

## Unusual Effects of Anisotropic Bonding in Cu(II) and Ni(II) Oxides with $K_2NiF_4$ Structure<sup>1</sup>

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Geometric constraints present in  $A_2BO_4$  compounds with the tetragonal-T structure of  $K_2NiF_4$  impose a strong pressure on the B—O<sub>II</sub>—B bonds and a stretching of the A—O<sub>I</sub>—A bonds in the basal planes if the tolerance factor is  $t \equiv R_{AO}/\sqrt{2}R_{BO} < 1$ , where  $R_{AO}$  and  $R_{BO}$  are the sums of the A—O and B—O ionic radii. The tetragonal-T phase of  $La_2NiO_4$  becomes monoclinic for  $Pr_2NiO_4$ , orthorhombic for  $La_2CuO_4$ , and tetragonal-T' for  $Pr_2CuO_4$ . The atomic displacements in these distorted phases are discussed and rationalized in terms of the chemistry of the various compounds. The strong pressure on the B—O<sub>II</sub>—B bonds produces itinerant  $\sigma_{x^2-y^2}$  bands and a relative stabilization of localized  $d_{z^2}$  orbitals. Magnetic susceptibility and transport data reveal an intersection of the Fermi energy with the  $d_{z^2}^2$  levels for half the copper ions in  $La_2CuO_4$ ; this intersection is responsible for an intrinsic localized moment associated with a configuration fluctuation; below 200 K the localized moment smoothly vanishes with decreasing temperature as the  $d_{z^2}^2$  level becomes filled. In  $La_2NiO_4$ , the localized moments for half-filled  $d_{z^2}$  orbitals induce strong correlations among the  $\sigma_{x^2-y^2}$  electrons above  $T_d \approx 200$  K; at lower temperatures the  $\sigma_{x^2-y^2}$  electrons appear to contribute nothing to the magnetic susceptibility, which obeys a Curie-Weiss law giving a  $\mu_{eff}$  corresponding to  $S = 1/2$ , but shows no magnetic order to lowest temperatures. These surprising results are verified by comparison with the mixed systems  $La_2Ni_{1-x}Cu_xO_4$  and  $La_{2-2x}Sr_{2x}Ni_{1-x}Ti_xO_4$ . The onset of a charge-density wave below 200 K is proposed for both  $La_2CuO_4$  and  $La_2NiO_4$ , but the atomic displacements would be short-range cooperative in mixed systems. The semiconductor-metallic transitions observed in several systems are found in many cases to obey the relation  $E_a \approx kT_{min}$ , where  $\rho = \rho_0 \exp(-E_a/kT)$  and  $T_{min}$  is the temperature of minimum resistivity  $\rho$ . This relation is interpreted in terms of a diffusive charge-carrier mobility with  $E_a \approx \Delta H_m \approx kT$  at  $T = T_{min}$ .

### Introduction

Although oxides with the tetragonal  $K_2NiF_4$  structure were known in the 1950s (1, 2), it was not until 1970 that their significance for the study of two-dimensional magnetic properties was fully appreciated (3).

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Longo and Raccach (4) were the first to signal an abrupt change in the  $c/a$  ratio on going from orthorhombic  $La_2CuO_4$  to tetragonal  $Pr_2CuO_4$ . Ganguly and Rao (5) reported that  $La_2CuO_4$  is essentially metallic whereas  $Sm_2CuO_4$  and  $Nd_2CuO_4$ , which have the  $Pr_2CuO_4$  structure, are semiconductors. Kenjo and Yajima (6) independently reported a similar result and, to explain their data, proposed a configuration change  $3d_{z^2}^1 4p_z^0 \rightarrow 4p_z^1 3d_{z^2}^0$ , which presumably implies the crossing of a half-filled, lo-

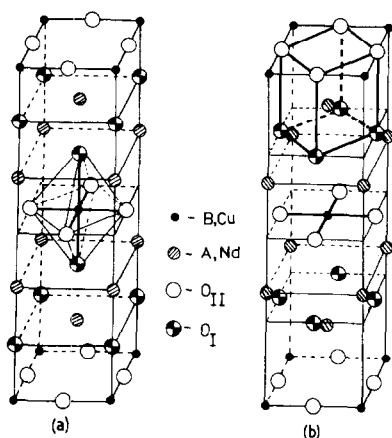


FIG. 1. Relation between (a) the  $K_2NiF_4$  structure of tetragonal-T  $A_2BO_4$  oxides and (b) the tetragonal-T'  $Nd_2CuO_4$  structure.

calized  $3d_{1/2}^1$  level by the conduction-band edge. In view of the stability of the  $Cu^+ : 3d^{10}$  configuration, such a model is quite unrealistic. Goodenough (7) suggested an alternate configuration change within the  $3d$ -state manifold:  $d_{z^2}^2 \sigma_{x^2-y^2}^{*1} \rightarrow d_{x^2-y^2}^1 \sigma_{x^2-y^2}^{*2}$ , where the  $d_{x^2-y^2}$  orbitals are broadened into a narrow  $\sigma_{x^2-y^2}^{*2}$  band by strong  $Cu-O-Cu$  interactions within the basal planes of  $La_2CuO_4$ . His model was based on the incorrect assumption that the tetragonal  $Pr_2CuO_4$  phase has the  $K_2NiF_4$  structure. As a result of the availability of considerably more structural, transport, and magnetic data, we suggest a more subtle configuration change in the present paper.

The correct structure of the tetragonal  $Pr_2CuO_4$  phase was first determined for  $Nd_2CuO_4$  by Müller-Buschbaum and Wollschlager (8); it is compared with the tetragonal  $K_2NiF_4$  structure in Fig. 1. The cations and the  $O_{II}$  atoms shared by the transition-metal (B) cations are in identical positions in the two structures. The remaining  $O_I$  atoms have five A-cation and one B-cation nearest neighbors in the tetragonal (T)  $K_2NiF_4$  structure; they are shifted in the tetragonal (T')  $Nd_2CuO_4$  structure to tetrahe-

dral interstices of the A-cation bilayers. Both tetragonal structures belong to space group  $I4/mmm$ .

The correct structure for the tetragonal-T' phase accounts well for the sharp increase in volume that accompanies the drop in  $c/a$  ratio and metal-semiconductor transition as the structure changes from orthorhombic (O) to tetragonal-T' with composition in the systems  $La_{2-x}Ln_xCuO_4$  (9, 22).

The distortion to orthorhombic symmetry may have one or two components. One component has been identified in  $Sm_2CoO_4$ , the other in  $La_2CoO_4$  (10). In  $Sm_2CoO_4$ , cooperative atomic displacements of the Sm(A) cations and the  $O_I$  atoms along the  $c$ -axis, see Fig. 2a, create two distinguishable A cations,  $Sm_I$  and  $Sm_{II}$ , as well as two distinguishable B cations,  $Co_I$  and  $Co_{II}$ . The displacements reduce the electrostatic repulsions between half the A cations and reduce every  $A-O_I$  bond length parallel to the  $c$ -axis. The  $Co-O_I$  bond lengths along the  $c$ -axis are different for  $Co_I$  and  $Co_{II}$  atoms. Along the orthorhombic  $b$ -axis, the  $A-O_I-A$  angle is reduced from  $180^\circ$ ; along the  $a$ -axis it remains nearly  $180^\circ$ . Therefore the  $b$ -axis decreases while the  $a$ -

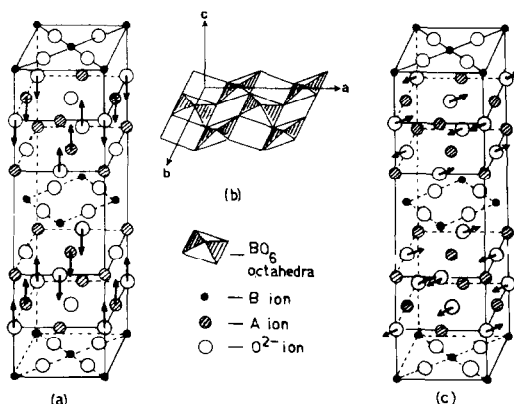


FIG. 2. Proposed atomic displacements for (a) the orthorhombic  $C_{2v}^{18}-Fmm2$  structure of  $Sm_2CoO_4$ , (b) the added component in the orthorhombic  $D_{2h}^{18}-Cmca$  structure of  $La_2CoO_4$ , and (c) the monoclinic structure of  $Pr_2NiO_4$ .

axis remains essentially constant. Such a relationship between the  $a$  and  $b$  axes of this orthorhombic phase, space group  $C_{2v}^{18}-Fmm2$ , has been nicely demonstrated in the system  $Ca_{1+x}Y_{1-x}CrO_4$ , which exhibits an orthorhombic-tetragonal phase change with increasing temperature (11, 12). The three phases of  $CaYCrO_4$  are particularly instructive as the structure shows an evolution with increasing temperature from an orthorhombic phase with two components below 840°C, to the orthorhombic phase with only the one component of  $Sm_2CoO_4$  in the interval 800°C <  $T$  < 1400°C, and a second transition to the tetragonal-T phase above 1400°C (12). The second component is represented by  $La_2CoO_4$ , space group  $D_{2h}^{18}-Cmca$  (or  $Abma$ ), which has been refined (10) in terms of a rotation of the  $CoO_6$  octahedra about the orthorhombic  $b$ -axis (see Fig. 2b). Such a rotation shortens the  $a$ -axis while leaving the  $b$ -axis unchanged. The temperature variation of the lattice parameters of  $CaYCrO_4$  (12) can be interpreted as follows: only the orthorhombic distortion represented by Fig. 2a is present in the temperature interval 840°C <  $T$  < 1400°C, so the  $b$ -axis decreases with decreasing temperature while the  $a$ -axis remains constant; below 840°C, the  $O_{II}$  atoms move in the sense of the rotations of Fig. 2b to superpose an additional distortive component, so the  $a$ -axis decreases with decreasing temperature from 840°C while the  $b$ -axis changes relatively little. At room temperature the magnitudes of the  $a$  and  $b$  axes approach each other, so that a transition at lower temperatures to a tetragonal ( $T''$ ) phase can be anticipated in which the unit-cell basal plane has double the area of that of the tetragonal T and  $T'$  phases.

Determination of the orthorhombic phase of  $La_2CuO_4$  was done on a single crystal prepared at high temperatures (13); the X-ray spectrum was refined in space group  $D_{2h}^{18}-Abma$  ( $Cmca$ ) on the basis of only the rotational component of Fig. 2b. Undoubt-

edly both components were present, especially as powder data taken on samples prepared at much lower temperatures and with controlled stoichiometry exhibit the  $(h + k) = 2n$ ,  $(k + l) = 2n$ , and  $(l + h) = 2n$  reflections consistent with space group  $C_{2v}^{18}-Fmm2$  (or  $Fmm$ ) rather than only the  $h + k = 2n$  reflections of  $D_{2h}^{18}-Cmca$ . We conclude that stoichiometric, orthorhombic  $La_2CuO_4$  contains primarily, if not exclusively, the distortive component represented by Fig. 2a. The  $O \rightleftharpoons T$  transition, which is second order, should not be confused with the first-order  $O \rightleftharpoons T'$  transition encountered with compositional variation  $x$  in the systems  $La_{2-x}Ln_xCuO_4$ .

