

Preparation and Optical Properties of Europium-Activated Rare Earth Oxysulfates

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The rare earth oxysulfate series $Ln_2O_2SO_4$ ($Ln = La, Gd, Y$) was synthesized by two different thermal decomposition methods. The complex ion $(LnO)_n^{n+}$ existing in the structure of various oxysalts seems to have a major effect on the appearance of the spectra. Then it is possible to derive sets of crystal field parameters simulating the spectra, by using the $C_{4v} \rightarrow C_{2v}$ descending symmetry procedure. Moreover, an alternative method for determining these parameters is described when a C_{2v} point site symmetry is distorted from D_{3h} .

Introduction

Rare earth oxysulfates, described by Pitha *et al.* (1) in 1947 as thermal decomposition products of the corresponding anhydrous sulfates, have been recognized since then as possible intermediate products formed when sulfur-containing rare earth compounds are heated in air. They have been extensively studied mainly for their interesting physical properties, including their fluorescence spectra (2, 3). First report on their structure gave a tetragonal unit cell for $La_2O_2SO_4$ (4), but subsequent study by Ballestracci and Mareschal (5) revealed the crystal system to be orthorhombic.

The unit cell parameters were determined for all lanthanoids including yttrium and they showed isostructurality (5) in con-

trast to the powder patterns published at the same time elsewhere for the lanthanum and gadolinium compounds (2). Ballestracci and Mareschal were also able to prepare single crystals suitable for X-ray study and to find out the main structural feature of these compounds: $La_2O_2SO_4$ has a $(LnO)_n^{n+}$ -type layer structure similar to that found, for example, in $La_2O_2MoO_4$ (6) and $LnOCl$ (7). The authors also noted the distortion of the sulfate groups, visible also in the ir spectra. All other details, including distances and angles, were left unreported, however, and a refinement of the structure has not yet appeared.

Recently, Fahey determined the structure of $La_2O_2SO_4$ from X-ray powder diffraction data (8). The body-centered orthorhombic cell ($a = 4.2861$, $b = 4.1938$, $c = 13.720$ Å) was confirmed and the space

group chosen was *I222*. The refinement of the structure, using, however, constrained symmetry for the sulfate group, showed that the lanthanum atom is coordinated by four oxygen anions from the $(LnO)_n^{n+}$ layer and by two oxygens from different sulfate groups. The $Ln-O$ distances are 2.40 and 2.41 Å in the $(LnO)_n^{n+}$ layer and 2.36 Å when sulfate oxygens are involved. The point symmetry around lanthanum is C_2 .

The present investigation was undertaken in order to study the symmetry and structure of the rare earth oxysulfates by using Eu^{3+} as an optical probe (9) and to compare the results obtained with available X-ray diffraction and ir data. Special emphasis was placed on the preparation of samples of good purity and crystallinity. Finally, a crystal field analysis was performed for the Eu^{3+} -doped lanthanum, gadolinium, and yttrium oxysulfates.

Materials and Methods

Preparation of the samples. The europium-activated (1%) oxysulfates were prepared by two different methods both employing thermal decomposition in air as the final step but differing essentially otherwise. In both cases the obtained products were checked by chemical analysis and X-ray diffraction. The starting materials were 99.99% rare earth oxides.

The sulfite method. Coprecipitation of two rare earth sulfite hydrates, viz., the activator and the host, offers a convenient initial step in the preparation of luminescent solid solutions. The method has been applied to the preparation of the activated oxysulfites and it has been described earlier by one of us (10).

In the case of the oxysulfates, the first step was also the coprecipitation of the sulfites but afterwards the heat treatment was performed in air. Under these conditions, dehydration takes place between 150 and 300°C and decomposition to oxysulfate be-

tween 500 and 750°C; the temperatures depend on the rare earth, heating rate, etc. (11, 12). It should also be noted that the stability range for the oxysulfate phase formed is limited, especially for the heavier lanthanoids and yttrium, and it may easily decompose further to oxide both in air and in an inert atmosphere (12, 13).

The use of cation exchange resins. Dowex 50W-X8 resin beds in H^+ form were loaded by placing them in a 0.1 M HCl solution containing the activator and host lanthanoid as chlorides. The quantity of the rare earth mixture used was less than that calculated to saturate the resin beds.

Thermal decomposition conditions were chosen after several preliminary tests (further details of this preparation are given in Ref. (9)). Based on these tests and literature data (13), heating 48 hr at 650°C was adopted for yttrium-loaded resins, while 48 hr at 850°C was employed for the resins containing lanthanum and gadolinium. The heating rate in all cases was 2°C/min up to the required temperature; afterwards a slow free cooling to room temperature was applied.

Under these conditions, the final products were found to be free of carbon and nonbound sulfur. Their crystallinity was also excellent and in the case of yttrium oxysulfate, better than with other methods. In the case of the lanthanum compounds, the sulfite method gave equally well crystallized products for gadolinium oxysulfate; the difference was not large either.

