

Topotactic Decomposition and Crystal Structure of White Molybdenum Trioxide-Monohydrate: Prediction of Structure by Topotaxy

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Single crystals of the white $\text{MoO}_3 \cdot \text{H}_2\text{O}$ modification (" α -molybdic acid") were transformed by heating to 160°C into perfect pseudomorphs built up from oriented MoO_3 crystallites of known structure. From the mutual orientation relationship of the unit cells of both phases involved in this topotactic reaction, as determined by X-ray photographs, a model for the so far unknown crystal structure of white $\text{MoO}_3 \cdot \text{H}_2\text{O}$ could be deduced.

Independently, this structure was determined by X-ray diffractometer data then: space group $P\bar{1}$, $a = 7.388$, $b = 3.700$, $c = 6.673 \text{ \AA}$, $\alpha = 107.8$, $\beta = 113.6$, $\gamma = 91.2^\circ$, $Z = 2$. The structure was solved from the Patterson function and refined until $R = 0.088$. It is built up from isolated double chains of strongly distorted $[\text{MoO}_5(\text{H}_2\text{O})]$ -octahedra sharing two common edges with each other.

This result agrees well with the model derived from topotaxy, and it becomes evident how the MoO_3 lattice is formed through corner linking of the isolated double chains after the water molecules are removed. The study of topotactic phenomena seems rather generally applicable to deduce the main features of structures involved and for better understanding of structural relationships.

Introduction

In an earlier investigation, the topotactic dehydrations of molybdenum trioxide-dihydrate and the yellow, monoclinic form of molybdenum trioxide-monohydrate have been followed by thermogravimetry, X-ray diffraction, infrared spectroscopy and scanning electron microscopy (1). It has been pointed out that another, white form of molybdenum trioxide-monohydrate is described in literature (2, 3), called $\alpha\text{-MoO}_3 \cdot \text{H}_2\text{O}$ when crystallized in well-shaped needles and $\beta\text{-MoO}_3 \cdot \text{H}_2\text{O}$ when the needle shape is less pronounced. As X-ray data of the " β -form" are missing, it may be suspected that it represents a microcrystalline variety of $\alpha\text{-MoO}_3 \cdot \text{H}_2\text{O}$.

Experimental Methods

For the preparation of $\text{MoO}_3 \cdot 2\text{H}_2\text{O}$, molybdenum trioxide has been dissolved in

concentrated hydrochloric acid, diluted and been kept for several days, following the preparation described by Carpéni (4). One batch of crystals of $\text{MoO}_3 \cdot 2\text{H}_2\text{O}$ was kept under the mother liquor for about three months, when the growth of bushels of white crystals could be observed (scanning electron micrograph see Fig. 1). These crystals have been identified as molybdenum trioxide-monohydrate by thermogravimetric determination of the weight loss (Mettler Thermoanalyzer TA 1) and powder X-ray diffraction (Guinier-de Wolff camera, CuK_α radiation) of the product of dehydration, anhydrous MoO_3 . They obviously represent the white, needle-shaped α -modification of $\text{MoO}_3 \cdot \text{H}_2\text{O}$. Single crystal X-ray diffraction patterns, although of quite poor quality, could be recorded by means of Buerger Precession and of Weissenberg cameras.



FIG. 1. Needles [010] of white molybdenum trioxide-monohydrate. Scanning electron micrograph ($\times 272$).

Crystallographic Data

Weissenberg photographs of various isolated single crystals show sharp, but elongated reflexions with a length of 3–30 mm, indicating “single crystals” built up from tilted subneedles (angle of tilt 6–60°). Nevertheless, the unit cell of the crystals could be determined: Triclinic, $a = 7.388 \text{ \AA}$, $b = 3.700 \text{ \AA}$, $c = 6.673 \text{ \AA}$, $\alpha = 107.8^\circ$, $\beta = 113.6^\circ$, $\gamma = 91.2^\circ$; b being parallel to the needle axis.

