

## Phase Relations of $\text{NH}_4\text{ClO}_4$ and $\text{NH}_4\text{BF}_4$ to High Pressures

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The high pressure phase diagrams of  $\text{NH}_4\text{ClO}_4$  and  $\text{NH}_4\text{BF}_4$  were studied by means of differential thermal analysis and volumetric techniques. The high temperature portions of these diagrams are intermediate between those of the corresponding potassium and rubidium salts, but at low temperatures the onset of hydrogen bonding causes the appearance of phases which are unique to the ammonium compounds.

### Introduction

The high pressure polymorphism of the univalent perchlorates was first studied by Bridgman (1) to 50 kbar and  $\sim 100^\circ\text{C}$ . There have been recent studies of the complete phase diagrams to  $\sim 40$  kbar of  $\text{NaBF}_4$ ,  $\text{NaClO}_4$  (2),  $\text{KClO}_4$ ,  $\text{KBF}_4$  (3),  $\text{RbClO}_4$ ,  $\text{RbBF}_4$  (4),  $\text{CsClO}_4$  and  $\text{CsBF}_4$  (5).

$\text{NH}_4\text{ClO}_4$  II and  $\text{NH}_4\text{BF}_4$  III under ambient conditions have the barite structure and are, therefore, isostructural with the ambient modifications of the corresponding potassium, thallous, rubidium and cesium salts (6), as well as with  $\text{NaClO}_4$  III and  $\text{NaBF}_4$  IV (2). These phases transform to cubic modifications (6) with the space group  $Fm\bar{3}m$  (2) at elevated temperatures. The disorder in the structure is not caused by free rotation of the anions, but is of a type which maximizes the cation-oxygen (or cation-fluorine) distances. This transition occurs at  $240^\circ\text{C}$  for  $\text{NH}_4\text{ClO}_4$  (7) and at  $199^\circ\text{C}$  for  $\text{NH}_4\text{BF}_4$  (8). For  $\text{KBF}_4$  (3) and  $\text{RbBF}_4$  (4), this phase transforms at still higher temperature and pressure to another modification which was suggested (4), on the basis of entropy considerations, also to be cubic, space group  $Fm\bar{3}m$ , and perhaps possessing the anti- $\text{NH}_4\text{Cl}$  structure (9, 10). In the case of  $\text{CsBF}_4$ , phase transitions to two other phases,  $\text{CsBF}_4$  V and  $\text{CsBF}_4$  VI, occur with probably free rotation of the anion tetrahedra in the  $\text{CsBF}_4$  V modification (5). No corresponding high temperature transitions could be found for the perchlorates of potassium, rubidium, and cesium due to thermal instability of the compounds in the range where such modifications might be expected.

Stammler *et al.* (11) reported a phase transition near  $-190^\circ\text{C}$  for both  $\text{NH}_4\text{BF}_4$  and  $\text{NH}_4\text{ClO}_4$  on the basis of changes in unindexed X-ray powder patterns. The heat capacity data for  $\text{NH}_4\text{ClO}_4$  (12) and  $\text{NH}_4\text{BF}_4$  (13) do not support the above results, however. Caron *et al.* (14) reported a subtle structural change within the orthorhombic system for  $\text{NH}_4\text{BF}_4$  at some temperature above  $-132^\circ\text{C}$ , which correlates with a rotational peak in the heat capacity curve of  $\text{NH}_4\text{BF}_4$  (13). Van Rensburg (15) found a transition near  $-190^\circ\text{C}$  for  $\text{NH}_4\text{ClO}_4$  and two transitions near  $-190^\circ\text{C}$  and  $-95^\circ\text{C}$  for  $\text{NH}_4\text{BF}_4$  by means of infrared spectroscopy. The transition at  $-95^\circ\text{C}$  was confirmed by means of single-crystal X-ray analysis.

### Experimental

$\text{NH}_4\text{ClO}_4$  with a purity of 99+ % was obtained from B.D.H. Technical grade  $\text{NH}_4\text{BF}_4$ , also obtained from B.D.H., was purified by recrystallization from an aqueous solution and thorough drying before use.

