

## Phase Relationships in the Systems $MS-Cr_2S_3-In_2S_3$ ( $M = Co, Cd, Hg$ )

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The phase diagrams of the quaternary systems  $MS-Cr_2S_3-In_2S_3$ , with  $M = Co, Cd$ , and  $Hg$ , were studied with the help of X-ray powder photographs of quenched samples, high-temperature X-ray diffraction patterns, DTA and TG measurements, and far-infrared spectra. Because indium sulfides do react with silica tubes, alumina crucibles must be used for annealing the samples. Complete series of mixed crystals are formed among the spinel-type compounds  $MCr_2S_4$ ,  $MIn_2S_4$  ( $M = Cd, Hg$ ), and  $In_2S_3$ .  $HgIn_2S_4$  is decomposed at temperatures above  $300^\circ C$ . In the sections  $CoCr_2S_4-CoIn_2S_4$  and  $CoCr_2S_4-In_2S_3$  relatively large miscibility gaps exist due to the change from normal to inverse spinel structure. But the interchangeability of both systems increases with increasing temperature, and at temperatures above  $1000^\circ C$ , complete series of solid solutions are formed, which can be quenched to ambient temperature. Superstructure ordering like that of ordered  $\alpha-In_2S_3$  has been found in the In-rich region of the  $MIn_2S_4-In_2S_3$  solid solutions. The unit cell dimensions of all stoichiometric and phase boundary compounds, e.g.,  $Cd_{1.15}In_{1.9}S_4$ , including the chromium spinels  $MCr_2S_4$  ( $M = Mn, Zn$ ) and  $ZnCr_2Se_4$ , are given and discussed in terms of possible deviations from stoichiometry.

### Introduction

The phase diagrams of the three component systems  $MS-Cr_2S_3-In_2S_3$ , with  $M = Mn, Fe, Co, Cd$ , and  $Hg$ , exhibit as the only ternary compounds the sulfide spinels  $MCr_2S_4$  and  $MIn_2S_4$ . The spinel phases crystallize partly in the normal structure, viz.,  $MCr_2S_4$  and  $HgIn_2S_4$ , and partly in the inverse structure, viz.,  $MnIn_2S_4$ ,  $FeIn_2S_4$ , and  $CoIn_2S_4$  (1). Additionally it is known that solid solutions between the spinel-type ternary compounds and indium sulfide, which also crystallizes in spinel structure, are formed. But little work has been done with regard to the exact phase boundaries, the possible formation of superstructures due to cation ordering, and the transition from normal spinels to inverse structures.

Whereas the binary sulfides  $MS, Cr_2S_3$ ,

and  $In_2S_3$ , as well as the stoichiometric spinels, are well known in the literature, only the following quasi-binary sections of the ternary phase diagrams under discussion have been studied:  $Cr_2S_3-In_2S_3$  (2, 3),  $MCr_2S_4-MIn_2S_4$  with  $M = Mn$  (4, 5),  $Fe$  (5-7),  $Co$  (5), and  $Cd$  (3, 8), and  $MS-In_2S_3$  with  $M = Fe$  (9),  $Co$  (10, 11), and  $Cd$  (12, 13). In the present work we report on the phase equilibria in the quasi-binary sections  $MS-In_2S_3$ ,  $MCr_2S_4-MIn_2S_4$ , and  $MCr_2S_4-In_2S_3$  ( $M = Co, Cd, Hg$ ) and upon possible nonstoichiometry of chromium chalcide spinels.

### Experimental Methods

Starting materials were cadmium sulfide (Schuchardt), mercury sulfide (cinnabar; Merck), chromium sulfide (Alfa Products),

and indium sulfide (Fluka).  $CoS$ , i.e., a mixture of  $Co_9S_8$  and  $Co_{1-x}S$  with a  $Co/S$  ratio of 1:1, was made from the elements cobalt (Merck) and sulfur (99.999%; Fluka). The ternary spinels  $MCr_2S_4$  and  $MIn_2S_4$  were obtained from stoichiometric amounts of the binary sulfides at  $800^\circ C$ .