Topotactic Relations and Proposal of Crystal Structure

An oriented crystal has been decomposed on the goniometer head, without altering its

orientation, during 3–4 hr at 160°C. Weissenberg photographs of the product show it to be anhydrous MoO_3 , with the following crystallographic orientation relations (real lattice):

$$\begin{aligned} (001)_{\text{MoO}_3 \cdot \text{H}_2\text{O}} \parallel (100)_{\text{MoO}_3} \quad \text{and} \\ [010]_{\text{MoO}_3 \cdot \text{H}_2\text{O}} \parallel [001]_{\text{MoO}_3} \quad (\text{needle axis}), \end{aligned}$$

the product remaining well oriented with respect to the educt, i.e., forming pseudomorphs as a consequence of a high degree of topotaxy.

A comparison of the unit cells of $\text{MoO}_3 \cdot \text{H}_2\text{O}$ and of MoO_3 (5, 6) shows that the length of the needle axis is altered only very slightly from $[010]_{\text{MoO}_3 \cdot \text{H}_2\text{O}} = 3.700 \text{ \AA}$ to $[001]_{\text{MoO}_3} =$

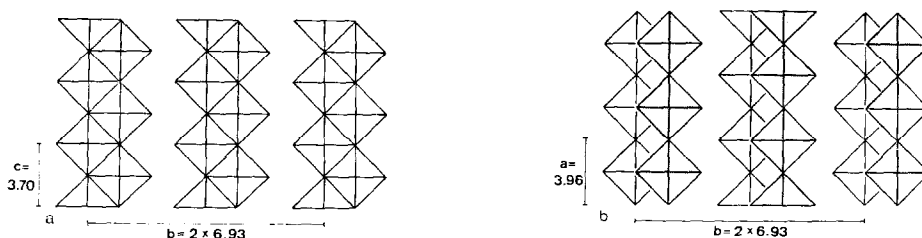


FIG. 2. Idealized drawings of the MoO_3 structure (unit cell dimensions in Å). (a) Plane $(100)_{\text{MoO}_3}$ with edge linked octahedral double chains. (b) Plane $(001)_{\text{MoO}_3}$. The octahedral double chains $[001]$ from Fig. 2a are linked in $[100]$ through common corners.

3.696 Å, and that the plane $(001)_{\text{MoO}_3 \cdot \text{H}_2\text{O}}$ with $2a = 14.776$, $b = 3.700$ Å and $\gamma = 91.2^\circ$ also remains almost unaffected by the decomposition reaction, leading to $(100)_{\text{MoO}_3}$ with $b = 13.855$, $c = 3.696$ Å, and $\alpha = 90.0^\circ$. However, the third axis changes considerably from $[001]_{\text{MoO}_3 \cdot \text{H}_2\text{O}} = 6.673$ Å, $\alpha_{\text{MoO}_3 \cdot \text{H}_2\text{O}} = 107.8$, $\beta_{\text{MoO}_3 \cdot \text{H}_2\text{O}} = 113.6^\circ$ to $[100]_{\text{MoO}_3} = 3.963$ Å, $\beta = 90.0$ and $\gamma = 90.0^\circ$.

To get an idea of the unknown crystal structure of white $\text{MoO}_3 \cdot \text{H}_2\text{O}$, the structure of MoO_3 (5, 6) has to be studied in the relevant orientations (Figs. 2a, 2b).

The planar arrays of edge and corner sharing octahedra extend perpendicular to $[010]_{\text{MoO}_3}$. As the topotactic relations show that the (100) plane of MoO_3 corresponds closely to (001) of the monohydrate, it may be assumed that the atomic arrangement within this plane is already preformed in the hydrate structure. On the other hand, the $[001]$ axis of the monohydrate differs considerably from $[100]_{\text{MoO}_3}$ in direction as well as in length, indicating that this distance is most affected by the loss of

water. Based on these arguments, a crystal structure may be proposed for $\text{MoO}_3 \cdot \text{H}_2\text{O}$, as represented in Figs. 3a, and 3b.

