# Structural, Electronic, and Magnetic Properties of $\mathrm{Fe}_{3} \mathbf{C}_{\mathbf{2}}$ Cluster 

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#### Abstract

On the basis of density-functional theory and all-electron numerical basis set, 20 stable isomers of $\mathrm{Fe}_{3} \mathrm{C}_{2}$ cluster are found through optimization calculations and frequency analysis from 108 initial structures. A nonplanar $C_{s}$ structure with nonet spin multiplicity and $482.978 \mathrm{kcal} / \mathrm{mol}$ of binding energy is found as the candidate of global minimum geometry of $\mathrm{Fe}_{3} \mathrm{C}_{2}$ cluster. The binding energies, the energy gaps between the highest occupied molecular orbital and the lowest unoccupied molecular orbital, and the magnetic moments of all the isomers are reported. The relationship between the molecular properties and geometrical structures is also investigated.


## 1. Introduction

The Fe-based nanoparticles are of great interest because they play an essential role in modern materials science. A large number of experimental and theoretical investigations of bare iron clusters ${ }^{1-19}$ have been carried out. For example, the polarizabilities of $\mathrm{Fe}_{n}(n \leq 4)$ clusters have been investigated by Calaminici. ${ }^{20}$ Recent investigation shows that iron clusters can act as a catalyst in the production of single-walled carbon nanotubes (SWNT). ${ }^{21}$ Some studies on the Fe-based nanoparticles including Fe with $\mathrm{O}^{22}$ and Fe with C have also been reported. The bonding of methane with magnetic $\mathrm{Fe}_{4}$ clusters have been investigated by Castro. ${ }^{23}$ More studies devoted to the $\mathrm{FeC}_{n}$ or $\mathrm{Fe}_{n} \mathrm{C}$ clusters can be found in the literature. Gutsev and Bauschlicher ${ }^{24}$ have computed the electronic and geometrical structures of the ground and excited states of $\mathrm{Fe}_{n} \mathrm{C}$, $\mathrm{Fe}_{n} \mathrm{C}^{-}$, and $\mathrm{Fe}_{n} \mathrm{C}^{+}(n=1-6)$ clusters using density functional theory (DFT). Nash et al. ${ }^{25}$ have calculated the equilibrium geometries, total energies, and electronic structures of $\mathrm{FeC}_{n}$ ( $n$ $\leq 3$ ) clusters using three levels of theory. They found that the density functional theory is accurate in explaining the experiment and can be used to study larger clusters of $\mathrm{FeC}_{n}$ reliably. The $\mathrm{FeC}_{2}$ molecule in its different geometric conformations and electronic states has been studied using the DFT (B3LYP) and CASSCF/CASPT2 methods. ${ }^{26}$ It is shown that the cyclic $\left(C_{2 v}\right)$ structure of $\mathrm{FeC}_{2}$ molecule is more stable than the linear ( $C_{\infty v}$ ) structure. Sosa et al. ${ }^{27}$ have computed triplet and quintet states of $\mathrm{Fe}_{5} \mathrm{C}$, neither of which is the ground-state of the cluster. Krause et al. ${ }^{28}$ have computed $\mathrm{Fe}_{21} \mathrm{C}$ and $\mathrm{Fe}_{27} \mathrm{C}$ at the assumed geometries to simulate two nonequivalent sites in bulk $\mathrm{Fe}_{4} \mathrm{C}$. Noya et al. have reported ab initio calculations of the structures, binding energies, and spin multiplicities of the clusters $\mathrm{Fe}_{2}, \mathrm{C}_{2}$, $\mathrm{FeC}_{n}(n=1-4)$, and $\mathrm{Fe}_{2} \mathrm{C}_{n}(n=1-3)$ using DFT method. ${ }^{29}$ They pointed out that all the dimetallic carbide clusters are predicted to have cyclic planar geometries that are stabilized by transannular bonds. ${ }^{29}$ They also found that the pentagonal geometries of $\mathrm{Fe}_{2} \mathrm{C}_{3}$ with transannular $\mathrm{Fe}-\mathrm{Fe}$ and $\mathrm{Fe}-\mathrm{C}$ bonds include a $\mathrm{FeC}_{2}$ unit that is almost identical to free $\mathrm{FeC}_{2}$. Subsequently, they expanded their investigation to $\mathrm{Fe}_{2} \mathrm{C}_{4}$ and found the ground-state structure is also a planar ring that feature nonadjacent Fe atoms. ${ }^{30} \mathrm{Fe}_{n} \mathrm{C}_{12}(n=2-8)$ clusters were

