

## Electrical Conductivity in Calcium Titanate\*

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The electrical conductivity of polycrystalline  $\text{CaTiO}_3$  was measured over the temperature range 800–1100°C while in thermodynamic equilibrium with oxygen partial pressures from  $10^{-22}$  to  $10^0$  atm. The data were found to be proportional to the  $-1/6$ th power of the oxygen partial pressure for the oxygen pressure range  $10^{-16}$ – $10^{-22}$  atm, proportional to  $P_{\text{O}_2}^{1/4}$  for the oxygen pressure range  $10^{-8}$ – $10^{-15}$  atm, and proportional to  $P_{\text{O}_2}^{+1/4}$  for the oxygen pressure range greater than  $10^{-4}$  atm. The region of linearity where the electrical conductivity varies as  $-1/4$ th power of  $P_{\text{O}_2}$  increased as the temperature was decreased. The observed data are consistent with the presence of small amounts of acceptor impurities in  $\text{CaTiO}_3$ . The band-gap energy (extrapolated to zero temperature) was estimated to be 3.46 eV.

### Introduction

In view of the important role played by alkaline earth titanates in ferroelectric and ferromagnetic phenomena, a brief investigation of the electrical properties of polycrystalline calcium titanate prepared by the liquid mix technique was carried out.  $\text{CaTiO}_3$  has an orthorhombic structure at room temperature (1), and the structure becomes tetragonal at 600°C and cubic at 1000°C (2). From the optical density studies on single-crystal  $\text{CaTiO}_3$ , Linz and Herrington (3) determined the band-gap energy of 3.4 eV (at 0°K). They found that the absorption characteristics are quite similar to those of  $\text{SrTiO}_3$  with the exception that the absorptions are shifted to shorter wavelengths.

Cox and Tredgold (4) measured the electrical conductivity of single-crystal  $\text{CaTiO}_3$  at 130°C and reported to be p-type, presumably after exposure to oxidizing atmo-

spheres. Thermopower measurement also indicated that electron holes are the majority carriers. It should be pointed out that the conductivity measurements at 130°C may not be reliable—the conductivity of the oxidized material must be less than  $10^{-10}$  ohm $^{-1}$  cm $^{-1}$ . George and Grace (5) examined the electrical conductivity and Seebeck coefficient of  $\text{CaTiO}_3$  in water-hydrogen atmospheres from 1100 to 1300°C. They concluded that an oxygen vacancy model was applicable to their results. George and Grace (6) investigated the diffusion of point defects in  $\text{CaTiO}_3$ . The reported studies on  $\text{CaTiO}_3$  indicate that there is an extensive range of low oxygen partial pressures ( $P_{\text{O}_2}$ ), where the conductivity increases with decreasing  $P_{\text{O}_2}$ , characteristic of n-type conduction related to oxygen deficiency. Walters and Grace (7) studied the electrical conductivity and Seebeck coefficient of  $\text{SrTiO}_3$  in damp hydrogen mixtures for a narrow range of oxygen partial pressure. Recently Balachan-

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dran and Eror (8) investigated the electrical conductivity of polycrystalline  $\text{SrTiO}_3$  in the  $P_{\text{O}_2}$  range of  $10^0$  to  $10^{-22}$  atm and temperature range of 800 to  $1050^\circ\text{C}$ . The structural analog  $\text{BaTiO}_3$  has been studied in much detail in both the polycrystalline (9–14) and single-crystal (15) states. All these studies on  $\text{BaTiO}_3$  and  $\text{SrTiO}_3$  indicate that in the  $P_{\text{O}_2}$  range near 1 atm, the conductivity increases with increasing  $P_{\text{O}_2}$ , characteristic of p-type conduction related to a stoichiometric excess of oxygen.  $\text{CaTiO}_3$ , however, has not been studied at elevated temperatures while in equilibrium with  $P_{\text{O}_2}$  near 1 atm.

In the present study, the high-temperature equilibrium electrical conductivity of polycrystalline  $\text{CaTiO}_3$  has been measured as a function of  $P_{\text{O}_2}$  in the range  $10^0$ – $10^{-22}$  atm. By matching the observed electrical characteristics to specific defect models the predominant defect structures are identified.

