# Synthesis and Characterization of Ternary Zinc-Antimony-Transition Metal Spinels

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Four series of ternary  $Zn_xMe_ySb_zO_4$  spinels, Me = Cr, Mn, Co, or Ni,  $y \le 0.778$ , have been prepared by solid state reaction from appropriate oxides. The spinels were characterized by the X-ray powder diffraction method. The efficiency of Me ions to form spinel structure measured by the temperature needed to obtain the pure spinel phase decreases in the order  $Cr \approx Mn > Co > Ni$ . The reaction temperature also becomes lower with increasing content of Me ions. The spinel lattice constants decrease linearly with increasing Me content, while the slope of curves depends on the ionic radii of Me ions. These results allow the lattice constant of more complex spinels to be estimated.

Crystal structures of  $(Zn_{1.000})[Zn_{0.633}Co_{0.700}Sb_{0.667}]O_4$ , a=0.85822(1) nm, and  $(Zn_{1.000})[Zn_{0.816}Cr_{0.778}Sb_{0.407}]O_4$ , a=0.84924(1) nm, spinels, where ( ) denotes tetrahedral and [ ] octahedral sites, are determined by Rietveld's method from X-ray powder diffraction data. The results show that Co(II), Cr(III), and Sb(V) are situated in the octahedral site. The tetrahedral site is occupied exclusively by Zn ions. The same cation distribution was postulated for all spinels. © 1994 Academic Press, Inc.

## INTRODUCTION

A large group of compounds with the general formula  $AB_2X_4$ , where A and B are different cations and X is an anion (usually oxygen), crystallize with the spinel (Sp) structure. These compounds are important not only as naturally occurring minerals, but also in many branches of solid state science.

Mixed oxides with Sp structure have very wide and diverse applications. They are known as pigments with high thermal and chemical stability suitable for coloring enamels and ceramics (1). Also, some Sp-type compounds are excellent refractory (2), magnetic (3), and catalytic materials (4, 5).

There are examples where Sp are components of some composite, multiphase systems. One such example is zinc oxide-based varistor ceramic which contains more than 10 mass% of Sp phase (6). Varistors are semiconductor electrical devices with nonlinear current–voltage characteristics having application as circuit protectors against transients and power overloads (7). The varistors are made by high-temperature (≥1200°C) sintering ZnO with small quantities of additives like oxides of Bi, Sb, Mn, Cr, Co, Ni, Si, and some other metals. The microstructure of varistors comprises ZnO grains, intergranular Bi<sub>2</sub>O<sub>3</sub>-rich phase, and Sp phase. In some cases a pyrochlore phase appears, as a minor constituent (8).

Because of system complexity the role of Sp phase in varistors is not very well understood. Possibly, the presence of Sp has an inhibiting effect on ZnO grain growth, thus raising the breakdown voltage of varistors (8). It is also assumed (9) that Sp phase interrupts the network of Bi<sub>2</sub>O<sub>3</sub>-rich phase, preventing the bypass current effect, which may degrade the nonlinearity.

There is general agreement that the formula of Sp phase in varistor ceramics is approximately Zn<sub>2,333</sub>Sb<sub>0,667</sub>O<sub>4</sub> (6, 10). However, this phase generally dissolves the other elements present in the system. For example, for a varistor system containing Bi<sub>2</sub>O<sub>3</sub>, Sb<sub>2</sub>O<sub>3</sub>, CoO, MnO, Cr<sub>2</sub>O<sub>3</sub>,

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and SiO<sub>2</sub>, as additives, it is suggested that all of Sb<sub>2</sub>O<sub>3</sub>, one-fourth of CoO, two-thirds of MnO, and five-sixths of Cr<sub>2</sub>O<sub>3</sub> added go into Sp phase (9). In the system containing NiO instead of SiO<sub>2</sub> (6), an electron-probe microanalysis showed the following composition of Sp phase: ZnO, 48-54.5%; Sb<sub>2</sub>O<sub>5</sub>, 33-35%; Cr<sub>2</sub>O<sub>3</sub>, 6-8%; MnO<sub>2</sub>, 2.5-3%; CoO, 1-1.5%; and NiO, 4-5% (the actual percentage depends on sintering conditions). Very similar composition was also reported by Bäther and co-workers (11).