The binary (or ternary) sulfides were equilibrated by the following procedure. Mixtures of the powdered sulfides in various molar ratios were homogenized in an oscillating mill and pressed into pellets. Coarse pieces of the pellets were heated in sealed evacuated silica ampoules or in alumina crucibles inserted in silica ampoules first at  $600^\circ C$  for 10 days, then twice at the equilibrium temperature, e.g., at  $800^\circ C$ , for 4 days. After each heat treatment the sintered material was ground and again pressed to pellets. Finally the samples were quenched to ambient temperature.

The obtained samples were analyzed with X-ray Guinier powder technique, using  $CrK\alpha_1$  radiation. Quartz was used as a standard ( $SiO_2$ ,  $a_0 = 491.36$  and  $c_0 = 540.54$

pm). Lattice constants were calculated by the least-squares method. High-temperature X-ray diffraction patterns were obtained using an Enraf-Nonius Guinier Simon camera.

From most samples the infrared spectra were recorded on Beckman Model FS 720 or Bruker Model IFS 114 Fourier-transform interferometers using Nujol mulls. The thermogravimetric (TG, DTG) and DTA measurements were made in a vacuum using a thermoanalyzer Linseis L 62 and a thermobalance L 81.

## Results

### System $CdS-In_2S_3-Cr_2S_3$

In the quaternary system  $CdS-In_2S_3-Cr_2S_3$  complete series of spinel solid solutions are formed within the whole triangular region  $CdCr_2S_4-CdIn_2S_4-In_2S_3$  of the ternary phase diagram (see Fig. 1). In the regions  $CdS-CdCr_2S_4-CdIn_2S_4$  and  $CdCr_2S_4-In_2S_3-Cr_2S_3$  the system is mostly

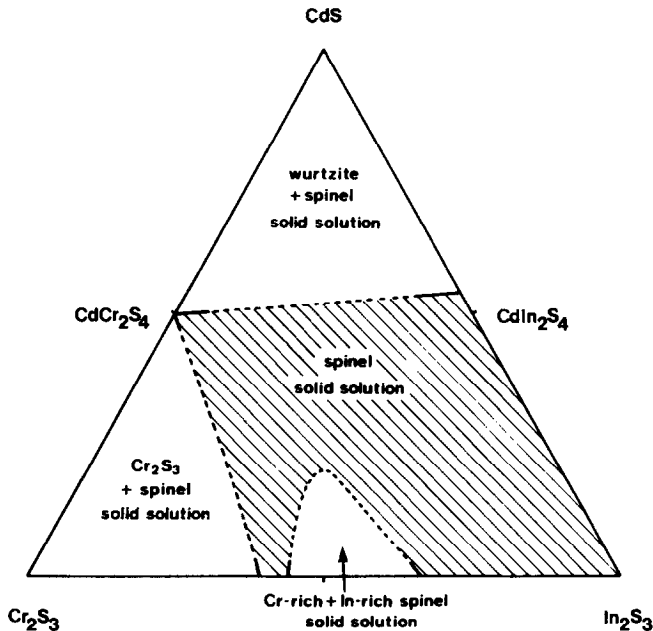


FIG. 1. Ternary phase diagram of the system  $CdS-In_2S_3-Cr_2S_3$  at  $800^\circ C$ .

two-phase. In the former region wurtzite-type and spinel-type solid solutions, and in the latter region two kinds of spinel-type or spinel-type and  $\text{Cr}_2\text{S}_3$  (2, 3, 8) mixed crystals coexist. These results were obtained from samples quenched from  $800^\circ\text{C}$ .

These studies, done some years ago, were complicated by the fact that indium sulfide spinels react with the wall of the silica tubes to form silicates of the metals present. This behavior, unknown in the literature so far, influenced the composition of the annealed samples. Therefore, the obtained results were not fully reproducible. After finding the reason for this trouble (see also Riedel and Karl (7), we reinvestigated the sections  $\text{CdS}-\text{In}_2\text{S}_3$ ,  $\text{CdCr}_2\text{S}_4-\text{CdIn}_2\text{S}_4$ , and  $\text{CdCr}_2\text{S}_4-\text{In}_2\text{S}_3$  using alumina crucibles, which do not react with indium chalcide spinels, inserted in silica ampoules as reacting capsules.