### Experimental

The specimens employed in this investigation were prepared by a liquid mix technique (16, 17). Required amounts of calcium carbonate (Mallinckrodt Chemical Works) and tetraisopropyl titanate solution (Tyzor, Dupont Co.) were dissolved in an ethylene glycol–citric acid solution. There was no evidence of any precipitation in the solutions as they were evaporated to a rigid transparent, uniformly colored polymeric glass. The glass retains homogeneity on an atomic scale and was calcined at  $900^\circ\text{C}$ —there was no evidence of a second phase in the as-calcined samples. These powder samples were pressed into thin circular disks (1.2 cm in diameter and 0.1 cm thick) under a load of 40,000 psi, and sintered in air at  $1350^\circ\text{C}$  for 12 hr. The density of the sintered disks was 94% of the theoretical density. Conductivity specimens were cut from this sintered disk using an airbrasive

unit. The specimens were wrapped with four 0.025-cm platinum wires as described in the literature (18, 19). Small notches were cut in the edges of the sample to aid in holding the platinum wires in place.

A conventional four-probe direct-current technique was employed for all electrical conductivity measurements. The four platinum leads were insulated from one another by recrystallized high-purity alumina insulators. A standard taper Pyrex joint to which capillary tubes had been sealed was mounted on top of the furnace reaction tube assembly. The platinum wires exited through the capillary tubes and were glass sealed vacuum tight into the tubes.

The oxygen partial pressures surrounding the samples were controlled by flowing metered mixtures of gases past the sample. The gases were oxygen, compressed air, argon with known amounts of oxygen,  $\text{CO}_2/\text{CO}$  mixtures, and  $\text{CO}_2/\text{H}_2$  mixtures. The error in volumetric ratio measurements of  $\text{CO}_2/\text{CO}$  mixtures resulted in an error of about 1% in the  $P_{\text{O}_2}$  value reported here. The conductivity was measured as a function of  $P_{\text{O}_2}$  in the temperature range  $800$ – $1100^\circ\text{C}$ . The conductivity was determined by measuring the voltage across the potential probes using a high-impedance ( $>10^{10}$  ohm) digital voltmeter (Keithley 191 Digital Multimeter). The current was supplied between the two outer leads by a constant-current source (Keithley 225 current source). The voltage was measured with the current in both forward and reverse directions, and the conductivity was calculated from the average values. After each variation of the gas atmosphere surrounding the sample the conductivity was measured as it changed to the new equilibrium value. The process of change in conductivity was recorded and if the conductivity no longer changed, it was assumed that the state of equilibrium had been attained. This state proved to be attainable reversibly from higher or lower oxygen partial pres-

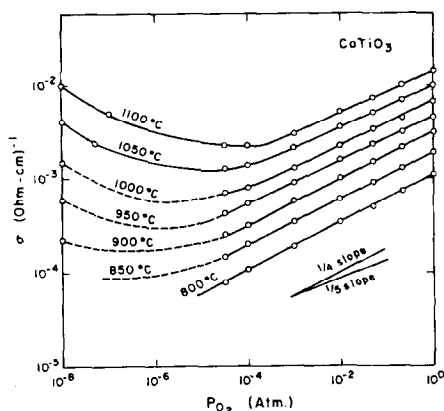


FIG. 1. The electrical conductivity of polycrystalline  $\text{CaTiO}_3$  as a function of oxygen partial pressure at constant temperature, from  $10^{-8}$  to  $10^0$  atm.

tures. Equilibrium was established as fast as the oxygen pressure could be changed from one value to another (which is usually less than 15 min). Current was varied from  $20 \mu\text{A}$  to 1 mA and no significant change in electrical conductivity was observed. Changing the ratio of the surface area to the volume by varying the size and geometry of the samples produced no detectable difference in the measured conductivity which indicated that the measured quantity was the bulk conductivity.

### Results and Discussion

The electrical conductivity of polycrystalline  $\text{CaTiO}_3$  in the temperature range  $800$ – $1100^\circ\text{C}$  and in equilibrium with oxygen partial pressures between  $10^{-8}$  and  $10^0$  atm is shown in Fig. 1. As can be seen, the conductivity shifts from p-type to n-type as  $P_{\text{O}_2}$  is decreased. The n-type electrical conductivity of  $\text{CaTiO}_3$  was extended to lower oxygen partial pressures by employing  $\text{CO}/\text{CO}_2$  and  $\text{H}_2/\text{CO}_2$  mixtures. The oxygen pressure dependence for conductivity changed from  $-1/4$ th to  $-1/6$ th power as the  $P_{\text{O}_2}$  is decreased in the n-type region and the different regions are treated separately in the following text.