Structural characteristics of Sp phase in varistors are not investigated in detail. It has been shown that the unit cell of Sp phase in real varistor samples is always smaller than the unit cell of Zn<sub>2,333</sub>Sb<sub>0,677</sub>O<sub>4</sub> (10-12).

In the present work, a systematic study of the ternary zinc-antimony-based spinels, where Zn or Zn and Sb are partially substituted by Cr, Mn, Co, or Ni ions, is described. In addition, crystal structures of  $(Zn_{1.000})$  [ $Zn_{0.633}Co_{0.700}Sb_{0.667}]O_4$  and  $(Zn_{1.000})$ [ $Zn_{0.816}Cr_{0.778}Sb_{0.407}]O_4$  spinels, where ( ) denotes tetrahedral and [ ] octahedral sites, are determined by Rietveld's method from X-ray powder diffraction (XRD) data.

#### **EXPERIMENTAL**

## Sample Preparation and Characterization

Besides the parent  $Zn_{2.333}Sb_{0.667}O_4$  spinel, four series of spinels with formula  $Zn_xMe_ySb_zO_4$ , where Me = Cr, Mn, Co, or Ni, have been prepared. Each series included three samples with gradually increasing content of Me ions (Table 1). In accordance with analytical data briefly discussed in the Introduction, Zn substitution was limited up to 30

| TABLE 1  |
|--|
| Composition, Final Synthetic Conditions, and Properties of Spinels |

|  | Thermal treatment, $t (^{\circ}C)/\tau (h)^{a}$ | •                  | Lattice parameter      |                            |
|--|---|--------------------|------------------------|----------------------------|
| Formula  |   | Color <sup>b</sup> | a <sub>obs</sub> (nm)  | $a_{\text{calc}}^{c}$ (nm) |
| Zn <sub>2,333</sub> Sb <sub>0.667</sub> O <sub>4</sub>                     | 900/3   | White              | 0.8594(1)              | 0.8594                     |
| Zn <sub>2 171</sub> Cr <sub>0.241</sub> Sb <sub>0.586</sub> O <sub>4</sub> | 1100/3  | Green              | 0.8564(1)              | 0.8555                     |
| Zn <sub>2.000</sub> Cr <sub>0.500</sub> Sb <sub>0.500</sub> O <sub>4</sub> | 1100/3  | Green              | 0.85259(7)             | 0.8526                     |
| $Zn_{1.815}Cr_{0.778}Sb_{0.407}O_4$  | 1100/3  | Green              | $0.8493(2)^d$          | 0.8488                     |
| Z <sub>Π2 171</sub> Mn <sub>0 241</sub> Sb <sub>0 586</sub> O <sub>4</sub> | 1100/3  | Brown              | 0.8573(1)              | 0.8574                     |
| Zn <sub>2,000</sub> Mn <sub>0,500</sub> Sb <sub>0,500</sub> O <sub>4</sub> | 1100/3  | Brown              | 0.8548(2)              | 0.8565                     |
| $Zn_{1.815}Mn_{0.778}Sb_{0.407}O_4$  | 1100/3  | Brown              | 0.8547(1) <sup>e</sup> | 0.8549                     |
| 1.515  | 1150/3  |                    | 0.8554(3)e             |                            |
|  | 1150/6  |                    | 0.85683(4)e            |                            |
| Zn <sub>2,100</sub> Co <sub>0,233</sub> Sb <sub>0,667</sub> O <sub>4</sub> | 1200/3  | Brown              | 0.8595(2)              | 0.8589                     |
|  |   |                    |                        | 0.8593                     |
| $Zn_{1.867}Co_{0.467}Sb_{0.667}O_4$  | 1150/8  | Brown              | 0.8587(2)              | 0.8587                     |
|  |   |                    |                        | 0.8592                     |
| $Zn_{1.633}Co_{0.700}Sb_{0.667}O_4$  | 1150/8  | Brown              | $0.8583(2)^d$          | 0.8580                     |
| •  |   |                    |                        | 0.8591 <sup>f</sup>        |
| Zn <sub>2,100</sub> Ni <sub>0,233</sub> Sb <sub>0,667</sub> O <sub>4</sub> | 1200/3  | Yellow-Green       | 0.8584(2)              | 0.8577                     |
| 2.700 0.255 0.007  |   |                    |                        | $0.8594^{f}$               |
| Zn <sub>1.867</sub> Ni <sub>0.467</sub> Sb <sub>0.667</sub> O <sub>4</sub> | 1200/3  | Yellow-Green       | 0.8573(1)              | 0.8563                     |
| •                                    |   |                    |                        | $0.8594^{f}$               |
| Zn <sub>1,633</sub> Ni <sub>0,700</sub> Sb <sub>0,667</sub> O <sub>4</sub> | 1150/3  | Brown-Green        | 0.8548(3)              | 0.8543                     |
| •••••  |   |                    |                        | $0.8594^{f}$               |
| $Zn_{1.991}Ni_{0.090}Co_{0.030}$<br>$Cr_{0.247}Mn_{0.090}Sb_{0.545}O_4$    | 1100/3  | Brown              | 0.8546(1)              | 0,8530                     |

