

## The Crystal Structure of the $\text{Cu}^+$ Ion Conductor, $(\text{C}_5\text{H}_5\text{NH})_2\text{Cu}_5\text{Br}_7^*$

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$(\text{C}_5\text{H}_5\text{NH})_2\text{Cu}_5\text{Br}_7$ , in which  $(\text{C}_5\text{H}_5\text{NH})^+$  is the pyridinium ion, belongs to space group  $P2_12_12_1$  with  $Z = 4$  and  $a = 13.09 \pm 0.03 \text{ \AA}$ ,  $b = 14.04 \pm 0.03 \text{ \AA}$ ,  $c = 11.78 \pm 0.02 \text{ \AA}$ . The 20  $\text{Cu}^+$  ions are distributed non-uniformly over 52 tetrahedral sites. The bromide tetrahedra share faces in such a manner that undulating channels are formed in the [100] and [010] directions, and right- and left-handed helical channels are formed in the  $c$ -direction. The channels are interconnected, thereby forming a three-dimensional solid electrolyte. A detailed examination of the conduction pathways and of  $\text{Cu}^+$  ion site occupancies leads to the predictions that  $\sigma_2$  ( $\parallel b$ ) should be somewhat greater than  $\sigma_1$  ( $\parallel a$ ) but  $\sigma_3$  ( $\parallel c$ ) should be substantially less than  $\sigma_1$ . ( $\sigma_i$  is the specific conductivity in the  $i$ th direction.) The ratio of available sites to current carriers and the percentage of unit cell volume attributable to the conduction pathways are both rather low and the average conductivity is rather high relative to AgI-based solid electrolytes.

### Introduction

Several crystal structures of solid electrolytes in which the  $\text{Ag}^+$  ion is the current carrier and mostly iodide ions form the "rigid framework" have been determined (1-4). The relation of these structures to the conductivity of the crystals has been discussed in some detail (1-11). Among the more important features of the AgI-based solid electrolyte structures is the network of pathways formed as a result of the face-sharing of the iodide ion

polyhedra<sup>1</sup> and the substantial excess of sites available to the  $\text{Ag}^+$  ions over  $\text{Ag}^+$  ions available as current carriers. The networks are different in detail in different structures; as might be intuitively expected, those crystals with simpler three-dimensional networks have the higher bulk conductivities. In an anisotropic solid electrolyte in which the network of pathways is three-dimensional, the highest conductivity is in the direction of the simplest pathways. Solid electrolytes in which the conductivity is not three-dimensional generally have low conductivities (see for example, Refs.

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<sup>1</sup> In  $\text{Ag}_{26}\text{I}_{18}\text{W}_4\text{O}_{16}$  (4), the oxygen atoms of the  $(\text{W}_4\text{O}_{16})^{8-}$  ion are also involved in the formation of the polyhedra in the conduction network. This is expected to be the case in other solid electrolytes that involve complex oxide anions.

(3, 6–9)). For discussion of other features of halogenide solid electrolytes, see Refs. (2–12).

A very large number of solid electrolytes based on AgI has been reported (12–16); however, there are so far not many solid electrolytes in which the  $\text{Cu}^+$  ion is the current carrier. It is not really clear why this is so, but it must be related, at least to some extent, to the sizes of the current carriers relative to the sizes and polarizabilities of the halide ions.

In this paper, we report the first structure determination of a double salt in which the  $\text{Cu}^+$  ion is the current carrier. The formula of this solid electrolyte is  $(\text{C}_5\text{H}_5\text{NH})_2\text{Cu}_3\text{Br}_7$  or  $\text{Py}_2\text{Cu}_3\text{Br}_7$ , in which  $\text{Py}^+$  is the pyridinium ion. This solid electrolyte was first reported by Sammells *et al.* (17). Crystals of the material have been grown (18) by one of us (P.M.S.) by means of a modified Bridgman technique.

Relative to methodology, this is the first of the solid electrolyte structures that we have determined by direct methods.

## Experimental

Crystals of  $\text{Py}_2\text{Cu}_3\text{Br}_7$  are sensitive to oxygen; therefore the handling of the crystals was done in a dry  $\text{N}_2$  atmosphere in a drybox. Initially, X-ray photographs of a crystal fragment coated with epoxy cement were taken on a Buerger precession camera; these photographs were the  $0kl$ – $4kl$  and the  $h0l$  levels. The data confirmed the reported (17, 18) orthorhombic space group,  $P2_12_12_1(D_2^4)$ ; that is, reflections  $h00$ ,  $0k0$ , and  $00l$  were present only when  $h$ ,  $k$ ,  $l$  were even. The lattice constants obtained from these photographs are  $a = 13.09 \pm 0.03 \text{ \AA}$ ,  $b = 14.04 \pm 0.03 \text{ \AA}$ , and  $c = 11.78 \pm 0.02 \text{ \AA}$ . The formula weight of  $\text{Py}_2\text{Cu}_3\text{Br}_7$  is 1037.50; the unit cell volume is  $2165 \text{ \AA}^3$ . The unit cell can contain only multiples of 4  $\text{Py}_2\text{Cu}_3\text{Br}_7$  in the most probable space group  $P2_12_12_1$ . With one multiple, i.e., 4  $\text{Py}_2\text{Cu}_3\text{Br}_7$ , the calculated X-ray density is  $3.18 \text{ g cm}^{-3}$ , which is in good

agreement with the value  $3.178 \text{ g cm}^{-3}$  reported (17) as the “observed” density.<sup>2</sup>

A crystal was ground to a sphere of radius 0.096 mm with a sphere grinder (19) similar to that described by Schuyff and Hulscher (20). (Dry  $\text{N}_2$  was used in the grinding process.) The spherical crystal was coated with epoxy cement, which was allowed to dry. The coated crystal was then put into a Lindeman capillary of 0.3-mm diam, 0.01-mm wall thickness. After the crystal was located near the closed end of the tube, a very small amount of epoxy cement was introduced to cause the crystal to remain attached to the wall of the capillary. The capillary was sealed off and mounted on a goniometer head.

