# Linear $C_n$ Clusters: Are They Acetylenic or Cumulenic?

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Uncapped linear  $C_n$  clusters have been studied with hybrid density functional theory focusing on the geometry, HOMO–LUMO gap, and the longitudinal optical (LO) vibrational mode. The latter two correlate well with the bond length alternation (BLA) of the optimized geometry. Due to end effects, the BLA is not constant along the chains. The degree of BLA changes continuously with increasing *n*: starting with essentially nonalternating structures (cumulenic), then turning into strongly alternating (acetylenic) structures. This transition has not yet been described or characterized and occurs at relatively large values of *n*. The implications for the widely observed characteristic LO vibrational bands of linear carbon clusters are discussed.

## 1. Introduction

Carbyne, the hypothetical linear allotrope of carbon, has attracted some interest both experimentally and among theorists.<sup>1–3</sup> It is an infinite chain formed exclusively by sp-hybridized carbon atoms,  $C_{\infty}$ . Therefore, it is often called the fourth allotrope of carbon, after diamond, graphite, and fullerenes and nanotubes.

From the perspective of formal chemical valence, two forms of infinite carbon chains might exist based on the degenerate pair of  $\pi$  orbitals on each carbon atom oriented perpendicular to the chain axis: *polycumulene*, (=C=)<sub>∞</sub>, an equidistant carbon chain and *polyyne*, (-C=C-)<sub>∞</sub>, which features a single-triple bond alternating pattern. All solid-state calculations<sup>4-10</sup> indicate that polyyne is more stable than polycumulene, because the latter has a degenerate pair of half-filled energy bands which are subject to Peierls distortion.<sup>11</sup> So do the oligomer methods by extrapolating properties from a series of finite carbon chain oligomers, to the infinite size limit.<sup>12</sup>

Linear  $C_n$  (*n* is finite) clusters are abundant in the interstellar clouds<sup>13–17</sup> and have been extensively studied in the laboratory.<sup>18–32</sup> It is generally understood that linear  $C_n$  (even or odd) carbon chains possess the cumulenic geometry with nearly equivalent bond lengths, as opposed to the possible acetylenic geometry with appreciable bond length alternation (BLA).<sup>24</sup> This is clearly in contrast to the acetylenic geometry found in the infinite linear carbon chain,  $C_{\infty}^{4-10}$  and in finite end-capped carbon chains.<sup>12,33</sup> In addition, discrepancies can also be found for other associated properties, such as the HOMO–LUMO gap ( $E_g$ ), and the characteristic bond stretching frequency of carbon chains. We will show that in these cases, one cannot predict the properties of  $C_{\infty}$  based on the extrapolation from short- and medium-sized  $C_n$  chains found in the literature.

In this work, we report theoretical investigations on the geometric and vibrational properties of uncapped linear  $C_n$  clusters, with the aim at finding the transition from the cumulenic short chains to the strongly alternating polymer,  $C_{\infty}$ . Implications for the important longitudinal optical Raman bands of linear carbon clusters are discussed. We show in this paper that the transition from a cumulenic (essentially nonalternating) structure to an alternating one occurs for relatively long chains.

The transition from the essentially nonalternating (cumulenic) form to the alternating (acetylenic) form occurs because of the Peierls driving force that becomes more and more pronounced as the chain length is increased.

## 2. Computational Details

All molecular and periodic boundary condition (PBC) calculations are carried out using the Gaussian03 program,<sup>34</sup> *except* for the frequency calculations of the infinite carbon chains, which were done with the PWSCF program.<sup>35</sup>

Due to the notorious basis set linear dependency problem<sup>36–40</sup> for carbon chains,<sup>6,9</sup> PBC calculations on the infinite carbon chain with adequate Gaussian-type basis sets can only be done at nonhybrid density functional theory (DFT) levels. On the other hand, in programs using plane wave basis sets, PBC codes for Hartree-Fock (HF) and hybrid DFT methods are not available. Therefore, with the reliable basis sets such as 6-31G\* or plane wave basis sets, both PBC calculations and oligomer extrapolation results are only available for pure DFT methods, including local density approximation (LDA) and generalized gradient-corrected approximation (GGA) levels. At these levels, we have shown that the oligomer extrapolation approach using hydrogen-capped polyyne oligomers (oligoynes,  $H-(C \equiv C)_m$ -H), agrees well with PBC results for BLA and gap for polyyne.<sup>41</sup> This validates the oligomer extrapolation approach based on end-capped oligoynes.