Low-temperature magnetic-susceptibility measurements on  $La_2CuO_4$  have indicated the presence of a localized-moment contribution corresponding to about 0.5  $\mu_B$  per mole of  $La_2CuO_4$  (14). This observation must be reconciled with the metallic character of  $La_2CuO_4$ . The existence of a localized-moment component has been confirmed in a sample exhibiting an ESR signal ( $g_{\parallel} = 3.04$  and  $g_{\perp} \approx 2.06$ ), and it was interpreted to represent a  $Cu^{2+}$ -ion moment at a concentration of about 3.5 mole% associated with a magnetic impurity of a copper-containing second phase even though no evidence of a second phase was found in the powder X-ray diffraction data (15). In this paper we argue that the localized moments are an intrinsic property of  $La_2CuO_4$ .

On the other hand, the tetragonal- $T'$  phases  $Ln_2CuO_4$  with  $Ln = Pr, Nd, \text{ or } Gd$ —although semiconducting—exhibit a magnetic susceptibility below 300 K that is entirely due to the rare-earth ions decoupled from any antiferromagnetic order that may be present among the  $Cu-O_{II}-Cu$  layers (16, 23). This observation must be reconciled with any model that is proposed for the  $Ln_2CuO_4$  phases.

In the Ni(II) oxides, structural refinement (17) of  $La_2NiO_4$  has confirmed the tetragonal-T structure and determined an

TABLE I  
CRYSTAL STRUCTURE AND LATTICE PARAMETERS OF  
THE SYSTEMS  $\text{La}_2\text{Ni}_{1-x}\text{Cu}_x\text{O}_4$ ,  $\text{La}_{2-2x}\text{Sr}_{2x}\text{Ni}_{1-x}\text{Ti}_x\text{O}_4$ ,  
 $\text{Pr}_2\text{Ni}_{1-x}\text{Cu}_x\text{O}_4$ ,  $\text{La}_{2-x}\text{Pr}_x\text{CuO}_4$ , AND  $\text{La}_{2-x}\text{Nd}_x\text{CuO}_4$

Compound	Crystal structure <sup>a</sup>	Lattice parameters (Å)			
		<i>a</i>	<i>b</i>	<i>c</i>	
$\text{La}_2\text{Ni}_{1-x}\text{Cu}_x\text{O}_4$	<i>x</i> = 0.0	T	3.85	—	12.65
	0.25	T	3.84	—	12.76
	0.50	T	3.82	—	12.93
	0.75	T	3.81	—	13.05
	0.90	O	5.37	5.39	13.13
	1.00	O	(3.804) <sup>b</sup> 5.36	5.41	13.17
$\text{Pr}_2\text{Ni}_{1-x}\text{Cu}_x\text{O}_4$	<i>x</i> = 0.0 <sup>c</sup>	M	3.841	3.853	12.44
	0.10 <sup>c</sup>	M	3.832	3.837	12.486
	0.25	T	3.83	—	12.56
	0.50	T	3.83	—	12.60
	0.75	T and T'	—	—	—
	0.90	T'	3.96	—	12.22
1.00	T'	3.96	—	12.18	
$\text{La}_{2-2x}\text{Sr}_{2x}\text{Ni}_{1-x}\text{Ti}_x\text{O}_4$	<i>x</i> = 0.25	T	3.86	—	12.67
	0.50	T	3.87	—	12.67
	0.75	T	3.87	—	12.63
	1.00	T	3.88	—	12.60
	$\text{La}_{2-x}\text{Pr}_x\text{CuO}_4$ <sup>d</sup>	<i>x</i> = 0.25	O	5.357 (3.804) <sup>b</sup>	5.404
0.50		O	5.357 (3.804) <sup>b</sup>	5.402	13.10
0.75		T'	3.976	—	12.56
1.25		T'	3.966	—	12.43
1.75		T'	3.962	—	12.38
2.00		T'	3.958	—	12.28
$\text{La}_{2-x}\text{Nd}_x\text{CuO}_4$ <sup>d</sup>		<i>x</i> = 0.10	O	5.356 (3.804) <sup>b</sup>	5.402
	0.25	T'	3.975	—	12.32
	0.50	T'	3.975	—	12.30
	1.50	T'	3.961	—	12.27
	1.75	T'	3.957	—	12.22
	2.00	T'	3.945	—	12.17

<sup>a</sup> T, tetragonal  $\text{K}_2\text{NiF}_4$  structure; T', tetragonal  $\text{Nd}_2\text{CuO}_4$  structure; O, orthorhombic structure; M, monoclinic structure. See text for more details.

<sup>b</sup> Pseudo-tetragonal *a* parameter.

<sup>c</sup>  $\gamma = 90.30^\circ$  for *x* = 0.0 and  $90.30^\circ$  for *x* = 0.10.

<sup>d</sup> Data reported earlier in Ref. (22).

$\text{La}-\text{O}_I$  bond length parallel to the *c*-axis of only 2.32 Å compared to the 2.62 Å predicted from the Shannon–Prewitt (18) ionic radii. The structure of  $\text{Pr}_2\text{NiO}_4$ , on the other hand, is monoclinic (M) (see Table I). This monoclinic phase is to be distinguished from that reported previously (36); it is not indexable on an orthorhombic cell

as it creates distinguishable  $\text{Ni}-\text{O}_{II}-\text{Ni}$  distances. It can be generated by an antiferroelectric displacement of the  $\text{O}_I$  ions of a bilayer along [100] and  $[\bar{1}00]$  directions of the T phase as illustrated in Fig. 2c.

The magnetic susceptibility of  $\text{La}_2\text{NiO}_4$  exhibits a Curie–Weiss law above 200 K, and an inflection at 200 K was attributed to the appearance at lower temperature of a weak ferromagnetism due to a Dzialoshinskii spin canting of an antiferromagnetically ordered system (19). However, neither a subsequent neutron-diffraction study (20) nor magnetic-susceptibility data (23) provide any evidence of antiferromagnetic order at lowest temperatures. In this paper we reinvestigate the low-temperature susceptibility in the systems  $\text{La}_2\text{Ni}_{1-x}\text{Cu}_x\text{O}_4$  and  $\text{La}_{2-2x}\text{Sr}_{2x}\text{Ni}_{1-x}\text{Ti}_x\text{O}_4$  to show that there is a reduction of the nickel magnetic moment below the inflection temperature. This finding is discussed in terms of an energy diagram proposed earlier (7) and on the subsequent emphasis on the evidence for a coexistence of localized and itinerant  $3d$  electrons in  $\text{La}_2\text{NiO}_4$  as a result of the anisotropic character of the structure (21).

The structural and conductivity data for the mixed systems  $(\text{La}, \text{Ln})_2\text{CuO}_4$  (*Ln* = Pr, Nd) and  $\text{La}_2(\text{Cu}, \text{Ni})\text{O}_4$  (22) as well as the magnetic data for  $\text{Ln}_2\text{CuO}_4$  and  $\text{Ln}_2\text{NiO}_4$  (*Ln* = La, Pr, Nd) (23) have been reported previously. In this paper we report the variations in the lattice parameters of these systems and some ir and ESR data in addition to some new magnetic and transport data. We comment on the relationship between the various phases that are encountered, and we discuss the physical properties in terms of the energy-band diagrams for the Cu(II) and Ni(II) systems. In particular, we note that a  $\text{K}_2\text{NiF}_4$  structure with tolerance factor *t* < 1 imposes a pressure contracting the  $\text{B}-\text{O}_{II}$  bond lengths in the basal plane, and we argue that this pressure produces some extraordinary properties wherever

the  $d_{x^2-y^2}$  orbitals may be thereby transformed in character from localized to itinerant.

## Experimental

### A. Preparation

The  $\text{La}_2\text{Ni}_{1-x}\text{Cu}_x\text{O}_4$  samples were identical to those for which the electrical properties have already been reported (22). The  $\text{Pr}_2\text{Ni}_{1-x}\text{Cu}_x\text{O}_4$  samples were prepared similarly, but with a final firing temperature of 1370 K.

The  $\text{La}_{2-2x}\text{Sr}_{2x}\text{Ni}_{1-x}\text{Ti}_x\text{O}_4$  compounds were prepared by thoroughly mixing and grinding under alcohol for several hours stoichiometric mixtures of  $\text{La}_2(\text{C}_2\text{O}_4)_3 \cdot n\text{H}_2\text{O}$  ( $n$  determined thermogravimetrically),  $\text{SrC}_2\text{O}_4 \cdot \text{H}_2\text{O}$ ,  $\text{NiC}_2\text{O}_4 \cdot 2\text{H}_2\text{O}$ , and  $\text{TiO}_2$ . The mixture was decomposed in air by slowly heating to 1270 K; the product was then heated at 1570 K for 72 hr with intermittent grinding and pelletizing.

The  $\text{La}_{2-x}\text{Ln}_x\text{CuO}_4$  ( $\text{Ln} = \text{Pr}, \text{Nd}$ ) samples were coprecipitated from solutions of the corresponding metal chlorides made up in the required proportions. The mixture of chlorides was added slowly to a fairly concentrated solution of  $\text{Na}_2\text{CO}_3$  with constant stirring, and the precipitated carbonate was washed to remove any excess  $\text{Na}_2\text{CO}_3$ . The precipitate was then decomposed and sintered at 1270 K for 48 hr with intermittent grinding and pelletizing repeated several times.

### B. X-Ray Diffraction

Temperature-dependent X-ray diffraction data were taken with a Philips-PW 1050/70 diffractometer and Ni-filtered  $\text{CuK}\alpha$  radiation. The data were collected at a scan rate of  $1/4^\circ$  per minute.