[^0]\[

$$
\begin{aligned}
& \begin{array}{lll}
\mathrm{Fe}_{2} & \mathrm{FeC} & \mathrm{C}_{2}
\end{array} \\
& \begin{array}{llll}
\mathrm{Fe}_{3} & \mathrm{Fe}_{2} \mathrm{C} & \mathrm{FeC}_{2} & \mathrm{C}_{3}
\end{array} \\
& \begin{array}{llllll}
\mathrm{Fe}_{4} & \mathrm{Fe}_{3} \mathrm{C} & \mathrm{Fe}_{2} \mathrm{C}_{2} & \mathrm{FeC}_{3} & \mathrm{C}_{4}
\end{array} \\
& \searrow \swarrow \searrow x^{\prime} \searrow \swarrow \searrow \measuredangle \\
& \begin{array}{lllllll}
\mathrm{Fe}_{5} & \mathrm{Fe}_{4} \mathrm{C} & \mathrm{Fe}_{3} \mathrm{C}_{2} & \mathrm{Fe}_{2} \mathrm{C}_{3} & \mathrm{FeC}_{4} & \mathrm{C}_{5}
\end{array}
\end{aligned}
$$
\]

Figure 1. The scheme of building initial structures for search of the stable structures for $\mathrm{Fe}_{m} \mathrm{C}_{n}$ [from ref 33].
experimentally studied by Pilgrim and Duncan, ${ }^{31}$ and DFT investigations of $\mathrm{Fe}_{n} \mathrm{C}_{12}(n=2-8)$ clusters were carried out by Harris and Dance ${ }^{32}$ very recently. On the basis of DFT calculations, Ryzhkov and co-workers have searched stable structures of $\mathrm{Fe}_{2} \mathrm{C}, \mathrm{FeC}_{2}, \mathrm{Fe}_{3} \mathrm{C}, \mathrm{FeC}_{3}$, and $\mathrm{Fe}_{2} \mathrm{C}_{2}$ using "binomial" scheme ${ }^{33}$ to build initial geometries. They found that the most stable planar structures for $\mathrm{FeC}_{3}$ and $\mathrm{Fe}_{2} \mathrm{C}_{2}$ are favored over the three-dimensional isomers, whereas for $\mathrm{Fe}_{3} \mathrm{C}$ the pyramidal configuration appeared to be the ground state. However, the investigations of $\mathrm{Fe}_{n} \mathrm{C}_{m}$ clusters are still inadequate, limiting the understanding of their roles in various chemical and physical processes.

Stimulated by the previous investigations of $\mathrm{Fe}_{2} \mathrm{C}_{2}$ and $\mathrm{Fe}_{3} \mathrm{C}$ clusters by Ryzhkov et al. ${ }^{33}$ and $\mathrm{Fe}_{2} \mathrm{C}_{3}$ clusters by Noya et al., ${ }^{29,30}$ we present an extended investigation of the $\mathrm{Fe}_{3} \mathrm{C}_{2}$ cluster. In the present work, we seek the stable isomers of the $\mathrm{Fe}_{3} \mathrm{C}_{2}$ cluster. The binding energies (BE), vibrational frequencies, energy gaps between highest occupied molecular orbital (HOMO) and lowest unoccupied molecular orbital (LUMO), and the magnetic moments of the stable structures are calculated and analyzed. It is expected that the present results can provide a basis for understanding the molecular properties of the various isomers of $\mathrm{Fe}_{3} \mathrm{C}_{2}$ cluster.

## 2. Computational Details

We search for the stable geometries of $\mathrm{Fe}_{3} \mathrm{C}_{2}$ cluster still following the binomial scheme ${ }^{33}$ [see Figure 1]. In the scheme, the Fe or C atom is made to approach the initial dimers $\mathrm{Fe}_{2}$, FeC , and $\mathrm{C}_{2}$ from all possible directions, which will result in some stable configurations of $\mathrm{Fe}_{2} \mathrm{C}, \mathrm{FeC}_{2}, \mathrm{Fe}_{3}$, and $\mathrm{C}_{3}$. Then these stable structures are served as basic units for generating the initial structures of tetraatomic clusters and so on. We extend the scheme to the $\mathrm{Fe}_{3} \mathrm{C}_{2}$ cluster containing five atoms in the

