

# A Theoretical Study of the Photodetachment and Intramolecular Hydrogen-Bonding Energies of Hydrogen Maleate Anions

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Three low-lying conformers of the hydrogen maleate anions (HMAs) regarding *cis*-HMA(HB) having the  $O^- \cdots HO$  intramolecular hydrogen bond (HB), *cis*-HMA(nHB) without the HB, and *trans*-HMA are studied by density functional theory (B3LYP) combined with natural bond orbital (NBO) and atoms-in-molecules (AIM) analyses. The photoelectron spectra of *cis*- and *trans*-HMA conformers recorded by Woo et al. (*J. Phys. Chem. A* 2005, 109, 10633) are reassigned on the basis of the present electron propagator theory calculations, indicating the significant energy differences between the Dyson orbitals and canonical molecular orbitals due to the electron-correlation and orbital relaxation effects considered in the electron propagator theory. The NBO associated with the natural resonance theory analyses and AIM electron topological study show that the strong  $O^- \cdots HO$  in *cis*-HMA(HB) has the remarkable characteristics of three-center four-electron hyperbond, and the bonding strength of ca. 30 kcal/mol is recommended with the reference calculations of the  $HO^- \cdots HOH$  complex. The further calculations for the microhydrated *cis*-HMA(HB) clusters indicate that the  $O^- \cdots HO$  bonding strength decreases in water solution.

## 1. Introduction

Recently, short-strong hydrogen bonds (SSHBs) attract considerable interest because of their possible role in biological activities, particularly in the enzymatic processes.<sup>1</sup> A typical SSHB, the homonuclear  $O \cdots HO$ , exhibits a short, linear HB with an extremely low barrier for the hydrogen transfer between two oxygen atoms. This SSHB is also noted as the low-barrier HB (LBHB).<sup>2</sup> A lots of studies have been designed to measure or calculate the strength of this strong HB. On the other hand, differing from the intermolecular HB cases in which the strength can be calculated routinely within a supermolecular scheme,<sup>3</sup> it is rather difficult to calculate the intramolecular HB strength directly from the properties of an unit molecule.<sup>4,5</sup> Hydrogen maleate anion (HMA) and diketone enol are good choice both for the experimental<sup>6</sup> and theoretical<sup>4</sup> studies of the intramolecular LBHB, but the reported solutions for the intramolecular HB strength are problematic. As for HMA shown in Figure 1, two *cis* and one *trans* species have been proved to be the low-lying conformers.<sup>4,6</sup> There are arguments on the intramolecular  $O^- \cdots HO$  HB strength and its nature in *cis*-HMA(HB). The HB strength of 0.5–5.5 kcal/mol depending on the solvent used has been estimated by the solvent equilibration experiments of Schwartz and Drueckhammer.<sup>6b</sup> The hydrogen maleate is 20 kcal/mol more stable than fumarate, according to the calculations of Garcia-Viloca et al.<sup>4a</sup> The intramolecular  $O^- \cdots HO$  HB strength in *cis*-HMA(HB) is predicted theoretically to be 14–28 kcal/mol depending on the choices of the reference structures.<sup>4b</sup> In fact, there are several problems in calculating the intramolecular HB strength via comparison with the reference structure. First, the stabilities of the different conformers strongly depend on the intramolecular interactions such as charge-transfer, electrostatic, and steric repulsive interactions among the groups

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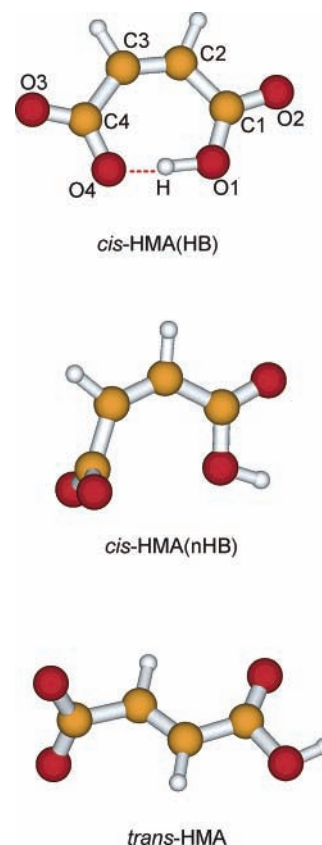


Figure 1. Three low-lying conformers of the hydrogen maleate anions.

in this molecule. Second, the intramolecular HB strength cannot be simply derived by comparison between a conformer with HB and another conformer without HB, due to the fact that the other intramolecular interactions are also different between these

two conformers. At least, one must be circumspective to select the proper reference molecule. Third, although the electrostatic interaction plays role in the normal inter- and intramolecular HBs, the nonelectrostatic contributions, in particular charge-transfer, are also important for the strong intramolecular HB.<sup>4c,5</sup> We have successfully explained that the charge-transfer for the strong intramolecular N $\cdots$ HO HB led to the band splitting in the photoelectron spectrum (PES) of proline.<sup>5a</sup> This method is potentially a solution to estimate the strength of the intramolecular HB.

The anionic intramolecular O $^- \cdots$ HO HB is of particular interest because this asymmetrical HB interaction is suspected to form the symmetrical delocalized three-center four-electron (3c-4e) [O $\cdots$ H $\cdots$ O] $^-$  hyperbond in the valence bond (VB) theory.<sup>4d,e</sup> To elucidate the nature of the remarkably strong intramolecular O $^- \cdots$ HO HB, an experimental photodetachment study of HMA conformers was performed by Woo et al.<sup>7</sup> Their powerful techniques can distinguish certain conformer produced from the corresponding species via the electrospray ionization through the recording of the PES by photodetachment.<sup>7</sup> There were the distinctly different features between *trans*-HMA and *cis*-HMA PES, and the *cis*-HMA(HB) was assigned to the PES on the basis of the adiabatic detachment energy calculations.<sup>7</sup> However, the higher states were not assigned in the PES, due to the seriously overlapped bands.<sup>7</sup> Moreover, the estimation of the intramolecular O $^- \cdots$ HO HB strength  $21.5 \pm 2.0$  kcal/mol by conformational comparison<sup>7</sup> is improper. In this work, we employ the electron propagator theory<sup>8</sup> to predict the photodetachment states for the valence canonical molecular orbitals (MOs) of three low-lying HMA conformers, and make reassignments to the PES. Natural bond orbital (NBO)<sup>9</sup> and atoms-in-molecules (AIM)<sup>10</sup> theorems are utilized to provide insights into the nature of the intramolecular O $^- \cdots$ HO HB in *cis*-HMA(HB).