Pressures up to 40 kbar were generated in a piston-cylinder apparatus (16, 17). Phase changes were studied by means of differential thermal analysis (DTA) (16, 18) using Chromel-Alumel thermocouples. Heating/cooling rates were in the order of  $0.3\text{--}1.4^\circ\text{C}/\text{sec}$ . The detailed experimental procedure has been described elsewhere (4, 5). Phase boundaries were taken to be the mean of the heating and cooling temperatures and were based on several consistent runs. The observed boundaries are believed to be

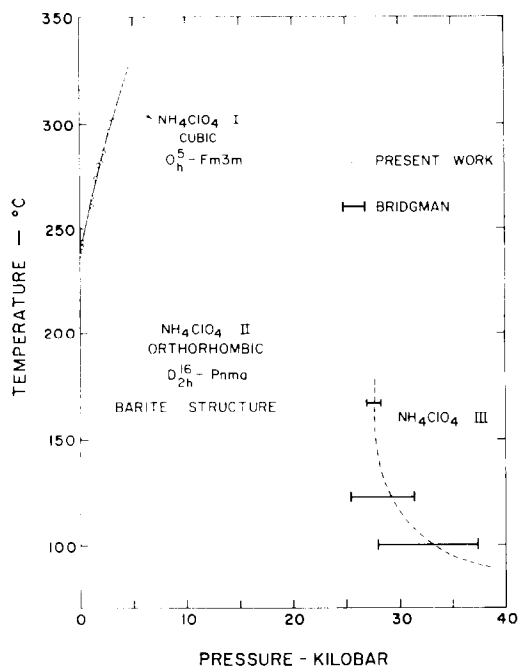


FIG. 1. Phase diagram of  $\text{NH}_4\text{ClO}_4$  to 40 kbar.

within  $2^\circ\text{C}$  and 0.5 kbar. High pressure phase changes were studied by means of volume displacement (5, 19) and piston-rotation techniques (17), also previously described (4).

**Results**

**Ammonium Perchlorate**

The phase diagram of  $\text{NH}_4\text{ClO}_4$  is shown in Fig. 1. The II/I transition yielded strong and clear signals at atmospheric pressure (Fig. 2(vi)). The dependence of the II/I transition temperature at atmospheric pressure on the heating/cooling rate is shown in Fig. 3. The transition temperature was found to be  $238.1 \pm 1.0^\circ\text{C}$ , being the mean of 18 determinations, as compared to the literature value of  $240^\circ\text{C}$  (8). The transition was followed to  $\sim 4$  kbar and  $300^\circ\text{C}$ .  $\text{NH}_4\text{ClO}_4$  exploded violently in the range  $330\text{--}350^\circ\text{C}$  at 2–3.6 kbar, although at atmospheric pressure it is known to explode only at  $\sim 440^\circ\text{C}$  (20, 21). The transition signals, though still clear, became smaller and broader at higher pressures. This is due to the large volume change upon transition, which causes a local pressure increase at