The room-temperature lattice parameters and  $c/a$  ratio for different values of  $x$  in the systems  $\text{La}_2\text{Ni}_{1-x}\text{Cu}_x\text{O}_4$  and  $\text{La}_{2-2x}\text{Sr}_{2x}\text{Ni}_{1-x}\text{Ti}_x\text{O}_4$  are given in Table I. Végard's

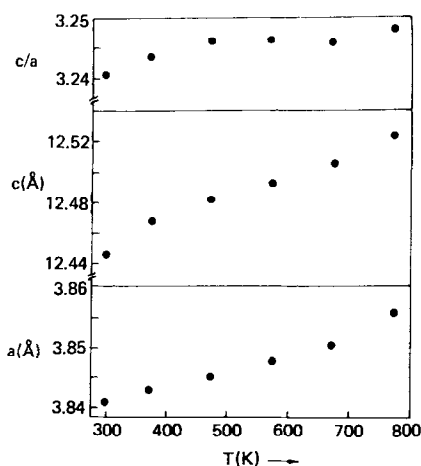


FIG. 3. Temperature dependence of the lattice parameters of  $\text{Pr}_2\text{NiO}_4$ .

law is obeyed for both systems, which indicates the formation of true solid solutions. Neither the X-ray nor the electron diffraction spectra showed any evidence of a superstructure in  $\text{La}_{2-2x}\text{Sr}_{2x}\text{Ni}_{1-x}\text{Ti}_x\text{O}_4$ , even for  $x = 0.5$ , so the  $\text{Ni}^{2+}$  and  $\text{Ti}^{4+}$  ions appear to be randomly distributed. It is to be noted that the mean Ni—O and Cu—O distances, averaged over all six nearest oxide-ion neighbors, are 2.02 and 2.07 Å, respectively, in  $\text{La}_2\text{NiO}_4$  (2) and  $\text{La}_2\text{CuO}_4$  (4); these are significantly smaller than the 2.09 and 2.13 Å distances calculated from the Shannon–Prewitt ionic radii.

Table I also gives the room-temperature structural data for several compositions in the systems  $\text{La}_{2-x}\text{Ln}_x\text{CuO}_4$  with  $\text{Ln} = \text{Pr}$  or  $\text{Nd}$  and  $\text{Pr}_2\text{Ni}_{1-x}\text{Cu}_x\text{O}_4$ . A structural change from orthorhombic to tetragonal-T' is apparent for the  $\text{La}_{2-x}\text{Ln}_x\text{CuO}_4$  systems at critical concentrations  $x_c$ , where  $0.5 < x_c < 0.75$  for  $\text{Ln} = \text{Pr}$  and  $0.10 < x_c < 0.25$  for  $\text{Ln} = \text{Nd}$ . A change from monoclinic-M to tetragonal-T also occurs in  $\text{Pr}_2\text{Ni}_{1-x}\text{Cu}_x\text{O}_4$  at an  $x_c$  in the range  $0.1 < x_c < 0.25$ ; the  $x = 0.75$  sample contains T and T' phases, and the T' phase is stabilized for  $x > 0.9$ .

The  $c/a$  ratio of  $\text{La}_2\text{NiO}_4$  increases with increasing temperature (21); and a similar,

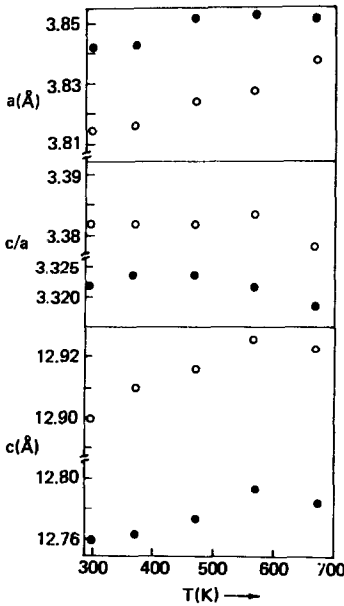


FIG. 4. Temperature dependence of the lattice parameters of  $\text{La}_2\text{Ni}_{1-x}\text{Cu}_x\text{O}_4$ ,  $x = 0.25$  (●) and  $0.5$  (○).

smaller increase was observed in  $\text{Pr}_2\text{NiO}_4$  (Fig. 3), which undergoes a smooth monoclinic-tetragonal transition at  $T_t \approx 670$  K. However, samples with  $x = 0.25$  and  $0.5$  in the system  $\text{La}_2\text{Ni}_{1-x}\text{Cu}_x\text{O}_4$  showed little temperature variation of the  $c/a$  ratio (see Fig. 4).

### C. Magnetic Susceptibility

Magnetic susceptibilities were obtained with a Faraday balance and a Cahn RG vacuum, recording electrobalance. A closed-cycle helium-refrigeration system gave a lower limit of 12 K to the temperature range; the upper limit was 1000 K.  $\text{HgCo}(\text{SCN})_4$  was used as a calibrant, and the susceptibility was measured at various fields up to 5000 G. All samples but  $\text{La}_2\text{CuO}_4$  had field-independent susceptibilities; extrapolation to  $H = 0$  of the weak field dependence of  $\text{La}_2\text{CuO}_4$  permitted determination of a weak ferromagnetic component below about 850 K. The field dependence was also found in  $\text{La}_2\text{CuO}_4$  samples

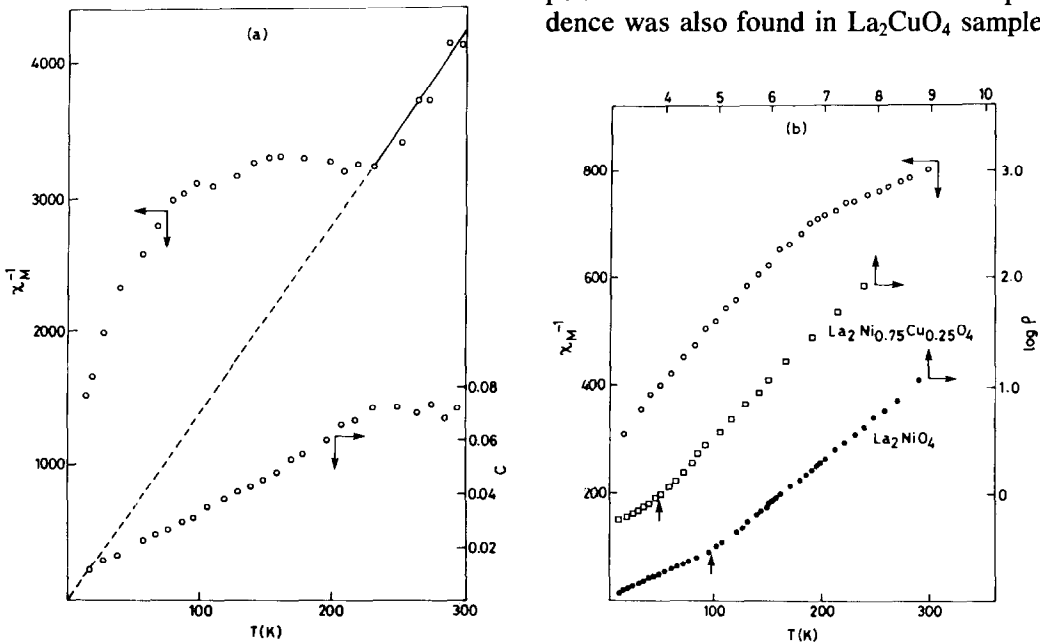


FIG. 5. Temperature dependence of molar magnetic susceptibility  $\chi_m$  and resistivity  $\rho$  for  $\text{La}_2\text{Ni}_{1-x}\text{Cu}_x\text{O}_4$ ,  $x = 0.0, 0.25$ , and  $1.0$ : (a)  $\chi_m^{-1}$  vs  $T$  plot of  $\text{La}_2\text{CuO}_4$  (without contribution from ferromagnetic impurity) and variation of Curie constant  $C$  based on a Curie law for all  $T$ ; (b)  $\chi_m^{-1}$  vs  $T$  of  $\text{La}_2\text{NiO}_4$  and  $\log \rho$  vs  $T^{-1}$  of  $\text{La}_2\text{NiO}_4$  and  $\text{La}_2\text{Ni}_{0.75}\text{Cu}_{0.25}\text{O}_4$ .

prepared from oxides of high purity by a ceramic method. Mehran and Machin (24) have reported a similar weak ferromagnetism in several oxides of copper whereas Saez Puche *et al.* (15) report no field dependence of the susceptibility of their sample of  $\text{La}_2\text{CuO}_4$ . We therefore presume that the ferromagnetism is not intrinsic to  $\text{La}_2\text{CuO}_4$ . This component saturates to a constant value of about  $0.004 \mu_B/\text{mole}$  below 300 K, and the paramagnetic susceptibility of  $\text{La}_2\text{CuO}_4$  shown in Fig. 5a was obtained from the slope of the straight-line portion of the  $M$  vs  $H$  plots at higher values of  $H$ .

In agreement with earlier work (19), the magnetic susceptibility of  $\text{La}_2\text{NiO}_4$  was found to obey a Curie-Weiss law above 200 K with a Weiss constant  $\theta = -500$  K and a  $\mu_{\text{eff}} \approx 3.03 \mu_B$  per  $\text{Ni}^{2+}$  ion, which is higher than the spin-only value of  $2.83 \mu_B$  for an  $S = 1$  system. However, a  $g \approx 2.12$  may be inferred for octahedral  $\text{Ni}^{2+}$  ions from the magnetization of the spinel  $\text{Fe}^{3+}[\text{Ni}^{2+}\text{Fe}^{3+}]\text{O}_4$  (39).

As can be seen in Fig. 5b, the inverse molar susceptibility  $\chi_m^{-1}$  versus temperature  $T$  has an inflection at  $T_d \approx 200$  K, where we define  $T_d$  as the inflection (or deflection) temperature. It is to be noted that below  $T_d$ , the magnetic susceptibility obeys a different Curie-Weiss law with a slope for  $\chi_m^{-1}$  vs  $T$  corresponding to a  $\mu_{\text{eff}} = 1.83 \mu_B$ , which is close to the spin-only value of  $1.73 \mu_B$  for an  $S = 1/2$  system. Moreover, the Weiss constant  $\theta \approx -120$  K is only a little smaller than would be deduced from the change in Curie constant  $C \approx \mu_{\text{eff}}^2/8$  and the relation  $\theta = CW$  for a constant Weiss molecular-field parameter  $W$ . Yet there is no evidence of any long-range order down to 12 K, which is consistent with the neutron-diffraction data (20).

Table II shows the parameters  $C$ ,  $\mu_{\text{eff}}$ , and  $\theta$  obtained above and below a  $T_d$  in the systems  $\text{La}_{2-2x}\text{Sr}_{2x}\text{Ni}_{1-x}\text{Ti}_x\text{O}_4$  and  $\text{La}_2\text{Ni}_{1-x}\text{Cu}_x\text{O}_4$ . The temperature  $T_d$  is not so

sharply defined in the mixed systems; but as can be seen from Figs. 5b and 6 for the  $\text{La}_2\text{Ni}_{1-x}\text{Cu}_x\text{O}_4$  system, the slope of the low-temperature inverse magnetic susceptibility gives a nearly constant  $\mu_{\text{eff}}$  per  $\text{Ni}^{2+}$  atom for  $x < 0.5$ ; only the magnitude of the Weiss constant  $\theta$  decreases. However, in the  $x = 0.75$  sample there is evidence of a contribution to the susceptibility from the  $\text{Cu}^{2+}$  ions. For all  $x$ , the high-temperature data remains consistent with a contribution from only the  $\text{Ni}^{2+}$  ions having, for  $T > T_d$ , a spin  $S = 1$  (see Table II).

