Chromium Site Specific Chemistry and Crystal Structure of LiCaCrF₆ and Related Chromium Doped Laser Materials

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The crystal structure of LiCaCrF₆, a fully Cr-substituted lithium metal hexafluoride representative of laser materials with the generic formula LiMe^{II}Me^{III} $_{-x}$ Cr $_x$ F₆ (Me^{III} = Ca, Sr; Me^{IIII} = Al) was determined by X-ray single crystal diffraction and neutron powder profile refinement. LiCaCrF₆ was confirmed as a LiCaAlF₆ (Colquiirite)-type (space group $P\overline{3}$ 1c (No. 163), Z=2, a=5.1054(08) Å, c=9.7786(10) Å, Li in 2c, Ca in 2b, Cr in 2d, and F in 12i with x,y,z of 0.3652(3), 0.0183(4), 0.1402(1)). Deviation from centrosymmetry (P31c; No. 159) and full occupation were examined and appear to be insignificant. We selected LiCaCrF₆ as a model compound for the determination of EXAFS phase shifts to provide Cr site specific information in 3% Cr-doped LiCaAlF₆ laser crystals where Cr occupies a slightly distorted CrF₆ octahedron with a Cr-F distance (1.89(8) Å) practically identical to Cr-F in LiCaCrF₆ (1.901 Å) and CrF₃ (1.899 Å). The pseudobinary laser material LiSrAl_{1-x}Cr_xF₆ forms a true solid solution over the complete composition range $0 \le x \le 1$. © 1993 Academic Press, Inc.

1. Introduction

Chromium-doped lithium metal hexafluorides (LMHF) of the general formula Li $Me^{II}Me^{III}_{1-x}Cr_xF_6$ ($Me^{II}=Ca$, Sr; $Me^{III}=AI$) gained considerable interest as a promising class of new solid state laser materials with a wide tuning range (1) (LiCa $AIF_6: Cr^{3+}$), and very recently in a newly developed 752-nm wing-pumped laser design (2) with high Cr-doping (LiSr $AI_{1-x}Cr_xF_6$, $x \ge 0.15$). The structure of the laser host material LiCaAIF₆ (Colquiirite) and the cell constants for some isotypic

compounds have been determined earlier (3). No crystal data for a fully chromiumsubstituted LMHF have been reported so far (4), however, and crystallographic data on the solid solution LiSr(Al,Cr)F₆ are not available as well. In view of the reported uncertainty of the LiCaCrF₆ structure (5) and the large variety of possible LMHF structure types (3, 6), we elected to determine the crystal structure of this fully chromium-substituted LMHF. In addition, Li CaCrF₆ can serve as a model substance providing information necessary for the determination of the chromium environment in slightly doped LiCaAlF₆: Cr³⁺ by means of Extended X-ray Absorption Fine Structure (EXAFS). The local Cr-F geometry is of

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TABLE I Crystallographic Data for LiCaCrF $_6$ as Determined by Single-Crystal X-Ray Diffraction

Compound Formula units per unit cell Lattice constants Space group Formula weight Calculated X-ray density Absorption coefficient Crystal dimensions $\theta/2\theta$ scans up to Range in hkl Total number of reflections Unique reflections Absorption coefficient Irransmission coefficient Inner residual Reflections with $I > 3\sigma I$ Number of variables Conventional residual Weighted residual Weights Scale factor			$Z = a = 5$ $P31c$ 213.0 $P_c = \mu$ (Mo 50 × 20 × 2137 333 from 1.204 $R_{int} = 304$ 16 $R_F(F_c R_w)(F)$	333 from ψ scans 1.204 (highest/lowest) $R_{\text{int}} = 0.074$ 304 16 $R_F(F_o) = 0.045$ $R_w(F_o) = 0.036$ $R_W = 1/\sigma^2$							
Atom	Position	n	x	у	z	U_{ii}	U_{22}	U_{33}	U_{12}	U_{13}	U_{23}
Ca Li	2 <i>b</i> 2 <i>c</i>	2.0	0	0 2/3	0	0.0112(4) 0.0149(22)	0.0112(4)	0.0080(4)	0.0056(2)		
Cr F	2d 12i	2.0 12.0	2/3 .3652(3)	1/3 .0183(4)	1/4 .1402(1)	0.0083(3) 0.0139(7)	0.0083(3) 0.0124(7)	0.0085(3) 0.0142(6)	0.0041(2) 0.0051(5)	0053(5)	0016(4)

Note. Numbers in parentheses give the estimated standard deviations σ of the last significant digits of refined parameters.

interest as asymmetric distortions in the local symmetry at the chromium site appear to reduce the adverse excited state absorption (7) in LiCaAlF₆: Cr^{3+} .