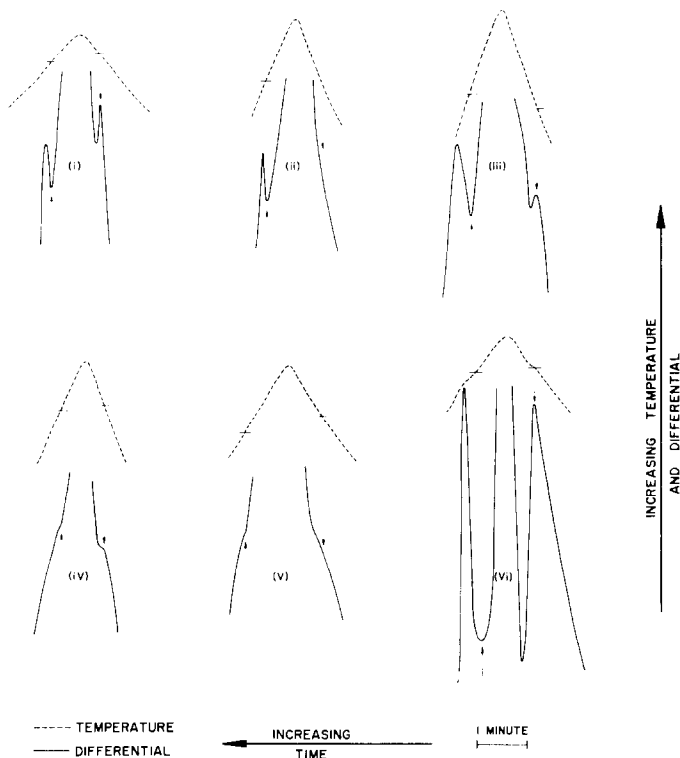


FIG. 2. Typical DTA signals obtained: (i)  $\text{NH}_4\text{BF}_4$  III/II at 0 kbar,  $192.2^\circ\text{C}$  heating,  $186.7^\circ\text{C}$  cooling. (ii)  $\text{NH}_4\text{BF}_4$  II/I at 14.3 kbar, cooling at  $581.5^\circ\text{C}$ . (iii)  $\text{NH}_4\text{BF}_4$  I/liquid at 5.9 kbar,  $597.2^\circ\text{C}$  heating,  $607.1^\circ\text{C}$  cooling. (iv)  $\text{NH}_4\text{BF}_4$  VI/II at 11.25 kbar,  $471.0^\circ\text{C}$  heating,  $467.8^\circ\text{C}$  cooling. (v)  $\text{NH}_4\text{BF}_4$  VI/I at 21.1 kbar,  $625.3^\circ\text{C}$  heating,  $617.3^\circ\text{C}$  cooling. (vi)  $\text{NH}_4\text{ClO}_4$  II/I at 0 kbar,  $241.2^\circ\text{C}$  heating,  $238.4^\circ\text{C}$  cooling.

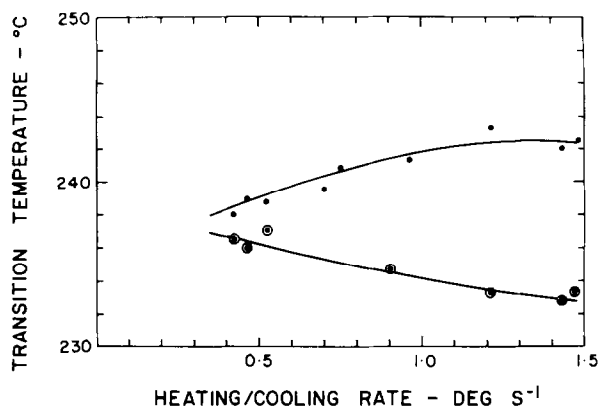


FIG. 3. Dependence on the rate of heating and cooling of the  $\text{NH}_4\text{ClO}_4$  II/I transition temperature at atmospheric pressure; ●—heating, ○—cooling.

the sample. No other transitions could be detected down to  $-150^\circ\text{C}$  at atmospheric pressure. The phase relations of  $\text{NH}_4\text{ClO}_4$  are summarized in Table I.

#### Ammonium Tetrafluoroborate

The phase diagram of  $\text{NH}_4\text{BF}_4$  is shown in Fig. 4. The  $\text{NH}_4\text{BF}_4$  III/II transition yielded sharp and clear DTA signals at atmospheric pressure (Fig. 2(i)). The signals became broader at higher pressures, as in the case of  $\text{NH}_4\text{ClO}_4$ , but remained clear. The  $\text{NH}_4\text{BF}_4$  III/II transition was less dependent on the heating/cooling rate than the corresponding  $\text{NH}_4\text{ClO}_4$  II/I transition (compare Figs. 3 and 5). The transition point at atmospheric pressure was  $188.8 \pm 0.5^\circ\text{C}$ , being the mean of 22 determinations.

This value is lower than the literature values of  $199^\circ\text{C}$  (8) and  $236^\circ\text{C}$  (11). The high literature values may be due to sublimation or decomposition known (22, 23) to occur when uncontained  $\text{NH}_4\text{BF}_4$  is heated above  $\sim 110^\circ\text{C}$ .