The crystal was aligned with the  $a$ -axis as rotation axis. Intensities of the independent reflections in the range  $10^\circ \leq 2\theta \leq 45^\circ$  ( $\text{Zr}$ -filtered,  $\text{MoK}\alpha$  radiation), were collected with a Buerger–Supper single-crystal diffractometer automated by a Nova 1200 computer. Each reciprocal lattice point was scanned at the rate of  $1.5^\circ/\text{min}$  over the range  $(1.5 + 0.7 \text{ Lp})$ , where Lp is the Lorentz–polarization–Tunnel factor. The maximum scan range for any peak was limited to  $5^\circ$ . Background counts were taken at the beginning and at the end of the scan interval at one-fourth the scan time of each scan. Intensities of data beyond  $2\theta = 45^\circ$  were not significant. The total number of independent reflections measured was 1591, of which 684 were below the 70-count threshold.

The linear absorption coefficient,  $\mu$ , of  $\text{Py}_2\text{Cu}_3\text{Br}_7$  for  $\text{MoK}\alpha$  radiation is  $186.8 \text{ cm}^{-1}$ , from which, for  $R = 0.096 \text{ mm}$ ,  $\mu R = 1.80$ . It should be noted that this absorption is high, and the scattering matter in the crystal low, relative to the AgI-based solid electrolytes. That is, the individual intensities for this crystal tended to be relatively low overall. The Nova computer does some of the data processing, applying the background, absorption, and Lorentz–polarization–Tunnel corrections and

<sup>2</sup> Although not so explicitly stated in Ref. (17), the measured density was obtained by the flotation method (private communication from B. B. Owens).

giving, on paper tape, the relative squares of the structure amplitudes.

### Determination and Refinement of the Structure

In the space group  $P2_12_12_1(D_2^4)$ , there are only the fourfold general positions. Thus in crystals of  $Py_2Cu_5Br_7$ , the formula unit is the asymmetric unit.

The structure was solved by direct methods with the FAMEB (21) and MULTANB programs (22); *E*-maps were calculated with FORDAPB (23). The trial model indicated that the seven independent  $Br^-$  ions were at the apices of a pentagonal bipyramid. A structure factor calculation<sup>3</sup> involving only the  $Br^-$  ions gave  $R = 0.44$  ( $R = \sum |F_o| - |F_c| / \sum |F_o|$ ). Two cycles of least-squares refinement with isotropic thermal parameters reduced  $R$  to 0.34.

The pentagonal bipyramid contains 5 face-sharing tetrahedra. A model of the four pentagonal bipyramids arranged in the unit cell showed that there were 8 more independent face-sharing tetrahedra connecting the bipyramids, thus giving a total of 13 independent face-sharing anion tetrahedra. Initially, the 5  $Cu^+$  ions per formula unit were assumed to be equally distributed over the 13 tetrahedral sites. Several least-squares cycles in which the site occupancies of the  $Cu^+$  ions were varied brought  $R$  to 0.20. In these calculations, positional parameters were varied, but not all at the same time. The thermal parameters in these cycles were all taken as isotropic.

The  $Br^-$  ions and the  $Cu^+$  ions in the three most populated ( $m > 0.80$ )<sup>4</sup> sites were assigned anisotropic thermal parameters; the remainder of the  $Cu^+$  ions were still assigned isotropic thermal parameters of  $7.5 \text{ \AA}^2$ . Further least-squares cycles reduced  $R$  to 0.12.

<sup>3</sup> All least-squares and structure factor calculations were carried out with NUCLS 5 (24).

<sup>4</sup>  $m$  = number of atoms in particular set of positions/number of equipoints in set of general positions.

The next step was to find the location of the  $Py^+$  ions. The surroundings of the  $Py^+$  ions in the structures of  $PyI$  (25),  $PyAg_3I_6$  (2), and  $Py_3Ag_{18}I_{23}$  (3) were studied to see whether any resemblance could be found to  $Br^-$  ion arrangements about as yet unfilled space in the model. This gave only some notion as to what to look for, but it was clear that the arrangement of  $Br^-$  ions surrounding the  $Py^+$  ions was not the same as the arrangement of iodide ions surrounding the  $Py^+$  ions in the iodide compounds. An approximately planar array of six  $Br^-$  ions arranged hexagonally was seen. One  $Py^+$ ,  $Py1$ , was estimated to lie approximately parallel to this hexagon; this also linked  $Py1$  to seven more  $Br^-$  ions on the side opposite that of the hexagon. Calculation of the 119 structure amplitudes, including the contribution from  $Py1$ ,<sup>5</sup> with the largest  $\Delta = ||F_o| - |F_c||$  showed significant improvement, i.e., a decrease of the average  $\Delta$ . Several least-squares cycles followed with  $Py1$  included, and anisotropic thermal parameters for two more  $Cu^+$  ions.  $R$  was thereby reduced to 0.09.

The second  $Py^+$  ion,  $Py2$ , could be seen to fit on the side of the  $Br^-$  ion hexagon opposite that of  $Py1$ , but its orientation was uncertain. One hundred twenty structure amplitudes with  $(\sin \theta)/\lambda < 0.3$  and with the largest  $\Delta$ 's were used to calculate a difference Fourier map which gave the orientation of  $Py2$ .

Least-squares calculations were continued. The imaginary parts of the atomic scattering factors (26) were introduced and one enantiomorph was found to give significantly better agreement than the other ( $R = 0.076$  vs 0.083). (The final parameters listed in Table I are for the more probable enantiomorph.)

Because of the rigid group refinement, the C and N atoms in the  $Py^+$  ion were not distinguished. With regard to the (independent)  $Cu^+$  ion sites, only five had fractional occupancies  $\geq 0.70$ . The remaining eight had

<sup>5</sup> In all calculations, each  $Py^+$  ion was treated as a rigid body benzene ring with a temperature factor  $7.8 \text{ \AA}^2$  for each atom of the ring.