2. Experimental

2.1. Materials Preparation

Crystals have been grown using the zonemelting (ZM) technique from starting materials prepared by reactive atmosphere processing (RAP) using hydrogen fluoride as the reactive gas. The RAP and ZM techniques and the equipment used have been reported previously in detail (8) and are described briefly as follows.

The starting materials LiF and AlF₃ were both high-purity, optical grade materials from Johnson Matthey or GFI Advanced Technologies; CrF₃ was the high-purity, ultra-dry grade from APL Engineering Materials. From these components, a precursor material for the crystal growth was prepared

by the standard RAP technique. The charges were prereacted in a platinum boat, heated to 800°C, and soaked at this temperature in an HF atmosphere for 4 hr. The prereacted RAP material was then zone refined in a graphite boat under argon atmosphere at a temperature of 850°C and a zone rate of 3 mm/hr. DTA (Differential Thermal Analysis) measurements displayed narrow and single melting and solidification peaks indicative of congruent melting and single phase nucleation.

2.2. X-Ray and Neutron Diffraction

A small fragment from a large, zone-melted LiCaCrF₆ single crystal was selected for the single-crystal X-ray diffraction study. Larger parts of the same crystal were powdered to a grain size smaller than 30 μ m to minimize effects of preferred orientation, and were sealed under helium in the 8 \times 50-mm cylindrical vanadium sample con-

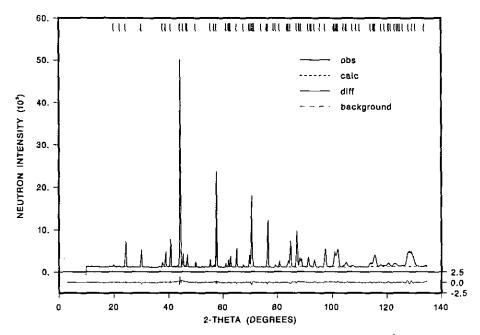


Fig. 1. Neutron powder diffraction pattern of LiCaCrF₆ (295 K, $\lambda = 1.7012$ Å). (—) Observed, (—) calculated, (—) difference, and (——) background values.

tainer used in the neutron diffraction experiment.

The single crystals were initially oriented along [001] and were examined by means of Cu $K\alpha$ Weissenberg photographs. X-ray intensity data were collected on an automatic Stoe 4-circle diffractometer in one hemisphere of the reciprocal space (sin $\theta/\lambda \le 0.8 \text{ Å}^{-1}$) using monochromatized Mo $K\alpha_1$ radiation (for details refer to Table I). Precise cell constants were obtained by least-squares refinement (9) of Guiner powder film data (≥20 reflections, focusing 114mm Guinier-Huber camera, monochromatized Cu $K\alpha_1$ radiation). High-purity germanium (99.9999%, $a_0(293 \text{ K}) = 5.657906$ A) was added to the sample powder as an internal calibration standard.

Neutron diffraction data were collected at 295 K on the DMC multidetector powder diffractometer (10) at the 10 MW SAPHIR reactor in Villigen, PSI, Switzerland (LN₂-cooled Si filter, vertically focusing Ge (311) monochromator, collimation 10'/-/12', wavelength 1.7012(5) Å). The diffrac-

tion patterns were refined employing the Rietveld method (11) using a modified code by Hewat (12) including options for anisotropic temperature factor refinement. Neutron scattering lengths and absorption cross sections were taken from a recent compilation by Sears (13); no absorption correction had to be applied for LiCaCrF₆.