## 2. Theoretical Methods

Ab initio MO calculations were performed with Gaussian 98 suite of program.<sup>11</sup> The Becke three-parameter hybrid functional combined with Lee–Yang–Parr (LYP) correlation functional (B3LYP)<sup>12</sup> was employed together with 6-311++G(2d,2p) basis set in the calculations. Geometrical parameters of three low-lying HMA conformers, *cis*-HMA(HB) ( $C_s$ -symmetry), *cis*-HMA(nHB) ( $C_s$ -symmetry), and *trans*-HMA ( $C_1$ -symmetry) shown in Figure 1, were fully optimized at the B3LYP/6-311++G(2d,2p) level. The conformations were proved to correspond to the minima on the potential energy surface by the vibrational frequency calculations. The vertical ionization potentials (IP $_v$ s) and electronic property analyses were performed over the optimized geometries.

In contrast to Koopmans' theorem (KT), the energies ( $\epsilon_p$ ) of electron detachment (i.e., IP $_v$  values) correspond to Dyson orbitals,

$$\phi_p(x_i) = \sqrt{N} \int \Psi_N(x_1, x_2, x_3, \dots, x_N) \Psi_{N-1,p}^*(x_2, x_3, x_4, \dots, x_N) dx_2 dx_3 dx_4 \cdots dx_N \quad (1)$$

where  $x_i$  is the space-spin coordinate of electron  $i$ . In the electron propagator formalism,<sup>8</sup>  $\epsilon_p$  can be calculated in a way similar to the self-consistent procedure

$$[F + \sum (\epsilon_p)] \phi_p = \epsilon_p \phi_p \quad (2)$$

where  $F$  is the Fock operator. To overcome the difficulties that the KT frequently predicts the unsatisfied lower IP $_v$  (with 1~2

eV errors), the partial third-order (P3) approximation considering self-energy effect has been introduced.<sup>13</sup> Then the Dyson orbital can be

$$\phi_p = \sqrt{P} \phi_p^{\text{HF}} \quad (3)$$

Here  $P$  is the pole-strength and the off-diagonal elements of the self-energy matrix are omitted.<sup>13</sup>  $\phi_p^{\text{HF}}$  is the canonical (Hartree–Fock) MO wavefunction. In general, the P3 corrections to the KT results are essential in assignments to PES because all orbital relaxation effects between initial and final states are included in the self-energy operator. The average absolute error is ca. 0.2 eV for the IP $_v$  of the organic molecules.<sup>8a,8b,13</sup> In this work, the IP $_v$  values were predicted at the P3/6-311G(2d,2p) level, and the pole strengths were found to be larger than 0.88.

To reveal the nature and bonding strength of the intramolecular HB, the NBO and AIM analyses were made using the B3LYP wave functions. The NBO analysis transfers the delocalized molecular orbitals into the localized ones that are closely tied to chemical bond concepts. Filled NBOs describe the hypothetical, strictly localized Lewis structure. The interaction between filled (lone pair electrons)  $\sigma$  and antibonding  $\sigma^*$  orbitals represents the deviation of the molecule from the Lewis structure and can be used as a measurement of charge-transfer due to the HB interactions. Since the occupancies of filled NBOs are highly condensed, the charge-transfer can be further treated by the second-perturbation energies  $E(2)$

$$E(2) = -n_\sigma \frac{\langle \sigma | F | \sigma^* \rangle^2}{\epsilon_{\sigma^*} - \epsilon_\sigma} = -n_\sigma \frac{F_{ij}^2}{\Delta\epsilon} \quad (4)$$

where  $F_{ij}$  is the Fock matrix element between the NBO  $i$  and  $j$ ,  $\epsilon_\sigma$  and  $\epsilon_{\sigma^*}$  are the energies of  $\sigma$  and  $\sigma^*$  NBOs, and  $n_\sigma$  is the population (it is a lone pair in the HB complex).<sup>9</sup> The topological features of the electron density  $\rho_b$  and its Laplace transform  $\nabla^2 \rho_b$  at the bond critical points (BCPs) were also computed with the Bader's AIM theory.<sup>10</sup> The NBO5.0<sup>14</sup> and AIM2000<sup>15</sup> programs were used in the above calculations.

The above NBO and AIM analyses were performed to reveal the characteristics of the intramolecular O $^- \cdots$ HO HB. Because of the remarkably differences of HMA conformers shown in Figure 1, neither *cis*-HMA(nHB) or *trans*-HMA was a proper reference to predict the O $^- \cdots$ HO HB strength using the method proposed before.<sup>5a</sup> An alternative way was to derive it by the energetic calculations for a candidate system HO $^- \cdots$ HOH, which exhibited similar properties compared with the C=O $^- \cdots$ H–O moiety in *cis*-HMA(HB) (see the following discussion). Thereby, the energetic calculations were further carried out both at the B3LYP and high-level CCSD(T)<sup>16</sup> levels of theory for the HO $^- \cdots$ H $_2$ O complex. The binding energies ( $\Delta E_{\text{bind}}$ ) was calculated by the energy differences between the complex and free monomers

$$\Delta E_{\text{bind}}(\text{ZPVE or TEC}) = E_{\text{tot}}^{\text{complex}} - E_{\text{tot}}^{\text{OH}^-} - E_{\text{tot}}^{\text{H}_2\text{O}} \quad (5)$$