TABLE I  
PARAMETERS AND STANDARD ERRORS OF  $\text{Cu}^+$  AND  $\text{Br}^-$  IONS IN  $\text{Py}_2\text{Cu}_3\text{Br}_7$

Ion	$m^a$	x	y	z	$\beta_{11}^b$	$\beta_{22}$	$\beta_{33}$	$\beta_{12}$	$\beta_{13}$	$\beta_{23}$
Br1	1.0	0.5672(4)	0.0704(4)	-0.2293(5)	26(3)	47(3)	119(7)	2(3)	-7(4)	17(4)
Br2	1.0	0.4283(4)	0.2388(4)	0.0346(5)	19(3)	54(4)	87(6)	16(3)	2(4)	5(4)
Br3	1.0	0.3825(4)	0.5235(4)	-0.0396(6)	29(3)	64(4)	117(6)	8(3)	6(4)	6(5)
Br4	1.0	0.6664(4)	0.1248(4)	-0.1409(5)	41(3)	57(4)	87(6)	7(3)	-3(4)	-1(4)
Br5	1.0	0.6738(4)	0.4058(4)	-0.0257(6)	18(3)	76(4)	107(6)	6(3)	29(4)	26(4)
Br6	1.0	0.1899(4)	0.3146(4)	-0.1947(5)	34(3)	63(4)	104(6)	-2(3)	-12(4)	-23(4)
Br7	1.0	0.4833(4)	0.3316(4)	-0.2909(6)	33(3)	62(4)	136(8)	-8(3)	16(5)	-6(5)
Cu1	0.80	0.4921(7)	0.1904(9)	-0.1746(10)	43(6)	117(9)	148(13)	-39(6)	10(7)	-40(9)
Cu2	0.11	0.534	0.138	-0.280	*					
Cu3	0.14	0.542	0.013	-0.261	*					
Cu4	0.70	0.4708(11)	-0.0481(13)	0.6440(13)	94(11)	145(14)	173(18)	-5(10)	-2(12)	-28(14)
Cu5	0.13	0.492	0.375	-0.080	*					
Cu6	0.10	0.564	0.276	-0.106	*					
Cu7	0.89	0.6196(7)	0.2385(7)	0.0009(10)	41(5)	71(6)	172(12)	-2(5)	-7(7)	27(7)
Cu8	0.07	0.741	0.243	-0.002	*					
Cu9	0.81	0.7907(7)	0.3154(8)	0.1009(9)	52(7)	71(7)	128(11)	-3(5)	1(7)	22(7)
Cu10	0.18	0.367	0.240	-0.170	*					
Cu11	0.70	0.3473(11)	0.3676(11)	-0.1101(13)	95(11)	125(12)	170(17)	-15(10)	20(11)	13(12)
Cu12	0.28	0.292	0.363	-0.015	*					
Cu13	0.10	0.347	0.449	-0.220	*					

<sup>a</sup>  $m$  = multiplier (see text).

<sup>b</sup> The form of the temperature factor is  $T = \exp[-(h^2\beta_{11} + k^2\beta_{22} + l^2\beta_{33} + 2hk\beta_{12} + 2hl\beta_{13} + 2kl\beta_{23})]$ ;  $\beta$  values  $\times 10^4$ .

\* A constant isotropic thermal parameters  $B = 7.5 \text{ \AA}^2$  was assigned to each of these  $\text{Cu}^+$  sites.

fractional occupancies  $\leq 0.28$ ; in most of the least-squares cycles (especially the last 10 or so) the positional and thermal parameters of these sites were held constant. However, their positions were adjusted after each computer run to give reasonable Cu–Br and Cu–Cu distances. In both cases, i.e., of the  $Py^+$  ions and of  $Cu^+$  ion sites, it seemed improbable that the data would allow individual parameter refinement.

In the antepenultimate cycle, the refinement of all the  $Cu^+$  ion multipliers gave a total of 4.76  $Cu^+$  ions per formula unit, with individual standard errors of 0.016. The 0.24  $Cu^+$  ion was distributed among the 10 sites with lowest occupancy. The multipliers were held constant in the last two cycles.

The final  $R$  value is 0.076 for 913 observed structure amplitudes. Among the 684 unobserved structure amplitudes, 29 gave calculated values higher than threshold. Including the  $\Delta$ 's for these in the numerator of  $R$ , the resulting value is 0.078. The standard error of an observation of unit weight is 1.11.

In the calculations, the data were weighted according to

$$\begin{aligned} F < 100, & \quad \sigma = 15 - 0.1F, \\ 100 \leq F < 150, & \quad \sigma = 0.05F, \\ F \geq 150, & \quad \sigma = \exp(F/74.45), \\ & \quad w = 1/\sigma^2. \end{aligned}$$

The atomic scattering factors for  $Cu^+$ ,  $Br^-$ , and C were those of Cromer and Mann (27). The real and imaginary parts of the anomalous dispersion were those given by Cromer and Liberman (26). A table listing the observed and calculated structure amplitudes is available.<sup>6</sup> Table I lists final parameters and standard errors for the  $Br^-$  ions and  $Cu^+$  ion

<sup>6</sup> See NAPS document No. 03217 for 9 pages of supplementary material. Order from ASIS/NAPS, Microfiche Publications, 440 Park Avenue South, New York, N.Y. 10016. Remit in advance \$3.00 for microfiche copy or for photocopy, \$5.00 up to 20 pages plus 25¢ for each additional page. All orders must be prepaid. Foreign orders add \$5.00 for postage and handling.

sites. Table II lists the final parameters of the rigid groups representing the pyridinium rings.

### Interionic Distances

Table III gives detailed information on each of the  $Cu^+$  ion sites: its fractional occupancy, the associated Br–Br distances<sup>7</sup> and their average, the Cu–Br distances and their average, the number of nearest-neighbor  $Cu^+$  ion sites, the distances thereto and their average, and the volume of the tetrahedron. Standard errors of Br–Br distances are between 0.008 and 0.010 Å. Standard errors of Cu–Br distances involving the sites with fractional occupancy  $\geq 0.70$  are 0.01 Å for Cu1, 7, 9 and 0.02 Å for Cu4 and Cu11. Because of the way in which the positions of the other  $Cu^+$  ion sites were obtained (see above), there is no estimate of the error of the other Cu–Br distances. This is also the case for Cu–Cu distances.

Table IV lists the number of nearest  $Br^-$  ion neighbors of each  $Br^-$  ion and their average distance. A table listing distances between the atoms in the  $Py^+$  ions and neighboring atoms will be sent to those requesting the  $F_c$  vs  $F_o$  tables from Microfiche Publications, Inc. (see footnote 6).