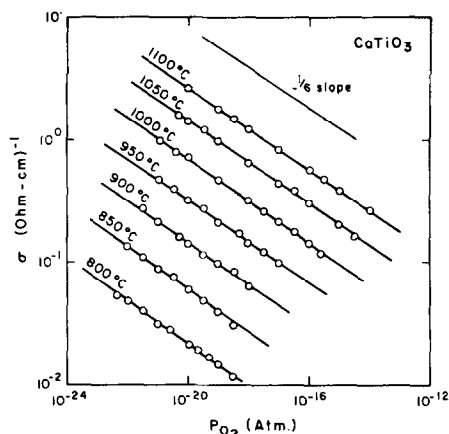


FIG. 2. The electrical conductivity of polycrystalline  $\text{CaTiO}_3$  as a function of oxygen partial pressure at constant temperature, from  $10^{-22}$  to  $10^{-18}$  atm.

#### Region I ( $P_{\text{O}_2} = 10^{-22}$ – $10^{-18}$ atm)

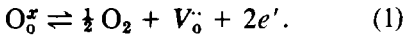
The variation of the electrical conductivity with oxygen partial pressure in this region is given in Fig. 2. The  $\log \sigma$  vs  $\log P_{\text{O}_2}$  data (see Fig. 2) are linear for as many as six decades of oxygen partial pressure for a given temperature (above  $1000^\circ\text{C}$ ) and linear for four decades of  $P_{\text{O}_2}$  for temperatures in the range  $800$ – $950^\circ\text{C}$ . This extensive region of linearity affords the opportunity to determine the defect model responsible for the n-type electrical conductivity in this region. A slope of approximately  $-1/6$  is found for the  $\log \sigma$  vs  $\log P_{\text{O}_2}$  data (see Table I). This slope is similar to that found for  $\text{BaTiO}_3$  (12–15) and  $\text{SrTiO}_3$  (7, 8), as well as to the results of George and Grace (5) for single-crystal  $\text{CaTiO}_3$  in the temperature range  $1100$ – $1300^\circ\text{C}$  and  $P_{\text{H}_2\text{O}}/P_{\text{H}_2}$  ratios from  $2 \times 10^{-4}$  to  $8 \times 10^{-2}$ .

The variation of the electrical conductivity with the oxygen partial pressure is calculated in terms of the oxygen vacancy defect model. The basis for the calculation is the reaction that represents the formation of a doubly ionized oxygen vacancy [ $V_{\text{O}}^{\bullet\bullet}$ ] and two electrons available for conduction by the removal of an oxygen from a normal

TABLE I  
 $P_{O_2}$  DEPENDENCE OF  
 CONDUCTIVITY IN THE REGION  
 $10^{-22}$ – $10^{-16}$  atm

$T$ (°C)	$m$ for $\sigma_n \propto P_{O_2}^{-1/m}$
800	5.90
850	5.95
900	5.95
950	6.04
1000	5.95
1050	5.95
1100	5.90

lattice site into the gas phase. The reaction is



The equilibrium constant for reaction (1) is

$$K_1 \equiv [V_o^{\cdot\cdot}] [n]^2 P_{O_2}^{1/2} = \exp\left(\frac{-\Delta G_f}{RT}\right), \quad (2)$$

where  $[n] \equiv [e']$ . With two electrons resulting from each oxygen vacancy, it follows that

$$[n] \equiv 2 [V_o^{\cdot\cdot}]. \quad (3)$$

Expressing the free energy change in terms of the enthalpy change,  $\Delta H_f$ , and entropy change,  $\Delta S_f$ , and substituting Eq. (3) into Eq. (2), the result for the electron concentration is

$$[n] = 2^{1/3} P_{O_2}^{-1/6} \exp\left[\frac{\Delta S_f}{3R}\right] \exp\left[\frac{-\Delta H_f}{3RT}\right], \quad (4)$$

and the electrical conductivity,  $\sigma$ , is given by

$$\sigma = 2^{1/3} P_{O_2}^{-1/6} e^\mu \exp\left[\frac{\Delta S_f}{3R}\right] \exp\left[\frac{-\Delta H_f}{3RT}\right], \quad (5)$$

where  $e$  is the electronic charge, and  $\mu$  is the mobility of the conduction electrons. At constant temperature, assuming that the mobility is independent of the change in concentration of oxygen vacancies, a plot

of the logarithm of the electrical conductivity vs the logarithm of the  $P_{O_2}$  should result in a straight line with a slope of  $-1/6$ . The data in Fig. 2 and Table I are in good agreement with the predicted  $-1/6$  dependence.