Here the zero-point vibrational energy (ZPVE) or thermal energy correction (TEC) was included. The enthalpy and free energy changes ( $\Delta H$  and  $\Delta G$ ) were also estimated in the similar way. The HB strength ( $\Delta E_{\text{HB}}$ ) was obtained with the energy difference between the complex and the monomers therein

$$\Delta E_{\text{HB}}(\text{BSSE}) = E_{\text{tot}}^{\text{complex}}(\text{complex}) - E_{\text{tot}}^{\text{OH}^-}(\text{complex}) - E_{\text{tot}}^{\text{H}_2\text{O}}(\text{complex}) \quad (6)$$

**TABLE 1: Optimized Geometrical Parameters (Bond Length in Å, Angle in Degree) and the Relative Energies ( $\delta E$  in kcal/mol)**

	<i>cis</i> -HMA(HB)	<i>cis</i> -HMA(nHB)	<i>trans</i> -HMA
$R(\text{O1H})$	1.094	0.965	0.966
$R(\text{C1O1})$	1.306	1.355	1.382
$R(\text{C1O2})$	1.227	1.224	1.217
$R(\text{C1C2})$	1.502	1.457	1.453
$R(\text{C2C3})$	1.340	1.347	1.343
$R(\text{C3C4})$	1.517	1.521	1.517
$R(\text{C4O3})$	1.238	1.248	1.253
$R(\text{C4O4})$	1.281	1.248	1.247
$R(\text{O4}^-\cdots\text{H})$	1.336		
$A(\text{O3C4O4})$	126.0	130.8	130.5
$\delta E$	0.00 <sup>a</sup>	19.47 <sup>a</sup>	14.66 <sup>a</sup>
	0.0 <sup>b</sup>	21.4 <sup>b</sup>	17.3 <sup>b</sup>

<sup>a</sup> This work, B3LYP/6-311++G(2d,2p) + ZPVE corrections. <sup>b</sup> From ref 7, CCSD/aug-cc-pVTZ + ZPVE (B3LYP/aug-cc-pVTZ).

The basis set superposition error (BSSE)<sup>17</sup> was considered by using the whole basis set in the calculations of the total energies of the monomers. To mimic the  $\text{O}^-\cdots\text{HO}$  HB strength of *cis*-HMA(HB) in water solution, the microhydrated clusters *cis*-HMA(HB)-(H<sub>2</sub>O)<sub>*n*</sub> (*n* = 1, 2, 3) were studied and compared with the free *cis*-HMA(HB).

### 3. Results and Discussion

**Ionization Potentials and Assignments to PES.** The geometrical parameters optimized at the B3LYP/6-311++G(2d,2p) level are listed in Table 1. One can find they are extremely close to the values obtained with the aug-cc-pVTZ basis set.<sup>7</sup> The stabilities with respect to the global minimum *cis*-HMA(HB) are 19.47 and 14.66 kcal/mol for *cis*-HMA(nHB) and *trans*-HMA, respectively. These relative energies  $\delta E$  are also in good agreement with the previous results.<sup>4b,7</sup> In *cis*-HMA(HB), the intramolecular HB distance  $R(\text{O4}^-\cdots\text{H})$  is predicted to be 1.336 Å with angle  $A(\text{O4}^-\cdots\text{HO1}) = 177.1^\circ$ , which are comparable with 1.30 Å and  $178.09^\circ$  (MP2/6-31+G(d,p)<sup>4a</sup>), 1.376 Å (QCISD/6-31+G\*\*<sup>4b</sup>), and 1.330 Å and  $176.9^\circ$  (B3LYP/aug-cc-pVTZ<sup>7</sup>). This intramolecular SSHB was regarded as a 3c-4e hyperbond by Gill et al.<sup>4d</sup> We will give the further proves of its hyperbond characteristics in the next section.

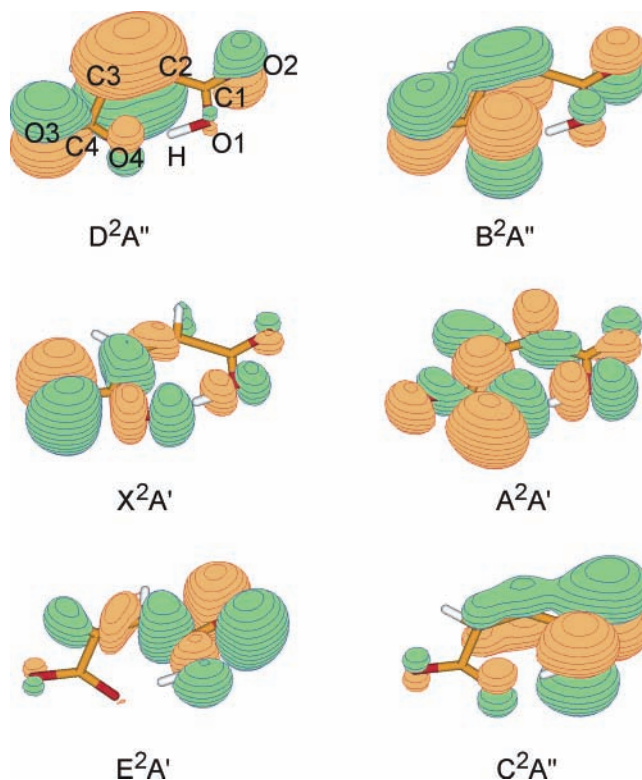
The  $\text{IP}_v$  values obtained from the P3 calculations, together with the KT values, are presented in Table 2. The corresponding experimental data<sup>7</sup> are also shown in Table 2, but the peaks are reassigned according to the present calculations. To our surprise, there are the significant differences for the photodetachment state sequences predicted between the P3 level and the Koopmans' approximation. The valence electron configurations are  $(3a'')^2(23a')^2(24a')^2(25a')^2(4a'')^2(5a'')^2$  for *cis*-HMA(HB),  $(6a'')^2(22a')^2(7a'')^2(8a'')^2$  for *cis*-HMA(nHB), and  $(27a)^2(28a)^2(29a)^2(30a)^2$  for *trans*-HMA. However, their corresponding Dyson orbital sequences are altered remarkably. In the canonical MO energy-level sequences (i.e., the KT sequences), the Dyson orbitals are plotted in Figures 2 and 3 for *cis*-HMA(HB) and *trans*-HMA, respectively. Although it is well-known that the P3 results often produce the different ordering of cationic states with respect to the KT,<sup>8a,8b,13</sup> such differences observed in this work are really profound. This order variance is mostly due to the electron correlation and orbital relaxation included in the P3 method.<sup>13</sup>