In the systems  $\text{La}_{2-x}\text{Pr}_x\text{CuO}_4$  and  $\text{La}_{2-x}\text{Nd}_x\text{CuO}_4$ , the magnetic susceptibility obeyed a Curie-Weiss law that was completely dominated by the rare-earth ion in both the O and T' phases.

#### D. Electrical Resistivity

The electrical resistivity of  $\text{La}_2\text{CuO}_4$  has a nearly temperature-independent resistivity of about 0.1 ohm-cm above 200 K except for a small maximum near 530 K that is associated with a smooth  $\text{O} \rightleftharpoons \text{T}$  transition at this temperature (5). The room-temperature Seebeck coefficient  $\alpha = 200 \mu\text{V}/\text{K}$  is large, positive, and apparently temperature-independent. The low-temperature ( $T < 200$  K) resistivity, on the other hand, shows a marked increase with decreasing temperature; the ratio of the resistivities at 14 and 200 K is about  $10^2$  (see Fig. 7).

The orthorhombic solid solutions  $\text{La}_{2-x}\text{Pr}_x\text{CuO}_4$ ,  $0 < x < 0.5 < x_c$ , also exhibit a nearly temperature-independent resistivity at high temperatures except for a small maximum near  $T_t$  for the  $\text{O} \rightleftharpoons \text{T}$  transition, which shifts to higher temperature with increasing  $x$  (22); and at low  $T$  they show the same sharp increase in resistivity as found in  $\text{La}_2\text{CuO}_4$ , but with an onset temperature that shifts to lower temperature with increasing  $x$  (see Fig. 8).

The electrical resistivity of  $\text{La}_2\text{NiO}_4$  can be separated into three distinct temperature intervals. A shallow minimum of about  $3 \times$

TABLE II  
MAGNETIC SUSCEPTIBILITY AND ELECTRICAL RESISTIVITY DATA  
OF  $\text{La}_2\text{Ni}_{1-x}\text{Cu}_x\text{O}_4$  AND  $\text{La}_{2-2x}\text{Sr}_{2x}\text{Ni}_{1-x}\text{Ti}_x\text{O}_4$

Compound	Magnetic susceptibility data <sup>a</sup>					
	$C$ (emu, K/mole)	$\mu_{\text{eff}}$ ( $\mu_B$ )	$\theta$ (K)	$T_d^b$ (K)	$T_{\text{min}}^c$ (K)	$E_a^d$ (eV)
$\text{La}_{2-2x}\text{Sr}_{2x}\text{Ni}_{1-x}\text{Ti}_x\text{O}_4$ $x = 0.0$	1.15	3.03	500	200	620	0.053
	(0.42)	(1.83)	117			(0.081)
	1.09	2.96	430	240		0.083
	0.50	1.05	2.90	300		
0.75	0.93	2.73	0			0.136
$\text{La}_2\text{Ni}_{1-x}\text{Cu}_x\text{O}_4$ $x = 0.25$	1.11	2.98	380	240	660	0.087
	(0.43)	(1.86)	( 42)			(0.104)
	1.02	2.86	270	280	735	0.107
	(0.40)	(1.79)	( 10)			
0.50	0.99	2.82	200	310	800	0.110
(0.57)	(2.14)	( 27)				

<sup>a</sup>  $C$  and  $\mu_{\text{eff}}$  are calculated per gram-atom of Ni. Figures in brackets refer to data below 100 K, all others are obtained from data above 300 K.

<sup>b</sup>  $T_d$  obtained from susceptibility data and refers to the temperature at which there is deviation from the high-temperature Curie-Weiss law.

<sup>c</sup>  $T_{\text{min}}$  is the temperature at which the resistivity shows a minimum. The electrical resistivity behavior is reported elsewhere (22).

<sup>d</sup> Activation energy obtained from data ( $T > 300$  K) reported in Ref. (22). Figures in brackets refer to  $E_a$  for  $T < T_d$ .

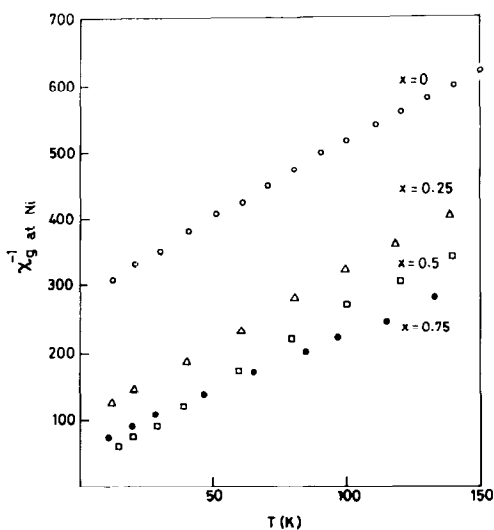


FIG. 6. Temperature dependence of susceptibilities of samples from the systems  $\text{La}_2\text{Ni}_{1-x}\text{Cu}_x\text{O}_4$  ( $T < 150$  K) calculated per gram-atom of Ni.

$10^{-2}$  ohm-cm occurring at  $T_{\text{min}} \approx 600$  K makes the compound metallic-like for  $T > T_{\text{min}}$  and semiconducting for  $T < T_{\text{min}}$ . The  $\log \rho$  versus  $T^{-1}$  plot shows a break in the slope at  $T_d \approx 200$  K; the activation energy  $E_a$  defined by  $\rho = \rho_0 \exp(-E_a/kT)$  changes from 0.082 eV for  $T < T_d$  to 0.053 eV for  $T > T_d$  (see Fig. 5b).

It is of interest to note that for  $T > T_d$ , the relation  $E_a \approx kT_{\text{min}}$  holds in  $\text{La}_2\text{NiO}_4$ . Such a relation is also found in the system  $\text{Pr}_2\text{Ni}_{1-x}\text{Cu}_x\text{O}_4$ , Table II and Fig. 9a, and in  $\text{Nd}_2\text{NiO}_4$  (25), which exhibit a similar resistivity minimum at high temperatures. An  $E_a > 0.82$  eV would make  $E_a/k > 1000$  K, which is beyond the range of our measurements; accordingly no resistivity minimum was observed for samples  $x = 0.25$  and 0.5 of the system  $\text{La}_{2-2x}\text{Sr}_{2x}\text{Ni}_{1-x}\text{Ti}_x\text{O}_4$  (see Fig. 9b).



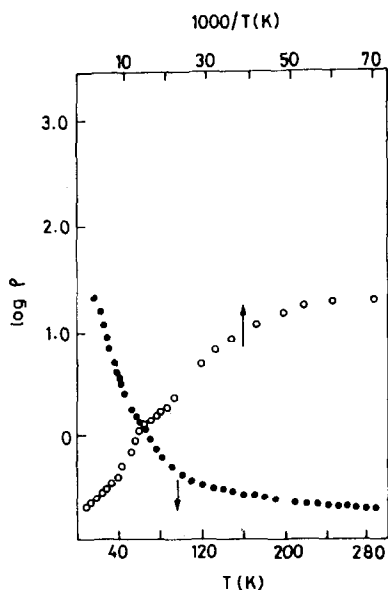


FIG. 7. Temperature dependence of electrical resistivity  $\rho$  in ohm-cm of  $\text{La}_2\text{CuO}_4$ :  $\log \rho$  vs  $T$  and  $\log \rho$  vs  $T^{-1}$ .

On the other hand, in the system  $\text{La}_2\text{Ni}_{1-x}\text{Cu}_x\text{O}_4$  the relation  $E_a = kT_{\text{min}}$  was not obeyed for  $x \neq 0$ , see Table II. In this system the break at  $T_d$  is still well-marked in the  $x = 0.25$  sample, see Fig. 5b, but for higher values of  $x$  the definition of  $T_d$  becomes blurred.

### E. Infrared Studies

The ir spectra in the range  $800\text{--}300\text{ cm}^{-1}$  are shown in Fig. 10 for  $\text{La}_2\text{NiO}_4$  and  $\text{Ln}_2\text{CuO}_4$  ( $\text{Ln} = \text{La}, \text{Pr}, \text{Nd}, \text{and Sm}$ ). They were taken with a Perkin-Elmer 580 spectrophotometer. The temperature-dependent ir spectra for  $\text{La}_2\text{Ni}_{0.75}\text{Cu}_{0.25}\text{O}_4$  (Fig. 11) and  $\text{Nd}_2\text{CuO}_4$  (Fig. 12) were obtained with a temperature-controlled Specac variable-temperature cell. The samples were mixed thoroughly with dry KBr (concentration of sample about 1 wt%) and pressed into disks of about 0.5-mm thickness.

The strong absorption band around  $680\text{ cm}^{-1}$  for orthorhombic  $\text{La}_2\text{CuO}_4$  is not present in the  $T'$  phases of the other  $\text{Ln}_2$

$\text{CuO}_4$  compounds (see Fig. 10). Since the difference in the two structures is a change in the  $\text{O}_I$ -atom position from a linear  $\text{La—O}_I\text{—Cu}$  linkage along the  $c$ -axis in the  $O$  phase to a tetrahedral interstice of the  $\text{Ln}_2$  bilayers in the  $T'$  phase, the absorption may be assigned to the very short  $\text{La—O}_I$  bond in  $\text{La}_2\text{CuO}_4$ ; it has a length of  $2.40\text{ \AA}$  compared to an average  $\text{La—O}$  separation of  $2.60\text{ \AA}$  (4). The other two bands of the  $\text{La}_2\text{CuO}_4$  spectrum may be assigned to asymmetric stretching and bending modes of the strong  $\text{Cu—O}_{II}$  linkages in the basal planes.

The tetragonal- $T$  phase of  $\text{La}_2\text{NiO}_4$  has a short  $\text{La—O}_I$  bond parallel to the  $c$ -axis analogous to that in  $\text{La}_2\text{CuO}_4$ , and all the  $\text{La}_2\text{Ni}_{1-x}\text{Cu}_x\text{O}_4$  compounds give spectra similar to that of  $\text{La}_2\text{CuO}_4$ . The band assigned to the short  $\text{La—O}_I$  distance shifts to higher energies with increasing copper content.

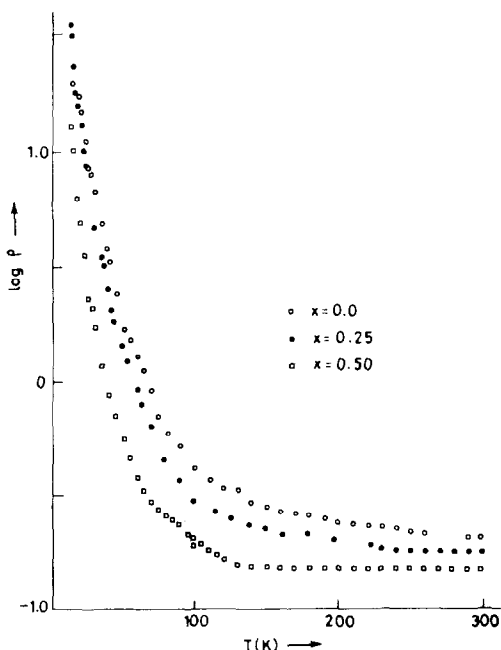


FIG. 8. Temperature dependence of electrical resistivity  $\rho$  in ohm-cm for  $\text{La}_{2-x}\text{Pr}_x\text{CuO}_4$  with  $x = 0.0, 0.25, \text{ and } 0.50$ .