An indication of the magnitude of  $\Delta H_f$ , the enthalpy of the oxygen extraction reaction, Eq. (1), is typically obtained from Arrhenius plots of the conductivity, as deduced from Eq. (5). This procedure neglects contributions from the temperature dependences of the carrier mobility or density of states. The values of  $\Delta H_f$  calculated from the slope of the Arrhenius plots in Fig. 3 are listed in Table II. An average value of 5.99 eV (138.18 kcal/mole) is estimated for  $\Delta H_f$ . George and Grace (5) obtained a value of 6.55 eV. Balachandran and Eror (8) determined a value for  $\Delta H_f$  of 4.85 eV for polycrystalline SrTiO<sub>3</sub> in this region. It must be pointed out, however, that in view of the lack of knowledge regarding the temperature dependence of the electron mobility, such estimation of the value of  $\Delta H_f$  must be taken with caution. No anomalous behavior is observed while

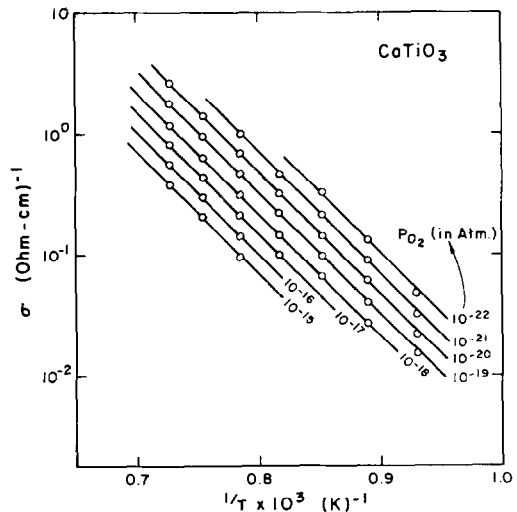


FIG. 3. Temperature dependence of electrical conductivity in polycrystalline CaTiO<sub>3</sub> in the  $P_{O_2}$  region  $10^{-22}$ – $10^{-15}$  atm.

TABLE II  
ACTIVATION ENTHALPIES FOR  
CONDUCTION IN THE REGION  
10<sup>-22</sup>–10<sup>-16</sup> atm

$P_{O_2}$ (atm)	Activation enthalpy (kcal/mole)
10 <sup>-22</sup>	137.19
10 <sup>-21</sup>	138.90
10 <sup>-20</sup>	138.90
10 <sup>-19</sup>	137.30
10 <sup>-18</sup>	137.30
10 <sup>-17</sup>	138.80
10 <sup>-16</sup>	138.90

measuring the electrical conductivity in the temperature range 800–1100°C, indicating that the tetragonal to cubic phase transition at ~1000°C has apparently no effect on the measured conductivity at these temperatures.

#### Region II ( $P_{O_2} = 10^{-8}$ – $10^{-15}$ atm)

A slope of ~1/4 is found for the log  $\sigma$  vs log  $P_{O_2}$  data (Fig. 4). Balachandran and Eror (8) observed a slope of approximately -1/4 from their log  $\sigma$  vs log  $P_{O_2}$  plot for SrTiO<sub>3</sub> in the  $P_{O_2}$  range 10<sup>-8</sup>–10<sup>-15</sup> atm and attributed it to the presence of small amounts of unknown acceptor impurities in the undoped SrTiO<sub>3</sub> sample. For the case of undoped BaTiO<sub>3</sub> prepared by the same technique as that used here, Chan and Smyth (14) reported a net acceptor impurities about 130 ppm (atomic). They proposed that all undoped material (BaTiO<sub>3</sub>) studied to date had a net excess of acceptor impurities, and attributed this to the fact that potential acceptor elements are naturally much more abundant than potential donor elements. We believe that our samples also contained some unknown acceptor impurities.

In discussing the concept of the impurity effect, it is helpful to consider a Kröger-Vink (20) diagram for a ternary oxide of the type  $ABO_3$  with an acceptor impu-

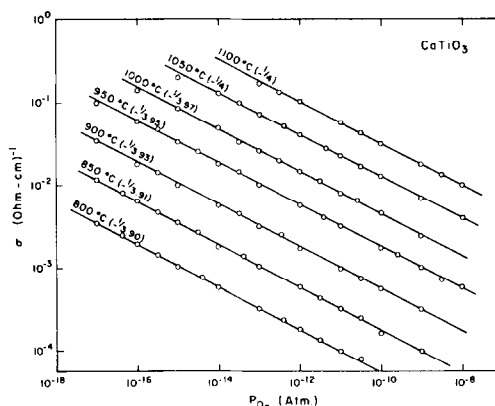


FIG. 4. The electrical conductivity of polycrystalline CaTiO<sub>3</sub> as a function of oxygen partial pressure at constant temperature, from 10<sup>-17</sup> to 10<sup>-8</sup> atm.