In the PES of *cis*-HMA, there is a huge shoulder in the low-energy range 4.9–6.0 eV.<sup>7</sup> The absence of *cis*-HMA(nHB) was proved by the adiabatic IP values calculated at the higher level of theory, namely, 4.26 eV for *cis*-HMA(nHB) and 4.85 eV for *cis*-HMA(HB).<sup>7</sup> The large  $\text{IP}_v$  difference 1.11 eV (5.30–4.19

**TABLE 2: Vertical Detachment Energies (VDEs in eV) Predicted at the P3/6-311G(2d,2p) Level and Within Koopmans' Theorem (KT) in Comparison with the Experimental Data**

assignment <sup>a</sup>	VDE <sub>theor</sub>		VDE <sub>exptl</sub> <sup>b</sup>
	P3	KT	
	<i>cis</i> -HMA(HB), $C_s$ -symmetric		
X <sup>2</sup> A'	5.30	7.17(25a')	(5.19) <sup>c</sup>
A <sup>2</sup> A'	5.60	7.23(24a')	
B <sup>2</sup> A''	5.89	7.00(4a'')	
C <sup>2</sup> A''	6.01	7.83(3a'')	
D <sup>2</sup> A''	6.32	6.70(5a'')	
	<i>cis</i> -HMA(nHB), $C_s$ -symmetric		
X <sup>2</sup> A'	4.19	5.76(22a')	6.31
A <sup>2</sup> A''	4.32	5.46(8a'')	
B <sup>2</sup> A''	4.33	5.55(7a'')	
C <sup>2</sup> A''	6.30	7.08(6a'')	
	<i>trans</i> -HMA, $C_1$ -symmetric		
X <sup>2</sup> A	4.36	5.95(28a)	4.22
A <sup>2</sup> A	4.44	5.53(30a)	(4.51)
B <sup>2</sup> A	4.47	5.70(29a)	4.51
C <sup>2</sup> A	6.23	7.05(27a)	6.23

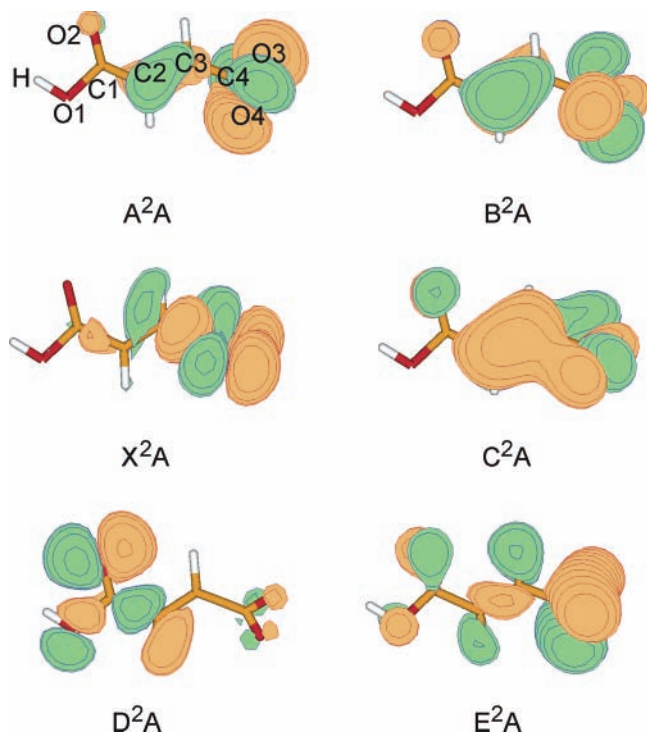
<sup>a</sup> According to the present P3 results. <sup>b</sup> From ref 7. <sup>c</sup> Calculated at the CCSD/aug-cc-pVTZ level in ref 7.



**Figure 2.** Dyson orbitals of *cis*-HMA(HB). The maps are presented from the upper-left to below-right in energy level sequence of the canonical molecular orbitals, with contour plots =  $\pm 0.03$ .

eV for the lowest  $\text{IP}_v$  values) obtained by the P3 method supports this conclusion. Although the band at  $\text{IP}_v \sim 5.7\text{--}6.0$  eV for the higher states cannot be resolved from the spectrum,<sup>7</sup> a plateau around 6.0 eV implies that there may be one or more cationic states. In fact, the P3 calculations predict B<sup>2</sup>A'' (5.89 eV, ionization from 4a'') and C<sup>2</sup>A'' states (6.01 eV, ionization from 3a''). Another state A<sup>2</sup>A' is predicted at 5.60 eV, and correspondingly a shoulder around 5.5 eV can be observed in the PES. D<sup>2</sup>A'' state at 6.32 eV is comfortably close to the experimental  $\text{IP}_v$  6.31 eV. The sharp peak assigned improperly with C state<sup>7</sup> may be due to the serious overlap between C<sup>2</sup>A''