Fluorescence measurements. Fluorescence measurements were performed at 4.2, 77, and 300K on $Ln_2O_2SO_4$ ($Ln = La, Gd, Y$) samples doped with 1% of Eu^{3+} . The routine excitation is obtained by a 200-W mercury lamp equipped with a wide-band filter centered at about 3500 Å to select the mercury lines. The fluorescence emission is analyzed through a 1-m Jarell-Ash monochromator in the 4000- to 7200-Å-wavelength range. The signal is de-

tected by standard techniques. Moreover, in order to avoid the superposition of lines occurring from different emitting levels (${}^5D_1 \rightarrow {}^7F_3$ and ${}^5D_0 \rightarrow {}^7F_1$ for instance), it is possible to excite selectively the 5D_0 level by a tunable dye laser set on the ${}^5D_0 \rightarrow {}^7F_0$ transition. It is then possible to attribute unambiguously all the recorded lines.

Analysis of the Spectra

The three compounds studied fluoresce reasonably well. The reddish appearance

under uv excitation shows that the most intense transitions are those with 5D_0 as emitting level, especially the ${}^5D_0 \rightarrow {}^7F_2$ transition (Fig. 1). The complete recording of the spectra presents a large number of lines (approx. 50) assigned as ${}^5D_J (J = 0, 1) \rightarrow {}^7F_J (J = 0-4)$ (Table I). In these series the spectra are very similar: only slight modifications in the line positions indicate evolution of J level splitting. The average linewidth is about 0.5 \AA , except for the ${}^5D_0 \rightarrow {}^7F_2$ transition ($\approx 2 \text{ \AA}$).

Analysis of the spectra at different tem-

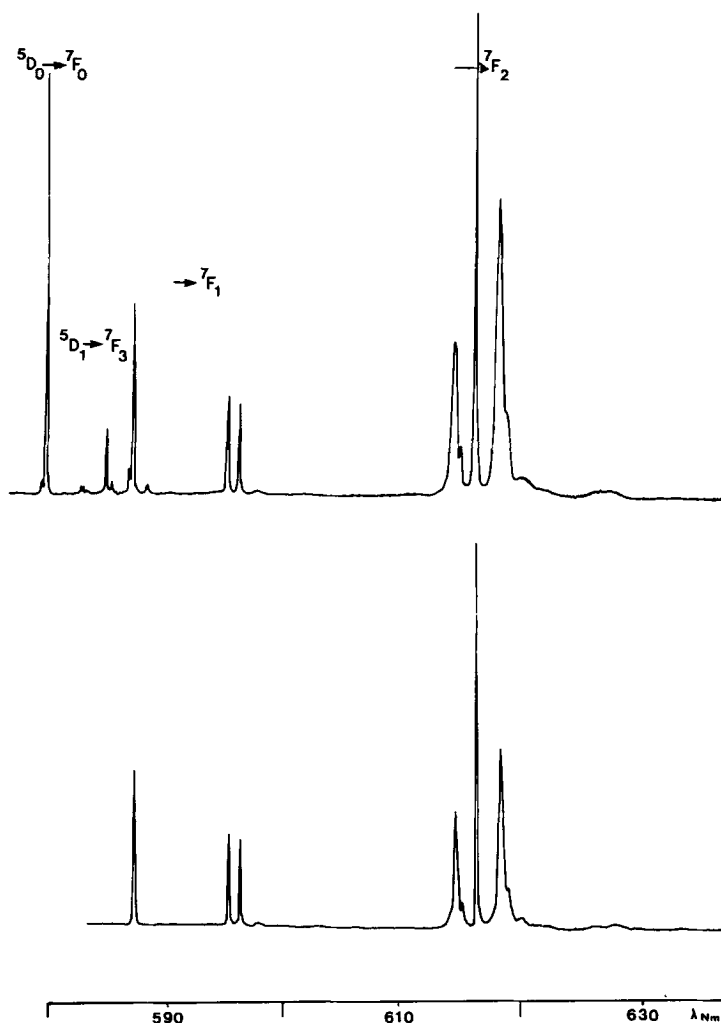


FIG. 1. Fluorescence spectra of $(\text{LaO})_2\text{SO}_4:\text{Eu}^{3+}$ at 77K under uv (top) and dye laser excitation.

TABLE I
 FLUORESCENCE TRANSITIONS OBSERVED AT 77K FOR
 (LnO)₂SO₄:Eu³⁺ (ALL UNITS IN cm⁻¹)

Assignment	(LaO) ₂ SO ₄ Eu ³⁺	(GdO) ₂ SO ₄ Eu ³⁺	(YO) ₂ SO ₄ Eu ³⁺
⁵ D ₁ → ⁷ F ₀	19,037		
	19,031		
	18,973	18,960	18,956
⁵ D ₁ → ⁷ F ₁	18,823	18,806	18,807
	18,816	18,792	18,792
	18,760	18,740	18,741
	18,594		
	18,587		
	18,564		18,525
	18,526	18,528	18,508
⁵ D ₁ → ⁷ F ₂	18,499	18,466	18,456
	18,057	18,061	18,056
	18,016	18,049	18,044
	18,011	18,032	18,027
	17,998	17,997	18,992
	17,982	17,981	17,974
	17,951	17,930	17,923
⁵ D ₀ → ⁷ F ₀	17,898	17,883	17,889
	17,258	17,240	17,237
⁵ D ₁ → ⁷ F ₃	17,176		
	17,169		
	17,161	17,157	17,155
	17,155	17,145	17,135
	17,110		
	17,097	17,094	17,087
	17,053	17,069	
	17,005		
	16,945		
	⁵ D ₀ → ⁷ F ₁	17,044	17,021
16,811		16,808	16,806
16,785		16,748	16,737
⁵ D ₀ → ⁷ F ₂	16,283	16,276	16,270
	16,268	16,263	16,257
	16,236	16,206	16,203
	16,184	16,161	16,157
⁵ D ₀ → ⁷ F ₃	15,398		
	15,385	15,369	15,368
	15,342	15,322	15,319
	15,291	15,288	15,286
	15,280	15,264	15,261
	15,256	15,232	15,225
	15,232	15,223	15,214
	14,529	14,509	14,502
⁵ D ₀ → ⁷ F ₄	14,415	14,406	14,411
	14,407	14,386	14,378
	14,356	14,340	14,335
	14,331	14,291	14,284
	14,272	14,256	14,253
	14,251	14,233	14,232
	14,227	14,204	14,200
	14,224	14,188	14,175

peratures underlines variations in the relative intensities of lines with different emitting levels. At 77 and 4K transitions from