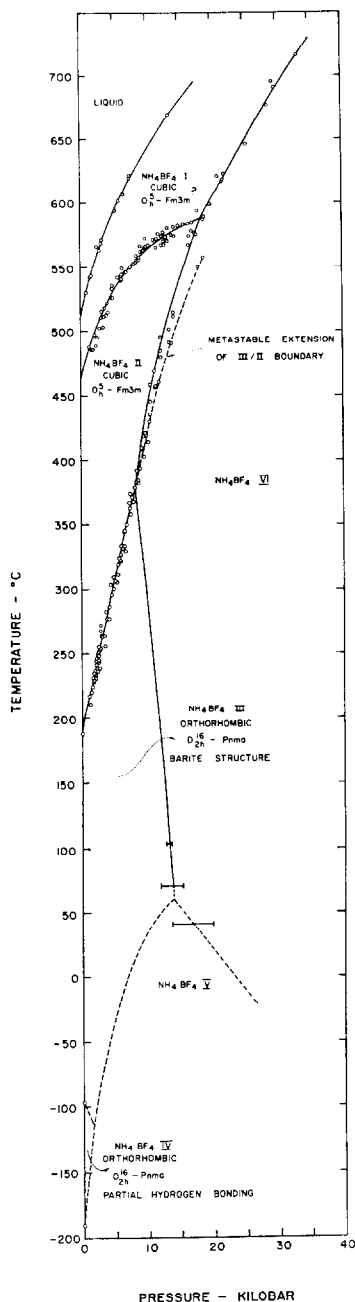
The III/II transition line rises steeply with pressure to a triple point  $\text{NH}_4\text{BF}_4$  III/II/VI at 8.3 kbar,  $379^\circ\text{C}$ , but it was possible to obtain several points on the metastable extension of the III/II phase boundary into the stability field of  $\text{NH}_4\text{BF}_4$  VI. The VI/II phase transition yielded broad DTA signals (Fig. 2(iv)) similar to those due to the III/II transition, and was terminated at a triple point  $\text{NH}_4\text{BF}_4$  VI/II/I at 18.3 kbar,  $587^\circ\text{C}$  with the appearance of a further new phase  $\text{NH}_4\text{BF}_4$  I. The VI/I transition yielded broad ill-defined DTA signals (Fig. 2(v)) which were difficult to measure accurately. The II/I transition, on the other hand, yielded only a broad inflection upon heating, but a clear and sharp signal upon cooling (Fig. 2(ii)). The II/I transition line is based only upon cooling points, and extrapolates to  $\sim 460^\circ\text{C}$  at atmospheric pressure.  $\text{NH}_4\text{BF}_4$  apparently decomposes at atmospheric pressure before this temperature is reached. For the same reason, no melting signals could be obtained at atmospheric pressure, but the melting curve of  $\text{NH}_4\text{BF}_4$  I at elevated pressures yielded sharp and clear DTA signals (Fig. 2(iii)). The melting curve extrapolates to  $\sim 510^\circ\text{C}$  at atmospheric pressure.

The  $\text{NH}_4\text{BF}_4$  III/VI phase transition, inferred above from the observation of a possible triple point III/II/VI, was confirmed by means of volume discontinuity. A typical plot of piston displacement

TABLE I  
PHASE RELATIONS OF  $\text{NH}_4\text{ClO}_4$  AND  $\text{NH}_4\text{BF}_4$

Transition line	Fit	Standard deviation
$\text{NH}_4\text{ClO}_4$ I/II	$t(^{\circ}\text{C}) = 21.6P + 238.1$	2.3 deg
$\text{NH}_4\text{BF}_4$ III/II	$t(^{\circ}\text{C}) = 189 + 24.7P - 0.221P^2$	0.37 kbar
$\text{NH}_4\text{BF}_4$ II/I	$t(^{\circ}\text{C}) = 460 + 18.5P - 1.02P^2 + 0.02P^3$	0.88 kbar
$\text{NH}_4\text{BF}_4$ I/liquid	$P/3.44 = (T/510)^{0.46} - 1$	2.7 deg
$\text{NH}_4\text{BF}_4$ VI/II	$t(^{\circ}\text{C}) = 379 + 30.4(P - 8.3) - 0.963(P - 8.3)^2$	0.4 kbar
$\text{NH}_4\text{BF}_4$ VI/I	$t(^{\circ}\text{C}) = 587 + 9.55(P - 18.3) - 0.056(P - 18.3)^2$	4.7 deg
<i>Triple point</i>	<i>Pressure (kbar)<sup>a</sup></i>	<i>Temperature (<math>^{\circ}\text{C}</math>)<sup>a</sup></i>
$\text{NH}_4\text{BF}_4$ VI/III/II	8.3	379
$\text{NH}_4\text{BF}_4$ I/VI/II	18.3	587
$\text{NH}_4\text{BF}_4$ VI/V/III	$\sim 14$	$\sim 56$
$\text{NH}_4\text{BF}_4$ V/IV/III	$\sim 3$	$\sim 120$