It is of interest to compare the Br–Br, Cu–Br, and Cu–Cu distances in  $Py_2Cu_3Br_7$  with those in  $\alpha$ - and  $\gamma$ -CuBr. The  $\beta$ - $\alpha$  transition of CuBr occurs at 470°C (30); the lattice constant of  $\alpha$ -CuBr is 4.601 Å at 485°C (31) (see also (32)). This phase has  $Br^-$  ions at corners and body center of the unit cell and  $Cu^+$  ions distributed over the 12 tetrahedral sites only (31);  $\alpha$ -CuBr is the solid electrolyte phase (33). In  $\alpha$ -CuBr at 485°C, the Cu–Br distances are 2.57 Å. There are two different Br–Br distances 3.98 Å and 4.60 Å, four of the former connecting corners to body centers and two of the latter connecting corner to

<sup>7</sup> Distances in Table III were calculated with the program ORFFEC (28). However, throughout this study, the ORTEP (29) program was used to check distances; ORTEP was also used to make all the figures.

TABLE II  
DERIVED PARAMETERS FOR THE RIGID GROUP ATOMS OF  $\text{Py}_2\text{Cu}_3\text{Br}_7$

Atom	x	y	z	$B$ ( $\text{\AA}^2$ )	Atom	x	y	z	$B$ ( $\text{\AA}^2$ )
A1	0.547(4)	0.403(3)	0.254(4)	7.8	A2	0.290(4)	0.167(4)	0.288(3)	7.8
B1	0.441(4)	0.413(3)	0.255(4)	7.8	B2	0.392(3)	0.157(4)	0.317(4)	7.8
C1	0.392(3)	0.448(4)	0.351(5)	7.8	C2	0.425(3)	0.178(4)	0.426(4)	7.8
D1	0.450(4)	0.474(3)	0.446(4)	7.8	D2	0.355(4)	0.211(4)	0.507(3)	7.8
E1	0.555(4)	0.464(4)	0.444(4)	7.8	E2	0.253(3)	0.221(4)	0.477(4)	7.8
F1	0.604(3)	0.428(4)	0.348(5)	7.8	F2	0.220(3)	0.200(4)	0.368(4)	7.8

Rigid group parameters						
Group	$x_c^a$	$y_c$	$z_c$	$\delta^b$	$\epsilon$	$\eta$
Py1	0.498(3)	0.4383(21)	0.350(3)	1.67(4)	2.67(3)	1.15(3)
Py2	0.323(3)	0.189(3)	0.397(3)	-1.83(3)	2.89(3)	1.87(3)

<sup>a</sup>  $x_c, y_c,$  and  $z_c$  are the fractional coordinates of the origin of the rigid group.

<sup>b</sup> The rigid group orientation angles  $\delta, \epsilon,$  and  $\eta$  (radians) have been defined previously: S. J. La Placa and J. A. Ibers, *Acta Crystallogr.* **18**, 511 (1965).



TABLE III  
BROMIDE TETRAHEDRA ABOUT THE  $\text{Cu}^+$  ION SITES

Site	Fractional occupancy	Br-Br <sup>a</sup> (Å)	Average Br-Br (Å)	Cu-Br (Å)	Average Cu-Br (Å)	No. of Cu neighbors	Cu-Cu (Å)	Average Cu-Cu (Å)	Volume (Å <sup>3</sup> )
Cu1	0.80	1-2 <sup>b</sup> 3.987	4.068	Br1 2.43	2.51	3	Cu2 1.55	1.69	7.87
		1-4 4.123	4.113	Br2 2.69	2.41		Cu6 1.73		
		1-7 4.036	4.158	Br7 2.41			Cu10 1.78		
Cu2	0.11	1-3 4.310	4.073	Br1 2.45	2.63	2	Cu1 1.55	1.66	8.86
		1-4 4.123	5.077	Br3 2.88	2.80		Cu3 1.77		
		1-7 4.036	4.158	Br7 2.80					
Cu3	0.14	1-3 4.310	4.073	Br1 2.46	2.58	3	Cu2 1.77	1.73	8.52
		1-4 4.123	4.215	Br3 2.55	2.64		Cu4 1.70		
		1-7 3.888	4.629	Br7 2.64			Cu13 1.72		
Cu4	0.70	1-3 4.310	4.160	Br1 2.61	2.51	2	Cu3 1.70	1.55	7.84
		1-5 3.735	4.215	Br3 2.49	2.49		Cu5 1.40		
		1-7 3.888	4.130	Br7 2.49					
Cu5	0.13	2-3 4.136	4.160	Br2 2.49	2.53	3	Cu4 1.40	1.68	8.70
		2-5 4.042	4.215	Br3 2.57	2.56		Cu6 1.70		
		2-7 4.113	4.130	Br7 2.56			Cu11 1.93		
Cu6	0.10	2-4 4.068	4.174	Br2 2.48	2.52	3	Cu1 1.73	1.66	8.20
		2-5 4.042	4.158	Br4 2.55	2.55		Cu5 1.70		
		2-7 4.113	4.130	Br7 2.55			Cu7 1.54		
Cu7	0.89	2-4 4.068	4.174	Br2 2.54	2.49	2	Cu6 1.54	1.57	7.88
		2-5 4.042	4.057	Br4 2.39	2.57		Cu8 1.59		
		2-6 3.981	4.046	Br6 2.57					
Cu8	0.07	2-4 4.122	4.174	Br2 2.50	2.51	3	Cu7 1.59	1.65	8.65
		2-5 3.903	4.057	Br4 2.53	2.54		Cu9 1.70		
		2-6 4.263	4.046	Br6 2.54			Cu12 1.65		
Cu9	0.81	1-2 3.987	3.903	Br1 2.42	2.49	2	Cu8 1.70	1.61	8.23
		1-5 3.943	4.263	Br2 2.52	2.51		Cu10 1.51		
		1-6 4.161	4.046	Br6 2.51					



Cu10	0.18	1-2	3.987	2-6	4.263	4.095	Br1	2.49	Br6	2.56	2.51	3	Cu1	1.78	1.74	8.06
		1-6	4.161	2-7	4.113		Br2	2.54	Br7	2.45			Cu9	1.51		
		1-7	4.036	6-7	4.012								Cu11	1.94	1.74	8.51
Cu11	0.70	2-3	4.136	3-6	4.279	4.170	Br2	2.70	Br6	2.41	2.58	4	Cu5	1.93		
		2-6	4.263	3-7	4.215		Br3	2.39	Br7	2.82			Cu10	1.94		
		2-7	4.113	6-7	4.012								Cu12	1.34		
													Cu13	1.73		
Cu12	0.28	2-3	4.136	3-4	4.107	4.161	Br2	2.56	Br4	2.47	2.55	2	Cu8	1.65	1.50	8.46
		2-4	4.122	3-6	4.279		Br3	2.56	Br6	2.60			Cu11	1.34		
		2-6	4.263	4-6	4.057											
Cu13	0.10	3-4	4.073	4-6	5.124	4.389	Br3	2.42	Br6	2.81	2.69	2	Cu3	1.72	1.73	9.43
		3-6	4.279	4-7	4.629		Br4	2.96	Br7	2.57			Cu11	1.73		
		3-7	4.215	6-7	4.012											

<sup>a</sup> There is one Br3-Br6 distance of 4.751(9) Å that is not an edge of a tetrahedron.