⁵D₁ are relatively intense, but quite extinguished at room temperature. This fact must be related to an important nonradiative deexcitation between ⁵D₁ and ⁵D₀, largely depending on the temperature. By using the selective dye laser excitation, only fluorescence from ⁵D₀ is recorded, permitting the construction of a partial energy level scheme for the ⁷F_J (J = 0–4) ground multiplet.

By applying both group theory and electronic transition selection rules, it is possible to estimate the point symmetry of the site occupied by the rare earth. For the rare earth oxysulfate series, the ⁵D₀ → ⁷F₀ transitions are always extremely intense. Due to its existence, one can deduce that the point site symmetry is C_n, C_{nv}, or C_s. The analysis of other transitions shows that not only the degeneracy of the J levels is completely lifted, but that nearly all transitions between Stark levels are observed. Three lines for ⁵D₀ → ⁷F₁ (magnetic dipole transition), seven lines for ⁵D₀ → ⁷F₃, and nine lines for ⁵D₀ → ⁷F₄ (electric dipole transitions) do not permit a point site symmetry higher than C₂. The only difficulty is the ⁵D₀ → ⁷F₂ transition for which three very intense lines are observed, and a fourth with lower intensity; this transition appears to be accompanied by various broad and/or tiny lines, which remain under selective excitation. These lines probably have a vibronic origin; some of them may correspond to the ⁵D₀ → ⁷F₀ transition since the vibrations of the sulfate group are around 1000 cm⁻¹ (4). Others may be vibronics associated with the ⁵D₀ → ⁷F₂ transitions. Finally, the ⁷F₂ Stark levels can be determined by comparing this transition with ⁵D₁ → ⁷F₂, this one having a magnetic dipolar and nonhypersensitive character. In spite of this, it is not possible to estimate the position of the fifth ⁷F₂ Stark level. This is important, since its calculated position is completely different for the two simulating procedures used later.

Point Site Symmetry Considered for Simulation

Spectroscopic as well as crystallographic results show that the symmetry of the point site occupied by the rare earth is no higher than C_2 . Due to the relative poorness of the energy level scheme (24 Stark levels) deduced from the data, it is unreasonable to simulate the crystal field (C.F.) effect by considering the fourteen C_2 C.F. parameters. We shall consider a C_{2v} symmetry carrying only nine parameters. In spite of this approximation, it is unsatisfactory to conduct a realistic simulation, since the irreducible representations associated with each Stark level are not deduced from experiments on powder. Probably, several sets of C.F. parameters can simulate the spectrum accurately (14). On the other hand, the P.C.E.M. method does not constitute a convenient *ab initio* determination of the C.F. parameters, especially when complex ions like SO_4^{2-} exist in the structure. However, the spectroscopic results clearly show that the C_2 (or C_{2v}) symmetry of the point site is very close to a higher symmetry. We can therefore apply the descending symmetry procedure, by considering a relatively high symmetry for the point site, involving a few C.F. parameters, then adding extra parameters in order to take into account the lowering of symmetry. The remaining problem is the choice of the higher symmetry of the point site:

(a) A point symmetry with a pseudo-ternary axis appears from the structure, since, according to Fahey (8), the symmetry of the polyhedron surrounding the rare earth is not far from a trigonal prism, with D_{3h} as point symmetry. In this case, the C_2 axis corresponds to the (001) axis and the C_3 axis to the (110) of the structure.

(b) A point symmetry with a pseudo-quaternary axis is apparent from spectroscopy, and is supported by crystallographic arguments. The whole appearance of the

spectra and the energy level scheme distribution shows great analogy with other oxysalts, such as oxyhalides (15, 16), oxymolybdates (17), and oxycarbonates (18). This is due to the existence of the $(LnO)_n^{n+}$ complex cation (19) in all these compounds. Consequently, the higher symmetry could be C_{4v} with (001) as z axis.