TABLE 1: the Calculation Results for $\mathrm{Fe}_{2} \mathrm{C}_{2}$ and $\mathrm{Fe}_{3} \mathbf{C}$ Clusters, Including Those of Ryzhkov et al

|  | symmetry |  |  | binding energy $(\mathrm{kcal} / \mathrm{mol})$ |  |
| :--- | :---: | :--- | :---: | :---: | :---: |
| isomers | present |  | present | Ryzhkov et al. ${ }^{32}$ |  |
| $\mathrm{Fe}_{2} \mathrm{C}_{2}-1$ | $C_{s}$ |  | 397.005 | 397 |  |
| $\mathrm{Fe}_{2} \mathrm{C}_{2}-2$ | $D_{2 h}$ |  | 391.182 | 391 |  |
| $\mathrm{Fe}_{2} \mathrm{C}_{2}-3$ | $D_{\infty h}$ |  | 389.034 | 389 |  |
| $\mathrm{Fe}_{2} \mathrm{C}_{2}-4$ | $C_{2 v}$ |  | 386.760 | 388 |  |
| $\mathrm{Fe}_{2} \mathrm{C}_{2}-5$ | $D_{2 h}$ |  | 381.544 | 383 |  |
| $\mathrm{Fe}_{2} \mathrm{C}_{2}-6$ | $C_{2 v}$ |  | 356.381 | 357 |  |
| $\mathrm{Fe}_{2} \mathrm{C}_{2}-7$ | $C_{\infty v}$ | 359.732 | 357 |  |  |
| $\mathrm{Fe}_{2} \mathrm{C}_{2}-8$ | $C_{1}$ | 340.749 | 341 |  |  |
| $\mathrm{Fe}_{2} \mathrm{C}_{2}-9$ | $C_{s}$ |  | 338.618 | 340 |  |
| $\mathrm{Fe}_{2} \mathrm{C}_{2}-10$ | $C_{s}$ | 333.561 | 334 |  |  |
| $\mathrm{Fe}_{2} \mathrm{C}_{2}-11$ | $C_{s}$ | 332.408 | 333 |  |  |
| $\mathrm{Fe}_{2} \mathrm{C}_{2}-12$ | $D_{\infty h}$ | 306.520 | 304 |  |  |
| $\mathrm{Fe}_{3} \mathrm{C}-1$ | $C_{3 v}$ | 322.644 | 323 |  |  |
| $\mathrm{Fe}_{3} \mathrm{C}-2$ | $C_{2 v}$ | 319.703 | 320 |  |  |
| $\mathrm{Fe}_{3} \mathrm{C}-3$ | $C_{2 v}$ | 314.669 | 315 |  |  |
| $\mathrm{Fe}_{3} \mathrm{C}-4$ | $C_{\infty v}$ | 289.006 | 289 |  |  |
|  |  |  |  |  |  |

present paper. According to the scheme, there are two ways to build initial structures for searching the stable configurations of $\mathrm{Fe}_{3} \mathrm{C}_{2}$. The first one is to add a Fe atom to the tetraatomic $\mathrm{Fe}_{2} \mathrm{C}_{2}$ cluster, and the other is to add a C atom to the $\mathrm{Fe}_{3} \mathrm{C}$ cluster. Hereinafter, they are represented by "a" and "b", respectively.