urity. We will, for the purpose of illustration, consider Schottky-Wagner disorder to describe the nonstoichiometry. Figure 5 illustrates the variation of defect concentrations as a function of oxygen partial pressure for the case of fully ionized atomic defects, electrons [ $n$ ], and electron holes [ $p$ ] in a pure ternary oxide  $ABO_3$  with both  $A$  and  $B$  site vacancies. It is assumed that the  $A$  and  $B$  content of the oxide is constant. Complete thermodynamic definition of a ternary oxide in equilibrium with only one crystal component, e.g., oxygen, requires the specification of three thermodynamic variables according to the phase rule. If both cationic species are sufficiently nonvolatile, the atomic ratio of the cations,  $A/B$ , whether known, or unknown but assumed constant, can be considered adequate in addition to temperature and total pressure while equilibrating with oxygen (21). The familiar [ $n$ ]  $\propto P_{O_2}^{-1/6}$  in the region with charge neutrality condition [ $n$ ]  $\approx 2[V'_O]$  is illustrated in Fig. 5. In Fig. 6, an acceptor impurity,  $I_m$ , is added that is always fully ionized,  $I_m$ , to the ternary oxide  $ABO_3$ . In Fig. 6 note that for sufficient departures from stoichiometry it may be possible for the electrical conductivity to be controlled by [ $n$ ]  $\approx 2[V'_O]$  and to thereby mask the

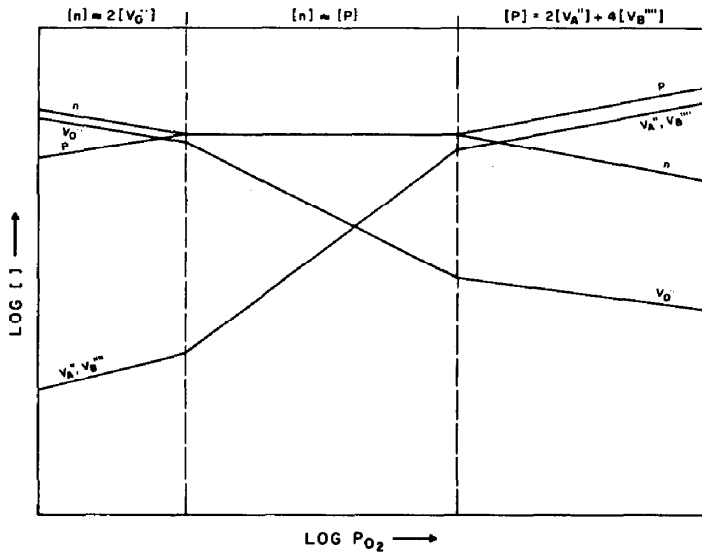


FIG. 5. Defect concentration vs the oxygen pressure in the ternary oxide of the type  $ABO_3$  with Schottky-Wagner disorder.

effect of the acceptor impurity. The two major points to be derived from Fig. 6 are that the electronic  $n$  to  $p$  transition has been shifted to lower oxygen partial pressures and the metal-excess to metal-deficit transition has been shifted to higher oxygen par-

tial pressures when an acceptor impurity is added to  $ABO_3$ .

In Fig. 6, there is a region with electrical neutrality condition  $[I_m'] \approx 2[V_O^•]$  in which the electron concentration varies as the  $-1/4$ th power and the electron hole con-

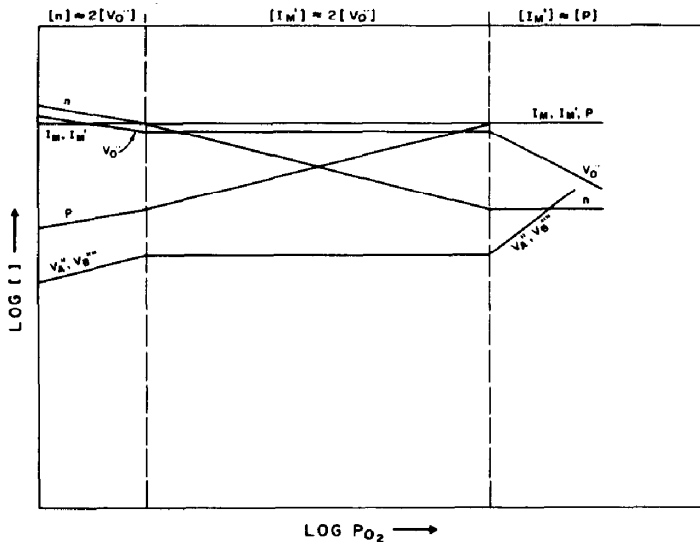


FIG. 6. Logarithm of the defect concentration for the ternary oxide  $ABO_3$  with a fully ionized acceptor impurity,  $I_m$ , and Schottky-Wagner disorder as a function of logarithm of oxygen pressure.