Our X-ray investigations indicate that Vegard's rule is obeyed in the section

$\text{CdCr}_2\text{S}_4-\text{CdIn}_2\text{S}_4$ , whereas in both the sections  $\text{CdCr}_2\text{S}_4-\text{In}_2\text{S}_3$  and  $\text{CdS}-\text{In}_2\text{S}_3$  Vegard's rule is not obeyed. This is also the case if the compositions of the solid solutions are taken as  $\text{Cd}_{1-x}\text{Cr}_{2-2x}\text{In}_{8x/3}\text{S}_4$  and  $\text{Cd}_{1-x}\text{In}_{2+2x/3}\text{S}_4$ , respectively. In particular the unit cell dimensions of the  $\text{In}_2\text{S}_3$ -rich solid solutions remain nearly unaffected by small cadmium and chromium concentrations. In the system  $\text{CdS}-\text{In}_2\text{S}_3$  the phase boundary of the spinel-type solid solutions has been found at a cadmium concentration which is larger than that given by the formula  $\text{CdIn}_2\text{S}_4$ . The obtained lattice constants are  $1084.5(1)$  pm in the case of pure  $\text{CdIn}_2\text{S}_4$  (13),  $1081.8$  (14) and  $1085.9(3)$  pm for the cadmium-richest mixed crystals of the approximate composition  $\text{Cd}_{1.15}\text{In}_{1.9}\text{S}_4$  (samples quenched from  $800^\circ\text{C}$ , see also (12, 15)).

#### System $\text{HgS}-\text{In}_2\text{S}_3-\text{Cr}_2\text{S}_3$

The phase relationships found in the qua-

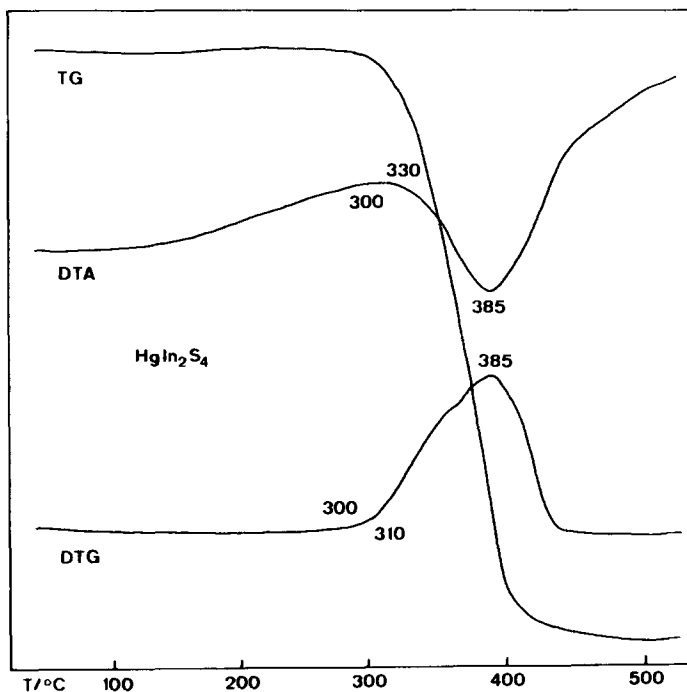


FIG. 2. Thermogram of  $\text{HgIn}_2\text{S}_4$  (vacuum, heating rate  $1^\circ\text{C}/\text{min}$ ).

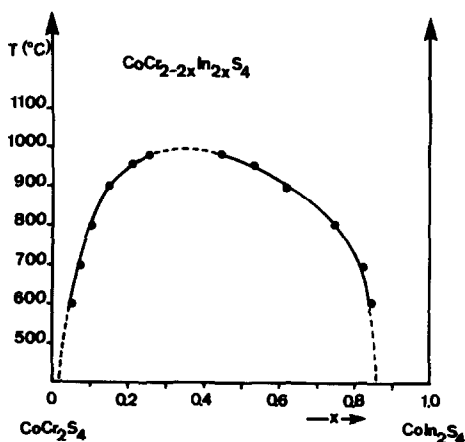


FIG. 3. Phase diagram of the quasi-binary system  $CoCr_2S_4-CoIn_2S_4$ .