This structure does no longer consist of planes of edge and corner sharing octahedra, but of linear double rows of edge sharing octahedra $[\text{MoO}_5(\text{H}_2\text{O})]$ parallel to $[010]_{\text{MoO}_3 \cdot \text{H}_2\text{O}}$, being responsible for the tilting disorder in the crystals, as these rows are supposed to be held together in $[100]$ and $[001]$ only by packing and van der Waals forces and most probably by hydrogen bonds.

The chain-like structure proposed is in good agreement with the fibrous morphology observed and with the scanning electron microscopical result that the water leaves the dehydrating crystals through cracks parallel to the needle axis, but otherwise unoriented, whereas the prism faces of the needles remain rather unaffected (Fig. 4).

After yellow $\text{MoO}_3 \cdot \text{H}_2\text{O}$, the here described white modification represents a second case, where the proposal of a crystal structure has been made possible by considerations on

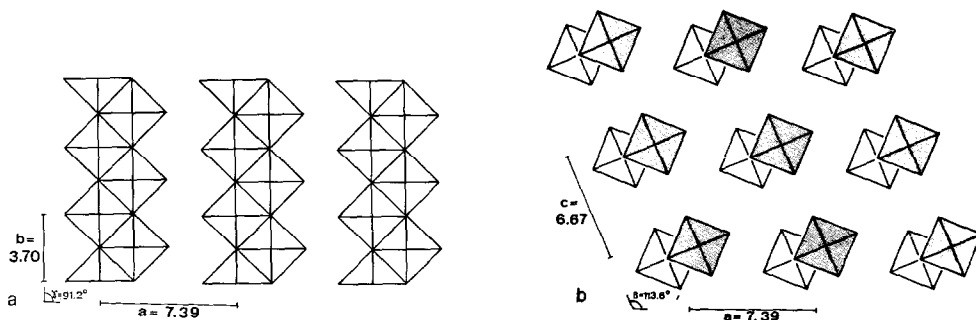


FIG. 3. Idealized model for the crystal structure of white $\text{MoO}_3 \cdot \text{H}_2\text{O}$ as derived from topotaxy (unit cell dimensions in Å). (a) Plane $(001)_{\text{MoO}_3 \cdot \text{H}_2\text{O}}$, to be compared with Fig. 2a. (b) Plane $(010)_{\text{MoO}_3 \cdot \text{H}_2\text{O}}$, to be compared with Fig. 2b.



FIG. 4. Scanning electron micrograph of molybdenum trioxide, pseudomorphous after white molybdenum trioxide-monohydrate. Cracks are running parallel to $[010]_{\text{MoO}_3 \cdot \text{H}_2\text{O}}$ ($\times 1440$).

topotaxy. In order to test the validity of these arguments, special attempts have been made to find a single crystal of white $\text{MoO}_3 \cdot \text{H}_2\text{O}$ with as small tilting disorder as possible, suitable to undertake a complete crystal structure determination by X-rays.

Crystal Structure Determination

A large number of needles of $\text{MoO}_3 \cdot \text{H}_2\text{O}$ were examined by Weissenberg photographs. Finally, a very thin needle with approximate dimensions $0.17 \times 0.02 \times 0.02 \text{ mm}^3$ could be

found, which showed a relatively small tilting disorder compared to other ones. This crystal was selected for data collection on a computer controlled Picker four-circle diffractometer (FACS-1 system). The intensity data were measured with MoK_α -radiation by a θ - 2θ scan over a relatively large 2θ range of 3° (plus the α_1 - α_2 dispersion) with a scan speed of $0.5^\circ/\text{min}$. Background counts were taken for 40 sec at either end of the 2θ scan for each reflexion. Crystal decomposition and instrument stability were monitored by measuring three standard reflexions after every 12 reflexions.

TABLE I
ATOMIC POSITIONAL COORDINATES IN WHITE
MoO₃·H₂O^a

Table with 4 columns: Atom, x, y, z. Rows include Mo, 0(1), 0(2), 0(3), 0(4) with their respective coordinates in parentheses.

^aStandard deviations in the last digit calculated from final least-squares refinement are given in parentheses.