Because the number of the possible initial structures of $\mathrm{Fe}_{3} \mathrm{C}_{2}$ is large, the work to search the stable geometries for $\mathrm{Fe}_{3} \mathrm{C}_{2}$ cluster cannot be fulfilled if there is no efficient computational method. As Ryzhkov et al. ${ }^{33}$ mentioned in their article, the DFTbased $\mathrm{DMol}^{3}$ method ${ }^{34}$ is very efficient and may serve our purpose, because it can search for optimum atomic positions based on the total energy gradient calculation. All the calculations for geometry optimization of $\mathrm{Fe}_{3} \mathrm{C}_{2}$ isomers are performed using the spin-polarized DFT calculations with the generalized gradient approximation (GGA) in "PW91" form. ${ }^{35,36}$ The molecular DFT DMOL ${ }^{3}$ package is employed in which double numerical plus d-functions (DND) are chosen to describe the electronic wave functions. It is a set of default basis set in the package, providing reasonable accuracy for modest computational cost.
At first, we recalculate the 16 stable structures of $\mathrm{Fe}_{2} \mathrm{C}_{2}$ and $\mathrm{Fe}_{3} \mathrm{C}$ reported by Ryzhkov et al. ${ }^{33}$ to confirm the convergence standard and parameters of the numerical calculations used in the present work. Our results and those of Ryzhkov et al. ${ }^{33}$ are collected in Table 1. In our calculations, optimization is performed by the convergence settings of $1.0 \times 10^{-5}$ Hartree for the energy, $5.0 \times 10^{-4}$ Hartree/Bohr for the maximum force and $0.002 \AA$ for the maximum displacement. The global orbital cutoff is $6.0 \AA$, which is better than the "fine" standard in $\mathrm{DMol}^{3}$. The smearing gap 0.005 is used to facilitate the convergence of the SCF iterations. Table 1 shows that our binding energies are in accord with those of Ryzhkov et al. ${ }^{33}$ although small differences exist in some structures. The above parameters are employed in all the following calculations to search the stable geometries. However, many optimization structures are found within a small energy range, which is a common character for the systems containing transition metal atoms. To obtain a more precise ordering of the optimization structures, produce better relaxation of the $\mathrm{Fe}-\mathrm{Fe}, \mathrm{Fe}-\mathrm{C}$, and $\mathrm{C}-\mathrm{C}$ bonds, and yield much better geometries, we recalculate all the optimization structures using much tighter convergence criteria ( $10^{-8}$ thresholds for the total energy and $10^{-5}$ for the forces).

It should be noted that the twelfth structure ( $D_{\infty h}$ ) reported by Ryzhkov et al. ${ }^{33}$ is not a stable geometry in our calculation
although the much tighter convergence criteria is employed. There are four imaginary vibrational frequencies in the twelfth structure although our BE is $306 \mathrm{kcal} /$ mole, which is close to their $304 \mathrm{kcal} / \mathrm{mol} .{ }^{33}$ However, we still use it to construct the $\mathrm{Fe}_{3} \mathrm{C}_{2}$ initial structures to avoid missing the possible stable isomers from this way.

## 3. Results and Discussions

3.1. Stable Geometries and Binding Energies. Following the two ways ("a" and "b") of building initial structures in Section 2, the Fe or C atom is added to the pre-existing $\mathrm{Fe}_{2} \mathrm{C}_{2}$ and $\mathrm{Fe}_{3} \mathrm{C}$ clusters from many spatial directions, and we obtain 108 initial geometries in total, including 83 from " $a$ " way and 25 from "b".

The initial geometries are subjected to geometrical optimization and frequency analysis, leading to 50 stable structures, including 39 stable structures for the initial structures from "a" and 11 stable structures from " b ". All the optimization structures are shown in Figure 2. To distinguish the additional Fe or C atom from the others more clearly, we delete the bonds connecting between the added atom and the other atoms in the figures, that is, the separate Fe atom is the added atom. As shown in Figure 2, the geometries include 31 planar and 19 threedimensional structures, and no linear structure has been found.

However, checking the geometries carefully, we find that the BEs and bond lengths of some structures have only small differences. The similar structures look like the same stable structure although their geometries belong to different point groups because they are optimized from initial structures with different symmetries. We guess that the similar stable structures may be the same geometry actually, and the small differences result from the errors of the same geometry calculated with the molecular orbital with different symmetries. To confirm the idea, we repeat optimizations and frequency calculations with much tighter convergence criteria using all the 50 structures as initial structures. This time, the same symmetry is used for the similar structures by a loose standard to determine the symmetries of the isomers. For example, $C_{s}$ symmetry is used in the recalculations for the similar geometries (the isomer numbers are 14, $15,16,17,18,20$, and 21). The new calculation results show that the differences of their BEs are smaller than $1.0 \mathrm{kcal} / \mathrm{mol}$ (chemical accuracy) although some of the bond lengths are different to some extent. We will treat them as the same structure in following discussions. Moreover, six other groups of the structures are the similar cases. The isomer numbers of the six groups are $23 / 24 / 25,31 / 32 / 33,37 / 38 / 39,40 / 41,42 / 43 / 44$, and 49/50, respectively. However, we have also noted that the BE difference between isomer 12 and isomer 21 is only $0.9 \mathrm{kcal} /$ mol , and the biggest difference of the bond lengths is $0.053 \AA$ in the first calculations. To our surprise, the reoptimizations show that the difference of their BEs is enlarged to $7.0 \mathrm{kcal} /$ mol , and the biggest difference of bond lengths is $0.327 \AA$. They are obviously not the same but two completely different stable structures. It is also found that 7 structures of the 50 geometries, that is, isomers $4,5,9,10,22,45$, and 48 are unstable geometries with imaginary frequencies in the recalculations. Besides, the recalculations of other 7 structures cannot reach the new tight convergence criteria in the SCF iterations or optimization. The different calculation results in the recalculations may be understood in that the different initial molecular orbitals (including the representations and occupations) of the SCF calculations have been used. As explained before, the twelfth structure reported by Ryzhkov et al. ${ }^{33}$ is not stable in our calculation, and we also have not obtained any stable structures of $\mathrm{Fe}_{3} \mathrm{C}_{2}$ from the initial structures by adding a Fe atom to it.