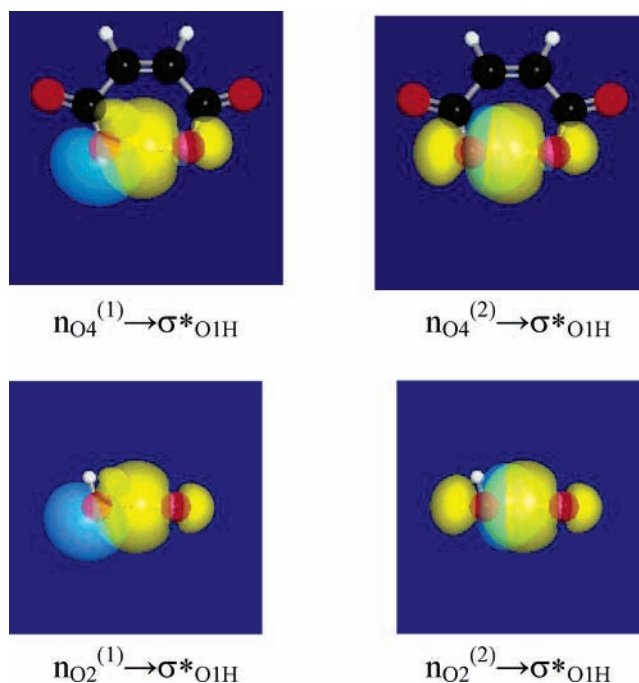


**Figure 3.** Dyson orbitals of *trans*-HMA. The maps are presented from the upper-left to below-right in energy level sequence of the canonical molecular orbitals, with contour plots =  $\pm 0.03$ .

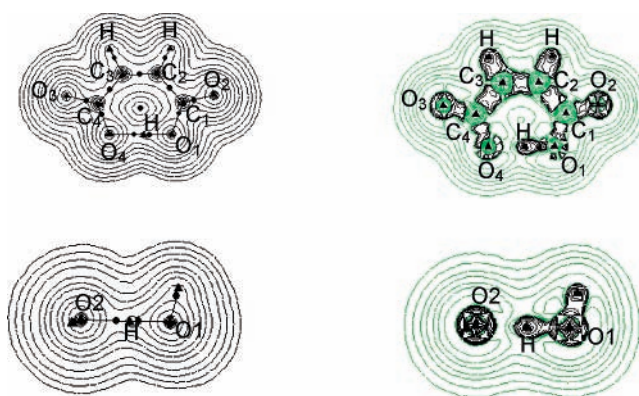
and  $D^2A''$  states predicted by the P3 calculations. Moreover, as shown in Figure 2, these two states can lead to the photodetachment-excited vibrations for the  $C_2=C_3$   $\pi$  orbital, which has been observed in the spectrum.<sup>7</sup>

Four cationic states, X, A (at 4.22 eV), B (at 4.51 eV), and C (at 6.23 eV), were assigned in the PES of *trans*-HMA.<sup>7</sup> They are reassigned precisely according to the present P3 calculations. Namely, they are  $X^2A$  (4.36 eV),  $A^2A$  (4.44 eV),  $B^2A$  (4.47 eV), and  $C^2A$  (6.23 eV), corresponding to the ionizations from the canonical MOs 28a, 30a, 29a, and 27a. Because of the vibrational structures in a range 4.2~5.0 eV, the previous assignments to the PES with A and B states<sup>7</sup> are improper, while three states (X, A, and B) should be assigned. In Figure 3, the Dyson orbitals ( $A^2A$  and  $B^2A$ ) show the predominant electron distributions of  $C_4O_3O_4$  group. This indicates the ionizations should yield the OCO vibrations, as the interpretation given by Woo et al.<sup>7</sup> The present P3 predictions are generally in good agreement the experimental data.

**Hydrogen-Bonding Strength and Electronic Properties of  $O^- \cdots HO$  in *cis*-HMA(HB).** The linear  $O^- \cdots HO$  and the other homonuclear HBs have been investigated both by experiments<sup>6</sup> and theoretical calculations.<sup>4,7</sup> It is interesting that the intramolecular  $O^- \cdots HO$  in *cis*-HMA(HB) was found to depend on the solution polarity. This LBHB becomes a symmetric  $[O \cdots H \cdots O]^-$  HB in a nonpolar solvent.<sup>4a</sup> Moreover, the *cis* conformer was greatly preferred in aprotic solvents while the *trans* conformer was found in protic solvents.<sup>6b</sup> The previous theoretical approaches provide the energetics of the height of the low barrier for the hydrogen transfer,<sup>4a,b,d,e</sup> and the electron topological analyses have been made for insights into the nature of electronic structures.<sup>4a-c</sup> However, it is still a challenge to estimate the intramolecular HB strength. Three typical methods, the conformational analysis,<sup>18</sup> and isodesmic reaction,<sup>19</sup> and the ortho-para comparison<sup>20</sup> methods have been proposed. As for the strong intramolecular  $O^- \cdots HO$  in *cis*-HMA(HB), the strength has been estimated to be 14–28 kcal/mol by the conventional



**Figure 4.** Charge-transfer interactions in *cis*-HMA(HB) (the upper panels) and  $HO^- \cdots HOH$  (the below panels) based on the NBO analyses.  $n_{O4}^{(1)}$  and  $n_{O4}^{(2)}$  denote the lone-pair orbitals of O atom in the different directions respective to OH bond, and  $\sigma^*_{O1H}$  is the antibond.



**Figure 5.** Contour maps of electron density  $\rho$  (the left) and the Laplacian  $\nabla^2\rho$  (the right) of *cis*-HMA(HB) and  $HO^- \cdots HOH$ . The molecular graphs (solid triangles) are superimposed. Lines connecting the nuclei are the bond paths and the small dots along them represent the bond critical points. Green lines denote regions of electronic charge depletion, and black lines denote regions of electronic charge depletion. The contours of the  $\nabla^2\rho$  increase (+)/decrease (-), respectively, from the zero contour in the order  $\pm 2 \times 10^{-n}$ ,  $\pm 4 \times 10^{-n}$ ,  $\pm 8 \times 10^{-n}$ , with  $n$  beginning from 3 and decreasing in steps of unity. The same set of contours is used through all figures.