Crystal Field Calculation

The $D_{3h} \rightarrow C_{2v}$ Case

The simplest way to describe a C.F. potential is to choose a reference axis system for which the z axis corresponds to the highest symmetry axis. It is, however, always possible to describe this potential by referring to any axis system of the space. For instance, the classical way to describe a D_{3h} potential is to consider the ternary axis as z axis. The x, y axes are then fixed, except the rotation around z . Consequently, the number of nonzero C.F. parameters is four, according to the group transformation properties of D_{3h} . We can also express the same C.F. potential by referring to a C_2 axis, also existing in the point group, and orthogonal to C_3 . In such a case the C.F. potential is described as C_{2v} by nine parameters, only four of them being independent. The respective Hamiltonians are written as

$$\begin{aligned}
 {}^H D_{3h} &= B_0^2 C_0^2 + B_0^4 C_0^4 \\
 &\quad + B_0^6 C_0^6 + B_6^6 (C_{-6}^6 + C_6^6), \\
 {}^H C_{2v} &= B_0^2 C_0^2 + B_2^2 (C_{-2}^2 + C_2^2) + B_0^4 C_0^4 \\
 &\quad + B_2^4 (C_{-2}^4 + C_2^4) + B_4^4 (C_{-4}^4 + C_4^4) + B_0^6 C_0^6 \\
 &\quad + B_2^6 (C_{-2}^6 + C_2^6) + B_4^6 (C_{-4}^6 + C_4^6) \\
 &\quad + B_6^6 (C_{-6}^6 + C_6^6).
 \end{aligned}$$

In order to find the relation between these two sets of parameters, we consider that under a rotation of the reference axis system, the "new" spherical harmonics should be written as a linear combination of

TABLE II
TRANSFORMATION MATRICES TO EXPRESS THE C_q^k OPERATORS
IN A C_{2v} SYMMETRY FROM A D_{3h} SYMMETRY (THE C_q^k , $q \neq 0$,
AND 6, ARE EQUAL TO ZERO FOR THE D_{3h} SYMMETRY)

$$\begin{array}{l}
 \begin{bmatrix} C_0^2 \\ C_2^2 \end{bmatrix} = \begin{bmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{\sqrt{2}} \\ -\frac{\sqrt{3}}{2\sqrt{2}} & \frac{1}{2} \end{bmatrix} \times \begin{bmatrix} C_0^2 \\ C_2^2 \end{bmatrix} \\
 \\
 \begin{bmatrix} C_0^4 \\ C_2^4 \\ C_4^4 \end{bmatrix} = \begin{bmatrix} \frac{3}{8} & \frac{\sqrt{10}}{4} & \frac{\sqrt{70}}{8} \\ \frac{\sqrt{5}}{4\sqrt{2}} & \frac{1}{2} & -\frac{\sqrt{7}}{4} \\ \frac{\sqrt{35}}{8\sqrt{2}} & -\frac{\sqrt{7}}{4} & \frac{1}{8} \end{bmatrix} \times \begin{bmatrix} C_0^4 \\ C_2^4 \\ C_4^4 \end{bmatrix} \\
 \\
 \begin{bmatrix} C_0^6 \\ C_2^6 \\ C_4^6 \\ C_6^6 \end{bmatrix} = \begin{bmatrix} -\frac{5}{16} & -\frac{\sqrt{105}}{16} & -\frac{3\sqrt{14}}{16} & -\frac{\sqrt{231}}{16} \\ -\frac{\sqrt{105}}{32} & -\frac{17}{32} & -\frac{\sqrt{30}}{32} & -\frac{3\sqrt{220}}{64} \\ -\frac{3\sqrt{7}}{16\sqrt{2}} & -\frac{\sqrt{30}}{32} & \frac{13}{16} & -\frac{\sqrt{66}}{32} \\ -\frac{\sqrt{231}}{32} & \frac{3\sqrt{220}}{64} & -\frac{\sqrt{66}}{32} & \frac{1}{32} \end{bmatrix} \times \begin{bmatrix} C_0^6 \\ C_2^6 \\ C_4^6 \\ C_6^6 \end{bmatrix}
 \end{array}$$

the "old" ones of the same rank,

$$C_q^k \xrightarrow{\text{Rot}} C_{q'}^k = \sum_q a_q C_q^k.$$

For this study we constructed the transformation matrix $D_{3h} \rightarrow C_{2v}$ (Table II) by using the quantitative expression of tensorial operators as given in Prather's monograph (20).

For D_{3h} , determination of the set of C.F. parameters is carried out rapidly since the 7F_1 splitting mainly depends on B_0^2 and the 7F_2 splitting on B_0^2 and B_0^4 . The precise calculation of the parameters is performed by minimizing the rms deviation $\sigma = \left(\frac{\sum \sigma_i^2}{N - P} \right)^{1/2}$, where σ_i is the individual

error, N the number of levels, and P the number of parameters involved. Table III shows the result. As expected, the rms is unsatisfactory (around 20 cm^{-1}). Moreover, the sign B_0^6 is not determined. Change in this sign does not modify the energy positions, but permutes the label of the A_1'' and A_2'' irreducible representations. This is why two starting parameter sets are considered for C_{2v} .

When C_{2v} symmetry is considered, the simulation is also carried out rapidly. Finally, the C.F. parameters are close to expected values of the D_{3h} point group described along the C_2 axis. However, the rms is rather poor, and it is impossible to choose the best set. The list of simulated energy levels is presented in Table IV. It is noteworthy that the nonobserved 7F_2 Stark