|  |  |  |  |
| :---: | :---: | :---: | :---: |
|  |  | - <br> 7* |  |
|  |  |  |  |
|  |  <br> 14 | 15 |  |
| 17 | 18 |  | Coser |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  | - <br> 36* |
|  |  | $39^{*}$ |  |
|  |  |  |  |



Figure 2. The 50 optimized geometries from the 108 initial structures of $\mathrm{Fe}_{3} \mathrm{C}_{2}$ cluster. They are arranged in order of increasing absolute values of BEs. Among them, only 20 structures turn out to be stable after recalculations. The asterisk represents that the corresponding structure is stable. The carbon atoms are given in gray, and iron atoms are shown in purple.

TABLE 2: The BEs, Bond Lengths and HLEGS of All the 20 Stable Isomers of $\mathrm{Fe}_{3} \mathbf{C}_{\mathbf{2}}$ Cluster

| isomer number | symmetry | BEs (kcal/mol) | $\mathrm{C}-\mathrm{C}$ bond $(\AA)$ | $\mathrm{Fe}-\mathrm{Fe}$ bond ( A ) |  | $\mathrm{Fe}-\mathrm{C}$ bond $(\AA)$ |  | HLEG (eV) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | min | max | min | max |  |
| 1 | $C_{s}$ | 420.829 | 3.013 | 2.431 | 5.744 | 1.669 | 4.374 | 0.587 |
| 2 | $C_{2 v}$ | 424.903 | 2.780 | 3.361 | 5.803 | 1.648 | 4.341 | 0.430 |
| 3 | $C_{s}$ | 425.392 | 2.876 | 2.504 | 5.681 | 1.680 | 4.218 | 0.500 |
| 6 | $C_{1}$ | 448.689 | 2.805 | 2.314 | 2.611 | 1.713 | 3.063 | 0.719 |
| 7 | $C_{2 v}$ | 449.910 | 1.392 | 2.333 | 5.813 | 1.864 | 4.143 | 0.404 |
| 12 | $C_{s}$ | 456.587 | 2.611 | 2.324 | 3.516 | 1.707 | 3.839 | 0.363 |
| 13 | $C_{s}$ | 460.499 | 2.594 | 2.464 | 3.503 | 1.710 | 3.864 | 0.064 |
| 21 | $C_{s}$ | 463.551 | 2.284 | 2.344 | 3.533 | 1.716 | 3.636 | 0.700 |
| 25 | $C_{s}$ | 465.435 | 2.401 | 2.356 | 2.528 | 1.740 | 3.078 | 0.574 |
| 28 | $D_{3 h}$ | 465.679 | 2.310 | 2.365 | 2.365 | 1.789 | 1.789 | 0.741 |
| 29 | $C_{1}$ | 467.755 | 1.420 | 2.240 | 3.482 | 1.869 | 2.071 | 0.468 |
| 30 | $C_{2 v}$ | 469.214 | 1.424 | 2.310 | 3.490 | 1.924 | 2.028 | 0.515 |
| 33 | $C_{s}$ | 471.412 | 1.405 | 2.308 | 3.630 | 1.826 | 2.984 | 0.547 |
| 35 | $C_{1}$ | 472.830 | 1.362 | 2.442 | 2.595 | 1.880 | 3.072 | 0.819 |
| 36 | $C_{s}$ | 473.686 | 1.325 | 2.197 | 3.707 | 1.780 | 3.111 | 0.459 |
| 39 | $C_{2 v}$ | 476.009 | 2.298 | 2.300 | 2.644 | 1.768 | 2.005 | 1.048 |
| 41 | $C_{2 v}$ | 478.745 | 1.305 | 2.389 | 4.365 | 1.798 | 2.988 | 0.699 |
| 43 | $C_{s}$ | 479.994 | 1.296 | 2.331 | 2.457 | 1.878 | 4.092 | 0.628 |
| 47 | $C_{s}$ | 482.859 | 1.348 | 2.273 | 2.309 | 1.843 | 2.890 | 0.653 |
| 50 | $C_{s}$ | 482.978 | 1.346 | 2.267 | 2.307 | 1.846 | 2.887 | 0.586 |