<sup>&</sup>lt;sup>a</sup> Only the final values are listed (for explanation see Experimental).

<sup>&</sup>lt;sup>b</sup> With increasing content of transition metal the color becomes darker.

<sup>&</sup>lt;sup>c</sup> Lattice parameters calculated using "cation-anion" distances given by Poix (15, 16). The tetrahedral site is occupied exclusively by Zn ions.

<sup>&</sup>lt;sup>d</sup> Structural investigations using X-ray powder diffraction data were performed.

The pure Sp phase was not obtained.

<sup>&</sup>lt;sup>f</sup> Lattice parameters calculated as given in footnote c. The tetrahedral site is occupied by Co + Zn or Ni + Zn ions.

mole%. Formulas of spinels were calculated in accordance with atomic,

$$x+y+z=3,$$

and charge balance;

$$2x + 2y + 5z = 8$$
 (for Co and Ni spinels)  
 $2x + 3y + 5z = 8$  (for Cr spinels).

It is known that Mn in Sp structures can exist in various oxidation states (13). Preliminary investigation of Mn spinels showed that, no matter what initial stoichiometry was chosen, its unit cells are smaller than the unit cell of the parent spinel. Considering ionic radii of  $Zn^{2+}$  and different  $Mn^{n+}$  ions (14) such behavior is possible only if Mn occurs as  $Mn^{3+}$ ,  $Mn^{4+}$ , or the mixture of both ions. The presence of  $Mn^{3+}$  ions was postulated and the formulas of Mn spinels are calculated in the same manner as the formulas of Cr spinels.

One complex spinel with formula  $Zn_{1.991}Ni_{0.090}Co_{0.030}Cr_{0.247}Mn_{0.090}Sb_{0.545}O_4$  was also synthesized for comparison.

The samples are prepared from the following oxides: ZnO, Sb<sub>2</sub>O<sub>3</sub>, Cr<sub>2</sub>O<sub>3</sub>, MnO<sub>2</sub>, Co<sub>3</sub>O<sub>4</sub>, and NiO, all of reagent-grade quality. The oxides in appropriate molar ratio (for 3 g of sample) are homogenized by dry milling in agate mortar for 0.5 hr. Thermal treatment was as follows:

the samples in platinum or porcelain crucible were put in the cool furnace, heated in air up to  $1100^{\circ}$ C, kept 3 hr at this temperature, and furnace cooled. The samples were then examined by the X-ray powder diffraction technique on a Philips PW 710 automatic diffractomer using monochromated Cu $K\alpha$  radiation. If the pure Sp was not obtained the heating time was first prolonged and then the temperature was raised.