Intensities were collected up to 2θ ≤ 40°, and the standard reflexions were used for an internal scaling of the 747 reflexions measured (including standards and Friedels pairs); 295 reflexions remained after averaging equivalent reflexions and 229 were judged to be observed according to the criterion I ≥ 3σ(I), σ(I) being the estimated standard deviation based on counting statistics. The agreement index between the equivalent Friedels pairs, Σ(|I - Ī|)/Σ(I), was 0.053. Absorption corrections were made using a linear absorption coefficient of μ = 39.4 cm⁻¹. The calculated

TABLE II
OBSERVED AND CALCULATED STRUCTURE FACTORS FOR WHITE MoO₃·H₂O^a

Large table with multiple columns showing observed and calculated structure factors for various hkl reflections. Includes labels like 0,0,L, 1,0,L, etc. and numerical values.

^a The columns are I, F_o, F_c. Unobserved reflections are those less than 3σ(I) and are marked by *.

absorption factors ranged from 1.063 to 1.106. The intensities were reduced to F_0 in the usual way by applying Lorentz and polarization factors.

All the computations, including subsequent refinement of the structure, were performed using the program system XRAY (7). The positions of the Mo atoms could readily be deduced from the peak location in a three-dimensional Patterson map. The resulting Mo–Mo distances of about 3.40 and 3.70 Å seemed to be reasonable values corresponding to MoO_6 -octahedra connected by common edges or corners found in related compounds as MoO_3 (6) and $(\text{NH}_4)_6\text{Mo}_8\text{O}_{27}\cdot 4\text{H}_2\text{O}$ (8).

Structure factor calculations based on refined positions of these Mo atoms yielded a conventional R index of 0.24

$$(R = \sum (||F_0| - |F_c||) / \sum (|F_0|))$$

The scattering factors used were those for the neutral atoms tabulated in International Tables for X-Ray Crystallography (9). A difference electron density map showed the positions of four oxygen atoms in the centric space group $P\bar{1}$ and of eight oxygen atoms in the acentric $P1$. Although the distribution of the intensities in a preliminary calculated Wilson plot showed acentric behaviour, all attempts of a refinement in $P1$ resulted in oscillations of the shifts in least-squares refinement and extremely large standard deviations of the calculated bond lengths. The subsequent refinement in the centric space group $P\bar{1}$ was more successful and was performed to a R -index of 0.14 with isotropic temperature factors. At this stage of the refinement 39 reflexions which were affected by uncertainties in the intensity measurements, e.g., by pronounced asymmetry of the background measurements or by incompletely corrected absorption effects were excluded from further calculations. Anisotropic least-squares refinement with unit weights for all reflexions decreased R to the final value of 0.088 including all of the remaining 204 observed reflexions. However, since anisotropic temperature factors shifted to negative values in this least-squares refinement and had to be set positive definite by the program, we do not assign physical meaning to the

calculated anisotropic temperature factors but consider it as a consequence of the anisotropic disorder in the crystal described earlier.

The final atomic positional coordinates are listed in Table I. Observed and calculated structure factors are presented in Table II.

Description of the Structure

Figures 5 and 6 show projections of the crystal structure of white $\text{MoO}_3\cdot\text{H}_2\text{O}$ parallel to $[001]$ respectively to $[010]$. The resemblance between the idealized prediction from Figs. 3a and 3b and the structure actually determined is evident.

The dominating element is an infinite double chain of edge-linked $[\text{MoO}_5(\text{H}_2\text{O})]$ -octahedra parallel to $[010]$. Each octahedron has two common edges with neighbored ones. In addition to the three bridge-forming oxygen atoms, each molybdenum atom is coordinated

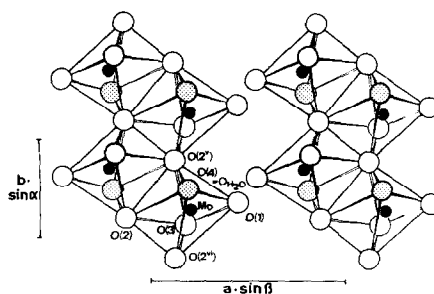


FIG. 5. Projection of the crystal structure of white molybdenum trioxide-mono hydrate parallel to $[001]$.