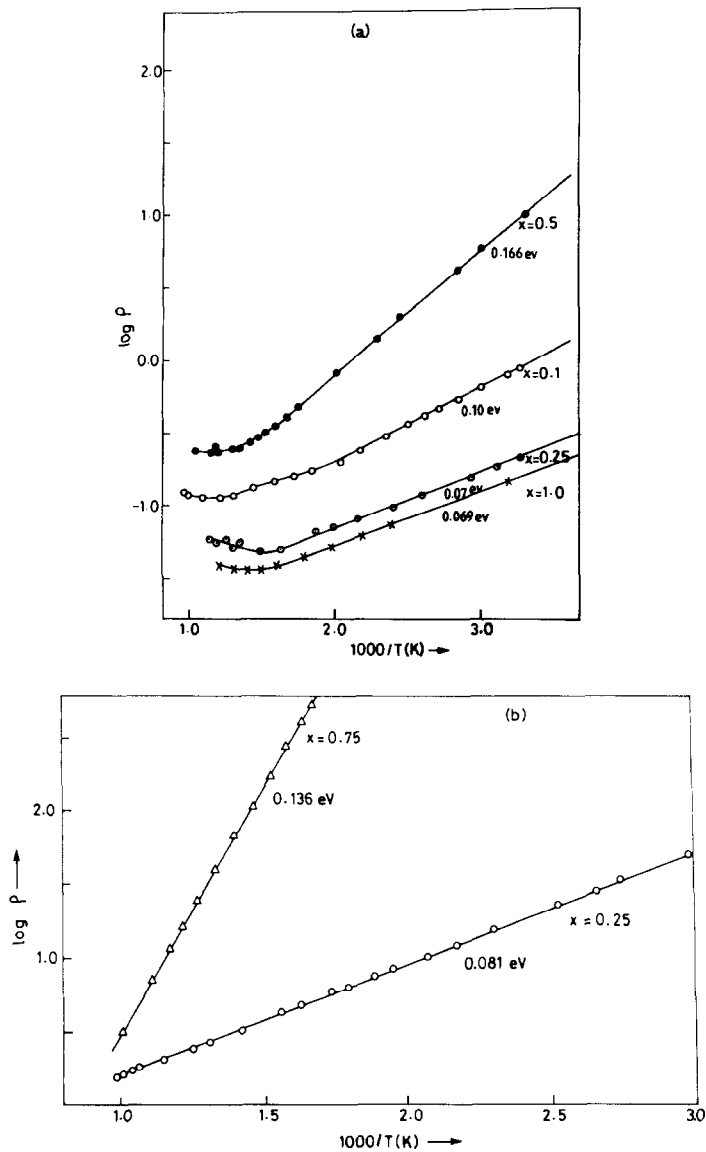


FIG. 9. Temperature dependence of electrical resistivity  $\rho$  in ohm-cm for (a)  $\text{Pr}_2\text{Ni}_{1-x}\text{Cu}_x\text{O}_4$  and (b)  $\text{La}_{2-2x}\text{Ni}_{1-x}\text{Ti}_x\text{O}_4$ .

Figure 11 shows that, for the  $x = 0.25$  sample, the frequency of the absorption band assigned to the  $\text{La}-\text{O}_I$  stretch increases with decreasing temperature, as expected for a stretching mode; it is consistent with the usual lattice-parameter contraction in a solid with the lowering of temperature. On the other hand, the fre-

quency of the other band remains essentially temperature-independent, which is consistent with a bond under great internal pressure. In  $\text{Nd}_2\text{CuO}_4$ , which has the  $T'$  phase and no such pressure on the  $\text{Cu}-\text{O}_{II}$  bond, the frequency of the absorption band increases with decreasing temperature in the usual way (see Fig. 12).

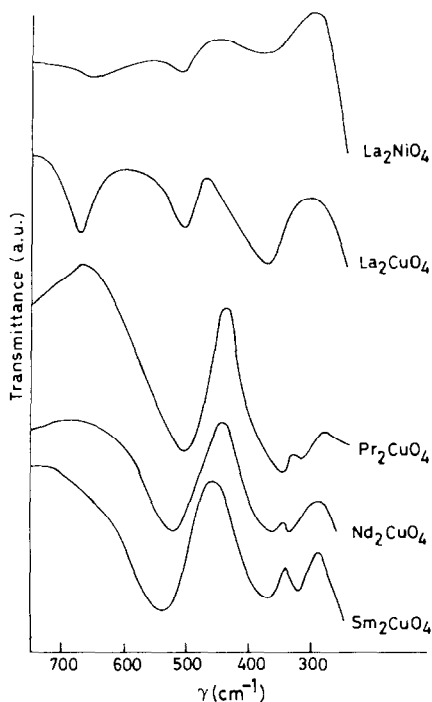


FIG. 10. Infrared spectra of  $\text{La}_2\text{NiO}_4$  and  $\text{Ln}_2\text{CuO}_4$  ( $\text{Ln} = \text{La}, \text{Pr}, \text{Nd}, \text{and Sm}$ ).

### F. ESR Study

Room-temperature ESR spectra for powdered specimens in magnetic fields ranging from 0 to 8 kG were recorded on a Varian E-109 spectrometer. Spectra of the  $\text{La}_{2-x}\text{Pr}_x\text{CuO}_4$  system are shown in Fig. 13. The important features are

(i)  $\text{La}_2\text{CuO}_4$  shows no ESR signal, con-

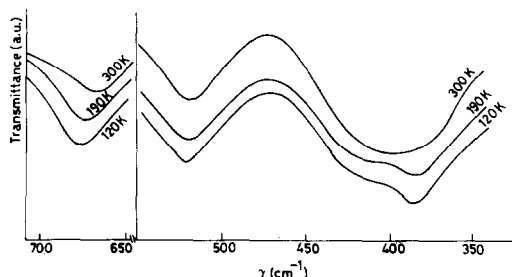


FIG. 11. Temperature dependence of infrared spectrum of  $\text{La}_2\text{Ni}_{0.75}\text{Cu}_{0.25}\text{O}_4$ .

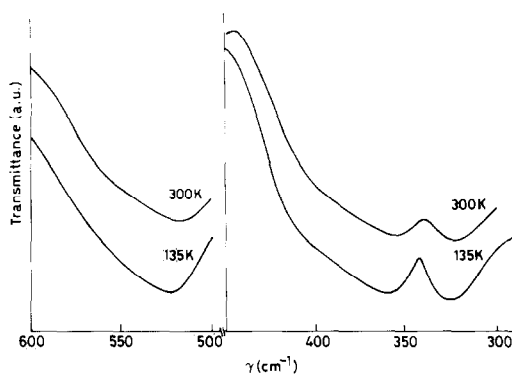


FIG. 12. Temperature dependence of infrared spectrum of  $\text{Nd}_2\text{CuO}_4$ .

trary to the sample of Saez Puche *et al.* (15).

(ii) Orthorhombic samples containing Pr gave a fairly isotropic signal with a  $g \approx 2.2$  (curves B and C).

(iii) The  $x = 0.75$  sample, curve D, gives a signal typical of a superposition on the isotropic signal of a signal from a square-coplanar coordination.

(iv) The  $x = 1.75$  sample, curve E, and pure  $\text{Pr}_2\text{CuO}_4$ , curves F and G (140 K), are entirely different. They indicate an axial  $S$

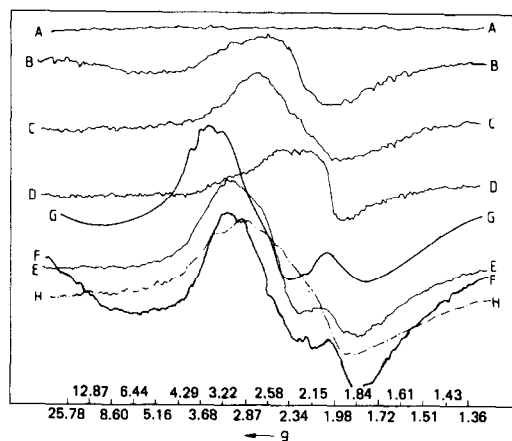


FIG. 13. Room-temperature X-band (9.04 GHz) ESR spectrum of  $\text{La}_{2-x}\text{Pr}_x\text{CuO}_4$ : (A)  $x = 0.0$ , (B)  $x = 0.25$ , (C)  $x = 0.50$ , (D)  $x = 0.75$ , (E)  $x = 1.75$ , (F)  $x = 2.00$ , (G)  $x = 2.00$  (147 K); and of  $\text{Sm}_2\text{CuO}_4$  (H).

= 1/2 ground state typical of  $\text{Cu}^{2+}$  ions in compressed octahedra (26) or in elongated octahedra with antiferrodistortive ordering (37).

(v) The ESR spectrum of  $\text{Sm}_2\text{CuO}_4$ , curve H, is again different. It is compatible with the behavior expected from exchange coupling between axial  $S = 1/2$  ground states of  $\text{Cu}^{2+}$  ions in compressed octahedra (26).

The systematics of these changes would seem to rule out the possibility that the ESR signals are due to copper ions in impurity phases. The absence of any localized-moment contribution from the copper to the magnetic susceptibility therefore suggests that the ESR signals are associated with an electron in an oxygen vacancy or other defect.

## Discussion

### A. Structural Considerations

It is useful to define a tolerance factor

$$t = R_{\text{AO}}/\sqrt{2} R_{\text{BO}} \quad (1)$$

for the tetragonal-T phase;  $R_{\text{AO}}$  and  $R_{\text{BO}}$  are the sums of the ionic radii for A or B cations and the oxide ion (27). Empirically, distortions from tetragonal symmetry are found where the tolerance factor is  $t < 0.87$ . They may also occur for  $0.87 < t < 1$  in certain cases.