Finally, we obtain 20 different stable isomers for $\mathrm{Fe}_{3} \mathrm{C}_{2}$ in total. Their geometrical properties in Figure 2 are updated according to the recalculation results. Their bond lengths and BEs are collected in Table 2. The largest bond length of $\mathrm{C}-\mathrm{C}$ is $3.013 \AA$ of isomer 1 , and the shortest is $1.296 \AA$ of isomer 43. There are 6 values of $\mathrm{Fe}-\mathrm{C}$ in every isomer. However, we only list the minima and the maxima in the Table 2. The minima for the all isomers range from 1.648 to $1.924 \AA$ and the maxima 1.789 to $4.374 \AA$. There are three values of $\mathrm{Fe}-\mathrm{Fe}$ in every isomer. We still list the minima and the maxima for the isomers.

In Figure 3, we plot the BEs and the bond lengths of all the isomers to show the relationship between the BEs and the structures of the isomers for $\mathrm{Fe}_{3} \mathrm{C}_{2}$. From the figure, we find that the larger BE clusters generally have more compact geometries. The $\mathrm{Fe}-\mathrm{Fe}$ maximum bond length of each isomer affects the BEs obviously, for example, isomers 1, 2, and 3 have obviously smaller BEs than those of the others, whereas their $\mathrm{Fe}-\mathrm{Fe}$ maxima are also obviously larger. It should be noted that the bond length of $\mathrm{C}-\mathrm{C}$ also plays an important role for the BEs. In particular, among structures $36,41,43,47,50$, and 28 , the structure 28 looks more compact than the others but has a smaller BE; however, it is not true because the $\mathrm{C}-\mathrm{C}$ bond length of the structure $28(2.310 \AA)$ is much larger than that of the others. Therefore the structure 28 should be less compact although its other bond lengths are slightly smaller. From Figure 3 and Table 2, we can conclude that isomer 50 with the largest BE of $482.978 \mathrm{kcal} / \mathrm{mol}$ can be regarded as the candidate for the global minimum of $\mathrm{Fe}_{3} \mathrm{C}_{2}$ cluster, and it means that the most stable structure energetically is also the most compact structure.

Ryzhkov et al. ${ }^{33}$ have concluded that for 3- and 4-atom nanoparticles of $\mathrm{Fe}_{n} \mathrm{C}_{m}$, linear structures cannot be the ground state even for the triatomic species, and highly symmetric structures for the cluster do not lead to the most stable geometry in general. The present investigation shows that for the $\mathrm{Fe}_{3} \mathrm{C}_{2}$ cluster the most stable structure is in the $C_{s}$ symmetry but not in $D_{3 h}$, and no linear structure is found to be stable, which is in agreement with the conclusion of Ryzhkov et al. As $\mathrm{Fe}_{2} \mathrm{C}_{n}$ ( $n$ $=1-3$ ) clusters reported in the literature, ${ }^{29,30} \mathrm{Fe}_{3} \mathrm{C}_{2}$ cluster also has planar structures. Seven stable cyclic planar geometries (isomer 12, 13, 21, 33, 36, 41, and 43) are found at the present calculational level.
3.2. HOMO-LUMO Energy Gaps. The electronic properties of $\mathrm{Fe}_{3} \mathrm{C}_{2}$ cluster can also be investigated through examining HOMO-LUMO energy gap (HLEG). The HLEGs for the all 20 stable structures are collected in Table 2. We can find from the table that the HLEGs for the isomers are obviously different, and the HLEGs range from 0.064 to 1.048 eV . It implies that the isomers of $\mathrm{Fe}_{3} \mathrm{C}_{2}$ cluster have various abilities to control electrons and can be used as different objectives for various chemical reactions. The one with the largest 1.048 eV of HLEG is isomer 39. As shown in Figure 4, for isomer 39, the HOMO is located partly on the C atom, and the LUMOs are almost completely located on the three Fe atoms. For isomer 13 with the smallest HLEG of 0.064 eV , its LUMO is located partly on C atom although the HOMO still is mainly on the Fe atoms. We also examine the HOMO and LUMO for all other isomers and find that the HOMOs for all isomers mainly locate on Fe atoms, while the LUMOs locate on a small part of the orbital