<sup>b</sup> The designation 1-2, for example, denotes the Br1-Br2 distance.

TABLE IV

COORDINATIONS OF THE  $Br^-$  IONS AND AVERAGE DISTANCES IN ÅNGSTROMS

Bromide designation	No. of $Br^-$ neighbors	Average <sup>a</sup> Br/Br distance (Å)
Br1	8	4.023
Br2	9	4.068
Br3	9	4.335
Br4	10	4.264
Br5	8	4.016
Br6	9	4.297
Br7	9	4.251

<sup>a</sup> See Table II for individual Br-Br distances. The standard error of all average distances is 0.009 Å.

yields the  $Cu^+$  ion sites 7, 8, 9, and 12, the group labeled *G*; the second yields  $Cu^+$  ion sites 2, 3, 4, and 13, the group labeled *I*. Thus there are 13 independent  $Cu^+$  ion tetrahedral sites and therefore a total of 52 such sites in the unit cell.

Figure 3 shows the arrangement of the pentagonal bipyramids (denoted by BP) and the groups of connecting tetrahedra *G* and *I*. The four *equivalent* bipyramids are numbered 1, 2, 3, 4 for ease of discussion. The symbol  $2_1(x, \frac{1}{4}, 0)$  (and analogous symbols) is intro-

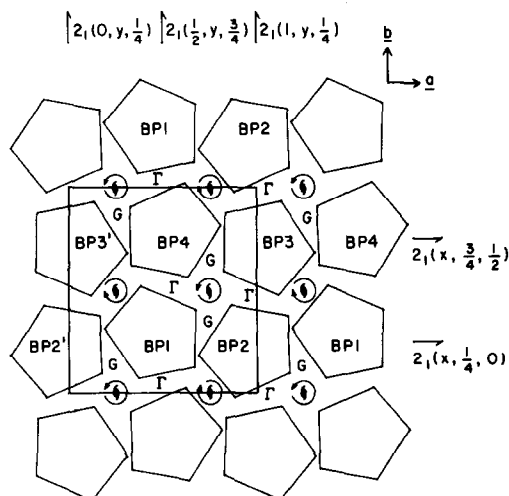


FIG. 3. Arrangement of the pentagonal bipyramids and *G* and *I* groups of bromide ion tetrahedra (see text).

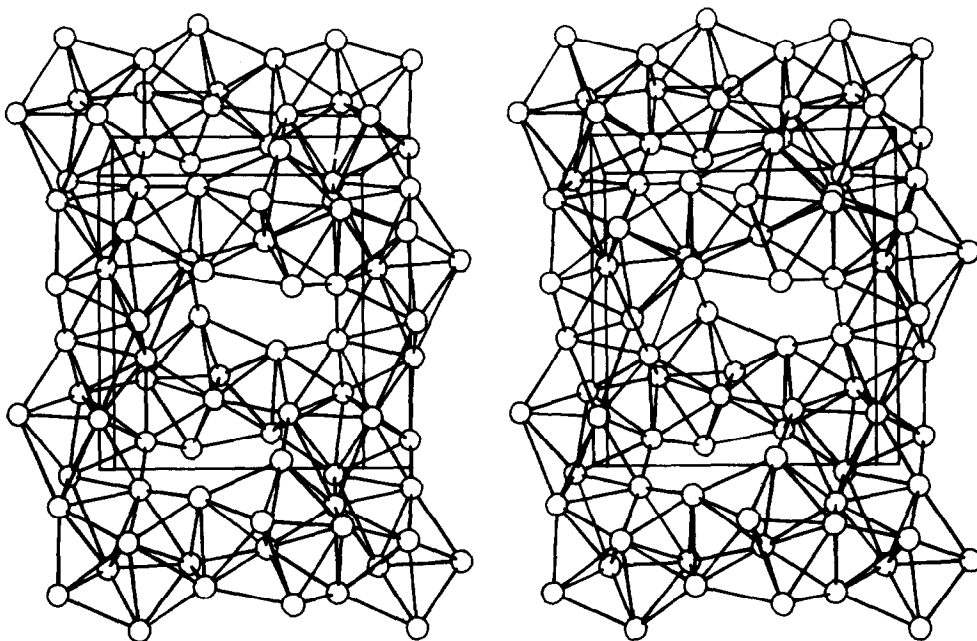


FIG. 4. Stereoscopic drawing of the  $\text{Br}^-$  ion arrangement in  $\text{Py}_2\text{Cu}_2\text{Br}_7$ , looking along the  $c$ -axis.

duced to denote a  $2_1$ -axis along  $a$  at  $y = \frac{1}{4}$ ,  $z = 0$ .

Conduction of  $\text{Cu}^+$  ions in the  $[100]$  direction occurs via  $\text{BP1} \rightarrow \text{G} \rightarrow \text{BP2} \rightarrow \text{G} \rightarrow \text{BP1}$  (in the next cell all along  $a$ ) and so on.  $\text{BP1}$  is transformed to  $\text{BP2}$  by  $2_1(x, \frac{1}{4}, 0)$ . The channel thus runs along  $a$ , centered about  $2_1(x, \frac{1}{4}, 0)$ , in an undulating fashion, the amplitude<sup>8</sup> in the  $c$ -direction being  $z = \pm 0.128$ .