2.3. X-Ray Absorption

Chromium K-edge EXAFS spectra were recorded on beamline X-11A at the Brookhaven National Synchrotron Light Source. The X-ray storage ring was operated at 2.53 GeV with electron beam currents of 120 to 160 mA. Silicon (111) monochromator crystals were used in combination with entrance slit widths of 0.5 mm, providing an energy resolution of about 0.5 eV at 5.7 keV. Powders of sample material were sealed in Kaptan tape or prepared as DUCO films to obtain transmission samples of uniform thickness corresponding to 1 to 2 absorption lengths. The LiCaCrF₆ sample was examined in conventional transmission geometry

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TABLE II
STRUCTURAL PARAMETERS OF LiCaCrF ₆ AT ROOM TEMPERATURE AS OBTAINED FROM NEUTRON POWDER
Profile Analysis

		Spa	ace group $P\overline{3}1c$ (N	No. 163)		
Atom	Position	x	y	z	В	n
Ca		0	0	0	0.54(11)	1.92(5)
Li	2c	1/3	2/3	1/4	0.57(26)	2.01(7)
Cr	2d	2/3	1/3	1/4	0.57(14)	2.00^{a}
F	12i	.3662(3)	.0192(4)	.1405(1)	0.93(03)	11.85(18)
	•					
		Sp	ace group P31c (N	Vo. 159)		
Atom	Position	Sp:	ace group P31c (N	No. 159) z	В	n
Atom Ca	Position 2a	•	ace group P31c (N	No. 159) z .0000 ^a	0.39(12)	n 1.90(5)
		x	у	z		
Ca	2 <i>a</i>	0	0 y	.0000 ^a	0.39(12)	1.90(5)
Ca Li	2a 2b	0 1/3	0 2/3	.0000° .2561(81)	0.39(12) 0.64(30)	1.90(5) 1.99(7)

Note. Numbers in parentheses give σ of the last significant digits of refined parameters; reliability factors were evaluated as defined in Ref. (23). Data for the centrosymmetric spacegroup $P\overline{3}Ic$ (No. 163) as well as for P31c (No. 159) are listed for comparison. A significance test evaluating the differences in the profile description revealed that the acentric model is not significantly better beyond a significance level of 70%. Neutron wavelength $\lambda = 1.7012$ Å. Units for B: Å², isotropic temperature factors of the form $e^{(-B_{liso}\sin^2\theta/\lambda^2)}$. Cell constants (Å): a = 5.1054(8), c = 9.7786(10).

(high Cr concentration) and the 3% Cr-doped LiCaAlF₆ in fluorescence mode (14) using a Lytle-type (15) detector. Chromium (1- μ m Cr on Al foil) was simultaneously scanned as an energy calibration reference during each measurement.

3. Results and Discussion

3.1. Crystal Structure of LiCaCrF₆

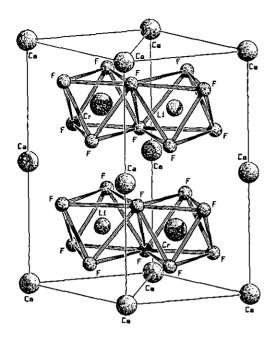
Weissenberg [001] photographs revealed trigonal, high Laue symmetry and the only extinction observed for $(hh2\bar{h}l) = 2n + 1$ indicated P31c (No. 159), and $P\bar{3}1c$ (No. 163) as the possible space groups. A first structural model was obtained using direct methods. As the statistical tests indicated the absence of a center of symmetry, the structural model was initially refined in the noncentrosymmetric space group P31c em-

ploying the STRUCSY program package (16).

 R_F -values at this stage were not better than $R_F = 0.053$ and $R_w = 0.040$, essentially confirming the atom arrangement as derived for centrosymmetric LiCaCrF₆. The lowscattering Li atoms were not convincingly revealed from a difference Fourier map $(F_{\text{obs}} - F_{\text{CaCrF}_6})$; however, when placed in the central voids of the F₆-octahedra, the Li atoms adopted reasonable isotropic temperature factors and a significant deficiency on one of the F sites $(n_{occ} = 0.89)$ was observed. The low residual values are in contrast to the statement of Viehbahn that a model derived from a double stacking of a Li₂ZrF₆-type cell (17) with alternate Li and Al (or Li and Cr) ordering a priori excludes the noncentrosymmetric space group P31c.