Figure 3. Binding energies and bond lengths of the 20 stable geometries of $\mathrm{Fe}_{3} \mathrm{C}_{2}$ cluster. Only the maxima and minima values for the $\mathrm{Fe}-\mathrm{Fe}$ and $\mathrm{Fe}-\mathrm{C}$ bonds of each isomer are plotted although there are 3 bonds for $\mathrm{Fe}-\mathrm{Fe}$ and 6 bonds for $\mathrm{Fe}-\mathrm{C}$. Here, the $x$-coordinate represents the numbers of the stable isomers.


Figure 4. The isodensity surfaces for the HOMO and LUMO of isomer 39 and isomer 13 of $\mathrm{Fe}_{3} \mathrm{C}_{2}$ cluster. Isomer 39 is the one with the largest HLEG while isomer 13 is the one with the smallest HLEG. The carbon atoms are given in gray, and iron atoms in purple.
on C atoms; for some isomers the C component is obvious, but for the others it is too small to display in the picture. Obviously the chemical stability is dependent on the Fe atom in the isomers.

The HOMO and LUMO molecular orbital in the most stable structure (structure 50) correspond to spin down $\mathrm{A}^{\prime}$ and up $\mathrm{A}^{\prime}$ irreducible representations of the $C_{s}$ point group, respectively. The HOMO contains $67.75 \%$ of the Fe 3d atomic orbital, with admixtures of Fe 4 s ( $10.72 \%$ ) and C 2 p ( $6.50 \%$ ) character, and for the LUMO the delocalized character is very obvious. The Fe 3d atomic orbital decreases to $29.76 \%$ with admixtures of Fe 4s (18.85\%), Fe 4p (13.88\%), C 2p (18.13\%), and C 2s ( $10.88 \%$ ) character. While for the least stable isomer (isomer 1), the HOMO and LUMO correspond to spin up orbital of $\mathrm{A}^{\prime}$ and $A^{\prime \prime}$ symmetries, respectively. The HOMO contains $61.53 \%$ 3d contributions from all Fe atoms, but the LUMO contains $89.04 \% \mathrm{Fe}$ 3d. Generally, the HOMO and LUMO of $\mathrm{Fe}_{3} \mathrm{C}_{2}$ isomers are more delocalized than the $\mathrm{Fe}_{2} \mathrm{C}$ isomer but similar components as the $\mathrm{Fe}_{3} \mathrm{C}$ isomers. ${ }^{35} \mathrm{We}$ also noted the HLEG of the most stable geometry (structure 50) energetically is 0.586 eV and is not the one having the largest HLEG of 1.048 eV .
3.3. Magnetic Moment. On the basis of the optimized stable geometries, the magnetic properties of the $20 \mathrm{Fe}_{3} \mathrm{C}_{2}$ isomers

TABLE 3: Magnetic Moments and Corresponding Spin States of the 20 Stable Isomers (in $\mu_{B}$ )