TABLE III
CRYSTAL FIELD PARAMETERS FOR THE $D_{3h} \rightarrow C_{2v}$ DESCENDING SYMMETRY OF THE
OXYSULFATE SERIES

Parameter	D_{3h}		C_{2v}	
	Along C_3 axis	Equivalent values C_2 axis sign +:sign -	Set 1 from sign +	Set 2 from sign -
1 B_0^2	$-830. \pm 23.$	415.	$455. \pm 13.$	$412. \pm 14.$
B_2^2		508.	$468. \pm 9.$	$486. \pm 10.$
B_0^4	$793. \pm 29.$	297.	$172. \pm 23.$	$670. \pm 24.$
B_2^4		313.	$485. \pm 16.$	$352. \pm 17.$
B_4^4		415.	$564. \pm 13.$	$421. \pm 14.$
B_0^6	$537. \pm 37.$	$-792. : 457.$	$-441. \pm 33.$	$294. \pm 28.$
B_2^6		$285. : -629.$	$462. \pm 18.$	$-509. \pm 18.$
B_4^6		$-355. : -22.$	$21. \pm 26.$	$320. \pm 18.$
B_6^6	$\pm 657. \pm 22.$	$-234. : -275.$	$-151. \pm 18.$	$-162. \pm 27.$
σ	21.		11.5	13.
2 B_0^2	$-878. \pm 24.$	439.	$532. \pm 14.$	$519. \pm 15.$
B_2^2		538.	$448. \pm 11.$	$472. \pm 11.$
B_0^4	$-752. \pm 31.$	282.	$188. \pm 24.$	$536. \pm 28.$
B_2^4		297.	$379. \pm 17.$	$280. \pm 19.$
B_4^4		393.	$494. \pm 16.$	$425. \pm 16.$
B_0^6	$579. \pm 37.$	$-791. : +429.$	$-823. \pm 30.$	$231. \pm 34.$
B_2^6		$261. : -632.$	$320. \pm 19.$	$-521. \pm 19.$
B_4^6		$-366. : -40.$	$86. \pm 17.$	$361. \pm 21.$
B_6^6	$\pm 642. \pm 24.$	$-255. : -295.$	$-254. \pm 20.$	$-324. \pm 18.$
σ	22.		13.	15.
3 B_0^2	$-881. \pm 25.$	440.	$564. \pm 14.$	$548. \pm 14.$
B_2^2		539.	$473. \pm 11.$	$471. \pm 11.$
B_0^4	$756. \pm 32.$	284.	$442. \pm 23.$	$534. \pm 26.$
B_2^4		299.	$159. \pm 20.$	$261. \pm 18.$
B_4^4		395.	$490. \pm 17.$	$447. \pm 15.$
B_0^6	$573. \pm 39.$	$-801. : 443.$	$-872. \pm 29.$	$223. \pm 32.$
B_2^6		$272. : -638.$	$262. \pm 25.$	$-531. \pm 18.$
B_4^6		$-367. : -36.$	$54. \pm 22.$	$389. \pm 20.$
B_6^6	$\pm 655. \pm 25.$	$-252. : -293.$	$-390. \pm 23.$	$-336. \pm 29.$
σ	22.		14.	14.

Note. 1 = $(LaO)_2SO_4$; 2 = $(GdO)_2SO_4$; 3 = $(YO)_2SO_4$.

level is the lowest, located at about 880 cm^{-1} .

The $C_{4v} \rightarrow C_{2v}$ Case

This possibility is simpler to analyze since the main symmetry axes are the

same. For C_{4v} the C.F. Hamiltonian is written as

$${}^H C_{4v} = B_0^2 C_0^2 + B_0^4 C_0^4 + B_4^4 (C_{-4}^4 + C_4^4) \\ + B_0^6 C_0^6 + B_4^6 (C_{-4}^6 + C_4^6).$$

Due to the great similarity of the energy level sequence of oxysulfates and oxyha-

TABLE IV
OBSERVED AND CALCULATED ENERGY LEVELS FOR Eu^{3+} EMBEDDED IN RARE EARTH OXYSULFATES. THE $D_{3h} \rightarrow C_{2v}$ CASE, (ALL UNITS IN cm^{-1})

