wavelength, can produce  $H_2O_2$  more rapidly than does the black light blue fluorescent lamp. The initial rate of formation of  $H_2O_2$  with the black light blue fluorescent lamp plateaus in the region of lower linear velocity because of its lower rate of formation.

Since the thickness of the film formed in the very neighborhood of the photocatalyst surface decreases with the increase of the linear velocity,<sup>17</sup> we suppose that the film must have strongly affected the amount of  $H_2O_2$  produced. In the following, therefore, this will be undertaken to explain using the mathematical model described above.

4.1.2. Determination of Kinetic Parameters and Mass-Transfer Coefficient. Figure 4, where the germicidal lamp was employed as a light source, clearly indicates that the initial rate of formation of H<sub>2</sub>O<sub>2</sub> becomes almost constant above a certain value of linear velocity. From the initial rate of formation in this region, the value of  $k_1$  was determined to be  $6.24 \times 10^{-6}$ mol m<sup>-2</sup> min<sup>-1</sup>. When decomposition of H<sub>2</sub>O<sub>2</sub> in an aqueous solution by UV light is carried out at a sufficiently large linear velocity, the initial rate of decomposition is expressed by eq 12, which takes into consideration the decomposition of H<sub>2</sub>O<sub>2</sub> in the film. Therefore, H<sub>2</sub>O<sub>2</sub> at an initial concentration of  $3.21 \times 10^{-2}$  mol m<sup>-3</sup> was decomposed using the photocatalyst irradiated with the UV light from the germicidal lamp. The result is shown in Figure 5. From these experimental data, the initial



Figure 5. Time courses of hydrogen peroxide concentration in decomposition of hydrogen peroxide by UV lights.

rate of decomposition,  $r_{H_2O_2,L}|_{t=0}$ , was determined to be 2.93 ×  $10^{-4}$  mol m<sup>-3</sup> min<sup>-1</sup>. Furthermore, this value and the value of  $k_1$  determined above were applied to eq 12, so that  $k_2$  was determined to be 4.17 ×  $10^{-4}$  mol m<sup>-2</sup> min<sup>-1</sup>. The values of  $k_1$  and  $k_2$  and the experimental data in Figure 4 were further applied to eq 13 to obtain the value of  $k_L$  for each linear velocity. The values of  $k_L$  thus determined are plotted against their respective linear velocities, as shown in Figure 6. Equation 14 was applied to the data in Figure 6 and the parameters included in the



Figure 6. Effect of linear velocity on mass-transfer coefficients determined from experimental data of photocatalytic reactions.

 
 TABLE 2: Kinetic Constants and Equations of Mass-Transfer Coefficient

		black light blue
	germicidal lamp	fluorescent lamp
$k_1 \pmod{m^{-2} \min^{-1}}$	$6.24 \times 10^{-6}$	$1.87 \times 10^{-6}$
$k_2 \pmod{m^{-2} \min^{-1}}$	$4.17 \times 10^{-4}$	$1.29 \times 10^{-4}$
$k_{\rm L} ({\rm m}{\rm min}^{-1})$	$1.71 \times 10^{-3} u^{0.621}$	$1.85 \times 10^{-3} u^{0.538}$

equation were determined by the least-squares method. As a result, the following equation was obtained.

$$k_{\rm L} = 1.71 \times 10^{-3} u^{0.621} \tag{15}$$

The same procedure was applied to the experimental data in Figure 4, where the black light blue fluorescent lamp was used as a light source, and the value of  $k_1$  was determined to be 1.87  $\times$  10<sup>-6</sup> mol m<sup>-2</sup> min<sup>-1</sup>. From the experimental result for the decomposition of  $H_2O_2$  at an initial concentration of 2.63  $\times$  $10^{-2}$  mol m<sup>-3</sup> (Figure 5), the value of  $r_{H_2O_2L}|_{t=0}$  was determined to be  $6.17 \times 10^{-5}$  mol m<sup>-3</sup> min<sup>-1</sup>. Furthermore, this value and the value of  $k_1$  determined above was applied to eq 12 and the value of  $k_2$  was determined to be  $1.29 \times 10^{-4} \text{ mol m}^{-2} \text{ min}^{-1}$ . The values of  $k_1$  and  $k_2$  and the data in Figure 4 were further applied to eq 13 in order to determine the value of  $k_{\rm L}$  for each linear velocity. The values of  $k_{\rm L}$  thus determined are plotted against their respective linear velocities, as shown in Figure 6. Equation 14 was therefore applied to the data in Figure 6 and the parameters involved in the equation were determined by the least-squares method. As a result, the following equation was obtained.

$$k_{\rm L} = 1.85 \times 10^{-3} u^{0.538} \tag{16}$$

The parameter values and mass-transfer coefficients for the two light sources are compared in Table 2. The kinetic constant for the formation of H<sub>2</sub>O<sub>2</sub>,  $k_1$ , with the germicidal lamp is 3.3 times larger than that with the black light blue fluorescent lamp. Similarly, the kinetic constant for the decomposition of H<sub>2</sub>O<sub>2</sub>,  $k_2$ , with the germicidal lamp is 3.2 times larger than that with the black light blue fluorescent lamp. In eq 8, the denominator on the right-hand side can be approximately written as  $1 + k_2/k_L \approx 1$ , and therefore, the apparent rate of formation of H<sub>2</sub>O<sub>2</sub>



Figure 7. Comparison between initial rates of formation of hydrogen peroxide from water and an aqueous solution of formic acid (light source: germicidal lamp).

on the photocatalyst irradiated with the UV light from the germicidal lamp is three times larger throughout the whole reaction time. It should be noted that the parameter values in the equations of mass-transfer coefficient for the germicidal lamp and black light blue fluorescent lamp are almost the same. This result is reasonable because the same reactor with either black light blue fluorescent lamp or germicidal lamp was used to carry out the photocatalytic reactions under the same liquid flow condition so that the mass-transfer coefficients must be fundamentally the same.