| isomer <br> number | C | C | Fe | Fe | Fe | total | spin <br> states |
| :---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 0.459 | 0.679 | -2.136 | -2.575 | -2.481 | -6.054 | 7 |
| 2 | 0.328 | 0.328 | 2.197 | -2.456 | -2.156 | -1.759 | 3 |
| 3 | -0.164 | 0.398 | 2.945 | -2.476 | -2.479 | -1.776 | 3 |
| 6 | 0.395 | 0.465 | -2.573 | -1.873 | -2.375 | -5.961 | 7 |
| 7 | 0.128 | 0.128 | -2.242 | 3.018 | -3.405 | -2.373 | 3 |
| 12 | 0.319 | 0.412 | -2.430 | -2.188 | -2.243 | -6.130 | 7 |
| 13 | -0.189 | 0.220 | 2.283 | -2.605 | -2.461 | -2.752 | 3 |
| 21 | 0.092 | 0.205 | 2.346 | -2.431 | -2.282 | -2.070 | 3 |
| 25 | -0.315 | -0.400 | 2.932 | 1.941 | 1.941 | 6.104 | 7 |
| 28 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 1 |
| 29 | -0.033 | -0.090 | 2.824 | 2.744 | 2.821 | 8.264 | 9 |
| 30 | -0.054 | -0.050 | 2.771 | 2.771 | 2.789 | 8.223 | 9 |
| 33 | 0.009 | 0.024 | 3.236 | -2.415 | 2.890 | 3.744 | 5 |
| 35 | 0.056 | 0.048 | 3.013 | -2.388 | 3.182 | 3.911 | 5 |
| 36 | -0.052 | 0.007 | 2.911 | 2.880 | 2.576 | 8.322 | 9 |
| 39 | 0.369 | 0.369 | -3.019 | -1.853 | -1.853 | -5.987 | 7 |
| 41 | 0.005 | 0.005 | 2.513 | 2.513 | 3.058 | 8.094 | 9 |
| 43 | 0.088 | 0.257 | 3.153 | 3.206 | 3.303 | 10.007 | 11 |
| 47 | -0.016 | -0.080 | 2.817 | 2.628 | 2.817 | 8.164 | 9 |
| 50 | -0.013 | -0.080 | 2.660 | 2.818 | 2.818 | 8.205 | 9 |

are investigated and the results are presented in Table 3. We also determine the corresponding spin states of the isomers by analyzing the orbital occupations. This determination is very important, because systems including transition metal Fe offer several spin states contained in a small energy range. Even if some spin states are higher energy states they may play an important role in the electronic, magnetic, or catalytic properties of the cluster. ${ }^{23}$ From Table 3, we can find that the total magnetic moment is mainly located on the Fe atoms, and some of the local moments on C atoms are found to align antiferromagnetically with respect to that on the Fe atoms. We also find the $\mathrm{Fe}_{3} \mathrm{C}_{2}$ isomers really have various spin states, ranging from singlet to hendecatet. It is interesting to find that the local moments on one Fe atom align antiferromagnetically with respect to that on the other two Fe atoms in 7 isomers, which results in the total magnetic moment smaller than $4 \mu_{\mathrm{B}}$, while the others are all about or larger than $6 \mu_{\mathrm{B}}$. The one with the largest magnetic moment is isomer 43 whose magnetic moment reaches $10.01 \mu_{\mathrm{B}}$, which is close to the $10.3 \mu_{\mathrm{B}}$ of the pure $\mathrm{Fe}_{3}$
cluster at the same computational level. In this structure, the local magnetic moment on C atoms is not the largest (the largest local magnetic moment on C atom, existing in isomer 1 , reaches $1.138 \mu_{\mathrm{B}}$, but it aligns antiferromagnetically with respect to that on the other three Fe atoms; therefore it makes the total magnetic moment of isomer 1 decrease). For the most stable structure (isomer 50), all local magnetic moments on the three Fe atoms are smaller than those of isomer 43, and the local magnetic moment on C atoms aligns antiferromagnetically with respect to those of Fe atoms. Therefore, the total magnetic moment is $8.205 \mu_{\mathrm{B}}$, which is obviously smaller than the largest $10.01 \mu_{\mathrm{B}}$ of isomer 43. Another particular case is that all the local magnetic moments on each atom are zero in isomer 28. It is the highest-symmetrical geometry ( $D_{3 h}$ ) among the 20 stable structures. By carefully examining the molecular orbital occupations of isomer 28, we find all the occupations of spin up and down always occur in pairs because the high-symmetrical point group provides enough degeneracy orbitals. Therefore, the total spin of each atom is zero.

## 4. Conclusions

Twenty stable geometries of $\mathrm{Fe}_{3} \mathrm{C}_{2}$ are found using spinpolarized DFT calculations with numerical basis sets DND. The stability of all clusters is confirmed by vibrational frequency analysis. It is found that the candidate of the global minimum structure is not the highest-symmetrical $D_{3 h}$ geometry but the most compact $C_{s}$ nonplanar structure (isomer 50). Some interesting structures, such as isomer 28 with zero magnetic moment are found. The values of the BEs, HLEGs, and magnetic moments of the $\mathrm{Fe}_{3} \mathrm{C}_{2}$ isomers span a large range. It implies that the $\mathrm{Fe}_{3} \mathrm{C}_{2}$ cluster, which has rich and colorful geometrical structures and molecular properties, can play an important role in various adsorption processes or catalytic reactions.

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