We used a few standard theoretical levels deemed reliable for carbon based systems, including HF, nonhybrid DFT, hybrid DFT, second-order Møller–Plesset perturbation theory (MP2), and CCSD(T) coupled cluster calculations. 6-31G\* basis sets are used as the standard Gaussian-type basis set, except that Dunning's correlation consistent triple- $\zeta$  basis sets (cc-pVTZ)<sup>42</sup> are used with CCSD(T). STO-3G and 3-21G basis sets are also used in some calculations where qualitative results are needed on extremely long carbon chains. In the PWSCF calculations on C<sub>∞</sub>, 327 eV cutoff energy for carbon and 73 irreducible *k* points are adopted.

#### 3. Results and Discussion

**3.1. Geometry of the Infinite Carbon Chain C**<sub>60</sub>. Consistent with literature results,<sup>4–12</sup> our PBC calculations at LDA and

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**Figure 1.** Bond lengths of linear  $C_n$  (n = 2-8) molecules in their ground states (singlet:  $C_2$ ,  $C_3$ ,  $C_5$ ,  $C_7$ ; triplet:  $C_4$ ,  $C_6$ ,  $C_8$ ), in angstroms. B3LYP/6-31G\*, CCSD(T)/cc-pVTZ, and available experimental results (ref 45 for  $C_2$  and ref 46 for  $C_3$ ) are listed from top to bottom, in plain, italic, and bold styles, respectively.

 TABLE 1: Relative Stability of Polyyne and Polycumulene Per C2 Unit at Various Theoretical Levels with Periodic Boundary Condition Calculations

theory	LDA/6-31G*	PBE/6-31G*	B3LYP/STO-3G
polycumulene (a.u.)	-75.7083554	-76.0717107	-75.2027478
polyyne (acetylenic form) (a.u.)	-75.7083909	-76.0717723	-75.2060947
$\Delta E$ (polyyne-polycumulene) (kcal/mol)	-0.02	-0.04	-2.10

GGA-PBE level with the 6-31G\* basis sets show that polyyne with alternating triple—single bond geometry is slightly more stable than the equidistant polycumulene geometry. The energy differences are listed in Table 1. Theoretical prediction for the energy difference values varies significantly with the levels of theory. With the more accurate Becke's three-parameter hybrid density functional scheme (B3)<sup>43</sup> in the form of B3LYP, but with minimum Gaussian-type basis sets, the energy difference is qualitatively larger at 2.10 kcal/mol per C<sub>2</sub>, which is also listed in Table 1. With the ab initio G3 theory and the oligomer extrapolation approach on linear chains including up to 10 carbon atoms, Rodriguez et al. predicted that polyyne is 3.8 kcal/mol per C<sub>2</sub> more stable than polycumulene.<sup>12</sup>

The vibrational calculations for the equidistant polycumulene at the GGA-PBE level with the PWSCF program gave an imaginary frequency at 2237i cm<sup>-1</sup> at  $\Gamma$  point corresponding to the longitudinal optical stretching mode. The same mode has a real frequency at 1155 cm<sup>-1</sup> for polyyne at the same theoretical level. This implies that the hypothetical polycumulene structure is actually a saddle point on the potential energy surface of linear  $C_{\infty}$ . As expected by the Peierls theorem, there is only one minimum for the infinite carbon chain, which is the bond alternating polyyne that has a significant band gap.