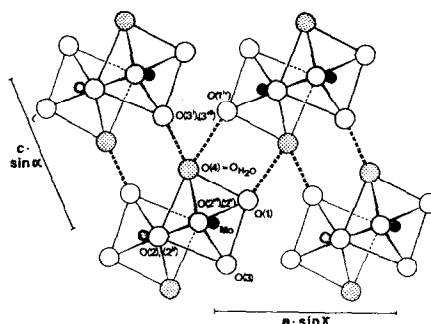


FIG. 6. Projection of the crystal structure of white molybdenum trioxide-mono hydrate parallel to $[010]$. Probable hydrogen bonds are indicated by dotted lines.

TABLE III
INTERATOMIC DISTANCES AND BOND ANGLES IN WHITE $\text{MoO}_3 \cdot \text{H}_2\text{O}$

(a) <i>Mo-O octahedron:</i>			
Mo-O(1)	1.66(3) Å	O(1)-Mo-O(2 ^{vi})	104.3
Mo-O(2)	2.28(3)	O(2)-Mo-O(3)	95.6
Mo-O(3)	1.65(4)	O(2)-Mo-O(4)	76.9
Mo-O(4)	2.37(4)	O(2)-Mo-O(2 ^v)	75.1
Mo-O(2 ^v)	1.98(3)	O(2)-Mo-O(2 ^{vi})	70.7
Mo-O(2 ^{vi})	1.91(3)	O(3)-Mo-O(4)	172.0
		O(3)-Mo-O(2 ^v)	96.8
O(1)-Mo-O(2)	161.0° ^b	O(3)-Mo-O(2 ^{vi})	98.3
O(1)-Mo-O(3)	103.3	O(4)-Mo-O(2 ^v)	78.9
O(1)-Mo-O(4)	84.3	O(4)-Mo-O(2 ^{vi})	81.9
O(1)-Mo-O(2 ^v)	104.1	O(2 ^v)-Mo-O(2 ^{vi})	143.7
(b) <i>Mo-Mo distances:</i>			
Mo-Mo ⁽ⁱⁱ⁾	3.700(5) Å	} Corner sharing octahedra	
Mo-Mo ⁽ⁱⁱⁱ⁾	3.700(5)		
Mo-Mo ^(v)	3.383(5)	} Edge sharing octahedra	
Mo-Mo ^(vi)	3.425(5)		
(c) <i>Short O-O distances between neighbored double chains, corresponding to possible hydrogen bonds:</i>			
O(4)-O(1 ^v)	2.76(4) Å		
O(4)-O(3 ⁱ)	2.85(4)		
O(4)-O(3 ⁱⁱⁱ)	3.14(5)		

^a Standard deviations are given in parenthesis. The superscripts indicate the transformations applied to the x, y, z values given in Table I: (i) $x, 1+y, 1+z$, (ii) $x, 1+y, z$, (iii) $x, -1+y, z$, (iv) $1-x, -y, 1-z$, (v) $-x, -y, -z$, (vi) $-x, -1-y, -z$, (vii) $x, y, 1+z$.

^b $\sigma_{(\text{O}-\text{Mo}-\text{O})} = 1.1-1.7^\circ$.

by two terminal oxygen atoms and one terminal water molecule. Although the hydrogen atoms could not be directly localized, it becomes evident from the interatomic distances that O(4) has to be the water oxygen atom.

The octahedral double chains are linked among each other through possible hydrogen bonds only. This fact can explain the characteristic needle shape of the crystals and the marked tendency to disorder by a more or less pronounced tilt of subneedles around [010].

Table III contains the most important interatomic distances and angles. The $[\text{MoO}_5(\text{H}_2\text{O})]$ -octahedron exhibits a strong characteristic distortion, containing two very short Mo-O bonds of 1.66 and 1.65 Å to the terminal oxygens O(1) and O(3), two medium Mo-O bonds of 1.98 and 1.91 Å to the bridge-

forming oxygens O(2^v) and O(2^{vi}), and finally two very long Mo-O distances of 2.28 and 2.37 Å to the third bridging oxygen atom O(2) and the water oxygen O(4). The average of the six Mo-O distances is 1.975 Å and lies very close to the respective value for MoO_3 of 1.981 Å (6).