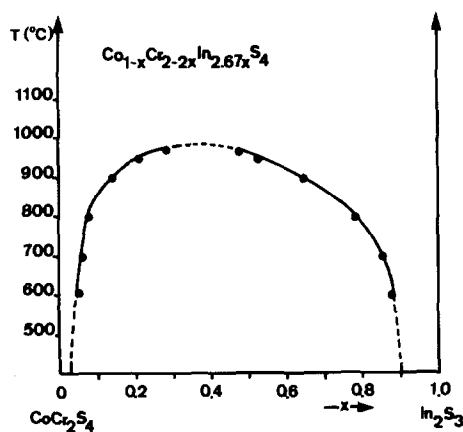


FIG. 4. Phase diagram of the system  $CoCr_2S_4-In_2S_3$ .

ternary system  $HgS-In_2S_3-Cr_2S_3$  are nearly equal to those of the corresponding cadmium sulfide system discussed above, i.e., complete series of spinel solid solutions are formed in the whole triangular region  $HgCr_2S_4-HgIn_2S_4-In_2S_3$  of the ternary phase diagram, but in the regions  $HgS-HgCr_2S_4-HgIn_2S_4$  and  $HgIn_2S_4-In_2S_3-Cr_2S_3$  the system is two-phase. In the section  $HgCr_2S_4-HgIn_2S_4$  Vegard's rule is obeyed. The unit cell dimensions of the stoichiometric  $HgIn_2S_4$  spinel have been

found to be 1085.3(1) pm (1083.3 pm (14)).

$HgIn_2S_4$  is thermally unstable. It decomposes at temperatures above 300°C, finally forming  $In_2S_3$ ,  $HgS$ , mercury, and sulfur (see Fig. 2) (16). Therefore, samples of  $HgIn_2S_4$  obtained by the usual procedure from silica ampoules are mostly not homogeneous. This is shown by the poor ir spectra of such samples (16), the occurrence of small amounts of elementary mercury, and the finding that the lattice constants of the remaining spinel-type compound are smaller than those given above.

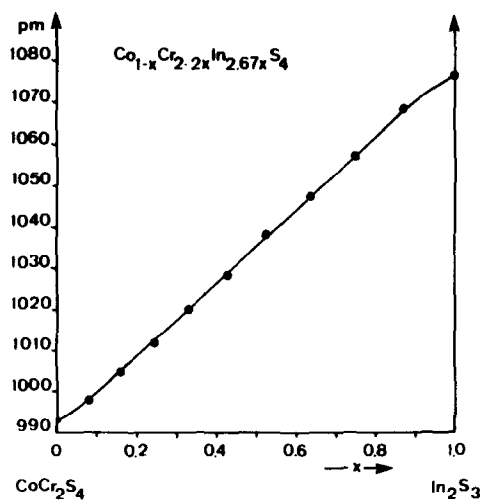
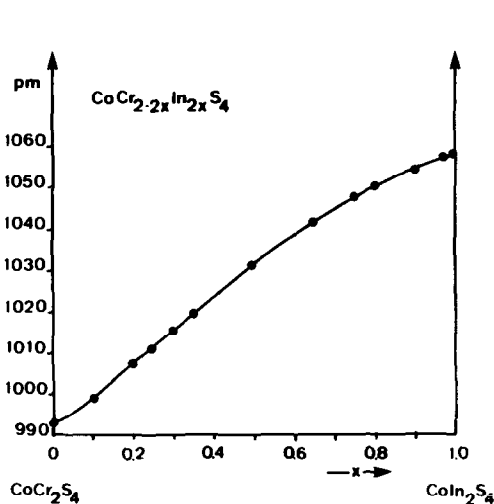


FIG. 5. Lattice constants of  $CoCr_{2-2x}In_{2x}S_4$  and  $Co_{1-x}Cr_{2-2x}In_{2.67x}S_4$  spinel-type solid solutions, quenched from 1050°C.

*Systems CoS–In<sub>2</sub>S<sub>3</sub>–Cr<sub>2</sub>S<sub>3</sub> and  
FeCr<sub>2</sub>S<sub>4</sub>–FeIn<sub>2</sub>S<sub>4</sub>*