**3.2. Geometry and Gap of Linear**  $C_n$  **Chains.** As opposed to the single-triple bond alternating (acetylenic) geometry of the infinite carbon chain,  $-(C \equiv C)_{\infty}$ -, shorter linear  $C_n$  chains have been predicted to have the cumulenic geometry, (: $C \equiv C \equiv \cdots \equiv C \equiv C$ :).<sup>24</sup> This is the case for both even- and odd-numbered linear carbon clusters, despite the fact that  $C_n$  chains possess a singlet ground state  ${}^{1}\Sigma_{g}^{+}$  when *n* is odd, or a triplet ground stated  ${}^{3}\Sigma_{g}^{-}$  when *n* is even, with the only exception in C<sub>2</sub> which is a singlet in the ground state.<sup>18,24</sup>

The B3LYP/6-31G\* theoretical level is used in this work for the prediction of the geometry of  $C_n$  chains. The only problem with the B3LYP theory is that it incorrectly predicts the ground state of  $C_2$  to be the triplet, but this error also occurs with other hybrid and nonhybrid DFT theories, in addition to HF and MP2. Multiconfiguration reference methods or coupled cluster methods are needed for the correct prediction of the ground state of  $C_2$ .<sup>18,24</sup> Since we are aiming at the evolution of the properties of linear  $C_n$  with size n, and the connection between  $C_n$  and  $C_{\infty}$ , this deficiency does not affect our study. Figure 1 shows that for the ground state geometry of  $C_n$  (n = 2-8), B3LYP/  $6-31G^*$  predictions agree well with our presented and with earlier<sup>44</sup> CCSD(T)/cc-pVTZ calculations and available experimental data.<sup>45,46</sup> This justifies our selection.

We did a series of geometry optimization calculations at the B3LYP/6-31G\* level on  $C_n$ , with *n* ranging from 2 to 64. Aside from the end effects, we also found equidistant cumulenic geometries for various small- and medium-sized even-numbered  $C_n$  chains with *n* ranging up to 40 and for all odd-numbered  $C_n$ in this study with n up to 63. This is consistent with literature results.<sup>24</sup> The geometry of C<sub>40</sub> is shown in Figure 2 as a representative example for an even-numbered linear carbon cluster, and that of  $C_{63}$  is shown in Figure 3 as a representative for an odd-numbered linear carbon cluster. There are clearly two series of bonds alternating along a  $C_n$  chain: the longer bonds and the shorter bonds. The only exceptions occur at the two ends of the chain where the first two bonds belong to the longer series. This is due to the strong valence deficiency at the two ends of the chain, which significantly elongates the first two C-C bonds. For the majority of the C-C bonds along the chains, the BLA (bond length differences between adjacent



**Figure 2.** Bond length of all the C–C bonds along the linear  $C_{40}$  chain at the B3LYP/6-31G\* level. "i" is numbered starting from one end to the other.



**Figure 3.** Bond length of all the C–C bonds along the linear  $C_{63}$  chain at the B3LYP/6-31G\* level. "i" is numbered starting from one end to the other.



**Figure 4.** Bond length of all the C–C bonds along the linear  $C_{52}$  chain at the B3LYP/6-31G\* level. "i" is numbered starting from one end to the other.

bonds) is less than 0.02 Å. For odd-numbered  $C_n$ , the BLA in the middle is zero by symmetry. Both  $C_{40}$  and  $C_{63}$  are essentially cumulenic, rather than acetylenic.