The  $2_1(\frac{3}{4}, \frac{1}{2}, z)$  axis transforms  $\text{BP1}$  into  $\text{BP3}$  and  $\text{BP2}$  into  $\text{BP4}$ ; therefore the channel  $\text{BP4} \rightarrow \text{G} \rightarrow \text{BP3} \rightarrow \text{G} \rightarrow \text{BP4}$  (in the next unit cell along  $a$ ) ... centered about  $2_1(x, \frac{3}{4}, \frac{1}{2})$  is also along the  $a$ -direction and is entirely equivalent to that centered about  $2_1(x, \frac{1}{4}, 0)$  (Fig. 3). Along the  $b$ -direction,  $\text{BP2}$  is connected to  $\text{BP3}$  via  $\Gamma$ , again forming an undulating channel:  $\text{BP2} \rightarrow \Gamma \rightarrow \text{BP3} \rightarrow \Gamma \rightarrow \Gamma \rightarrow \text{BP2}$  (in the next unit cell along  $b$ ) ... centered about  $2_1(1, y, \frac{1}{4})$ ; the amplitude of this channel in the  $c$ -direction is  $z = \pm 0.122$ . The  $2_1(1, y, \frac{1}{4})$  (Fig. 3) axis transforms  $\text{BP2}$  into  $\text{BP3}$ . The  $2_1(\frac{3}{4}, \frac{1}{2}, x)$  axis trans-

forms the whole channel centered at  $2_1(1, y, \frac{1}{4})$  into the channel centered at  $2_1(\frac{1}{2}, y, \frac{3}{4})$ . As indicated earlier, the two channels are entirely equivalent; however, the designation (Fig. 3) is now  $\text{BP1}$  (next unit cell along  $b$ )  $\rightarrow \Gamma \rightarrow \text{BP4} \rightarrow \Gamma \rightarrow \text{BP1} \dots$

The stereoscopic drawing (Fig. 4) looking down the  $c$ -axis shows the conduction passageways along  $a$  and  $b$ . Figures 3 and 4 show that the channels in the  $a$ -direction are interconnected, as are the channels in the  $b$ -direction. Moreover, the channels in the  $a$ - and  $b$ -directions are interconnected. There is zero *average* change in the  $c$ -direction when a  $\text{Cu}^+$  ion moves along a *single* channel in either the  $a$ - or  $b$ -direction. However, a net change occurs along  $c$  when the  $\text{Cu}^+$  ion moves from one channel to another.

The above description does not yet distinguish the most probable individual pathways in the crystal. These are obtained by a more detailed examination of Table III, which gives the interconnections of  $\text{Cu}^+$  ion sites and the site occupancies. There is no obvious reason for the observed distribution which is mar-

<sup>8</sup> The amplitude is defined as the perpendicular distance of the midpoint between  $\text{Br2}$  and  $\text{Br7}$  to the appropriate  $2_1$ -axis, in this *particular* case,  $2_1(x, \frac{1}{4}, 0)$ .

edly nonuniform, as might be expected from the results of the studies of the AgI-based solid electrolytes (1-9). It should be clear, however, that the total fractional occupancy of two adjacent sites must be  $\leq 1.0$ . The equivalent to high fractional occupancy is high residence time. High residence time means that the contribution of the ions in such sites to the average mobility in a particular direction, is lower than for ions in less populated sites.<sup>9</sup>

The detailed pathways along  $a$  and  $b$  are shown schematically in Fig. 5. Along  $a$ , the most probable path is  $6 \rightarrow 7 \rightarrow 8 \rightarrow 12 \rightarrow 11 \rightarrow 5 \rightarrow 6 \dots$ . This path includes two highly occupied sites, Cu7 and Cu11, per increment. The alternate path  $6 \rightarrow 7 \rightarrow 8 \rightarrow 9 \rightarrow 10 \rightarrow 1 \rightarrow 6 \dots$  includes three highly occupied sites per increment, namely, Cu7, Cu9, and Cu1. Along

<sup>9</sup> It should be mentioned here that the application of an electric field to the crystal could conceivably change the equilibrium distribution that exists in the unperturbed crystal.

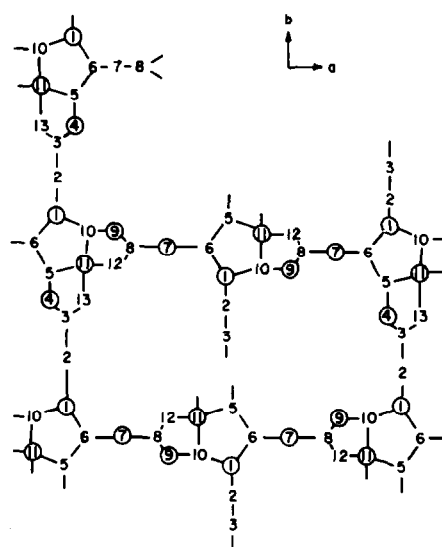


FIG. 5. Schematic representation of conduction pathways in  $a$ - and  $b$  directions. The numbers denote  $Cu^+$  ion sites as in Table III. Circled numbers indicate fractional occupancy  $\geq 0.70$ .