Despite the statistical tests being in favor of a noncentrosymmetric structure, the re-

^a When refined individually, these parameters remained within less than one σ . They were thus held fixed in subsequent refinement cycles.



Ftg. 2. Crystal structure of LiCaCrF₆ which can be described as a network of MeF_6 octahedra with a varying degree of distortion (shown in Table III). The CaF₆ octahedral network is omitted to better emphasize the larger LiF₆ and smaller CrF₆ octahedra. Drawing by the SCHAKAL program (25) based on crystal data from this work.

finement in $P\overline{3}1c$ as isotypic with LiCaAlF₆ arrived at marginally improved residual values $R_F = 0.045$ and $R_w = 0.036$. The geometrical deviations of the two independent fluorine atoms $(6c_1$ and $6c_2)$ in P31c from their ideal position (12i) in $P\overline{3}1c$ are very small and do not appear to justify a loss of centrosymmetry. In addition, refinement of the Ca and F atoms revealed no significant deviations from a full occupancy in the centrosymmetric case (see Table I for a complete listing of positional and thermal parameters).

In order to confirm and complement the structural information derived from our X-ray work (especially in regard to the Li atoms, which were not directly accessible in the X-ray single-crystal study) we recorded additional neutron diffraction powder profiles. As the negative neutron scattering length of Li critically determines the accu-

racy of the refinement of the Li positions, we verified the Li isotope ratio in our samples (and starting material) by means of secondary ion mass spectroscopy (SIMS). We obtained a relative isotope abundance of 8.74(36)% for ⁶Li and of 91.26(36)% for ⁷Li. Combining the individual scattering lengths for each isotope, an average scattering length \bar{b} of -1.85(3) fm results. This value was used in the profile refinement.

The neutron diffraction profiles (Fig. 1) were refined either in the centrosymmetric space group $P\overline{3}1c$ or in the noncentric in P31c (see Table II for a comparison of the refinement results). In either refinement, all occupational factors remained within less than 2σ of the full occupation (the minute underoccupation at the Ca site is associated with a matching deficiency at the fluorine sites and thus the crystal's charge remains balanced) and both the deviation of the Li z-parameter from its ideal position and the splitting of fluorine 12i into two 6c positions are marginal. In addition, a significance test evaluating the differences in the profile description (18) confirmed that the acentric model is not significantly better beyond a confidence level of about 70%. In accordance with the single-crystal X-ray data, we find thus little justification to presume the acentric space group P31c.

3.2. EXAFS Spectroscopy of Chromium Sites

The local Cr environment in very lightly doped (3%) LiCaAlF₆: Cr³⁺ cannot directly be accessed by diffraction methods. In this case EXAFS spectroscopy (19) provides a tool to investigate local-site geometry and site-specific chemistry of the chromium ion. In order to extract bond distances from the measured EXAFS signal, the phase shifts for the corresponding central atom and backscattering neighbor atoms must be known. These phase shifts can be obtained experimentally from suitable reference substances of known structure. CrF₃ contains chromium ions in an octahedral environ-

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TABLE III COORDINATION GEOMETRY AND DISTANCE OF FIRST TWO COORDINATION SHELLS IN LiCaCrF₆, LiCaAlF₆, and CrF₃ ($R\overline{3}c$, Obverse Hexagonal Setting)

Compound	Central atom	Ligand atoms	Coord. No.	Distance (Å) ^a	Bond angles (±0.1°)	Coord. type ^b
LiCaCrF ₆	Cr (2d)	F (12i)	6	1.901	176.3, 86.1, 91.3	DO
-	Cr (2d)	Li (2c)	3	2.948	120.0	T
	Li (2c)	F (12c)	6	2.028	171.8, 79.5, 91.6, 94.7	Н
	Li (2c)	Cr (2d)	3	2.948	120.0	T
	Ca (2b)	F(12i)	6	2.282	180.0, 87.5, 92.5	DO
	Ca (2b)	F (12i)	6	3.562	180.0, 73.9, 106.1	TA
LiCaAlF ₆	Al (2d)	F (12i)	6	1.800	177.22, 87.2, 90.9, 91.2	DO
	A1 (2d)	Li (2c)	3	2.885	120.0	T
	Li (2c)	F (12c)	6	2.009	169.6, 76.3, 91.8, 96.4	Н
	Li (2c)	Al (2d)	3	2.885	120.0	T
	Ca (2b)	F(12i)	6	2.273	180.0, 86.7, 92.5	DO
	Ca (2b)	F (12i)	6	3.490	180.0, 74.7, 105.3	TA
CrF ₃	Cr (6b)	F (18e)	6	1.899	180.0, 89.8, 90.2	О
÷	Cr (6b)	Cr (6b)	6^{c}	3.927	180.0, 87.0, 93.0	TA