For the even-numbered carbon chain series starting with  $C_{48}$ , the BLA first decreases from one end toward the middle of the chain; then it slightly increases near the middle. This transition to an alternating middle section is slightly more visible in  $C_{52}$ as shown in Figure 4. As *n* further increases, the alternating character becomes dominant.  $C_{52}$  is near the changeover from the cumulenic character preferred by the end effect in linear  $C_n$ chains and the acetylenic character stabilized by the Peierls distortion in very long or infinite carbon chains. The geometry of a typical longer alternating  $C_n$  chain is shown in Figure 5 with  $C_{64}$  as an example. Beyond the crucial chain length, the oligomer extrapolation approach can be applied to predict the properties of  $C_{\infty}$ . This radical change of the geometry with increasing *n* establishes the link between the geometry of long linear  $C_n$  chains and  $C_{\infty}$  which was mentioned in the Introduction



**Figure 5.** Bond length of all the C–C bonds along the linear  $C_{64}$  chain at the B3LYP/6-31G\* level. "i" is numbered starting from one end to the other.



**Figure 6.** Bond length alternation pattern along various linear  $C_{2m}$  clusters at the B3LYP/6-31G\* level, with 2m = 16, 24, 32, 40, 52, 56, and 64, are selectively shown. All chains are centered on the vertical dotted line. "j" is the bond numbered from the center.

and also explains why extrapolations from shorter chains to the infinite chain should not be pursued for these systems.

The bond length alternation pattern changes along an evennumbered  $C_n$  (n = 2m) chain and between different  $C_{2m}$  clusters are illustrated in Figure 6. The cumulenic to acetylenic transition is predicted to occur at about n = 48-52. Accompanying the geometric transition from the cumulenic structure of short C<sub>2m</sub> to the acetylenic character for long  $C_{2m}$ , the electronic and vibrational properties of C<sub>2m</sub> also undergo fundamental changes. B3LYP/6-31G\* calculations on the properties of long  $C_{2m}$  chains are limited by the strong linear dependency problems known for this system<sup>6,9</sup> and by the computational resources. To reveal properties at longer C<sub>2m</sub> region qualitatively with smaller basis sets, we did a basis set convergence study. Figure 7 shows how, with three different basis sets, the bond length alternation at the center of  $C_{2m}$  varies with the size 2m. The predicted geometric differences between 6-31G\* and 3-21G are very small, implying that 3-21G basis sets might be sufficient for the systems under study. B3LYP with the STO-3G minimum



**Figure 7.** Dependence of the bond length alternation at the center of even-numbered linear  $C_n$  clusters with the cluster size n = 2m.



**Figure 8.** HOMO–LUMO gap of linear  $C_n$  clusters changes with size n = 2m.

basis set predicts this geometric transition only qualitatively. The transition in Figure 7 is around 2m = 30 at B3LYP/STO-3G level, compared with 2m = 52 predicted with 3-21G and 6-31G\* basis sets.

The HOMO-LUMO gap ( $E_g$ ) of conjugated systems is strongly correlated with the degree of BLA.<sup>4,11</sup> The consequence of this relationship leads to a changeover of the gap as a function of increasing chain size: first a decreasing gap of the nonalternating chains and, then, a sudden rise of the gap as the alternation develops in longer chains. The gap value of longer linear C<sub>2m</sub> clusters approaches that of the infinite alternating chain<sup>41</sup> as 2m increases. This crossover is shown in Figure 8 for various C<sub>2m</sub> chains. The three different basis sets behave similarly as in the BLA versus 2m curve. Again, B3LYP/STO-3G predicts that the cumulenic-acetylenic transition occurs at 2m = 30, earlier than that happens with 3-21G and 6-31G\* basis sets (2m = 52). The predicted gap with B3LYP/STO-3G is larger than B3LYP/3-21G and B3LYP/6-31G\*, mostly due to the larger BLA predicted by the minimum basis set.

**3.3. Differences between Even and Odd Linear**  $C_n$  **Clusters.** For the odd-numbered  $C_n$  series, the geometry remains cumulenic for all the chains studied at the B3LYP/6-31G\* level with *n* up to 63 and at B3LYP/3-21G level with *n* up to 75. B3LYP calculations with STO-3G basis sets are performed to



**Figure 9.** Bond length of all the C–C bonds along the linear  $C_{131}$  chain at the B3LYP/STO-3G level. "i" is numbered starting from one end to the other. The two dashed lines represent the bond length values of polyyne from periodic boundary condition calculations at the same level.