centration increases as the +1/4th power of oxygen partial pressure. In this region, for certain values of  $P_{O_2}$ , the electron concentration is greater than electron hole concentration and, hence, the conductivity is n-type with a  $-1/4$ th dependence on  $P_{O_2}$ . As the oxygen partial pressure increases, the electron hole concentration becomes greater than the electron concentration after a certain value of  $P_{O_2}$  and the material becomes p-type with a  $+1/4$ th dependence for conductivity on  $P_{O_2}$ . When the  $P_{O_2}$  value is increased further, the electron hole concentration becomes equal to the acceptor concentration, which is constant, and, hence, the electrical conductivity is independent of  $P_{O_2}$ , with the charge neutrality condition  $[I'_m] \approx [p]$  as shown in Fig. 6.

The observed slope of  $\sim -1/4$  from the  $\log \sigma$  vs  $\log P_{O_2}$  data (Fig. 4) in this region of  $P_{O_2}$  is interpreted in terms of the presence of accidental acceptor impurities, such as Fe, Al, or Cr on Ti sites. Thus, the condition of charge neutrality in this region can be

$$[I'_m] \approx 2 [V'_o]. \quad (6)$$

With this neutrality condition and Eqs. (1) and (2), the electrical conductivity varies with oxygen partial pressure as shown in

$$\sigma = 2^{1/2} \frac{1}{[I'_m]^{1/2}} P_{O_2}^{-1/4} e \mu \times \exp\left[\frac{\Delta S_f}{2R}\right] \exp\left[\frac{-\Delta H_f}{2RT}\right]. \quad (7)$$

The slopes of the lines drawn in Fig. 4 are in excellent agreement with the predicted value of  $-1/4$  by the above impurity model. The activation enthalpies of conduction derived from the Arrhenius slopes (see Fig. 7) are shown in Table III. An average value of 5.16 eV (118.90 kcal/mole) is estimated for this region.

#### Transition Region

Becker and Frederikse (22) showed that

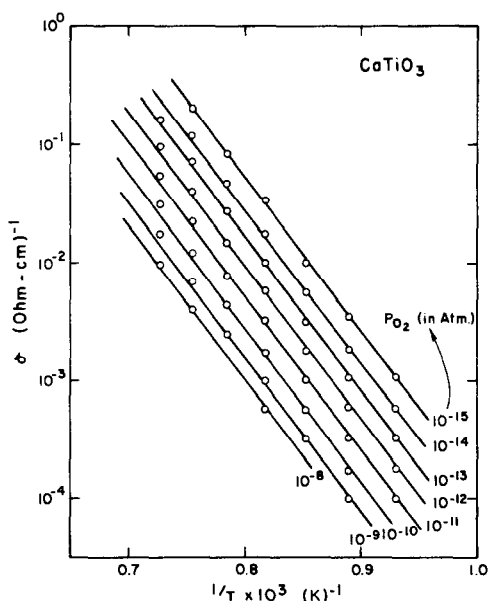


FIG. 7. Temperature dependence of conductivity of polycrystalline CaTiO<sub>3</sub> in the  $P_{O_2}$  region  $10^{-15}$ – $10^{-8}$  atm.

the band-gap energy (extrapolated to zero temperature) of a semiconductor which exhibits a p to n transition may be determined from the Arrhenius plots of the conductivity minima. The  $\log \sigma_{\min}$  vs  $1/T$  data in Fig. 8 indicate a value  $E_g^0 = 3.46$  eV (79.79 kcal/mole) as the band gap for the polycrystalline CaTiO<sub>3</sub> extrapolated to 0°K.

TABLE III  
ACTIVATION ENTHALPIES FOR  
CONDUCTION IN THE REGION  
 $10^{-15}$ – $10^{-8}$  atm

$P_{O_2}$ (atm)	Activation enthalpy (kcal/mole)
$10^{-15}$	118.90
$10^{-14}$	117.75
$10^{-13}$	120.61
$10^{-12}$	118.90
$10^{-11}$	118.30
$10^{-10}$	118.90
$10^{-9}$	118.90
$10^{-8}$	118.90

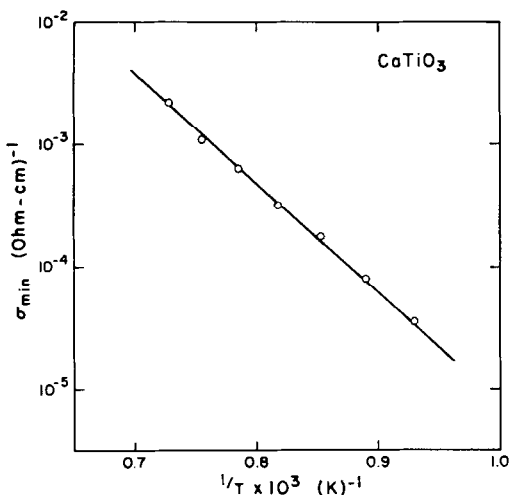


Fig. 8. Temperature dependence of the conductivity minimum of polycrystalline  $\text{CaTiO}_3$ .