^a Due to the imperfect coordination geometry the distances vary slightly for different atoms in one coordination shell. A full listing of individual bond distances and angles and can be easily obtained using the SEXIE program (24).

ment (20) and could be considered a suitable reference substance. In rhombohedral CrF₃, though, the CrF₆-octahedra are connected via their corners, whereas in the complex fluorides of the LiCaAlF₆-type the octahedra share a common edge (Fig. 2). For this series of compounds, isotypic LiCaCrF₆ serves as an appropriate model substance. For a review of the stability of the different cation ordering in AMe^{II}Me^{III}F₆ fluorides as a function of cation size we refer the reader to a series of papers by Courbion and co-workers (see, e.g., Ref. 21).

We have listed bond distances, bond angles, and coordination information for LiCaCrF₆, LiCaAlF₆, and CrF₃ in Table III. From a comparison of the next nearest neighbor coordination around Al and Li in LiCaAlF₆ one can infer that the second shell looks different depending on whether Cr

substitutes an Al or a Li atom, respectively: The second coordination shell comprises Li when Cr is located at an Al (2d) site, and Al when Cr occupies a Li (2c) position. The small difference in the scattering amplitudes between Li and Al in combination with a low coordination number of 3, however, did not suffice to permit a direct determination of the Cr location in LiCaCrF₆ by the EXAFS technique.

Nevertheless, the Cr-F distance (1.901 Å) and coordination information obtained from the LiCaCrF₆ neutron diffraction data could be used to derive an experimental phase shift for the Cr-F nearest neighbor shell in the X-ray absorption process. This phase shift was used in a phase-corrected Fourier transform for the Cr³⁺ site in LiCaAlF₆: Cr³⁺ to derive the actual Cr-F distance (Fig. 3). We find that the Cr-F distance of 1.89(8) Å in LiCaAlF₆: Cr³⁺ is prac-

^b O, nearly ideal octahedron; DO, slightly distorted octahedron; TA, trigonal antiprismatically distorted octahedron; H, severely distorted octahedron; and T, planar triangle.

^c The second C_r coordination shell in CrF₃ actually comprises an additional F₆ antiprismatic subshell at a slightly larger distance yielding a total coordination number of 12.

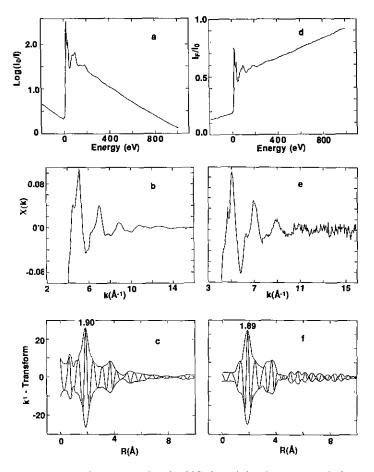


Fig. 3. EXAFS spectra and processed data for LiCaCrF₆ (left column, transmission technique) and LiCaAlF₆: Cr³⁺ (right column, fluorescence technique). (a,d) Experimental Cr K-edge EXAFS spectra; (b,e) extracted EXAFS signal plotted as $\psi(k)$ vs wave number k; (c,f) phase-corrected k^1 — Fourier transform of the extracted signal showing the radial distribution of scattering neighbor atom distances around the Cr center. The energy zero in (a,d) was determined by the first inflection point in the derivative spectrum of the Cr metal reference.

tically identical to the Cr-F distance found in the Cr-rich model compound (and in CrF₃ as well), indicating a very stable CrF₆ octahedral configuration in LiCa AlF₆: Cr³⁺ with little distortion even in the case of low chromium doping. The actual degree of the distortion cannot be determined, but from the data in Table III it becomes evident that the "softer" LiF₆ octahedra suffer the most distortion which allows the "harder" CrF₆ octahedra to assume a nearly ideal configuration. In addition to arguments from charge distribution

and optical spectroscopy (1), this strongly indicates that Cr in fact occupies the 2d (Al) sites in LiCaAlF₆: Cr^{3+} .