The strongly bonded terminal oxygen atoms O(1) and O(3) stand in *cis* position to each other, whereas the longest distance to a bridge-forming oxygen O(2) and the bond to the water molecule O(4) are located in *trans* position relative to O(1) and O(3). This kind of octahedral distortion with two very short *cis*-Mo-O bonds, two very long bonds in *trans* position to them and two medium distances to the remaining oxygen atoms seems quite common in molybdenum compounds with oxygen and has been found, e.g.,

in MoO_3 (5, 6) and in $\text{Na}_2\text{Mo}_2\text{O}_7$ (10) as well. The Mo–O bonds in the order of 1.66 Å to the terminal oxygens belong to the shortest ones which were ever found in molybdenum–oxygen compounds and point to a considerable amount of π -bonding character.

If the two ligands with the longest Mo–O distances are neglected, the structure may be alternatively described as built up from chains [010] of corner-linked distorted MoO_4 -tetrahedra and isolated water molecules. In a very similar way, Kihlborg (6) has characterized the structure of MoO_3 as a transitional state between octahedral and tetrahedral coordination.

Evidence for hydrogen bonds between the octahedral double chains follows from the O–O distances around the water oxygen O(4) in Table III. Relatively short distances from O(4) to oxygen atoms of neighbored octahedral double chains are 2.76 Å to O(1^{iv}), 2.85 Å to O(3ⁱ), and 3.14 Å to O(3^{vi}). These values are suggesting medium strength, respectively, weak hydrogen bonding between otherwise isolated chains. If one of the water hydrogen atoms is assumed definitely bonded to O(1^{iv}), it remains open whether one of the two other contacts represents the second water hydrogen bridge. If both of them should be involved in hydrogen bond formation, a statistical distribution of the second water hydrogen atoms over both possibilities had to be adopted. In Fig. 6, the most probable hydrogen bonds are indicated by dotted lines.

Conclusions

From the comparison between the structure proposal for white $\text{MoO}_3 \cdot \text{H}_2\text{O}$ derived by means of topotactical considerations and its independently determined actual crystal structure follows that the study of topotaxy can represent a powerful tool in predicting structures. In the present case, a so far unknown educt crystal decomposes by loss of one water molecule per formula unit into a perfect pseudomorph built up from highly oriented crystallites of a known product structure. There happens nothing else than an escape of the O(4) atoms as water, a subsequent

linking of the octahedral double chains over common corners O(3) to form layers and finally a shift of the triclinic angles α , β , γ to the 90° angles of the orthorhombic MoO_3 structure.

One could of course imagine also the reverse case, where an educt crystal of known structure is topotactically transformed into a highly oriented, but structurally unknown product, and conclusions about the product structure may be drawn. In between there is the case treated by Günter (1): An educt $\text{MoO}_3 \cdot 2\text{H}_2\text{O}$ is transformed into a product MoO_3 , both of known structure, with the yellow form of $\text{MoO}_3 \cdot \text{H}_2\text{O}$ acting as a structurally unknown intermediate. Although the proposal for its structure derived from topotaxy has not yet been verified independently, the result of this work is well suited to support it.

Even when all of the structures involved in a chemical reaction are already known, the study of topotactical phenomena can be of considerable interest, enhancing the understanding for structural relationships and enabling conclusions regarding reaction mechanisms. Specially well suited for such studies are all structures with pronounced elements like chains or layers. They are by no means restricted to thermal decompositions, but can be undertaken in solid–liquid, solid–gas, and solid–solid reactions as well.

Note. After completion of this work we were informed that I. Bösch and B. Krebs (Kiel, German Fed. Rep.) have undertaken an independent X-ray crystallographic structure determination of white α - $\text{MoO}_3 \cdot \text{H}_2\text{O}$, which is going to be published in *Acta Crystallographica*.

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