This is in good agreement with the range of values 3.2–3.4 eV reported from optical absorption data (3, 4, 23) on single-crystalline  $\text{CaTiO}_3$ . Extrapolation was used to obtain a continuous plot for the  $\log \sigma$  vs  $\log P_{\text{O}_2}$  data in the entire oxygen partial pressure range used in this work and from these plots the conductivity minima in the temperature range 800–1000°C were obtained. Frederikse *et al.* (24) found a band-type conduction process in the structural analog  $\text{SrTiO}_3$ . Assuming a band-type conduction model for  $\text{CaTiO}_3$ , the full expression for the  $\log \sigma_{\text{min}}$  vs  $1/T$  plot is

$$\frac{\partial \ln \sigma_{\text{min}}}{\partial (RT)^{-1}} = \frac{\partial}{\partial (RT)^{-1}} \left[ \frac{\ln \mu_n \mu_p}{2} + \ln N_c N_v \right] - \frac{E_g^\circ}{2}, \quad (8)$$

where  $N_c$  and  $N_v$  are the density of states near the conduction and valence band edges, respectively. Assuming that the temperature dependence of the mobilities is the same for electrons and electron holes, and if both  $N_c$  and  $N_v$  are proportional to  $T^{+3/2}$ , mobility and density of state terms cancel each other, and the Arrhenius slope is directly proportional to  $E_g^\circ$ .

#### *p*-Type Region ( $P_{\text{O}_2} > 10^{-4}$ atm)

The conductivity data obtained in the range  $10^{-8} < P_{\text{O}_2} < 1$  atm are shown in Fig. 1. The conductivity in the region of  $P_{\text{O}_2}$  greater than  $10^{-4}$  atm increases with increasing oxygen partial pressure, indicative of *p*-type, or oxygen-excess, conductivity. The region of linearity in the *p*-type region increases in width with decreasing temperature as the *p*-*n* transition moves to lower  $P_{\text{O}_2}$ . The slopes of the oxygen pressure dependence for conductivity given in Table IV indicate that the values are tending toward 1/4 with decreasing temperature where the range of linearity is greatest. Arrhenius plots of the data at constant oxygen pressure are shown in Fig. 9, and the activation enthalpies of conduction derived from the slopes are given in Table V. A value of about 2.16 eV (49.84 kcal/mole) appears to be typical. Balachandran and Eror (8) obtained a value of 1.59 eV (36.7 kcal/mole) in the *p*-type region for  $\text{SrTiO}_3$ .

It is apparent that a stoichiometric excess of oxygen can be incorporated into the  $\text{CaTiO}_3$  lattice by a remarkably favorable process. In contrast to the value of 2.16 eV obtained in this work, enthalpies of oxygen addition for a large number of rare earth and alkaline earth oxides are of the order of 3–6 eV (25).

It has been shown in  $\text{BaTiO}_3$  (11, 14, 15)

TABLE IV  
 $P_{\text{O}_2}$  DEPENDENCE OF  
CONDUCTIVITY FOR THE *p*-TYPE  
REGION

$T$ (°C)	$m$ for $\sigma_p \propto P_{\text{O}_2}^{+1/m}$
800	4.00
850	4.05
900	4.00
950	4.20
1000	4.28
1050	4.50
1100	4.50



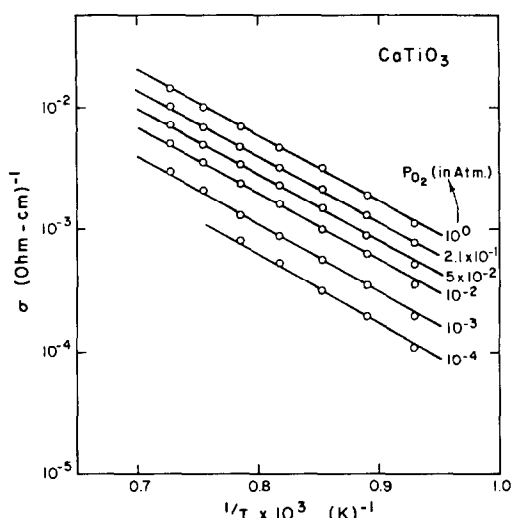
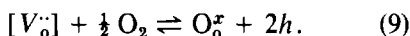