The phase relationships of the quaternary system CoS–In<sub>2</sub>S<sub>3</sub>–Cr<sub>2</sub>S<sub>3</sub> differ from those discussed above. Whereas in the section CoIn<sub>2</sub>S<sub>4</sub>–In<sub>2</sub>S<sub>3</sub> a complete series of solid solutions has been found like in the corresponding systems with CdS and HgS, in both the systems CoCr<sub>2</sub>S<sub>4</sub>–CoIn<sub>2</sub>S<sub>4</sub> and CoCr<sub>2</sub>S<sub>4</sub>–In<sub>2</sub>S<sub>3</sub> relatively large miscibility gaps exist (see Figs. 3 and 4). The solubility limits of the Cr-rich solid solutions have been found to be CoCr<sub>1.89</sub>In<sub>0.11</sub>S<sub>4</sub> and Co<sub>0.96</sub>Cr<sub>1.92</sub>In<sub>0.11</sub>S<sub>4</sub>, respectively, and of the In-rich mixed crystals CoCr<sub>0.33</sub>In<sub>1.67</sub>S<sub>4</sub> and Co<sub>0.11</sub>Cr<sub>0.21</sub>In<sub>2.38</sub>S<sub>4</sub>, respectively, all at 600°C. But the mutual solid solubility of the two spinels increases with increasing temperature, as shown by high-temperature X-ray powder photographs. At temperatures above 1000°C complete series of mixed crystals are formed. The mixed crystals obtained at these temperatures can be quenched to ambient temperature without decomposition. We have some indications that the system FeCr<sub>2</sub>S<sub>4</sub>–FeIn<sub>2</sub>S<sub>4</sub> also exhibits a small miscibility gap near the composition FeCrInS<sub>4</sub> at 600°C.

From the X-ray studies it is shown that Vegard's rule is not obeyed for all sections under investigation (see Fig. 5). Thus the curve, lattice constants vs composition of the CoCr<sub>2</sub>S<sub>4</sub>–CoIn<sub>2</sub>S<sub>4</sub> solid solutions, is S-shaped with the steepest slope in the middle. The lattice constant of CoIn<sub>2</sub>S<sub>4</sub> has been determined to be 1057.8(1) pm (1058.0 pm (14)). Smaller unit cell dimensions also found are due to sulfur deficiency. Contrary to the CdS–In<sub>2</sub>S<sub>3</sub>–system, CoIn<sub>2</sub>S<sub>4</sub> is the Co-richest spinel in the section CoS–In<sub>2</sub>S<sub>3</sub>.

*Sections MS–Cr<sub>2</sub>S<sub>3</sub>*

In the systems MS–Cr<sub>2</sub>S<sub>3</sub> the solubility limits of both Cr<sub>2</sub>S<sub>3</sub> in MS and MS in Cr<sub>2</sub>S<sub>3</sub> are small (17). The same is said for the phase width of the ternary spinel-type com-

pounds MCr<sub>2</sub>S<sub>4</sub>. In this work we reinvestigated to what extent the composition of the spinels MCr<sub>2</sub>S<sub>4</sub>, with M = Mn, Zn, and Cd, and ZnCr<sub>2</sub>Se<sub>4</sub> can vary. In the case of MnCr<sub>2</sub>S<sub>4</sub> and ZnCr<sub>2</sub>S<sub>4</sub> no deviations from stoichiometry were found with the help of X-ray Guinier technique, i.e., alterations of the unit cell dimensions of samples prepared in the presence of excess MS, Cr<sub>2</sub>S<sub>3</sub>, M, or S<sub>8</sub> are found to be ≤0.1 pm. The lattice constants obtained are 1010.94(5) pm (1011.0 pm (14)) and 998.79(3) pm (998.6 pm (14)), respectively. CoCr<sub>2</sub>S<sub>4</sub>, CdCr<sub>2</sub>S<sub>4</sub>, and ZnCr<sub>2</sub>Se<sub>4</sub>, however, show some amount of nonstoichiometry detectable from X-ray powder photographs. The unit cell dimensions of these spinels vary from 991.5(1) to 992.4(1), from 1023.7(1) to 1024.3(1) (see also (18, 19)), and from 1049.7(1) to 1050.2(2) pm, respectively, depending on the method of preparation.

*Superstructure Ordering*

The X-ray powder photographs of the obtained solid solutions do not show any superstructure reflections due to ordering of the vacancies or metal ions on the tetrahedral or octahedral sites of the spinel lattice (20). The fir-spectra of the spinel solid solutions (see Fig. 6 and 7), however, indicate that superstructure ordering occurs to some extent, at least in the case of In<sub>2</sub>S<sub>3</sub>-rich samples in the systems MIn<sub>2</sub>S<sub>4</sub>–In<sub>2</sub>S<sub>3</sub> (see Fig. 6). The ordering of the vacancies seems to be like that of "ordered" α-In<sub>2</sub>S<sub>3</sub> (21), which, however, is obviously due to ordering on the tetrahedral sites and not on the octahedral sites as claimed by Kambas *et al.* (21).