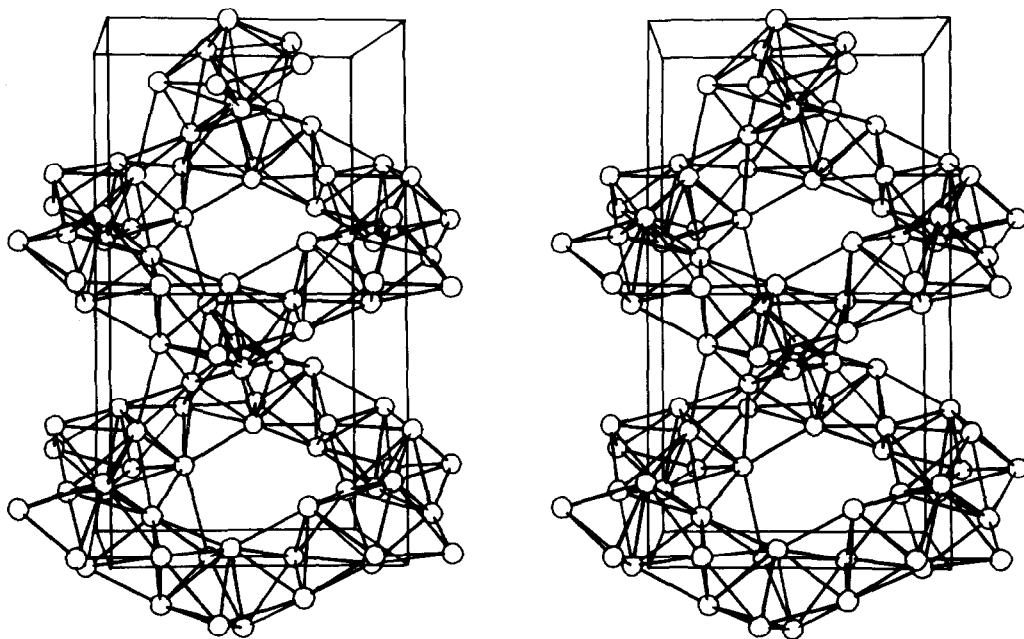


FIG. 6. Stereoscopic drawing of the  $Br^-$  ion arrangement in  $Py_2Cu_5Br_7$ , looking along  $b$ . Two unit cells along  $c$  are shown.

$b$ , two paths appear to be about equally probable; these are  $1 \rightarrow 2 \rightarrow 3 \rightarrow 4 \rightarrow 5 \rightarrow 6 \rightarrow 1 \dots$  and  $1 \rightarrow 2 \rightarrow 3 \rightarrow 13 \rightarrow 11 \rightarrow 10 \rightarrow 1 \dots$ . Each increment contains two highly occupied sites.

The sites in the pentagonal bipyramids connect channels along  $a$  and  $b$ , but groups  $G$  and  $\Gamma$  are strictly in the  $a$  and  $b$  channels, respectively.

An electric field in the  $c$ -direction must result in a *net* drift of  $\text{Cu}^+$  ions in this direction. The two most efficient pathways which allow motion of the  $\text{Cu}^+$  ions effectively in the  $c$ -direction are right- and left-handed

helical paths. The right-handed path is  $\text{BP1} \rightarrow \text{G} \rightarrow \text{BP2} \rightarrow \Gamma \rightarrow \text{BP3} \rightarrow \text{G} \rightarrow \text{BP4} \rightarrow \Gamma \rightarrow \text{BP1}$  (in the next cell along  $c$ )  $\rightarrow \dots$ ; the spiral is about the  $2_1(\frac{1}{4}, \frac{1}{2}, z)$  axis. The left-handed helical path is  $\text{BP1} \rightarrow \text{G} \rightarrow \text{BP2}'$  (i.e., in the next unit cell along  $-b$ )  $\rightarrow \Gamma \rightarrow \text{BP3}' \rightarrow \text{G} \rightarrow \text{BP4} \rightarrow \Gamma \rightarrow \text{BP1}$  (in the next unit cell along  $c$ )  $\rightarrow \dots$ ; the spiral is about the  $2_1(\frac{1}{4}, \frac{1}{2}, z)$  axis. Figure 3 shows how the network of helical paths is arranged. The symbols  $\odot$  and  $\ominus$  denote right- and left-handed rotation, respectively, of the helical paths in the (positive)  $c$ -axis direction. Each helical path is surrounded by four nearest-neighbor helical paths with opposite

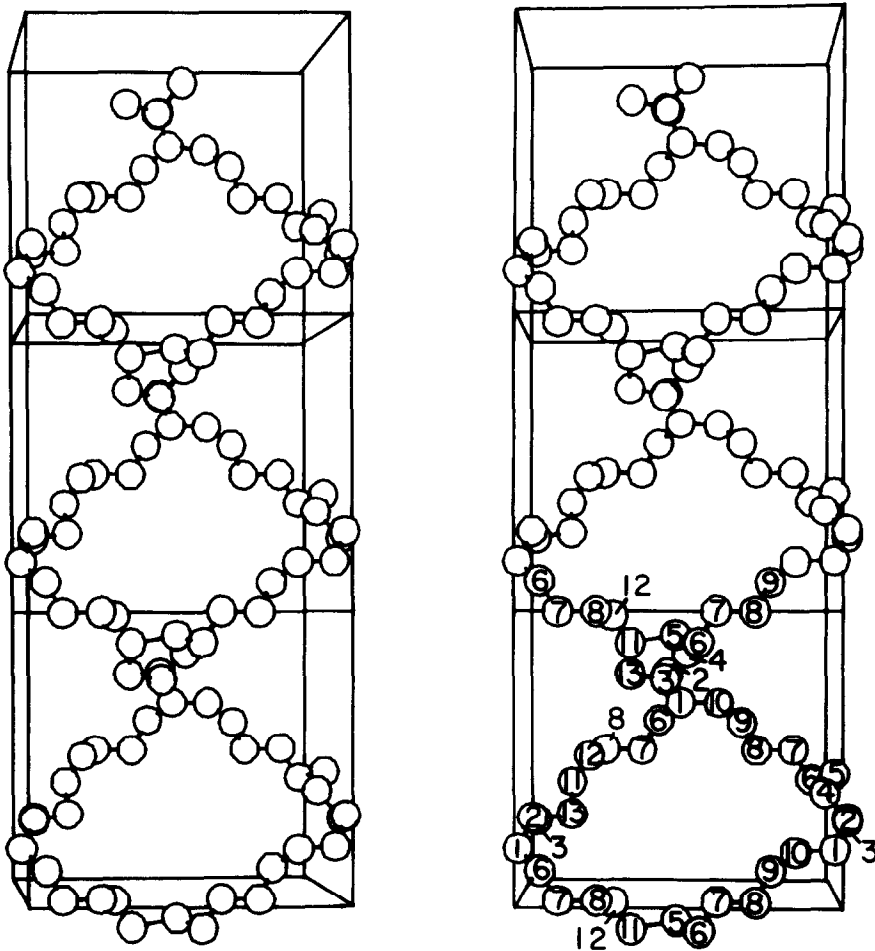


FIG. 7. Stereoscopic drawings of the conduction paths of the  $\text{Cu}^+$  ions, looking along  $b$ . The numbers correspond to those listed in Table I. Three unit cells along the  $c$ -axis are shown.

chirality and four next-nearest-neighbor helical paths with the same chirality. In a single turn, a particular helix shares four bipyramids (BP's) with these eight neighbors, and 2  $G$ 's and 2  $F$ 's with the four nearest neighbors.