Synthetic conditions, color, and lattice parameters of spinels are listed in Table 1.

The lattice constants were calculated by least-square technique (Program LSUCRIPC) (17).

## XRD Data Collection and Structure Refinements

Experimental conditions and crystal data for the spinels investigated are listed in Table 2.

The refinements were made by Rietveld's method (18) using the DBWS-9006PC program (19) on an IBM PC AT compatible computer. The program minimizes the function  $\sum w_i(y_{io} - y_{ic})^2$ , where  $y_{io}$  and  $y_{ic}$  are the observed and calculated data points and  $w_i = 1/y_{io}$ . The data are not corrected for absorption and extinction. Preferred orientation is not detected. Peaks below 40°  $2\theta$  are corrected for asymmetry. Background was refined as a four-parameter function.

Structures of  $\text{Co}_3\text{O}_4$  and  $\text{NiCo}_2\text{O}_4$  spinels (20) were taken as the starting model: Zn1 is fixed at  $\frac{1}{8}$ ,  $\frac{1}{8}$ ,  $\frac{1}{8}$  (8a position), Zn2 and the other metal ions are fixed at  $\frac{1}{2}$ ,  $\frac{1}{2}$ ,

TABLE 2 Experimental Conditions and Crystal Data for  $(Zn_{1.000})[Zn_{0.633}Co_{0.700}Sb_{0.667}]O_4$  and  $(Zn_{1.000})[Zn_{0.815}Cr_{0.778}Sb_{0.407}]O_4$  Spinels

|   | Co spinel                                | Cr spinel  |  |
|---|--|------------|--|
| Diffractometer  | PW1710                                   |            |  |
| X-ray tube  | Cu LFF, 40 kV, 30 mA                     |            |  |
| Wavelength (nm)   | 0.15405, 0.15443                         |            |  |
| Profile range (°2θ)   | 10-120                                   |            |  |
| Step width (°2\theta)   | 0.025                                    |            |  |
| Step time (s)   | 5  |            |  |
| Peak range (number of FWHM) <sup>a</sup>  | 12.0                                     |            |  |
| Number of observations  | 4400                                     |            |  |
| Number of maxima in the examined $2\theta$ range                                | 70                                       | 69         |  |
| Space group   | te group $Fd3m$ , No. 227 (origin at cen |            |  |
| a (nm)  | 0.85822(1)                               | 0.84924(1) |  |
| $R_{\text{exp}} (=100 \cdot [(N-P)/\sum w_i y_{i0}^2]^{1/2})$                   | 9.17                                     | 8.88       |  |
| $R_{\rm p} = 100 \cdot \sum  y_{i0} - y_{ic} / y_{i0} $                         | 11.17                                    | 9.41       |  |
| $R_{wo} (= 100 \cdot [\sum w_i (y_{io} - y_{ic})^2 / \sum w_i y_{io}^2]^{1/2})$ | 14.94                                    | 13.74      |  |
| $R_{\rm B} = (100 \cdot \Sigma  I_{\rm o} - I_{\rm c} /\Sigma I_{\rm o})$       | 4.15                                     | 3.60       |  |
| $R_F (=100 \cdot \sum  F_0 - F_c /\sum F_c)$                                    | 3.22                                     | 3.21       |  |

<sup>&</sup>lt;sup>a</sup> FWHM is the full width at half-maximum of individual reflections and is given by a second-degree polynomial of the form FWHM<sup>2</sup> =  $Utg\theta^2 + Vtg\theta + W$ , where U, V, and W are empirical parameters to be refined in addition to the structural parameters and a background function.