(LaO) ₂ SO ₄ :Eu ³⁺												(YbO) ₂ SO ₄ :Eu ³⁺																
D_{3h}				C_{2v}				D_{3h}				C_{2v}				D_{3h}				C_{2v}								
Exp level	Calc	Irr rep		Calc	Irr rep	Exp level	Calc	Irr rep	Calc set.2	Irr rep		Calc	Irr rep	Exp level	Calc	Irr rep	Calc set.1	Irr rep	Calc set.2	Irr rep	Exp level	Calc	Irr rep	Calc set.1	Irr rep	Calc set.2	Irr rep	
0	0	A ₁ ⁺		0	A ₁ ⁺	0	0	A ₁ ⁺	0	A ₁ ⁺	0	0	A ₁ ⁺	0	0	A ₁ ⁺	0	A ₁ ⁺	0	A ₁ ⁺	0	0	A ₁ ⁺	0	A ₁ ⁺	0	A ₁ ⁺	
214	206	A ₂ ⁺		207	B ₂	219	201	A ₂ ⁺	210	A ₂ ⁺	216	202	A ₂ ⁺	216	202	A ₂ ⁺	205	B ₂	206	B ₂	206	206	B ₂	205	B ₂	206	B ₂	
447	464	E ⁺		452	B ₁	432	469	E ⁺	442	B ₁	431	472	E ⁺	444	B ₁	444	472	E ⁺	444	B ₁	446	B ₁	444	472	E ⁺	446	B ₁	
473	464	E ⁺		474	A ₂	492	469	A ₂	492	A ₂	500	472	E ⁺	496	A ₂	496	472	E ⁺	496	A ₂	496	496	A ₂	496	472	E ⁺	496	A ₂
975	872	A ₁ ⁺		849	A ₁	858	875	A ₁ ⁺	858	A ₁	863	876	A ₁ ⁺	866	A ₁	866	876	A ₁ ⁺	866	A ₁	864	864	A ₁	866	876	A ₁ ⁺	864	A ₁
990	982	E ⁺		983	A ₂	965	979	E ⁺	969	A ₂	967	979	E ⁺	969	A ₂	967	979	E ⁺	967	A ₂	960	960	A ₂	967	979	E ⁺	960	A ₂
1021	1050	E ⁺		988	B ₁	1006	979	B ₁	992	B ₁	980	979	B ₁	1001	B ₁	980	979	B ₁	989	B ₁	1003	1003	B ₁	989	979	B ₁	1003	B ₁
1075	1050	E ⁺		1017	B ₂	1024	1034	A ₁	1025	B ₂	1034	1034	A ₁	1030	A ₁	1034	1034	A ₁	1033	A ₁	1032	1032	A ₁	1033	1034	A ₁	1032	A ₁
1860	1891	E ⁺		1071	A ₁	1068	1079	B ₂	1069	A ₁	1080	1052	E ⁺	1065	B ₂	1080	1052	E ⁺	1071	B ₂	1070	1070	B ₂	1071	1070	B ₂	1070	B ₂
1873	1891	A ₂ ⁺ or A ₁ ⁺		1866	A ₁	1872	1895	E ⁺	1868	A ₁	1869	1895	E ⁺	1878	A ₁	1869	1895	E ⁺	1880	A ₁	1878	1878	A ₁	1880	1895	E ⁺	1878	A ₁
1916	1911	E ⁺		1884	B ₂	1892	1895	B ₂	1908	B ₂	1918	1895	B ₂	1905	B ₂	1918	1895	B ₂	1915	B ₂	1906	1906	B ₂	1915	1911	A ₂ ⁺ or A ₁ ⁺	1915	B ₂
1967	1944	E ⁺		1928	A ₂	1912	1943	A ₂	1925	A ₂	1918	1911	A ₂ ⁺ or A ₁ ⁺	1912	B ₁	1918	1911	A ₂ ⁺ or A ₁ ⁺	1922	A ₂	1911	1911	A ₂ ⁺ or A ₁ ⁺	1922	A ₂	1911	B ₁	
1978	1944	E ⁺		1943	B ₁	1954	1943	B ₁	1937	B ₁	1951	1945	E ⁺	1951	B ₁	1951	1945	E ⁺	1931	B ₁	1950	1950	B ₁	1931	1945	E ⁺	1950	B ₁
2002	1996	A ₂ ⁺		1974	B ₂	1967	1976	B ₂	1970	A ₂	1976	1943	E ⁺	1963	B ₂	1976	1943	E ⁺	1969	A ₂	1967	1967	A ₂	1969	1945	E ⁺	1967	A ₂
2026	2051	A ₁ ⁺ or A ₂ ⁺		1986	B ₂	1991	2008	B ₂	1995	B ₂	2008	1996	A ₂ ⁺	1993	B ₂	2012	1998	A ₂ ⁺	1996	B ₂	1996	1996	B ₂	1996	1996	B ₂	1996	B ₂
2729	2708	A ₂ ⁺ or A ₁ ⁺		2039	B ₁	2044	2017	A ₂	2050	A ₁ ⁺ or A ₂ ⁺	2023	2055	A ₁ ⁺ or A ₂ ⁺	2045	A ₂	2023	2055	A ₁ ⁺ or A ₂ ⁺	2051	B ₁	2049	2049	B ₁	2051	2051	B ₁	2049	A ₂
2843	2861	E ⁺		2724	A ₂	2721	2731	B ₁	2728	A ₂	2735	2718	A ₂ ⁺ or A ₁ ⁺	2729	B ₁	2735	2718	A ₂ ⁺ or A ₁ ⁺	2732	A ₂	2730	2730	B ₁	2732	A ₂	2730	B ₁	
2851	2861	E ⁺		2841	B ₂	2844	2834	B ₂	2844	A ₁	2826	2864	E ⁺	2839	A ₁	2826	2864	E ⁺	2842	A ₁	2830	2830	A ₁	2842	A ₁	2830	A ₁	
2902	2893	A ₁ ⁺ or A ₂ ⁺		2847	A ₁	2854	2854	A ₁	2859	B ₂	2859	2864	E ⁺	2872	B ₂	2859	2864	E ⁺	2863	B ₂	2877	2877	B ₂	2863	B ₂	2877	B ₂	
2927	2967	A ₁ ⁺		2889	B ₁	2891	2900	A ₂	2900	B ₁	2902	2900	A ₁ ⁺ or A ₂ ⁺	2894	B ₂	2902	2900	A ₁ ⁺ or A ₂ ⁺	2893	B ₁	2898	2898	A ₂	2893	B ₁	2898	A ₂	
2986	2980	E ⁺		2940	A ₁	2937	2949	A ₁	2941	A ₁	2953	2968	A ₁	2947	A ₁	2953	2968	A ₁	2945	A ₁	2950	2950	A ₁	2945	A ₁	2950	A ₁	
3007	2980	E ⁺		2986	B ₁	2990	2984	B ₁	2985	B ₁	2984	2985	E ⁺	2996	B ₁	2984	2985	E ⁺	2984	B ₁	2989	2989	B ₁	2984	B ₁	2989	B ₁	
3031	3030	E ⁺		3006	B ₂	3001	3007	A ₂	3004	A ₂	3005	2984	E ⁺	2996	A ₂	3005	2984	E ⁺	3000	A ₂	2996	2996	A ₂	3000	A ₂	2996	A ₂	
3034	3030	E ⁺		3029	A ₂	3022	3036	B ₂	3035	A ₁	3037	3037	E ⁺	3025	A ₂	3037	3036	E ⁺	3048	A ₁	3027	3027	B ₂	3048	A ₁	3027	B ₂	
				3043	A ₁	3051	3052	A ₁	3047	B ₂	3052	3037	E ⁺	3053	B ₂	3052	3037	E ⁺	3059	B ₂	3062	3062	A ₁	3059	B ₂	3062	A ₁	