Figure 10. Longitudinal optical (LO) mode of alternating carbon chains.

qualitatively investigate the possible cumulenic-acetylenic transition in longer odd linear carbon chains. Although cumulenic geometry is still dominant for odd-numbered  $C_n$  with n up to 59 at the B3LYP/STO-3G level, acetylenic character is found to emerge as n increases to 63. This transition n value is about doubled compared with the transition point at around  $C_{30}$ for even-numbered carbon clusters at the same theoretical level. This is because for odd  $C_n$  the two ends of the chain possess the cumulenic geometry due to the end effect, and the center of the chain is also equidistant by symmetry. As a result, an oddnumbered  $C_n$  is essentially divided into two halves of evennumbered clusters. The cumulenic to acetylenic transition occurs at the center of *both* halves when *n* is large enough to overcome the end effect of  $C_n$ . In other words, acetylenic character starts to grow near the one-quarter and three-quarter points of the original  $C_n$  chain. Therefore, it is reasonable to estimate that at the B3LYP/6-31G\* level, the cumulenic-acetylenic transition in odd-numbered carbon clusters will be reached at twice of the transition size for the even-numbered clusters: in the n =96-104 region.

With PBC calculations at the B3LYP/STO-3G level, the short and long bonds of polyyne are predicted to be 1.240 and 1.360 Å, respectively, and the BLA is 0.120 Å. Figure 9 shows that the convergency of odd-numbered  $C_n$  to the polymer limit is already achieved in  $C_{131}$  at the B3LYP/STO-3G level. As can be expected, the convergency is reached about 2 times faster at the same theoretical level for even-numbered  $C_n$  as previously shown in Figure 7.

**3.4. Vibrational Properties of Linear Carbon Clusters.** There is a well-known connection between bond length alternation and the longitudinal carbon–carbon bond stretching modes in linear carbon chains.<sup>8,47</sup> For the bond length alternating polyyne, there is only one Raman-active bond stretching mode which is called the longitudinal optical (LO) mode, as shown in Figure 10. This is an all in-phase stretching mode for all short bonds and for all long bonds. This mode is enhanced as



**Figure 11.** Longitudinal optical (LO) mode frequencies of short linear  $C_n$  clusters at the B3LYP/6-31G\* level.



**Figure 12.** Longitudinal optical (LO) mode frequencies of  $C_{2m}$  carbon clusters as a function of the inverse of the size 1/2m, at the B3LYP/ 6-31G\* level. The lines are drawn to guide the eye and are discussed in the text. The filled circle on the vertical axis represents the LO mode frequency of polyyne from ref 48.

the size of the chain increases. For the hypothetical equidistant polycumulene, adjacent carbon–carbon stretches cancel each other and the mode would be inactive.<sup>47</sup>

In finite linear carbon clusters  $C_n$ , there are several optically active longitudinal modes, one of which corresponds best to the one shown in Figure 10 determined by the phases of the stretching motions in the different carbon–carbon bonds along the chain. For the rest of this paper we refer to this mode when talking about the LO mode of the finite linear carbon chains. By symmetry, the LO mode is Raman active when *n* is even or IR active when *n* is odd. The LO mode frequencies of the short  $C_n$  clusters at the B3LYP/6-31G\* level are shown in Figure 11. Despite the frequency differences between nearby even- and odd-numbered carbon clusters, they show the same trend as the oligomer size increases. Considering the slow convergency of odd-numbered  $C_n$ , in the following we only study the vibrational properties of even-numbered  $C_n$  clusters.