3.3. Solid Solution LiSr(Al,Cr)F₆

The existence of a solid solution in the pseudobinary LMHF system LiSr AlF₆-LiSrCrF₆ was first indicated by DTA and finally verified by X-ray diffraction. A complete analysis of the thermodynamic data and descriptions of the hydrofluorination process and single crystal growth are presented elsewhere (22). With the excep-

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TABLE IV
SELECTED CELL CONSTANTS OF FLUORIDES $LiMe^{II}Me^{III}F_{6}$ ($Me^{II}=Ca$, Sr; $Me^{III}=Al$, Cr) and of
$LiSrAl_{1-x}Cr_xF_6 (0 \le x \le 1)$

Compound formula	a (Å)	b (Å)	V (ų)	c/a	Ref.a
LiCaAlF ₆	4.996	9.636	208.3	1.929	
LiCaCrF ₆	5.095	9.720	218.5	1.908	3
LiCaCrF ₆	5.1042	9.7767	220.59	1.915	SX
LiCaCrF ₆	5.1054(08)	9.7786(10)	220.73(07)	1.9153(40	ND
LiSrCrF ₆	5.170	10.34	239.3	2.000	3
LiSrCrF ₆	5.1764(13)	10.3723(70)	240.69(20)	2.0038(14)	GN
LiSrAl _{0.2} Cr _{0.8} F ₆	5.1573(10)	10.3384(63)	238.13(17)	2.0046(13)	GN
LiSrAl _{0.4} Cr _{0.6} F ₆	5.1419(10)	10.3137(45)	236.16(14)	2.0058(10)	GN
LiSrAl _{0.6} Cr _{0.4} F ₆	5.1208(07)	10.2813(35)	233.48(10)	2.0078(07)	GN
LiSrAl _{0.8} Cr _{0.2} F ₆	5.1003(19)	10.2396(58)	230.68(21)	2.0076(14)	GN
LiSrAl _{0.96} Cr _{0.04} F ₆	5.0847(12)	10.2237(52)	228.91(16)	2.0107(11)	GN
LiSrAlF ₆	5.0838(13)	10.2184(31)	228.71(13)	2.0100(8)	GN
LiSrAlF ₆	5.084	10.21	228.54	2.008	. 3

Note. Numbers in parentheses give σ of the last significant digits.

tion of one procured "single crystal" with 4% Cr³⁺-doping, all samples were single phase and the powder diffraction intensities agreed well with those calculated assuming

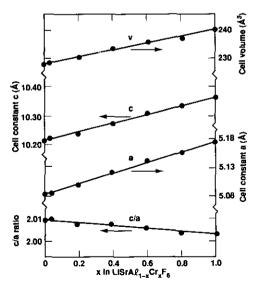


Fig. 4. Variation of cell dimensions vs chromium substitution in the pseudobinary system LiSr $Al_{1-x}Cr_xF_6$. No observable deviations from Vegard's law confirm the existence of an ideal solid solution.

the LiCaAlF₆ structure type. Cell constants of the solid solution were refined from the Guinier powder films and are listed in Table IV. No significant deviations from Vegard's law are displayed (Fig. 4) and a truly continuous solid solution exists. The increase of the cell constants with increasing substitution of Al with the larger Cr ions is about 20% more pronounced in the a direction (as indicated by the decreasing c/a ratio in Fig. 4) and can be interpreted in geometric terms: Along the c-axis the LiMe^{II}Me^{III}CrF₆ structure is to a large extent determined by the network of Me^{II}-(Ca) octahedra only, while in the a-direction both the Me^{II} and the Me^{I,III}-(Li,Al,Cr) octahedra contribute to the cell dimensions.

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^a SX, single-crystal X-ray data; ND, neutron powder diffraction; and GN, Guinier powder film technique; all obtained for this work.

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