TABLE V
CRYSTAL FIELD PARAMETERS FOR THE $C_{4v} \rightarrow C_{2v}$
DECREASING SYMMETRY OF THE OXYSULFATE
SERIES

1	B_0^0	$-993. \pm 18.$	$-981. \pm 9.$	$-991. \pm 16.$
	B_2^0		$\pm 117. \pm 7.$	$\pm 68. \pm 9.$
	B_4^0	$-687. \pm 22.$	$-651. \pm 12.$	$-674. \pm 19.$
	B_2^2		$\pm 258. \pm 10.$	$\pm 114. \pm 33.$
	B_4^2	$\pm 686. \pm 18.$	$-720. \pm 10.$	$685. \pm 15.$
	B_6^0	$702. \pm 30.$	$556. \pm 20.$	$675. \pm 27.$
	B_6^2		$\mp 120. \pm 22.$	$\mp 56. \pm 17.$
	B_6^4	$\pm 250. \pm 16.$	$-278. \pm 9.$	$250 \pm 15.$
	B_8^0		$\pm 25. \pm 13.$	$\mp 88. \pm 21.$
	σ	16.	8.	13.
2	B_0^0	$-967. \pm 20.$	$-968. \pm 9.$	$-960. \pm 9.$
	B_2^0		$\pm 195. \pm 6.$	$\pm 84. \pm 7.$
	B_4^0	$-716. \pm 23.$	$-783. \pm 11.$	$-707. \pm 12.$
	B_2^2		$\pm 348. \pm 12.$	$\pm 41 \pm 10.$
	B_4^2	$\pm 667. \pm 20.$	$-585. \pm 11.$	$650. \pm 10.$
	B_6^0	$733. \pm 32.$	$636. \pm 18.$	$714. \pm 19.$
	B_6^2		$\pm 187. \pm 34.$	$\pm 73. \pm 22.$
	B_6^4	$\pm 273. \pm 18.$	$-241. \pm 9.$	$278. \pm 9.$
	B_8^0		$\mp 27. \pm 15.$	$\mp 109. \pm 14.$
	σ	17.	7.2	12.
3	B_0^0	$-987. \pm 20.$	$-1007. \pm 9.$	$-983. \pm 15.$
	B_2^0		$\pm 204. \pm 5.$	$\pm 92. \pm 9.$
	B_4^0	$-723. \pm 24.$	$-784. \pm 10.$	$-710. \pm 18.$
	B_2^2		$\pm 348. \pm 11.$	$\pm 47. \pm 32.$
	B_4^2	$\pm 626. \pm 20.$	$-582. \pm 10.$	$617. \pm 15.$
	B_6^0	$669. \pm 35.$	$684. \pm 12.$	$655. \pm 25.$
	B_6^2		$\pm 192. \pm 31.$	$\mp 69. \pm 20.$
	B_6^4	$\pm 294. \pm 10.$	$-224. \pm 16.$	$300. \pm 14.$
	B_8^0		$\mp 49. \pm 14.$	$\mp 105. \pm 19.$
	σ	18.	6.9	13.

Note. 1 = $(LaO)_2SO_4$; 2 = $(GdO)_2SO_4$; 3 = $(YO)_2SO_4$.

lides (16, 17), and also due to the presence of the same $(LnO)_n^{n+}$ layer, we may use the C.F. parameters of the oxyhalides as starting values. Final C_{4v} C.F. parameters of the oxysulfates are not very different (Table V). When the $B_{\frac{1}{2},6}^{\frac{1}{2}}$ extra parameters are added the rms decreases to 8 cm^{-1} , giving a good simulation of experimental levels (Table VI). Only one of the C_{4v} starting C.F. parameter sets gives a good simulation, contrary to the preceding case. If this type of simulation is correct, it means that we can now fix the sign of the B_4^2 parameters for the rare earth oxyhalides series. This time, the nonobserved 7F_2 level is the upper one.

Conclusion

Finally, the procedure of descending symmetries can be applied to any simulation of an energy level scheme, when spectroscopic evidence shows that the real point site symmetry can be considered as distorted from a higher symmetry, and when measurements on single crystals are not performed. For the oxysulfate case, we determined sets of C.F. parameters simulating the experiment more or less correctly. Curiously, it appears that one of the ways to decide on the best procedure should be the observation of the fifth 7F_2 Stark level, with completely different positions in the two simulations. In fact, the $C_{4v} \rightarrow C_{2v}$ descending symmetry procedure is probably the most realistic. This is not only because of a better rms since the C_{2v} symmetry is always only approximate, but because the observed spectra are very similar to those of other oxysalts. More precisely, some of them (the oxyhalides) have a pure C_{4v} point symmetry, and their spectra resemble those of the oxysulfates. Also, we note that the ${}^5D_0 \rightarrow {}^7F_0$ transition is intense. This is a further argument in favor of this procedure, since this transition is also allowed in C_{4v} , but prohibited in D_{3h} ; if the slight symmetry distortion is conserved, a low intensity can be expected for this transition in the $D_{3h} \rightarrow C_{2v}$ case.