Vibrational calculations on medium to long even-numbered  $C_{2m}$  clusters are performed at the B3LYP/6-31G\* level, with 2m up to 64. The dependence of the LO mode frequency with the inverse of the cluster size (1/2m) is shown in Figure 12. It is apparent that as the cluster size increases (1/2m decreases), the LO mode frequency decreases until a sharp upturn is observed at 2m = 52. This critical size is the same as discussed in the transition of the geometry and band gap above. On the



**Figure 13.** Calculated Raman scattering intensity for the longitudinal optical (LO) mode of linear  $C_{2m}$  and  $H-C_{2m}-H$  chains as a function of the oligomer size of the chains, at the B3LYP/6-31G\* theoretical level.

basis of the cumulenic  $C_{2m}$  ( $2m \le 52$ ) region, the LO mode frequency is expected to be extrapolated to a very small number at the polymer limit  $(1/2m \rightarrow 0)$ , shown as the dotted line in the figure. This is because all the cumulenic  $C_{2m}$  chains have a very small bond length alternation. If the BLA is zero, then the LO mode frequency extrapolation will go exactly to zero. The harmonic LO mode frequency of polyyne at the same theoretical level was recently predicted to be 1795 cm<sup>-1</sup>,<sup>48</sup> labeled as a dark circle on the vertical axis in Figure 12. It is obtained by extrapolating the frequencies of  $H-(C=C)_m-H$  (48  $\leq 2m \leq$ 72) oligoynes to the  $1/2m \rightarrow 0$  limit. A series of vibrational calculations on acetylenic  $C_{2m}$  linear clusters with 2m > 56should be included in the extrapolation to correctly predict the vibrational properties of polyyne. The longer the clusters calculated, the more accurate the extrapolation will be.<sup>49</sup> Currently this cannot be done due to the limitations arising from the aforementioned linear dependence problem and the limitations of computer resources. However, it is clear that the properties of the uncapped long chains and the infinite extrapolated properties of H-capped alternating chains match as accurately as expected. The extrapolation based on shorter  $C_n$ oligomers have nothing to do with the properties of very long chains. With properly terminated oligomers, such as the  $H-(C \equiv$  $C_{m}$ -H oligores, the convergency of properties is continuous: there is no transition from a qualitatively low alternation to a large alternation as for the  $C_n$  chains.

The LO mode intensity of the carbon chain oligomers is dependent on both the size of the oligomer and the BLA of the chain. Figure 13 shows that at the same size, the LO mode intensity of the hydrogen end-capped oligoynes are much larger than that of the  $C_n$  carbon clusters. This is due to the differences in the BLA which is much larger for H-capped chains than for the cumulenic short  $C_n$  chains. Analysis shows that the intensity for both oligomer series varies roughly as a power function of the size 2m, as shown in Figure 14. It is interesting to note that the intensity for the end-capped oligoyne series is proportional to the 5.3 power of the size, roughly doubled compared with the 2.8 power on the size for oligoenes which was analytically derived with Hückel theory.<sup>50</sup>



Figure 14. Relationship between the longitudinal optical (LO) mode Raman scattering intensity (Int) and the oligomer size for linear  $C_{2m}$ clusters, predicted by B3LYP/6-31G\* calculations.

### 4. Conclusions

With state of the art theoretical calculations, we investigated the properties of long linear carbon clusters. For the first time we observed a transition for long linear  $C_n$  chains, from essentially nonalternating cumulenic structures to bond length alternating acetylenic structures. This dramatic structural change is reflected in the very unusual dependences of the HOMO-LUMO gap and the LO mode frequency on the size of the linear carbon clusters. The interpretation of this vibrational band critically depends on the bond length alternation. This mode plays an important role in the IR Raman spectroscopy of linear carbons, including the recently discovered very long carbon chains encapsulated in carbon nanotubes.<sup>51-54</sup> One cannot predict the properties of  $C_{\infty}$  based on the extrapolation from short- and medium-sized  $C_n$  chains found in the literature. But with the cumulenic-acetylenic transition found in this work, extrapolations to the properties of infinite  $C_{\infty}$  polyyne can be obtained once sufficiently long  $C_n$  chains or chains capped with Hs are studied.

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