<sup>a</sup> The accuracy of the triple points is best judged from Fig. 4.


 FIG. 4. Phase diagram of  $\text{NH}_4\text{BF}_4$  to 40 kbar.

versus load is shown in Fig. 6. The volume change was found to be

$$\Delta V_{\text{VI/III}} = 0.9 \text{ cm}^3/\text{mole}$$

at 104° and 70.8°C. A run at 41.6°C, however, yielded a volume change of only 0.5 cm<sup>3</sup>/mole, and a transition pressure considerably higher than expected. This tentatively implies the possibility of

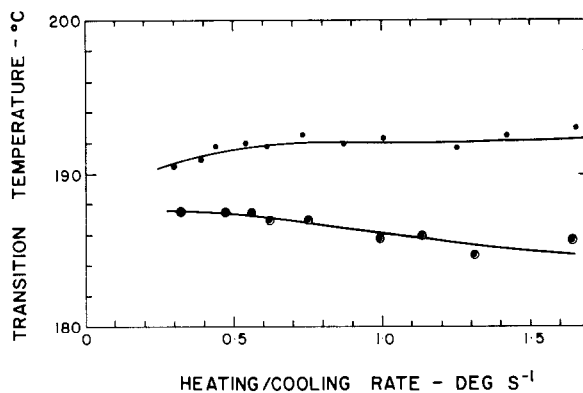


FIG. 5. Dependence on the rate of heating and cooling of the  $\text{NH}_4\text{BF}_4$  II/III transition temperature at atmospheric pressure; ●—heating, ○—cooling.

a further triple point near 14 kbar, 56°C, which will be further discussed below. No clear indications of a transition could be observed at 23°C. The transition pressures obtained by piston rotation are listed in Table II.

The phase relations of  $\text{NH}_4\text{BF}_4$  are summarized in Table I.

## Discussion

Van Rensburg (15) recently showed that  $\text{NH}_4\text{BF}_4$  IV, the phase stable between  $-95^\circ\text{C}$  and  $-190^\circ\text{C}$  at atmospheric pressure, is orthorhombic with the same space group as  $\text{NH}_4\text{BF}_4$  III. The structure of  $\text{NH}_4\text{BF}_4$  IV differs from that of  $\text{NH}_4\text{BF}_4$  III in that partial hydrogen bonds H—F exist, thereby distorting the barite structure slightly. Geometrical considerations prevent complete hydrogen bonding of all adjacent H—F pairs. Furthermore, the III/IV transition takes place with an increase in volume, i.e.,  $\text{NH}_4\text{BF}_4$  IV is  $\sim 1\%$  denser than  $\text{NH}_4\text{BF}_4$  III at the transition point. It is to be expected that  $\text{NH}_4\text{BF}_4$  V below  $-190^\circ\text{C}$  will exhibit complete hydrogen bonding of all adjacent H—F pairs, and that  $\text{NH}_4\text{BF}_4$  V will be denser than  $\text{NH}_4\text{BF}_4$  V at  $-190^\circ\text{C}$ . These results are in agreement with the present observation of a possible triple point  $\text{NH}_4\text{BF}_4$  VI/V/III near 14 kbar, 56°C. The difference of 0.4 cm<sup>3</sup>/mole between  $\Delta V_{\text{VI/III}}$  and  $\Delta V_{\text{VI/V}}$  implies that

$$\Delta V_{\text{V/III}} = 0.4 \text{ cm}^3/\text{mole}$$

near the  $\text{NH}_4\text{BF}_4$  VI/V/III triple point, and the dotted phase boundaries drawn in Fig. 4 become plausible. In particular, it is only possible to obtain a consistent phase diagram if the  $\text{NH}_4\text{BF}_4$  V/IV/III triple point is located below  $\sim 5$  kbar. This implies