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TABLE 3
Final Atomic Coordinates, Isotropic Thermal Parameters, and
Metal-Oxygen Distances (nm)

|             | x                     | у  | z                     | $B (\times 10^2 \text{ nm}^2)$ |
|-------------|-----------------------|--|-----------------------|--------------------------------|
|             | $(Zn_{1.000})[Zn_0]$  | . <sub>633</sub> Co <sub>0,700</sub> Sb <sub>0,667</sub> ] | $O_4$ , $a = 0.85822$ | (1) nm                         |
| O           | 0.2587(3)             | 0.2587(3)  | 0.2587(3)             | 0.74(9)                        |
| Zn1         | 0.1250                | 0.1250   | 0.1250                | 0.69(4)                        |
| Zn2         | 0.5000                | 0.5000   | 0.5000                | 0.68(3)                        |
| Co          | 0.5000                | 0.5000   | 0.5000                | 0.68(3)                        |
| Sb          | 0.5000                | 0.5000   | 0.5000                | 0.68(3)                        |
| Me-O        | distances             |  |                       |                                |
| Tetra       | ahedral               | 0.1992   |                       |                                |
| Octa        | hedral                | 0.2071   |                       |                                |
|             | $(Zn_{1,mn})[Zn_{0}]$ | 815CT0 778Sb0 407]1  | $O_4$ , $a = 0.84924$ | (1) nm                         |
| O           | 0.2593(2)             | 0.2593(2)  | 0.2593(2)             | 0.58(7)                        |
| Znl         | 0.1250                | 0.1250   | 0.1250                | 0.52(3)                        |
| Zn2         | 0.5000                | 0.5000   | 0.5000                | 0.50(2)                        |
| Cr          | 0.5000                | 0.5000   | 0.5000                | 0.50(2)                        |
| Sb          | 0.5000                | 0.5000   | 0.5000                | 0.50(2)                        |
| Me-O        | distances             |  |                       |                                |
| Tetrahedral |                       | 0.1971   |                       |                                |
| Octa        | hedral                | 0.2050   |                       |                                |

 $\frac{1}{2}$  (16d position), while coordinates of O atoms (u, u, u); position 32e) are varied with starting value 0.25. Occupation numbers were determined according to the formula

$$(Zn_{1.000})[Zn_{0.633}Co_{0.700}Sb_{0.667}]O_4$$
, bzw,  
 $(Zn_{1.000})[Zn_{0.816}Cr_{0.778}Sb_{0.406}]O_4$ .

Two profile shape functions, pseudo-Voigt and Pearson VII, are tested during refinement and both gave very similar R values. Results presented in Table 2 are for the pseudo-Voigt function. The functions are 46.8 and 47.2% Lorentzian for Co and Cr spinels, respectively.

A total of 17 parameters were varied in the last cycle of refinement ( $\Delta/\sigma < 0.05$ ). Final atomic coordinates, isotropic thermal parameters, and Me-O distances are summarized in Table 3.

After refinement several very weak peaks (I < 2.0%) with d values of 0.2940, 0.2509, 0.2347, 0.1601, and 0.1472 nm are located in the pattern of the Cr spinel. These peaks can be attributed to the trace of another Sp phase.

## RESULTS AND DISCUSSION

Stability and Lattice Constants of Spinel Phases

The data listed in Table 1 show that the mixed oxides with Sp structure are obtained in nearly all cases. The only exception is the sample with nominal composition Zn<sub>1.815</sub>Mn<sub>0.778</sub>Sb<sub>0.407</sub>O<sub>4</sub>. In contrast to the two Mn spinels with lower Mn content this sample contains a small

amount of  $Mn_2Sb_2O_7$  phase. The peak intensities of  $Mn_2Sb_2O_7$  phase gradually decrease from  $I_{max} = 3.0\%$  to  $I_{max} = 1.6\%$  with prolonged heat treatment. At the same time, an increase of the Sp lattice parameter was observed. Although not investigated in detail, such behavior could be explained by formation of a different Sp phase with the formula  $Zn_{1.815}Mn_p^2+Mn_q^3+Sb_rO_4$ .