conformational analyses.<sup>4,7</sup> The problem of this method is that only the normal electrostatic interaction is stressed, while an additional covalent interaction energy should be considered<sup>4c</sup> for the LBHBs and SSHBs with the polar covalent bonding characteristics.<sup>6b</sup> A proper reference system,  $HO^- \cdots HOH$ , is selected to estimate the intramolecular HB strength of *cis*-HMA(HB), because these two HB moieties are extremely similar. First, the HB length  $O^- \cdots H$  in  $HO^- \cdots H_2O$  is 1.436 Å predicted at the B3LYP/6-311++G(2d,2p) level, which is close to that in *cis*-HMA(HB). Second, the natural atomic populations of the HB moieties indicate that the negative unit charge is mostly embedded on  $C_4O_3O_4$  group in *cis*-HMA(HB) or O2H radical in the  $HO^- \cdots H_2O$  complex. Third, as shown in Figures 4 and 5 and Tables 3–5, the hyperconjugative interactions, bonding

**TABLE 3: Hyperconjugative Interaction Energies of *cis*-HMA(HB) and HO<sup>-</sup>⋯HOH**

	NBO Analysis			E(2) (kcal/mol)
	charge-transfer <sup>a</sup>	$\delta\epsilon(\text{au})$	$F_{ij}(\text{au})$	
<i>cis</i> -HMA(HB)				
B3LYP/6-311G(2d,2p)	$n_{\text{O}4^{(1)}} \rightarrow \sigma_{\text{O}1\text{H}}^*$	0.90	0.085	9.35
	$n_{\text{O}4^{(2)}} \rightarrow \sigma_{\text{O}1\text{H}}^*$	0.71	0.241	100.56
B3LYP/6-311++G(2d,2p)	$n_{\text{O}4^{(1)}} \rightarrow \sigma_{\text{O}1\text{H}}^*$	0.92	0.087	9.58
	$n_{\text{O}4^{(2)}} \rightarrow \sigma_{\text{O}1\text{H}}^*$	0.72	0.242	99.85
HO <sup>-</sup> ⋯HOH				
B3LYP/6-311++G(2d,2p)	$n_{\text{O}2^{(1)}} \rightarrow \sigma_{\text{O}1\text{H}}^*$	0.94	0.071	6.17
	$n_{\text{O}2^{(2)}} \rightarrow \sigma_{\text{O}1\text{H}}^*$	0.72	0.247	105.14

<sup>a</sup> See discussion in text and Figure 4.**TABLE 4: Natural Bond Orders in *cis*-HMA(HB) and HO<sup>-</sup>⋯HOH**

<i>cis</i> -HMA	O1H	O4 <sup>-</sup> ⋯H
B3LYP/6-311G(2d,2p)		
total	0.582	0.314
covalent	0.211	0.068
ionic	0.372	0.246
B3LYP/6-311++G(2d,2p)		
total	0.575	0.323
covalent	0.206	0.068
ionic	0.368	0.256
HO2 <sup>-</sup> ⋯HO1H	O1H	O2 <sup>-</sup> ⋯H
B3LYP/6-311++G(2d,2p)		
total	0.620	0.379
covalent	0.206	0.080
ionic	0.414	0.299

indexes, and electron densities are extremely similar for these two HB moieties. Basically, the strong hyperconjugative interaction energies (99.85 kcal/mol for *cis*-HMA(HB) and 105.14 kcal/mol for HO<sup>-</sup>⋯H<sub>2</sub>O) of  $n_{\text{O}} \rightarrow \sigma_{\text{OH}}^*$  and the high  $\rho_{\text{b}}$  values (0.1210 au for *cis*-HMA(HB) and 0.1176 au for HO<sup>-</sup>⋯H<sub>2</sub>O) at the BCPs indicate these two HBs have comparable strengths. Thereby, it is reasonable to estimate the intramolecular HB strength in *cis*-HMA(HB) using the similar one in HO<sup>-</sup>⋯H<sub>2</sub>O.

$\Delta E_{\text{bind}}(\text{ZPVE})$ ,  $\Delta E_{\text{bind}}(\text{TEC})$ ,  $\Delta H_{\text{bind}}$ ,  $\Delta G_{\text{bind}}$ , and  $\Delta E_{\text{HB}}(\text{BSSE})$  values calculated according to eqs 5 and 6 are given in Table 6.  $\Delta E_{\text{HB}}(\text{BSSE})$  values obtained at the B3LYP and CCSD(T) levels of theory are a little larger than the previously reported data. Here we recommend that the HB strength of O<sup>-</sup>⋯HO in *cis*-HMA(HB) is about 30 kcal/mol. In the proline conformers, the strong intramolecular N⋯HO HB leads to the high IP<sub>v</sub> value of the canonical highest-occupied MO having the predominant lone-pair of N atom.<sup>5a</sup> In that work, the N⋯HO HB strength can be derived from the IP<sub>v</sub> value difference between the conformers with and without the N⋯HO HB, because those two conformers are extremely similar

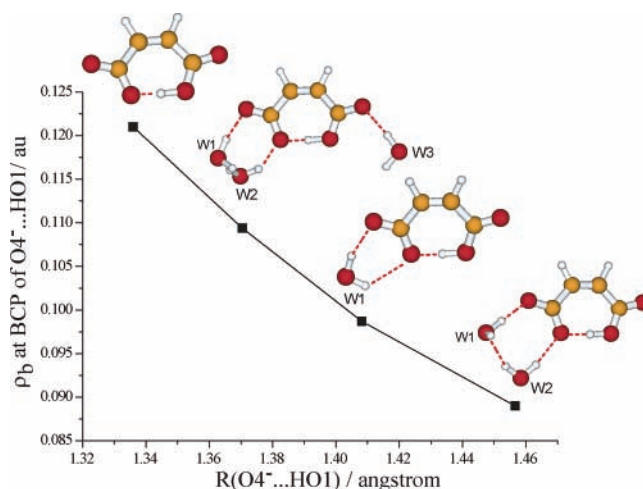
**TABLE 5: Topological Properties in (au) of the Electronic Charge Density in the BCPs of *cis*-HMA(HB) and HO<sup>-</sup>⋯HOH Predicted at the B3LYP/6-311++G(2d,2p) Level<sup>a</sup>**