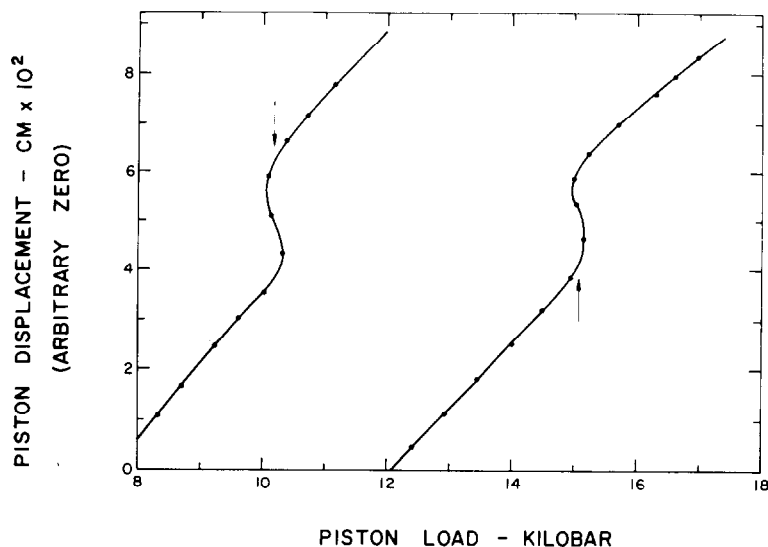


FIG. 6. Curves of piston displacement versus piston load for  $\text{NH}_4\text{BF}_4$  at  $104^\circ\text{C}$ , showing the III/IV transition. The S-shape of the curves may be due to nucleation phenomena.

that  $\text{NH}_4\text{BF}_4$  IV is more or less merely an intervening phase which is stabilized mainly by the interplay between thermal disorder, on the one hand, and the geometrical distortion caused by the tendency towards hydrogen bonding, on the other. This tendency can be expected to be somewhat weaker in  $\text{NH}_4\text{ClO}_4$ , and it is therefore not surprising that no phase similar to  $\text{NH}_4\text{BF}_4$  IV is found in the phase diagram of  $\text{NH}_4\text{ClO}_4$ . Instead, the transition from the barite-type structure to the, presumably, ordered hydrogen-bonded structure occurs directly as for  $\text{NH}_4\text{BF}_4$  above  $\sim 5$  kbar.

The  $\text{NH}_4\text{BF}_4$  V/VI transition is extremely sluggish even at  $41.6^\circ\text{C}$ , and becomes unobservable, as was the III/V transition, at room temperature. The III/VI transition, however, runs slowly, but with only a small region of indifference, at  $\sim 100^\circ\text{C}$ . Nevertheless, the fact that the metastable extension of the III/II phase boundary could be followed by means of rapid DTA methods to considerably

beyond the  $\text{NH}_4\text{BF}_4$  VI/III/II triple point indicates that even at this temperature the III/VI transition is still a slow phase change.

The slope of the  $\text{NH}_4\text{ClO}_4$  II/I transition line is  $21.6$  deg/kbar, which, together with the observed transition entropy, viz.,  $18.8$  J/mole-deg (24), yields

$$\Delta V_{\text{II/I}} = 4.1 \text{ cm}^3/\text{mole}$$

for the volume change upon transition. Due to the onset of sublimation even below the transition point, the entropy of the  $\text{NH}_4\text{BF}_4$  III/II transition is not known. However, the entropy of the corresponding transitions from barite-type to cubic  $Fm\bar{3}m$  is close to  $R \ln 8$  for  $\text{NH}_4\text{ClO}_4$  as well as the perchlorates and tetrafluoroborates of Cs, Rb, Tl and K, and it may be assumed that this is the case also for the  $\text{NH}_4\text{BF}_4$  III/II transition. The initial slope of the transition line is  $24.7$  deg/kbar, yielding, therefore,

$$(\Delta V_{\text{III/II}})_{P=0} = 4.3 \text{ cm}^3/\text{mole},$$

while at the  $\text{NH}_4\text{BF}_4$  VI/III/II triple point, with a slope of  $21.1$  deg/kbar and assuming that  $\Delta S_{\text{III/II}}$  still nearly equals  $R \ln 8$ ,

$$(\Delta V_{\text{III/II}})_{P=8.3 \text{ kbar}} = 3.7 \text{ cm}^3/\text{mole}.$$