The pure Zn<sub>2,333</sub>Sb<sub>0,667</sub>O<sub>4</sub> appears in two crystal modifications (21). According to Kasper (21) the compound Zn<sub>2,333</sub>Sb<sub>0.667</sub>O<sub>4</sub> with Sp structure was prepared at 900°C. Its lattice parameter (Table I) is in agreement with the Kaspers value (0.8597 nm), but it is higher than the value given in JCPDS file card 15-687 (a = 0.8585 nm; 22). The orthorhombic form named  $\beta$ -Zn<sub>2.333</sub>Sb<sub>0.667</sub>O<sub>4</sub> is stable between 960 and 1260°C. The cubic, i.e., spinel form, is stable below and above this range (21). In the present investigation the  $\beta$ -modification appeared only in the samples  $Zn_{2.100}Co_{0.233}Sb_{0.667}O_4$ ,  $Zn_{2.100}Ni_{0.233}Sb_{0.667}O_4$ , and  $Zn_{1.867}Ni_{0.467}Sb_{0.667}O_4$  heated at 1100 and 1150°C. It is evident (Table 1) that all ternary spinels were obtained within the range of stability of  $\beta$ -Zn<sub>2,333</sub>Sb<sub>0.667</sub>O<sub>4</sub>. These observations confirm Inada's conclusion (12) that dissolved ions stabilize Sp modification of Zn<sub>2,333</sub>Sb<sub>9,667</sub>O<sub>4</sub>. This also explains why  $\beta$ -modification is never observed in the real varistor samples.

The data (Table 1) show that the temperature needed for the complete reaction is lowered with increasing content of Me ions. However, the efficiency of transition metals decreases in the order  $Cr \approx Mn > Co > Ni$ , i.e. the more charged and smaller ions are more efficient. The introduction of only 0.029 mol of  $Cr^{3+}$  ions into the parent spinel (in an additional experiment) also yielded the pure Sp phase already at 1100°C. Therefore, it seems that  $Cr^{3+}$  ion has the greatest stabilizing effect in the systems examined.

Lattice parameters of Sp phases are shown in Fig. 1. Values of a and their changes within individual series for Ni, Mn, and Cr spinels are in accordance with ionic radii (14–16, 23).

Shannon's ionic radius for Co<sup>2+</sup> is bigger than the radius of Zn<sup>2+</sup> (0.0745 vs 0.074 nm, respectively) (14). However, our experimental results indicate that Shannon's ionic radius for Co<sup>2+</sup> is not valid for Sp-type structures. This is in agreement with other authors' data (15, 16, 23).

With the exception of the sample with nominal composition  $Zn_{1.815}Mn_{0.778}Sb_{0.407}O_4$  (see above) all experimental values of a lie on the straight line (Fig. 1). The correlation coefficients (R) obtained by linear regression analysis are better than 0.97 for Mn, Ni, and Cr spinels. The value of R is somewhat smaller (0.92) for Co spinels. This is probably due to the very close values for Zn and Co ionic radii.

Calculated lattice constant (a = 0.8512 nm) for  $Zn_{1.000}Ni_{1.333}Sb_{0.667}O_4$  spinel, derived by extrapolation of our experimental data shows reasonable fit with the re-

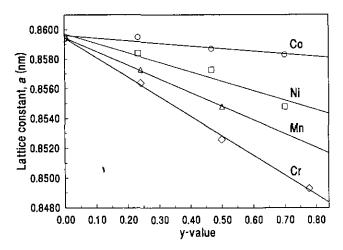


FIG. 1. Lattice parameters of spinels  $Zn_xMe_ySb_zO_4$  (Me=Cr, Mn, Co, and Ni). The data for the sample with a nominal composition  $Zn_{1.815}Mn_{0.778}Sb_{0.407}O_4$  (Table 1) are not included.

ported value a = 0.8516 nm (21). Also, the estimated value a = 0.8593 nm for the spinel  $Zn_{2.167}Co_{0.167}Sb_{0.667}O_4$  agrees well with the value a = 0.8590 nm published earlier (21).