FIG. 9. Temperature dependence of the conductivity of polycrystalline CaTiO<sub>3</sub>, in the p-type region.

and SrTiO<sub>3</sub> (8) that the p-type conductivity arises from the incorporation of oxygen into the impurity-related oxygen vacancies, where the reaction is



The condition of charge neutrality in the near-stoichiometric region is the same as that observed in region II, i.e.,

$$[I_m] \approx 2 [V_o^{\cdot\cdot}].$$

The chemical mass action expression for Eq. (9) is

$$\begin{aligned} \frac{[p]^2}{[V_o^{\cdot\cdot}]} &= K_9 P_{O_2}^{1/2} \\ &= K_9' P_{O_2}^{1/2} \exp\left(\frac{-\Delta H_p}{RT}\right). \quad (10) \end{aligned}$$

Combination of Eq. (6) with Eq. (10) gives

$$\begin{aligned} [p] &= \left(\frac{K_9' [I_m]}{2}\right)^{1/2} \\ &P_{O_2}^{1/4} \exp\left(\frac{-\Delta H_p}{2RT}\right). \quad (11) \end{aligned}$$

This gives

$$\sigma \propto P_{O_2}^{1/4} \quad (12)$$

TABLE V  
ACTIVATION ENTHALPIES FOR  
CONDUCTION IN THE p-TYPE REGION

$P_{O_2}$ (atm)	Activation enthalpies (kcal/mole)
10 <sup>0</sup>	49.84
2.1 × 10 <sup>-1</sup>	50.30
5.0 × 10 <sup>-2</sup>	49.16
10 <sup>-2</sup>	49.16
10 <sup>-3</sup>	50.30
10 <sup>-4</sup>	50.30

as observed, as long as only a minor fraction of the impurity-related  $V_o^{\cdot\cdot}$  is filled. The trend toward shallower slopes at higher temperatures represents an intrusion of the transition region leading to the conductivity minima which are moving toward higher  $P_{O_2}$  with increasing temperature. The ready availability of oxygen vacancies explains the unusual ease with which the material accepts a stoichiometric excess of oxygen.

The estimated acceptor impurity in our sample is approximately 400 ppm. These impurities and their charge-compensating partner,  $V_o^{\cdot\cdot}$ , dominate the charge neutrality condition in a wide range of  $P_{O_2}$  ( $>10^{-16}$  atm). Impurity-insensitive behavior is observed in the range of lowest  $P_{O_2}$ , where the electrical conductivity varies as  $P_{O_2}^{-1/6}$ .

The pressure and temperature dependences, as well as the absolute values of the electrical conductivity, obtained in this study agree very well with the values (at 1100°C) reported by George and Grace (5) in single-crystal CaTiO<sub>3</sub> in the impurity-insensitive region. This agreement between the polycrystalline sample used in this investigation and the single crystal used by George and Grace (5) indicates that grain boundaries have no significant effect on the electronic transport in this range of experimental conditions, even though the grain boundaries often play an important role in determining the physical properties of polar

crystalline solids at ordinary temperatures (26).

### Conclusions

The experimental results agree well with the predictions based on the doubly ionized oxygen vacancy defect model, Eq. (1), at the lowest  $P_{O_2}$  and temperature range 800–1100°C. The  $P_{O_2}$  region in which the doubly ionized oxygen vacancies are dominant defects becomes narrow as the temperature is decreased. The logarithm of the electrical conductivity is a linear function of the logarithm of  $P_{O_2}$  at constant temperature with a slope of  $-1/6$  and this agrees with the predicted value.

The defect chemistry of undoped  $CaTiO_3$  is dominated by accidental acceptor impurities and their related oxygen vacancies, Eq. (6), for  $P_{O_2} > 10^{-16}$  atm. Because of the acceptor impurities, a region in which the conductivity varies as the  $-1/4$ th power of oxygen partial pressure is observed. Intrinsic ionic disorder never plays a significant role because of the high ionic charges and the lack of suitable interstitial sites. The band gap is sufficiently high (3.46 eV) to keep intrinsic electronic disorder below the net acceptor impurity content of the material.

The p-type behavior observed in the region  $P_{O_2} > 10^{-4}$  atm results from incorporation of oxygen into the impurity-related oxygen vacancies, Eq. (9). The ready availability of oxygen vacancies results in low enthalpy for the oxygen incorporation reaction.

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