4.1.3. Comparison of the Calculated Results. The kinetic parameters and mass-transfer coefficients determined above were applied to eq 9 in order to determine the relationship between the kinetic parameters and mass-transfer coefficients. The calculated results for the germicidal lamp and black light blue fluorescent lamp are shown by solid and broken lines, respectively, in Figure 4. The calculated lines are in good agreement with their respective experimental values, indicating that there is a close relationship between the film formed in the neighborhood of the photocatalyst surface and the observed result that the initial rate of formation of  $H_2O_2$  initially increases with the linear velocity and then plateaus.

**4.2. Formic Acid**-H<sub>2</sub>O System. In a previous paper,<sup>21</sup> we have revealed that H<sub>2</sub>O<sub>2</sub> is also formed in the process of the photocatalytic decomposition of formic acid. Therefore, the H<sub>2</sub>O<sub>2</sub> concentration becomes higher in the photocatalytic treatment of H<sub>2</sub>O containing formic acid than in the photocatalytic treatment of H<sub>2</sub>O alone. Figures 7 and 8 show the relationships between the initial rate of formation of H<sub>2</sub>O<sub>2</sub> and the linear velocity when H<sub>2</sub>O containing formic acid at an initial concentration of 0.45 mol m<sup>-3</sup> was photocatalytically treated using the germicidal lamp and black light blue fluorescent lamp, respectively. For comparison, each figure also includes the initial rate of formation of H<sub>2</sub>O<sub>2</sub> in the photocatalytic treatment of H<sub>2</sub>O alone. It is clear that despite the kind of the light source, the initial rate of formation is remarkably increased in the presence of formic acid. This is explained as follows. The intermediate product HCOOH is known to be a scavenger of the hole h<sup>+</sup> in the recombination reaction described as  $h^+ + e^- \rightarrow$  heat and causes the competitive reaction described as  $h^+ + HCOO^- \rightarrow$ HCOO<sup>•</sup>, leading to the formation of a larger amount of H<sub>2</sub>O<sub>2</sub>



Figure 8. Comparison between initial rates of formation of hydrogen peroxide from water and an aqueous solution of formic acid (light source: black light blue fluorescent lamp).

according to the subsequent reactions described as  $e^- + O_2 \rightarrow$  $O_2^{-\bullet} \rightarrow \cdots \rightarrow H_2O_2.$ 

Interestingly, the initial rate of formation of H<sub>2</sub>O<sub>2</sub> for the germicidal lamp is lower than that for the black light blue fluorescent lamp in the region of low linear velocity, rapidly increasing with the increase of linear velocity and finally becoming higher. Considering the fact that the germicidal lamp emits more powerful UV light than does the black light blue fluorescent lamp, the experimental result is evidently contradictory. This can be explained as follows. When the linear velocity is low and the film is relatively thick, the H<sub>2</sub>O<sub>2</sub> produced on the photocatalyst surface must move slowly by diffusion through the film to the bulk liquid. As a result,  $H_2O_2$  is exposed for a longer time to a highly reactive circumstance in the film, crowded by a larger amount of radicals produced under irradiation with the UV light from the germicidal lamp, and the majority of H<sub>2</sub>O<sub>2</sub> is quickly decomposed in the film. In the region of high linear velocity, however, the thickness of the film is thin and the H<sub>2</sub>O<sub>2</sub> produced can quickly move out of the film or is withdrawn from the film into the bulk liquid by the recirculation flow passing through the neighborhood of the photocatalyst surface, thereby increasing the H<sub>2</sub>O<sub>2</sub> concentration in the bulk liquid. Even when the film becomes very thin due to a higher linear liquid velocity and the system is reactioncontrolled, H<sub>2</sub>O<sub>2</sub> is decomposed by the radicals that are continuously produced on the photocatalyst surface and by the UV light in the bulk liquid. Consequently, the H<sub>2</sub>O<sub>2</sub> concentration in the bulk liquid takes a constant value at a point where the rate of formation of H<sub>2</sub>O<sub>2</sub> is equal to the rate of decomposition of  $H_2O_2$ .

#### 5. Conclusion

In the present work, we investigated the relationship between the rate of formation of H<sub>2</sub>O<sub>2</sub> and the recirculation flow rate (linear velocity) in the photocatalytic reaction using a batch recirculation reactor to elucidate the effect of film formed in the neighborhood of the photocatalyst on the photocatalytic reaction. As a result, we obtained the following conclusions.

(1) The rate of formation of  $H_2O_2$  in the photocatalytic reaction apparently increases with the increase of the linear velocity.

(2) This is probably because the thickness of the film becomes thin with the increase of the linear velocity and the  $H_2O_2$  formed on the photocatalyst surface can easily move through the film to the bulk liquid.

(3) This phenomenon can successfully be explained by using a mathematical model for the overall photocatalytic reaction that takes into consideration the diffusion of H<sub>2</sub>O<sub>2</sub> through the film.

(4) One of the reasons other researchers could not detect  $H_2O_2$ in the photocatalytic reaction is that the reaction experiments were performed under the conditions where  $H_2O_2$  formed on the photocatalyst was so quickly decomposed in the film that the H<sub>2</sub>O<sub>2</sub> concentration in the bulk liquid did not become high.

(5) As a result, it is concluded that a diffusion film formed in the neighborhood of the photocatalyst surface is responsible for a reduction in the H<sub>2</sub>O<sub>2</sub> concentration.

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