Structures of 
$$(Zn_{1.000})[Zn_{0.633}Co_{0.700}Sb_{0.667}]O_4$$
 and  $(Zn_{1.000})[Zn_{0.815}Cr_{0.778}Sb_{0.407}]O_4$  Spinels

Because of its completed d-shell ( $d^{10}$  electronic configuration) cation  $Zn^{2+}$  has no ligand field stabilization energy (24). However, it has been shown (25–27) that the  $Zn^{2+}$  ion in spinels has very large tetrahedral site preference. On the other hand, practically all Cr(III) compounds are hexacoordinate with octahedral geometry (28) and  $Cr^{3+}$  ion has the largest octahedral site preference of the considered ions in Sp structures. The ions  $Mn^{3+}$  and  $Ni^{2+}$  also have relatively high octahedral site preference energy. However,  $Co^{2+}$  belongs to the ions with small octahedral site preference (25, 27), or even to the ions with tetrahedral site preference (26). To our knowledge, site preference energy of Sb(V) species has not been investigated. However, in all antimony(V)–oxygen systems SbO<sub>6</sub> octahedra were found (29).

From the preceding discussion it follows that the total occupancy of tetrahedral sites by Zn<sup>2+</sup> ions could be expected with a high probability in all Mn, Cr, and Ni spinels and with a low probability in Co spinels. Thus, Co and Cr spinels are the end members in the series and it was reasonable to choose them for more detailed crystallographic investigation.

The results of structure refinement are listed in Table 3. In the normal  $Me^{2+}Me_2^{3+}O_4$  spinel, 32 oxygen anions and 24 (8 + 16) cations form the unit cell. Oxygen anions for the coordinate u = 0.25 build up a cubic close packed array and a regular tetrahedral coordination polyhedron about an 8a site and a regular octahedron about a 16d site

(23, 30). In this case the octahedral cation—anion distance is 1.155 times larger than the corresponding tetrahedral distance. As u increases, the oxygens displace along the [111] direction, causing the tetrahedral site to enlarge at the expense of the octahedral site. The cation—anion distances, d, are given by (23)

$$d_{\text{tet}} = a\sqrt{3}(u - \frac{1}{8})$$
$$d_{\text{oct}} = a(3u^2 - 2u + \frac{3}{8})^{1/2}.$$

In our examples, calculated  $d_{\text{tet}}$  and  $d_{\text{oct}}$  are 0.1987 and 0.2074 nm for Co spinel and 0.1975 and 0.2047 nm for Cr spinel. These values are in good agreement with experimental values given in Table 3.

The coordinates of O atoms (Table 3) are close to the values found in some  $\mathrm{Mn_{1+2x}Cr_{2-3x}Sb_xO_4}$  (0.05  $\leq x \leq$  0.30) spinels (31) and in  $\mathrm{NiCo_2O_4}$  (21). They are also identical within  $3\sigma$  limits. Therefore, the decreasing of lattice parameters reflects the decreasing of the Me-O distances in tetrahedral and octahedral sites. In the case of Cr spinel the Me-O distances correspond to the values given by Poix (15, 16) ( $d_{\mathrm{oct}}$  calculated as the mean value for the present ions). For Co spinel the observed  $d_{\mathrm{tet}}$  is longer and  $d_{\mathrm{oct}}$  is shorter than the calculated value.