bond	$\rho_{\text{b}}$	$\nabla^2\rho_{\text{b}}$	$\lambda_1$	$\lambda_2$	$\lambda_3$	$G_{\text{b}}$	$V_{\text{b}}$	$e$	$ \lambda_1/\lambda_3 $	$G_{\text{b}}/\rho_{\text{b}}$	$ V_{\text{b}}/G_{\text{b}} $
<i>cis</i> -HMA(HB)											
O1H	0.2428	-1.2388	-1.0241	-1.0115	0.7968	0.0894	-0.3991	0.0125	1.2853	0.3682	4.4642
O4 <sup>-</sup> ⋯H	0.1210	0.0318	-0.3308	-0.3249	0.6875	0.0784	-0.0705	0.0182	0.4812	0.6479	0.8992
HO2 <sup>-</sup> ⋯HO1H											
O1H	0.2204	-0.9406	-0.8669	-0.8481	0.7744	0.0849	-0.3201	-0.2352	1.1194	0.3852	3.7703
O2 <sup>-</sup> ⋯H	0.1176	0.0162	-0.3122	-0.3040	0.6324	0.0712	-0.0671	0.0041	0.4937	0.6054	0.9424

<sup>a</sup> See text for the explanation of symbols.**TABLE 6: Energies of the Hydrogen-Bonding Complex HO<sup>-</sup>⋯HOH Used To Simulate the Intramolecular Hydrogen-Bonding Interaction in *cis*-HMA(HB)<sup>a</sup>**

	B3LYP	CCSD(T)
$\Delta E_{\text{bind}}(\text{ZPVE})^a$	28.35	26.94
$\Delta E_{\text{bind}}(\text{TEC})^b$	28.98	27.57
$\Delta H_{\text{bind}}$	29.58	28.16
$\Delta G_{\text{bind}}$	22.11	20.73
$\Delta E_{\text{HB}}(\text{BSSE})^c$	38.85	30.89

<sup>a</sup> Including the zero-point vibrational energy (ZPVE) correction. <sup>b</sup> Including the thermal energy correction ( $T = 298.15$  K). <sup>c</sup> Including the superposition basis set error (BSSE) correction.

**Figure 6.** Plot of the electron density  $\rho_{\text{b}}$  at BCP in terms of the O4<sup>-</sup>⋯HO1 hydrogen bond length to simulate the solution effect for *cis*-HMA(HB).

in structures except for the HBs.<sup>5a</sup> However, it is unfeasible that the O<sup>-</sup>⋯HO bonding strength in *cis*-HMA(HB) 21.6 kcal/mol was obtained according to the adiabatic IP difference between the trans/cis conformers or 21.4 kcal/mol from the relative stability energy between *cis*-HMA(HB) and *cis*-HMA(nHB).<sup>7</sup> The internal COO<sup>-</sup> group rotations in HMA should yield the great changes of the other intramolecular interactions, e.g., steric-repulsive, electrostatic interactions, etc. As for the intramolecular N⋯HO HB strength in proline,<sup>5a</sup> two similar conformers having the same pyrrolidine puckering ring, i.e., Ia and IIa, or Ib and IIb, are selected; thus, the conformational analysis method is reliable in that case.

To elucidate the solvent effects on this HB strength which has been observed by Schwartz and Drueckhammer,<sup>6b</sup> the microhydrated *cis*-HMA(HB) clusters are studied in this work. In Figure 6, the  $\rho_{\text{b}}$  values at the BCPs of O<sup>-</sup>⋯HO are distinctly different in the various clusters. Moreover, the O<sup>-</sup>⋯HO HB lengths are sensitive to the hydrated positions around *cis*-HMA(HB). The intermolecular HB interactions between two water molecules (w1 + w2) and the COO<sup>-</sup> group result in the significant elongation of O<sup>-</sup>⋯HO HB length. In general, the