**Discussion**

The miscibility gaps in the CoCr<sub>2</sub>S<sub>4</sub>–CoIn<sub>2</sub>S<sub>4</sub> and CoCr<sub>2</sub>S<sub>4</sub>–In<sub>2</sub>S<sub>3</sub> (and FeCr<sub>2</sub>S<sub>4</sub>–FeIn<sub>2</sub>S<sub>4</sub>) spinel systems unknown so far in the literature (5–7), but not in contradiction with the data reported, are probably

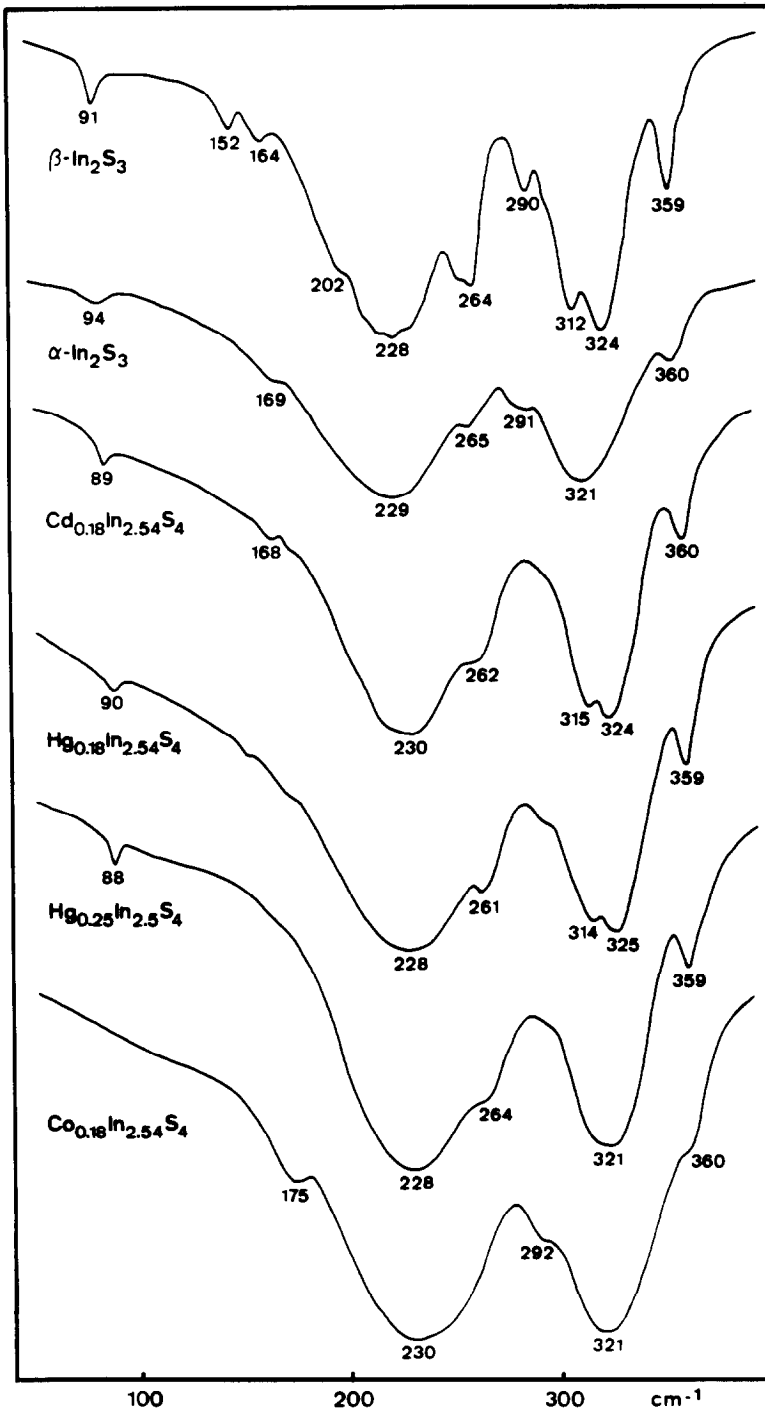


FIG. 6. Far-infrared spectra of  $\beta$ - and  $\alpha$ - $In_2S_3$ , i.e., with and without ordering of the vacancies, and of  $Cd_{1-x}In_{2+2x/3}S_4$  and  $Hg_{1-x}In_{2+2x/3}S_4$  solid solutions.