#### Cation Distribution

The cation distribution was checked in the course of the crystal structure refinement. The XRD data for Cr spinel clearly confirmed the presence of Cr<sup>3+</sup> and Sb<sup>V</sup> species in the octahedral sites. The other combinations of site occupancy yielded nonpositive definite thermal parameters of some ions.

The cation distribution in Co spinel was tested in two ways. If the occupation numbers are fixed in accordance with the formula  $(Zn_{0.300}Co_{0.700})[Zn_{1.333}Sb_{0.667}]O_4$  somewhat higher  $R_p$  and  $R_{wp}$  values (12.87 and 16.70%) and much higher  $R_B$  and  $R_F$  (9.30 and 6.01%) were obtained after refinement. On the other hand, when occupation numbers are varied during refinement, least squares converged with tetrahedral site totally occupied with  $Zn^{2+}$  ions. Both results confirm the octahedral position of  $Co^{2+}$  ions.

The cation distribution was also tested by calculation of lattice parameters from tetrahedral and octahedral Me-O bond distances listed by Poix (15, 16). Using the invariant character of the "cation-anion" distance Poix established the equation

$$a = 2.0995 d_{\text{tet}} + [5.8182(d_{\text{oct}})^2 - 1,4107(d_{\text{tet}})^2]^{1/2},$$

which should be valid for all Sp-type structures. This equation was first tested on the parent Zn<sub>2.333</sub>Sb<sub>0.667</sub>O<sub>4</sub>

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spinel. It was found that the Sb-O distance given by Poix (0.1895 nm) is too short. In order to obtain better agreement between the observed and calculated a-value we used 0.1980 nm for the Sb-O bond distance [which actually is the sum of Shannon's ionic radii for Sb(V) and  $O^{2-}$ ]. Then the lattice parameters for all synthetized spinels were calculated given the assumption that the tetrahedral site is occupied exclusively by  $Zn^{2+}$  ions. It can be seen from data listed in Table 1 that the differences between  $a_{\rm obs}$  and  $a_{\rm calc}$  are in the most cases less than 0.001 nm (a maximum value is 0.0017 nm).

As a consequence of the strong octahedral preferences of  $Cr^{3+}$  and  $Mn^{3+}$  ions the corresponding tetrahedral  $Me^{3+}$ -O distances are not known. Therefore, the other possible Me cation distribution,  $(Me_yZn_{1-y})[Zn_{x-1+y}Sb_z]O_4$ , was tested only for Co and Ni spinels. The calculated a-values for all Ni spinels are identical (Table 1), which is not in agreement with the experimental values. As stated above the radii of  $Zn^{2+}$  and  $Co^{2+}$  ions are very close and the calculated a-values for different cation distributions are very similar. This means that the choice between different cation distributions is possible only from the results of XRD data.

The results presented strongly support supposed cation distribution  $(Zn_1)[Zn_{x-1}Me_ySb_z]O_4$ . The fact that lattice parameters depend linearly on spinel composition also confirms the same cation distribution within each series.

#### CONCLUDING REMARKS

These results enable the use of the curves in Fig. 1 for the characterization of Zn<sub>2.333</sub>Sb<sub>0.667</sub>O<sub>4</sub> spinel doped with various Me ions (Me = Cr, Mn, Co, or Ni). By assuming that the contribution of each ionic species to the lattice parameter of resulting Sp phases is additive, it could be possible to estimate lattice constants of more complex spinels with similar composition. For example, the estimated value for Zn<sub>1.991</sub> Ni<sub>0.090</sub>Co<sub>0.030</sub>Cr<sub>0.247</sub>Mn<sub>0.090</sub>Sb<sub>0.545</sub>O<sub>4</sub> spinel (0.8547 nm) is in excellent agreement with the experimental value (Table 1). We suppose that with a known composition of initial varistor mixture and an experimentally determined lattice constant of resulting Sp phase in sintered material, it will be possible to estimate the

composition of Sp phase. This will be the object of our future studies.

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