- (2) (a) Frey, P. A.; Whitt, S. A.; Tobin, J. B. *Science* **1994**, *264*, 1972. (b) Cleland, W. W.; Kreevoy, M. M. *Science* **1995**, *269*, 104. (c) Frey, P. A. *Science* **1995**, *269*, 104. (d) Lin, J.; Frey, P. A. *J. Am. Chem. Soc.* **2000**, *122*, 11258.
- (3) (a) Scheiner, S. *Hydrogen Bonding*; Oxford University Press: New York, 1997. (b) Steiner, T. *Angew. Chem., Int. Ed. Engl.* **2002**, *41*, 48. (c) Hobza, P.; Havlas, Z. *Chem. Rev.* **2000**, *100*, 4253.
- (4) (a) Garcia-Viloca, M.; Gonzalez-Lafont, A.; Lluch, J. M. *J. Am. Chem. Soc.* **1997**, *119*, 1081. (b) Bach, R. D.; Dmitrenko, O.; Glukhovstev, M. N. *J. Am. Chem. Soc.* **2001**, *123*, 7134. (c) Schiøtt, B.; Iversen, B.; Madsen, G. K. H.; Larsen, F. K.; Bruice, A. T. *Proc. Natl. Acad. Sci. U.S.A. (PNAS)* **1998**, *95*, 12799. (d) Gilli, P.; Bertolasi, V.; Ferretti, V.; Gilli, G. *J. Am. Chem. Soc.* **1994**, *116*, 909. (e) Gilli, P.; Bertolasi, V.; Ferretti, V.; Gilli, G. *J. Am. Chem. Soc.* **2004**, *126*, 3845. (f) McAllister, M. A. *Can. J. Chem.* **1997**, *75*, 1195.
- (5) (a) Tian, S. X.; Yang, J. *Angew. Chem., Int. Ed.* **2006**, *45*, 2069. (b) Tian, S. X. *J. Phys. Chem. A* **2006**, *110*, 3961. (c) Tian, S. X. *J. Chem. Phys.* **2005**, *123*, 24310.
- (6) (a) Perrin, C. L.; Thoburn, J. D. *J. Am. Chem. Soc.* **1992**, *114*, 8559, and references cited therein. (b) Schwartz, B.; Drueckhammer, D. G. *J. Am. Chem. Soc.* **1995**, *117*, 11902.
- (7) Woo, H.-K.; Wang, X.-B.; Wang, L.-S.; Lau, K.-C. *J. Phys. Chem. A* **2005**, *109*, 10633.
- (8) (a) Ortiz, J. V.; Zakrzewski, V. G. *J. Chem. Phys.* **1996**, *105*, 2762. (b) Ferreira, A. M.; Seabra, G.; Dolgounitcheva, O.; Zakrzewski, V. G.; Ortiz, J. V. In *Quantum-Mechanical Prediction of Thermochemical Data*; Cioslowski, J. Ed.; Kluwer: Dordrecht, The Netherlands, 2001; p131. (c) Linderberg, J.; Öhrn, Y. *Propagators in Quantum Chemistry*; Academic Press: New York, 1973.
- (9) Reed, A.; Curtiss, L. A.; Weinhold, F. *Chem. Rev.* **1988**, *88*, 899.
- (10) Bader, R. F. W. *Atoms in Molecules: A Quantum Theory*; Clarendon: Oxford, U.K., 1990.
- (11) Frisch, M. J.; Trucks, G. W.; Schlegel, H. B.; Scuseria, G. E.; Robb, M. A.; Cheeseman, J. R.; Zakrzewski, V. G.; Montgomery, J. A., Jr.; Stratmann, R. E.; Burant, J. C.; Dapprich, S.; Millam, J. M.; Daniels, A. D.; Kudin, K. N.; Strain, M. C.; Farkas, O.; Tomasi, J.; Barone, V.; Cossi, M.; Cammi, R.; Mennucci, B.; Pomelli, C.; Adamo, C.; Clifford, S.; Ochterski, J.; Petersson, G. A.; Ayala, P. Y.; Cui, Q.; Morokuma, K.; Malick, D. K.; Rabuck, A. D.; Raghavachari, K.; Foresman, J. B.; Cioslowski, J.; Ortiz, J. V.; Baboul, A. G.; Stefanov, B. B.; Liu, G.; Liashenko, A.; Piskorz, P.; Komaromi, I.; Gomperts, R.; Martin, R. L.; Fox, D. J.; Keith, T.; Al-Laham, M. A.; Peng, C. Y.; Nanayakkara, A.; Gonzalez, C.; Challacombe, M.; Gill, P. M. W.; Johnson, B.; Chen, W.; Wong, M. W.; Andres, J. L.; Gonzalez, C.; Head-Gordon, M.; Replogle, E. S.; Pople, J. A. *GAUSSIAN 98*; Gaussian, Inc.: Pittsburgh, PA, 1998.
- (12) (a) Becke, A. D. *J. Chem. Phys.* **1993**, *98*, 5648. (b) Lee, C.; Yang, W.; Parr, R. G. *Phys. Rev. B* **1988**, *41*, 785.
- (13) Ortiz, J. V. *J. Chem. Phys.* **1996**, *104*, 7599.
- (14) Glendening, E. D.; Badenhop, J. K.; Reed, A. E.; Carpenter, J. E.; Bohmann, J. A.; Morales, C. M.; Weinhold, F. *NBO 5.0*; Theoretical Chemistry Institute: University of Wisconsin, Madison, WI, 2001.
- (15) *AIM 2000: A Program to Analyze and Visualize Atoms in Molecules*; <http://www.aim2000.de/>.
- (16) (a) Pople, J. A.; Krishnan, R.; Schlegel, H. B.; Binkley, J. S. *Int. J. Quantum Chem.* **1978**, *15*, 545. (b) Scuseria, G. E.; Schaefer, H. F. III *J. Chem. Phys.* **1989**, *90*, 3700.
- (17) Boys, S. F.; Bernardi, F. *Mol. Phys.* **1970**, *19*, 553.
- (18) (a) Kovacs, A.; Szabo, A.; Hargittai, I. *Acc. Chem. Res.* **2002**, *35*, 887. (b) Zhang, H.-Y.; Sun, Y.-M.; Wang, X.-L. *Chem.—Eur. J.* **2003**, *9*, 502.
- (19) (a) Rozas, I.; Alkorta, I.; Elguero, J. *J. Phys. Chem. A* **2001**, *105*, 10462. (b) Pratt, D. A.; de Heer, M. I.; Mulder, P.; Ingold, K. U. *J. Am. Chem. Soc.* **2001**, *123*, 5518.
- (20) Estacio, S. G.; do Couto, P. C.; Cabral, B. J. C.; da Piedade, M. E. M.; Simoes, J. A. M. *J. Phys. Chem. A* **2004**, *108*, 10834.
- (21) Coulson, C. A. *J. Chem. Soc.* **1964**, 1442.
- (22) (a) Glendening, E. D.; Weinhold, F. *J. Comput. Chem.* **1998**, *19*, 593. (b) Glendening, E. D.; Weinhold, F. *J. Comput. Chem.* **1998**, *19*, 610. (c) Glendening, E. D.; Badenhop, J. K.; Weinhold, F. *J. Comput. Chem.* **1998**, *19*, 628.
- (23) Tian, S. X. *J. Phys. Chem. B* **2004**, *108*, 20388.
- (24) Koch, U.; Popelier, P. L. A. *J. Phys. Chem.* **1995**, *99*, 9747.
- (25) As for the OH bond in methanol,  $\rho_b = 0.3778$  au,  $\nabla^2\rho_b = -2.7066$  au,  $|\lambda_1|/\lambda_3 = 1.9838$ , and  $|\lambda_1|/\lambda_3 > 1$ ,  $G_b/\rho_b = 0.2149$  au at the BCP are obtained by the B3LYP/6-311+G(2d,2p) calculations.