The mean slope of the III/VI boundary is  $-56$  deg/kbar, and  $\Delta V_{\text{III/VI}} = -0.9$   $\text{cm}^3/\text{mole}$ . Therefore,

$$\Delta S_{\text{III/VI}} \simeq 1.7 \text{ J/mole-deg}$$

and, if we assume approximate constancy of the entropy changes along the transition lines,

$$\Delta S_{\text{VI/II}} \simeq 15.6 \text{ J/mole-deg}$$

TABLE II

TRANSITION PRESSURES AFTER PISTON ROTATION

Transition line	Upstroke pressure (kbar)	Downstroke pressure (kbar)	Temperature ( $^\circ\text{C}$ )
$\text{NH}_4\text{BF}_4$ III/VI	13.65	13.17	104.0
	15.49	12.09	70.8
$\text{NH}_4\text{BF}_4$ V/VI	20.04	13.77	41.6

and

$$(\Delta V_{\text{VI/II}})_{P=8.3\text{kbar}} \simeq 4.6 \text{ cm}^3/\text{mole}$$

from the additive relations at the triple point. The independent calculation from the initial slope of the VI/II transition line, viz., 30.4 deg/kbar, yields

$$(\Delta V_{\text{VI/II}})_{P=8.3\text{kbar}} \simeq 4.8 \text{ cm}^3/\text{mole}$$

in excellent agreement.

An extension of these arguments to involve  $\text{NH}_4\text{BF}_4$  I, while possible, is of little value in view of the experimental uncertainty in the slope of the VI/II phase boundary near the VI/II/I triple point. It is clear from Fig. 4, for instance, that this triple point could equally well be located as low as 17 kbar. This would markedly affect the curvature and final slope of the VI/II transition line.

The curvature of the melting curve of  $\text{NH}_4\text{BF}_4$  I suggests that a triple point  $\text{NH}_4\text{BF}_4$  VI/I/liquid may occur near  $\sim 50$  kbar, above which pressure  $\text{NH}_4\text{BF}_4$  VI will melt directly.

A comparison of the phase diagram of  $\text{NH}_4\text{BF}_4$  with that of, for instance,  $\text{KBF}_4$  (3),  $\text{RbBF}_4$  (4) or  $\text{CsBF}_4$  (5), reveals close similarities. Specifically, it would appear probable that  $\text{NH}_4\text{BF}_4$  I is a phase similar to  $\text{KBF}_4$  III,  $\text{RbBF}_4$  IV and  $\text{CsBF}_4$  I, while  $\text{NH}_4\text{BF}_4$  VI is similar to  $\text{RbBF}_4$  III and  $\text{CsBF}_4$  IV. The low temperature phases  $\text{NH}_4\text{BF}_4$  IV and V cannot, on the basis of the structural information (15), be expected to have counterparts in the phase diagrams of simpler tetrafluoroborates or perchlorates.

It is tempting to assume that the anomalous curvature of Bridgman's (1)  $\text{NH}_4\text{ClO}_4$  II/III transition line near  $100^\circ\text{C}$  is due to a triple point involving the phase found at atmospheric pressure below  $-190^\circ\text{C}$ . This is possible, but it should be kept in mind that no sudden decrease in the transition volume change was found in this case. Nevertheless, it would be surprising if  $\text{NH}_4\text{ClO}_4$  III prove to have a structure different from  $\text{NH}_4\text{BF}_4$  VI.

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sponsible for the manufacture of the furnace parts. Calculations were carried out on the IBM System 360/65 H of the National Research Institute for Mathematical Sciences.

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