If a T phase has  $t < 1$ , geometry imposes the following constraint: in the basal planes, the  $\text{B—O}_{\text{II}}\text{—B}$  distance is shortened and the  $\text{A—O}_{\text{I}}\text{—A}$  distance is lengthened relative to  $2R_{\text{BO}}$  and  $2R_{\text{AO}}$ . In other words, the  $\text{A—O}_{\text{I}}\text{—A}$  bonding, which is stretched, applies pressure on the  $\text{B—O}_{\text{II}}\text{—B}$  bonds. Because of the asymmetric potential function, shortening of the  $\text{B—O}_{\text{II}}\text{—B}$  bonds tends to be less than the stretching of the  $\text{A—O}_{\text{I}}\text{—A}$  bonds despite there being double the number of bonds in an  $\text{A—O}_{\text{I}}$  bilayer relative to a  $\text{B—O}_{\text{II}}$  monolayer. Nevertheless, the in-plane pressure

on the  $\text{B—O}_{\text{II}}$  bonds is large as  $t$  approaches the limiting value of  $t \approx 0.87$ . This fact is of critical importance for the energy-band models to be proposed.

In addition, each cation will adjust the  $c$ -axis  $\text{A—O}_{\text{I}}$  and  $\text{B—O}_{\text{I}}$  bond lengths so as to balance the mean  $\text{M—O}$  distance of its nearest neighbors, which means that the  $c$ -axis  $\text{A—O}_{\text{I}}$  bond lengths are shortened and the  $\text{B—O}_{\text{I}}$  bond lengths are lengthened. At a transition-metal B cation, the  $d_{z^2}$  orbitals are stabilized relative to the  $d_{x^2-y^2}$  orbitals and the  $d_{yz}d_{zx}$  orbitals are stabilized relative to the  $d_{xy}$  orbitals. This fact is manifest in significantly larger axial ratios  $c/a$  if the B cation is a Jahn-Teller ion such as high-spin  $\text{Mn}^{3+}$ , low-spin  $\text{Ni}^{\text{III}}$ , or  $\text{Cu}^{2+}$ , which have  $E_g$  ground states in octahedral symmetry.

The  $c$ -axis  $\text{A—O}_{\text{I}}$  and  $\text{B—O}_{\text{I}}$  bond lengths are also influenced by two other factors: (i) the relative strengths of the  $\text{A—O}_{\text{I}}$  and  $\text{B—O}_{\text{I}}$  bonding in an  $\text{A—O}_{\text{I}}\text{—B}$  linkage and (ii) the  $\text{A—A}$  electrostatic repulsion between  $c$ -axis near neighbors (see Fig. 1). In compounds with trivalent A cations and divalent B cations, the  $\text{A—O}_{\text{I}}$  interaction competes favorably with the  $\text{B—O}_{\text{I}}$  interaction along the  $c$ -axis, and the  $\text{B—O}_{\text{I}}$  bond lengths are longer than  $\text{B—O}_{\text{II}}$  bond lengths.

The tolerance factor for  $\text{La}_2\text{NiO}_4$  is  $t \approx 0.89$ , so the  $\text{Ni—O}_{\text{II}}$  bond length in the basal plane is reduced to 1.93 Å, significantly shorter than the  $R_{\text{NiO}} = 2.09$  Å obtained from the Shannon–Prewitt radii. This produces an unusually strong  $\text{Ni}: d_{x^2-y^2}\text{—O}_{\text{II}}: p_{\sigma}\text{—Ni}: d_{x^2-y^2}$  interaction. In view of the high Néel temperature in  $\text{NiO}$ , which shows that the  $\text{Ni}: e_g\text{—O}: p_{\sigma}\text{—Ni}: e_g$  interactions approach the limit where the super exchange perturbation expansion breaks down even with normal bond lengths, it is at once apparent that the  $d_{x^2-y^2}$  orbitals must be represented by a narrow  $\sigma_{x^2-y^2}$  band of itinerant-electron states (7, 28). The only issue to be resolved experimentally is the strength of the correlations

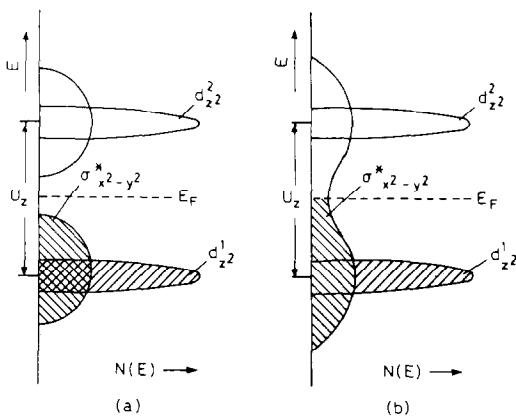


FIG. 14. Schematic density of states vs energy diagrams for the  $\sigma$ -bonding  $3d$  electrons of  $\text{La}_2\text{NiO}_4$ .  $U_z$  is the correlation splitting of  $d_{z^2}^2$  and  $d_{z^2}^1$  levels. Not shown are filled  $\text{O}^{2-} : 2p^6$  and  $\text{Ni}^{2+} : t_{2g}^6$  bands, empty  $\text{Ni}^{2+} 4s$  and  $\text{La}^{3+} : 6s$  and  $5d$  bands. (a)  $\sigma_{x^2-y^2}^*$  band split by either electron correlations or a charge-density wave, (b) no splitting of  $\sigma_{x^2-y^2}^*$  band (after Ref. (21)).

in this narrow band. Since the Ni— $\text{O}_I$ —La— $\square$ —La— $\text{O}_I$ —Ni and Ni— $\text{O}_I$ — $\text{O}_I$ —Ni interactions are negligible or small and, from the geometry of the overlap integrals, the Ni:  $d_{z^2}$ — $\text{O}_{II}$ :  $p_\sigma$ —Ni:  $d_{z^2}$  interaction is sharply reduced relative to the Ni:  $d_{x^2-y^2}$ — $\text{O}_{II}$ :  $p_\sigma$ —Ni:  $d_{x^2-y^2}$  interaction, the Ni:  $d_{z^2}$  orbitals are strongly correlated and can be considered localized in the sense that the Ni— $\text{O}_{II}$ —Ni interaction can be described by a superexchange second-order perturbation theory. Since the  $d_{z^2}^1$  energy is lower than the mean energy of the occupied states of the half-filled  $\sigma_{x^2-y^2}^*$  band and the  $d_{z^2}^2$  configuration is split from the  $d_{z^2}^1$  configuration by a correlation splitting approaching 3 eV, as determined for NiO (29), we obtain the schematic energy diagram shown in Fig. 14 (21). Since the Fermi energy  $E_F$  lies well above the  $\text{O}^{2-} : 2p^6$  band edge (29), the nickel orbitals of  $t_{2g}$  parentage and the  $\text{O}^{2-} : 2p^6$  bands need not be considered; similarly, the Ni:  $4s$  band lies several eV from  $E_F$ , so it also is omitted from the diagram.

The tolerance factor for  $\text{La}_2\text{CuO}_4$  is  $t \approx$

0.87, but this departure from unity is considerably relieved ( $t_{\text{eff}} = 0.95$  for  $R_{\text{BO}} = \text{Cu—O}$  distance in  $\text{CuO}$ ) by an ordering of the  $\sigma$ -bonding  $3d$  electrons into the configuration  $\text{Cu}^{2+} : d_{z^2}^2 \sigma_{x^2-y^2}^* 1$  as previously suggested (see Fig. 15a) (7). However, it now appears that this energy diagram is only applicable to the T'-phase where the  $d_{z^2}^2$  energy level is stabilized by removal of the  $\text{O}_I$ -atom near neighbors from the  $c$ -axis. In the T-phase, the  $d_{z^2}^2$  levels probably do not fall completely below  $E_F$ , as will be argued in connection with the interpretation of the magnetic and transport data for  $\text{La}_2\text{CuO}_4$  and the  $\text{T} \rightleftharpoons \text{O}$  transition that occurs with increasing  $x$  in the system  $\text{La}_2\text{Ni}_{1-x}\text{Cu}_x\text{O}_4$ .

The orthorhombic distortion distinguishes two types of copper, each with a different Cu— $\text{O}_I$  distance. Those with the longer Cu— $\text{O}_I$  bond length have a more stable  $d_{z^2}^2$  configuration; those with a shorter Cu— $\text{O}_I$  bond length may have a  $d_{z^2}^2$  configuration at an energy high enough to be intersected by  $E_F$  as illustrated in Fig. 15b. Such a situation would lead to physical properties analogous to those observed in the rare-earth compounds having "mixed configurations" (commonly referred to as intermediate valences) as a result of a

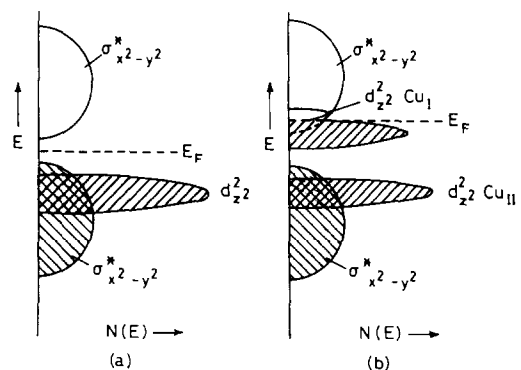


FIG. 15. Schematic density of states vs energy diagrams for the  $\sigma$ -bonding  $3d$  electrons of (a)  $\text{Pr}_2\text{CuO}_4$  with correlation splitting of the  $\sigma_{x^2-y^2}^*$  band and (b)  $\text{La}_2\text{CuO}_4$ . Not shown are filled and empty bands as in Fig. 14.

Fermi energy of a partially filled conduction band intersecting a localized  $4f^n$ -configurational energy to create a  $4f^{n+1}/4f^n$  couple. We will argue that the configuration change on going across the  $T' \rightleftharpoons O$  transition is represented by the change from that of Fig. 15a with correlation splitting of the  $\sigma_{x^2-y^2}$  band and a more normal Cu—O<sub>II</sub> bond length to that of Fig. 15b with the anomalously short Cu—O<sub>II</sub> bond lengths.

In cubic perovskites, distortions from cubic to orthorhombic symmetry selectively optimize some of the A—O bond lengths where a  $t < 1$  stretches them in the cubic phase. In the tetragonal  $K_2NiF_4$  structures under study, distortions to the orthorhombic structure appear to be stabilized by other factors besides a  $t < 1$ , which makes close correlation with a  $t \approx 0.87$  more difficult. In the system  $Pr_2Ni_{1-x}Cu_xO_4$ , the  $M \rightleftharpoons T$  transition (at  $t \approx 0.87$ ) with increasing  $x$  is consistent with the average tolerance factor  $t$  increasing with  $x$  as a result of the ordering of the  $Cu^{2+}:3d^9$  electrons as  $d_{z^2}\sigma_{x^2-y^2}^*$ . However, the  $T \rightleftharpoons O$  transition with increasing  $x$  in the system  $La_2Ni_{1-x}Cu_xO_4$  does not then follow logically unless, in  $La_2CuO_4$ , there is an inability to stabilize  $d_{z^2}$  configurations on all the  $Cu^{2+}$  ions in accordance with the energy diagram of Fig. 15a. A distortion to orthorhombic symmetry that distinguished two types of  $Cu^{2+}$  ions would tend to stabilize the  $d_{z^2}$  configurations of half the  $Cu^{2+}$  ions (Fig. 15b), and it appears that the orthorhombic structure may be stabilized in  $La_2CuO_4$  for this reason despite a  $t_{eff} = 0.95$ .