It appears that all atoms of the same type, surrounding a central ion, do not have the same "spectroscopic weight," when the nature of bonding creates a complement to the classical properties of the symmetry. In the special case of oxysalts, the available data show that the $(LnO)_n^{n+}$ complex cation has something like a "spectroscopic identity," leaving its "finger print" on the spectrum, the remaining ions being less important. We believe this to be of considerable interest for the prediction of the crystal field effect for these types of compounds.

TABLE VI
OBSERVED AND CALCULATED ENERGY LEVELS FOR $(LaO)_2SO_4:Eu^{3+}$ FOR THE $C_{4v} \rightarrow C_{2v}$ CASE (ALL UNITS IN cm^{-1})

Level	$(LaO)_2SO_4:Eu^{3+}$						$(GdO)_2SO_4:Eu^{3+}$						$(YbO)_2SO_4:Eu^{3+}$						
	C_{4v}			C_{2v}			C_{4v}			C_{2v}			C_{4v}			C_{2v}			
	Exp value	Calc value	Irr rep	Calc value	Irr rep	Exp value	Calc value	Irr rep	Calc value	Irr rep	Exp value	Calc value	Irr rep	Calc value	Irr rep	Exp value	Calc value	Irr rep	
7F_0	0	0	A ₁	0	A ₁	0	0	A ₁	0	A ₁	0	0	A ₁	0	A ₁	0	0	A ₁	0
7F_2	214	209	A ₂	209	A ₂	219	219	A ₂	220	A ₂	216	216	A ₂	215	A ₂	216	216	A ₂	215
	447	461	E	445	B ₁	432	464	E	427	B ₁	431	466	E	430	B ₁	431	466	E	430
	473			480	B ₂	492			496	B ₂	500			501	B ₂				501
7F_2	975	979	E	969	B ₂	964	979	E	965	B ₂	967	979	E	968	B ₂	967	979	E	968
	990			999	A ₂	977			988	B ₁	980			988	B ₁	980			988
	1021	1014	B ₂	1019	B ₁	1034	1017	B ₂	1028	A ₂	1034	1024	B ₂	1032	A ₂	1034	1024	B ₂	1032
7F_3	1075	1084	A ₁	1073	A ₁	1079	1089	A ₁	1072	A ₁	1080	1088	A ₁	1073	A ₁	1080	1088	A ₁	1073
		1264	B ₁	1312	A ₁		1261	B ₁	1271	A ₁		1261	B ₁	1275	A ₂		1254	B ₁	1275
	1860	1878	A ₂	1866	A ₂	1871	1882	A ₂	1867	B ₁	1869	1882	A ₂	1866	B ₁	1869	1882	A ₂	1866
7F_3	1873	1902	E	1870	B ₁	1918	1905	E	1870	A ₂	1918	1908	E	1870	A ₂	1918	1908	E	1870
	1916			1929	B ₂				1922	B ₂				1919	B ₂				1919
	1967	1958	E	1966	B ₁	1952	1959	E	1945	B ₁	1951	1959	E	1947	B ₁	1951	1959	E	1947
7F_4	1978			1976	B ₂	1976			1974	B ₂	1976			1975	B ₂	1976			1975
	2002	2007	B ₁	1994	A ₁	2008	2014	B ₁	2008	A ₁	2012	2019	B ₁	2009	A ₁	2012	2019	B ₁	2009
	2026	2023	B ₂	2022	A ₂	2017	2025	B ₂	2023	A ₂	2023	2026	B ₂	2029	A ₂	2023	2026	B ₂	2029
7F_4	2729	2723	A ₁	2723	A ₁	2731	2720	A ₁	2735	A ₁	2735	2724	A ₁	2738	A ₁	2735	2724	A ₁	2738
	2843	2840	A ₂	2841	A ₂	2834	2842	A ₁	2830	A ₂	2826	2841	A ₂	2828	A ₂	2826	2841	A ₂	2828
	2851	2887	E	2847	B ₁	2854	2890	E	2859	B ₁	2859	2899	E	2860	B ₁	2859	2899	E	2860
7F_4	2902			2909	A ₁	2900	2939	A ₁	2902	A ₁	2902	2943	A ₁	2901	A ₁	2902	2943	A ₁	2901
	2927	2936	A ₁	2922	B ₂	2949	2939	A ₁	2934	B ₂	2953	2943	A ₁	2936	B ₂	2953	2943	A ₁	2936
	2986	2988	E	2994	B ₁	2984	2990	E	2990	B ₂	2984	2993	E	2993	B ₂	2984	2993	E	2993
7F_4	3007			3013	B ₂	3007	3027	B ₁	3004	B ₁	3005	3029	B ₁	3003	B ₁	3005	3029	B ₁	3003
	3031	3017	B ₁	3028	A ₁	3036	3054	B ₂	3042	A ₁	3037	3044	B ₂	3045	A ₁	3037	3044	B ₂	3045
	3034	3051	B ₂	3033	A ₂	3052	3054	B ₂	3050	A ₂	3052	3057	B ₂	3057	A ₂	3052	3057	B ₂	3057

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