The stereoscopic drawing shown in Fig. 6 illustrates the  $Br^-$  ion tetrahedra forming the two spirals of different chirality. These spirals are the only paths that will allow  $Cu^+$  ions to move in the  $c$ -direction. Figure 7 is a stereoscopic drawing depicting the "spiral routes" by means of the equilibrium  $Cu^+$  ion sites only. The most effective routes, in terms of  $Cu^+$  ion site designations, are: right-handed,  $5 \rightarrow 6 \rightarrow 7 \rightarrow 8 \rightarrow 9 \rightarrow 10 \rightarrow 1 \rightarrow 2 \rightarrow 3 \rightarrow 4 \rightarrow 5 \dots$ ; left-handed,  $11 \rightarrow 12 \rightarrow 8 \rightarrow 7 \rightarrow 6 \rightarrow 1 \rightarrow 2 \rightarrow 3 \rightarrow 13 \rightarrow 11 \dots$ . Of these the more probable is the latter; it contains 9 as opposed to 10 sites per increment and three as opposed to four highly occupied sites per increment of the former.

The stereoscopic drawing in Fig. 8 shows the surroundings of the  $Py^+$  rings. The rings in each pair ( $Py1$  and  $Py2$ ) are approximately parallel (a *small* resemblance to the arrangement in  $PyCl$  (35)).  $Py1$  is approximately parallel to the (distorted) hexagon of  $Br^-$  ions, 2, 5, 1, 5, 3, 6 nearby;  $Py2$  is at an angle to the symmetry-related  $Br^-$  ion hexagon nearby.  $Py1$  has 13  $Br^-$  ion near neighbors and  $Py2$

has 12  $Br^-$  ion near neighbors. Although C and N have not been distinguished in the refinement, the best candidates for the N atom are C1 of  $Py1$  and A2 of  $Py2$ , because of the particular way the  $Br^-$  ions surrounding the  $Py^+$  ions are arranged (see also Ref. (3)).

### Further Discussion

The average conductivity of  $Py_2Cu_3Br_7$  reported by Skarstad and Parker (18) is  $0.017 (\Omega \text{ cm})^{-1}$  at  $292^\circ K$ . We intend to measure the directional conductivity of  $Py_2Cu_3Br_7$ .<sup>10</sup> We can predict from the observations given above that the conductivity in the  $b$ -direction will be *somewhat* higher than that in the  $a$ -direction, and that the conductivity in the  $c$ -direction will be *substantially* lower than that in the  $a$ -direction.

The total number of  $Cu^+$  ion sites in the unit cell is 52; the total number of  $Cu^+$  ions in the unit cell is 20, giving a ratio of 2.6 available sites per mobile carrier. This is even lower than the lowest for any of the  $AgI$ -based solid electrolytes of which the structures have been determined. The lowest is 3.06 for  $Py_5Ag_{18}I_{23}$  (7, 9). The average conductivity, 0.008 (3) or

<sup>10</sup> Some time will elapse before we have the required crystals which we intend to grow by the Czochralski technique (18).

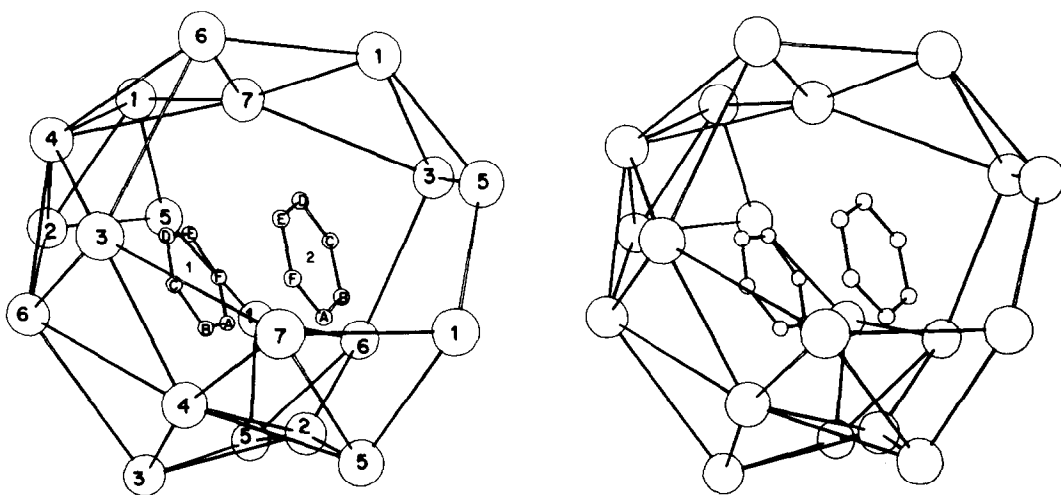


FIG. 8. Stereoscopic drawing showing  $Br^-$  ion arrangement about two independent  $Py^+$  ions in  $Py_2Cu_3Br_7$ .

0.011 (11) ( $\Omega \text{ cm}$ )<sup>-1</sup>, of  $\text{Py}_5\text{Ag}_{18}\text{I}_{23}$  is comparable with that of  $\text{Py}_2\text{Cu}_5\text{Br}_7$ , but that of the former is lower, probably mainly because it is only a two-dimensional solid electrolyte.

The volumes of the  $\text{Br}^-$  tetrahedra calculated by assuming the individual tetrahedron to be formed by the positions of the Br nuclei are listed in Table III. The total volume occupied by the  $\text{Br}^-$  ion tetrahedra per unit cell is 436.8  $\text{\AA}^3$ , which is only 20.2% of the unit cell volume. This is very low relative to the lowest observed, 31.6%, again that of  $\text{Py}_5\text{Ag}_{18}\text{I}_{23}$ . This result could also support the thesis that a three-dimensional solid electrolyte is apt to be better than a two-dimensional one, even when the other parameters are not as favorable. The carrier concentrations of  $\text{Py}_2\text{Cu}_5\text{Br}_7$  and  $\text{Py}_5\text{Ag}_{18}\text{I}_{23}$  (7, 9) are 0.92 and  $0.89 \times 10^{22}$ , respectively, and the site concentrations are 2.40 and  $2.72 \times 10^{22}$ , respectively.

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