Stabilization of an orthorhombic distortion rather than a monoclinic-M or tetragonal-T' distortion appears, empirically, to be associated with larger and more basic A cations. Although  $Pr_2CuO_4$  has a tolerance factor  $t \approx 0.85$ , the Cu—O distance of  $CuO$  gives a  $t_{eff} = 0.91$ . Nevertheless, the T' phase is stabilized. Stabilization of this phase, which has an expanded basal plane allowing a Cu—O<sub>II</sub> square-coplanar dis-

tance similar to that found in  $CuO$ , would seem to require (i) an A cation small enough to prevent stretching of a B—O<sub>II</sub> bond length beyond  $R_{BO}$  and (ii) a reduced A—B electrostatic repulsion along the  $c$ -axis. Ordering of  $d_{z^2}$  electrons along the  $c$ -axis at a  $Cu^{2+}$  ion provides an important screening of this latter repulsion, which accounts for the known stabilization of this phase exclusively with the Cu(II) oxides. The smaller size and greater acidity of the  $Pr^{3+}$  compared to the  $La^{3+}$  ion also favor the T' phase in  $Pr_2CuO_4$  relative to  $La_2CuO_4$ ; and it is satisfying to note that the T' phase is stabilized for the  $Ln_2CuO_4$  compounds containing  $Ln = Pr$  to  $Gd$  with an  $x_c$  for the  $O \rightleftharpoons T'$  transition in  $La_{2-x}Ln_xCuO_4$  that is larger for  $Ln = Pr$  than for  $Ln = Nd$  (see Table I).

In  $Pr_2NiO_4$  ( $t = 0.86$ ), where there can be no reduction of the  $Pr^{3+}-Ni^{2+}$  electrostatic repulsion by ordering of electrons into  $d_{z^2}$  orbitals to form a  $d_{z^2}$  configuration, the distortion is to monoclinic symmetry. This symmetry is compatible with a cooperative antiferroelectric displacement of  $O_I$  atoms along [100] and  $[\bar{1}00]$  directions of the T phase (see Fig. 2c), rather than a displacement through an A-cation face to a tetrahedral position as in the T' phase. (The  $O_{II}$  atom may also be displaced slightly in the direction of a cooperative rotation about the [010] axis.) Such a displacement of the  $O_I$  atom reduces the length of the  $c$ -axis and allows stronger A— $O_I$  bonding without removing all screening of the A—B electrostatic repulsion. The Ni— $O_{II}$  bond length appears to be little changed by the  $T \rightleftharpoons M$  distortion, so the  $\sigma_{x^2-y^2}$  bandwidth should not be significantly reduced on traversing this smooth transition. Similarly, little change in the  $\sigma_{x^2-y^2}$  bandwidth will occur at a smooth  $O \rightleftharpoons T$  transition; but the situation is dramatically changed at a first-order  $O - T'$  transition, which exhibits a discontinuous change in the Cu— $O_{II}$ —Cu distance.

### B. $\text{La}_2\text{CuO}_4$

The fact that the impurity phase encountered in our sample of  $\text{La}_2\text{CuO}_4$  is ferromagnetic would seem to raise doubts that the localized atomic moment, which is observed consistently in different laboratories, can also be due to an impurity phase, as has been assumed by Saez Puche *et al.* (15). This suspicion is reinforced by the close correlation between the low-temperature rise in the electrical resistivity with decreasing temperature and the magnetic anomaly below 200 K. Assignment of the magnetic anomaly to antiferromagnetic order (15) is also inconsistent with a Curie law and zero Weiss constant. However, interpretation of the magnetic and transport properties as intrinsic to  $\text{La}_2\text{CuO}_4$  follows from the band diagram of Fig. 15b.

At temperatures  $T > 200$  K, the Curie law is generated by a fixed number of holes in the  $d_{z^2}$  configuration. Each hole corresponds to a "localized"  $d_{z^2}^{1/2}$  configuration carrying a spin  $S = 1/2$ ; the electron creating that hole is donated to the  $\sigma_{x^2-y^2}^*$  band, which is itinerant with a low density of states at the Fermi energy. At temperatures  $T < 200$  K, there is a smooth shifting of the position of the  $d_{z^2}$  level relative to the Fermi energy, and the number of localized holes decreases monotonically with decreasing temperature. Since the localized holes give rise to a Curie law at  $T > 200$  K, they should continue to do so at  $T < 200$  K. Therefore Fig. 5a shows the variation in the Curie constant  $C$  in emu K/mole; it is constant down to 200 K and then decreases nearly linearly with decreasing temperature below 200 K. The absence of an ESR signal is presumably due to the short lifetime of an  $S = 1/2$  state in this mixed-configuration system; and the absence of any interatomic interaction, which would lead to a Weiss constant  $\theta$  and a Curie-Weiss law, may also be attributed to the mobile character and low concentration of the  $S = 1/2$  states.

Assignment of the origin of the shift in the position of  $E_F$  relative to the  $d_{z^2}$  level must be more speculative; a structural refinement below 200 K is needed to test our hypothesis. In view of the distinction between  $\text{Cu}_I^{2+}$  and  $\text{Cu}_{II}^{2+}$  ions in  $\text{La}_2\text{CuO}_4$ , it is reasonable to anticipate a shift of the  $O_{II}$  ions away from the copper with shorter  $\text{Cu}-O_I$  bonds toward the copper with a larger  $\text{Cu}-O_I$  bond. Such a motion would make the average  $\text{Cu}-O$  distance the same for each type of copper; but it would also change the translational symmetry in the basal plane so as to open up further any energy gap in the middle of the  $\sigma_{x^2-y^2}^*$  band. Thus a smooth, cooperative shift of the  $O_{II}$  ions that increased in amplitude with decreasing temperature below 200 K would further split the  $\sigma_{x^2-y^2}^*$  band and shift the Fermi energy relative to the  $d_{z^2}$  level as required to make the compound a semiconductor at the lowest temperatures.

The conductivity,  $\sigma \approx 10 \text{ ohm}^{-1} \text{ cm}^{-1}$ , is temperature-independent, but low for a metallic compound. The lower limit for conductivity in a partially filled band follows from the expression  $\sigma = ne^2\tau/m^*$  and the requirement, imposed by the Heisenberg uncertainty principle, that the bandwidth  $w = \hbar^2(\pi/a_0)^2/2m^*$  be related to the mean-free time  $\tau$  between electron scattering events by  $\tau > \hbar/w$ . For a charge-carrier density  $n = c/a_0^3$ , it follows that

$$\sigma_{\min} \approx 0.2g^2c(e^2/\hbar a_0) = c \times 10^2 \Omega^{-1} \text{ cm}^{-1} \quad (2)$$

where  $c$  is the concentration of mobile charge carriers per copper atom and  $g \approx 1/3$  is the density-of-states reduction factor at the mobility edge (38). In this limit the mean-free path between scattering events is about one lattice parameter, which is reasonable in a system with a fluctuating configuration. The mobile electrons tend to become trapped in the localized  $d_{z^2}$  orbitals.

On the other hand, it might be preferable, in such a situation, to consider that the

charge carriers move with a diffusive motion, so that  $\sigma = ne^2D/kT$ . The upper limit for conductivity by this process occurs where the motional enthalpy appearing in the diffusion coefficient is  $\Delta H_m < kT$ . In this limit, the diffusion coefficient becomes  $D \sim a_0^2\nu_0$ , where  $\nu_0$  is the attempt frequency and  $a_0$  is the jump distance. The maximum room-temperature conductivity in this regime is, therefore,

$$\sigma_{\max} \approx cg^2(h\nu_0/kT)(e^2/\hbar a_0) \approx 10^3 \times c(h\nu_0/kT) \quad (3)$$

where, for an attempt frequency  $\nu_0 \approx 10^{12} \text{ sec}^{-1}$ , the room-temperature ratio  $(h\nu_0/kT) \approx 0.1$  makes  $\sigma_{\min}(\text{band}) \approx \sigma_{\max}(\text{diffusion})$ .

With either model, it is necessary to assume a small charge-carrier concentration  $c \approx 0.1$  to account for a temperature-independent  $\sigma \approx 10 \Omega^{-1} \text{ cm}^{-1}$ . On the other hand, such a small charge-carrier concentration is consistent with a temperature-independent Seebeck coefficient given by (for small  $c$ )  $\alpha \approx -(k/e)\ln c \approx 200 \mu\text{V/K}$ . The positive sign can be attributed to the shape of the combined density of states. Moreover, a concentration  $c \approx 0.1$  of mobile, positive charge carriers agrees with the concentration of localized moments as determined from the Curie constant.

The fact that the number of  $\sigma_{x^2-y^2}$ -band charge carriers is about equal to the concentration of localized spins leads to the conclusion that, even at high temperatures, the  $\sigma_{x^2-y^2}$  band may be split in two, or nearly so, by the translational symmetry because of the two distinguishable copper atoms in the orthorhombic unit cell. Such a splitting would be increased by cooperative motions of  $\text{O}_{\text{II}}$  atoms in the basal plane below 200 K. This conclusion is also consistent with the apparent lack of any significant temperature-independent term in the magnetic susceptibility. In the absence of any Weiss constant in the temperature dependence of the magnetic susceptibility, there is no basis for postulating an electron-

correlation band splitting as was done previously (7); but the character of the orthorhombic distortion makes this unnecessary. Moreover, a  $\sigma_{x^2-y^2}$  band that is too broad to sustain spontaneous magnetization is consistent with the magnetic properties of  $\text{CuO}$  (30), which indicate itinerant-electron antiferromagnetism, since the  $\text{Cu}-\text{O}_{\text{II}}-\text{Cu}$  linkages form  $180^\circ$  bonds in  $\text{La}_2\text{CuO}_4$  and the  $\text{Cu}-\text{O}_{\text{II}}$  distance of  $1.90 \text{ \AA}$  is significantly shorter than the  $1.95 \text{ \AA}$  of the short  $\text{Cu}-\text{O}$  bond in  $\text{Cu}-\text{O}$ . The low charge-carrier mobility is well accounted for by configuration fluctuations  $d_{1/2}^2 \rightleftharpoons d_{3/2}^2$  on the copper ions.

According to the model of Fig. 15b, in which the concentration of mobile  $\sigma_{x^2-y^2}$ -band charge carriers is equal to the concentration of localized spins, the density of charge carriers contributing to the conductivity would decrease approximately linearly with  $T$  as does the Curie constant  $C$  (see Fig. 5a). As the charge-carrier density decreases, a motional enthalpy  $\Delta H_m > kT$  can be expected to affect the mobility, so the resistivity increases more sharply than linearly at the lowest temperatures.