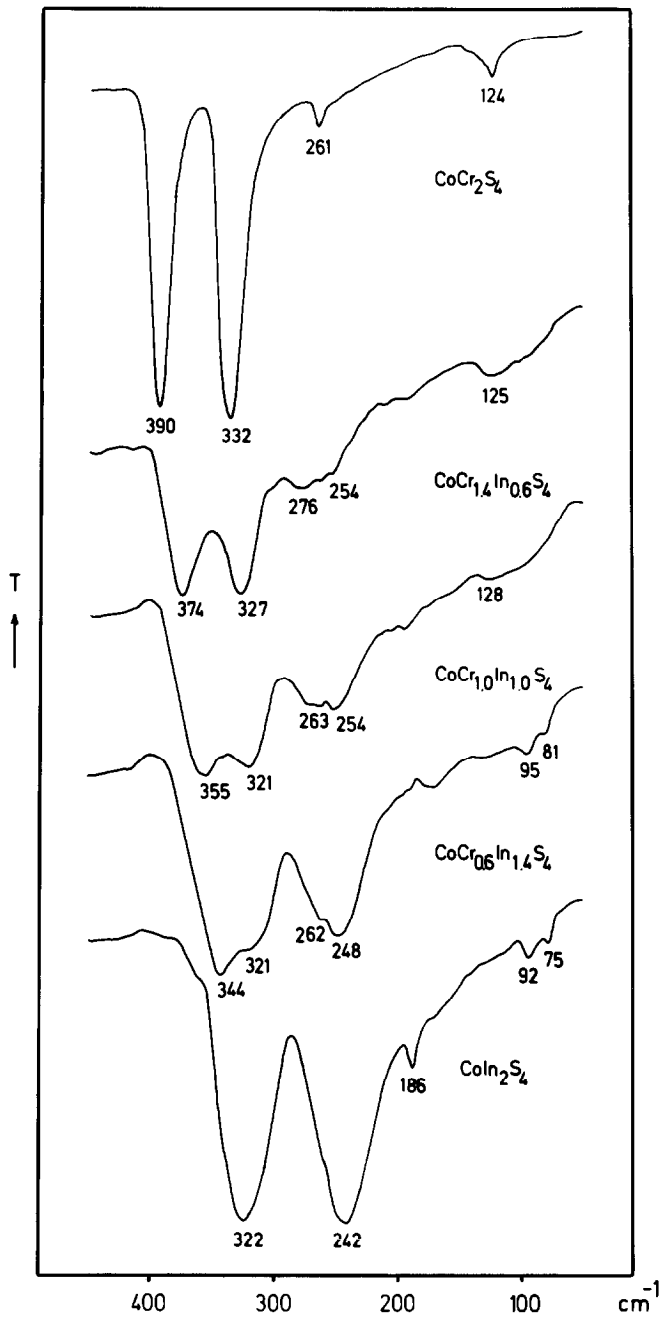


FIG. 7. Far-infrared spectra of  $\text{CoCr}_2\text{S}_4$ ,  $\text{CoIn}_2\text{S}_4$ , and  $\text{CoCr}_{2-x}\text{In}_x\text{S}_4$  solid solutions.

due to the different cation ordering of the chromium and the indium spinels, viz., the normal spinel,  $\text{CoCr}_2\text{S}_4$ , and the inverse spinel,  $\text{CoIn}_2\text{S}_4$ . Thus in the case of the cor-

responding systems with cadmium and mercury complete series of spinel solid solutions also exist at lower temperatures because both the chromium and the indium

compounds are normal spinels. We therefore assume that in the system  $MnCr_2S_4-MnIn_2S_4$  (4, 5), structurally similar to the  $CoCr_2S_4-CoIn_2S_4$  system, a miscibility gap is also present, at least at low temperatures.

The possible nonstoichiometry of some chromium spinels, as found in this work, must be borne in mind if using the unit cell dimensions as an analytical tool in determining the composition of spinel solid solutions.

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