The orthorhombic solid solutions in the systems  $\text{La}_{2-x}\text{Pr}_x\text{CuO}_4$ ,  $0 < x < 0.50$ , exhibit a thermal variation of the resistivity that is similar to that of the end member  $\text{La}_2\text{CuO}_4$  (see Fig. 8). The principal evolution with increasing  $x$  is a slightly higher conductivity at higher temperatures and a shifting of the onset of the low-temperature rise in resistivity to lower temperatures. This observation shows that the observations on  $\text{La}_2\text{CuO}_4$  are not sample specific, which is consistent with the localized moments and low-temperature anomalies reflecting an intrinsic material property; it is also consistent with a decrease in all the unit-cell parameters with increasing  $x$ , Table I, which would increase the width of the  $\sigma_{x^2-y^2}$  band.

For all  $x$ , a  $\log \rho$  versus  $\log T$  plot is linear below 100 K with a slope corresponding to the relation  $\rho \sim T^{-2.4}$ .



### C. $\text{La}_2\text{NiO}_4$

The magnetic susceptibility of  $\text{La}_2\text{NiO}_4$  shows a Curie–Weiss law at high temperatures that is compatible with the energy diagram of Fig. 14 and strong correlations among the  $\sigma_{x^2-y^2}^*$  electrons. A Weiss constant  $\theta < 0$  indicates antiferromagnetic coupling in accordance with the superexchange rules for interactions between half-filled  $d_{x^2-y^2}$  orbitals—or for correlations in a half-filled  $\sigma_{x^2-y^2}^*$  band (28). From Table II, the high-temperature  $\mu_{\text{eff}} = 3.03 \mu_B$  is a little larger than the spin-only value  $2.83 \mu_B$  that would be expected for a localized-electron  $S = 1$  configuration and a constant Weiss molecular-field parameter  $W$ . On the other hand, the low-temperature ( $T < T_d$ ) susceptibility gives a measured  $\mu_{\text{eff}} = 1.83 \mu_B$ , which is closer to the localized-electron  $S = 1/2$  value of  $1.73 \mu_B$ . Since the low-temperature susceptibility is field-independent, there is no evidence of a weak ferromagnetism below  $T_d$ , which agrees with the neutron-diffraction data. We seem forced to conclude that below  $T_d$  the strong correlations among the  $\sigma_{x^2-y^2}^*$  electrons have either collapsed or changed their character so as not to provide interatomic interactions.

If the correlations among the itinerant  $\sigma_{x^2-y^2}^*$  electrons are induced only by intraatomic-exchange coupling to the “localized”  $d_{z^2}$  electrons, then the magnetic susceptibility may only asymptotically approach a localized-electron Curie–Weiss law at the highest temperatures as shown in Fig. 16 (28). In this case, a measured  $\mu_{\text{eff}}$  larger than the theoretical  $\mu_{\text{eff}}$  would be obtained from lower temperature susceptibility data, and the magnitude of the Weiss constant  $\theta$  would be high relative to any observed magnetic-ordering temperature  $T_N$ . Since  $\mu_{\text{eff}}$  is larger than the theoretical value for  $T > T_d$ , we may assume that the measured Weiss constant  $\theta = -500 \text{ K}$  may be somewhat larger in magnitude than could be expected from the strength of the

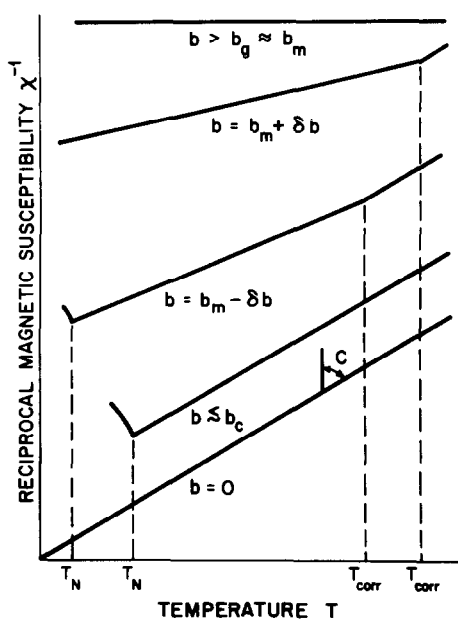
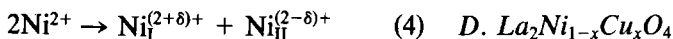


FIG. 16. Predicted variations with  $b$  in the temperature variation of the inverse paramagnetic susceptibility for  $n_1 = 1$ , after Ref. (28).

interatomic exchange interactions.

The smooth, but abrupt collapse in the contribution of the  $\sigma_{x^2-y^2}^*$  electrons to the magnetic susceptibility implies that a spin pairing among the  $\sigma_{x^2-y^2}^*$  electrons is stabilized relative to an enhancement of the electron correlations via intraatomic exchange interactions. Moreover, the spin pairing cannot be a long-range antiferromagnetic order as the localized  $d_{z^2}$  moments remain decoupled. Such a situation could occur were there a disproportionation among the narrow-band  $\sigma_{x^2-y^2}^*$  electrons that was brought about by a cooperative displacement of the in-plane  $\text{O}_{\text{II}}$  atoms toward one set of nickel atoms and away from another. Unless such displacements are accompanied by a distortion to orthorhombic symmetry at low temperatures of the type found in  $\text{La}_2\text{CuO}_4$ , the disproportionation would represent a two-dimensional charge-density wave in which the disproportionation reaction



occurs. Lack of long-range ordering between basal planes could have obscured observation of a doubling of the basal plane of the unit cell in the neutron-diffraction experiments (20).

Nevertheless, such a speculation does not account for the apparent absence of any evidence of antiferromagnetic ordering—even short-range—down to 12 K in the presence of a low-temperature  $\theta \approx -120$  K.

At  $T_{\min} \approx 600$  K, the resistivity has a minimum value; it corresponds to a  $\sigma_{\min} \approx 35 \Omega^{-1} \text{cm}^{-1}$  for the metallic phase at temperatures  $T > T_{\min}$ , which is in good accord with Eq. (2). At lower temperatures, an activation energy  $E_a = 0.053 \text{ eV} \approx kT_{\min}$  suggests a motional enthalpy is responsible for the observed activation energy:  $E_a = \Delta H_m$ . Such a situation is quite compatible with strong correlations among the  $\sigma_{x^2-y^2}^*$  electrons that are induced by intraatomic-exchange interactions with localized  $d_{z^2}$  electrons. The charge-carrier mobility would be reduced by the formation of small magnetic polarons. However, the increase in activation energy below  $T_d$ , although small ( $E_a = 0.082 \text{ eV}$ ), must be correlated with an apparent collapse in the contribution of the  $\sigma_{x^2-y^2}^*$  electrons to the paramagnetic susceptibility. Whatever is pairing the  $\sigma_{x^2-y^2}^*$  electrons below  $T_d$  appears to be opening up an energy gap that splits occupied from empty band states. Stabilization of the charge-density wave discussed above would accomplish this.

The above discussion is based on the assumption that the apparent Curie-Weiss law below  $T_d$  is meaningful and that a  $\mu_{\text{eff}} \approx 1.83 \mu_B$  taken from the slope of the  $\chi_m^{-1}$  versus  $T$  curve in this temperature range is not fortuitous, but is a measure of the atomic moment at magnetically disordered nickel atoms. To test this assumption, it is useful to investigate some solid solutions with  $\text{La}_2\text{NiO}_4$ .

Substitution of copper for nickel in the tetragonal-T phase gives a paramagnetic susceptibility per  $\text{Ni}^{2+}$  ion similar to that found in  $\text{La}_2\text{NiO}_4$ . However, the measured  $\mu_{\text{eff}}$  at high temperatures decreases toward the theoretical value with increasing  $x$  as though the  $\sigma_{x^2-y^2}^*$  band were being narrowed by the introduction of foreign cations. The initial increase in  $c/a$  ratio with  $x$  signals that the  $\text{Cu}^{2+}$  ions have a  $d_{z^2}^2$  configuration stabilized below the Fermi energy, which would account for the lack of any contribution to the magnetic susceptibility from the copper. With a diamagnetic  $d_{z^2}^2$  configuration, there is no local moment to magnetize the  $\sigma_{x^2-y^2}^*$  electrons at a  $\text{Cu}^{2+}$  ion. This introduces a reduction in the stabilization of the high-temperature state having correlated  $\sigma_{x^2-y^2}^*$  electrons, so  $T_d$  increases with  $x$ . At the same time  $T_d$  becomes less well defined. However, the  $x = 0.25$  sample still shows a break in the resistivity at  $T_d$  (see Fig. 5a). Below  $T_d$ , the  $\mu_{\text{eff}}$  remains close to the theoretical value of  $S = 1/2$  per  $\text{Ni}^{2+}$  ion, which would seem to confirm the hypothesis that only the  $d_{z^2}^1$  configurations are contributing to the magnetic susceptibility. Further support comes from the observation (Table II and Fig. 6) that the  $x = 0.75$  sample shows a larger  $\mu_{\text{eff}}$  at low temperatures. Given the band diagram of Fig. 15b for  $\text{La}_2\text{CuO}_4$ , this enhancement would seem to indicate the introduction of holes into the  $d_{z^2}^2$  level at the  $\text{Cu}^{2+}$  ions at higher copper concentrations and hence the prefiguration of a distortion from the T to the O structure. Indeed, the O structure is found at room temperature in the  $x = 0.9$  sample.

Thus the behavior of the system  $\text{La}_2\text{Ni}_{1-x}\text{Cu}_x\text{O}_4$  makes good contact with the models proposed for the two end members. Moreover, it would appear that the transition at  $T_d$  in the T phase and that at 200 K in  $\text{La}_2\text{CuO}_4$  have a common crystallographic origin. For each we have postulated the for-

mation of a charge-density wave in the  $\sigma_{x^2-y^2}^*$  bands as the result of a cooperative displacement of the  $O_{II}$  atoms.

### E. $La_{2-2x}Sr_{2x}Ni_{1-x}Ti_xO_4$

The tetragonal-T system  $La_{2-2x}Sr_{2x}Ni_{1-x}Ti_xO_4$  has a magnetic susceptibility per  $Ni^{2+}$  ion that is very similar, for  $0 < x < 0.5$ , to that of the system  $La_2Ni_{1-x}Cu_xO_4$  with the same values of  $x$ , see Fig. 6a. As can be seen from Table II, the high-temperature  $\mu_{\text{eff}}$  approaches the theoretical value of  $2.83 \mu_B$  for  $S = 1$ , and the high-temperature Weiss constant  $\theta$  decreases with increasing  $x$ . Although  $T_d$  is not sharply defined in either system, the low-temperature susceptibility has a continuous change of slope of the  $\chi_m^{-1}$  versus  $T$  curve that seems to approach asymptotically a Curie law. Moreover, the high-temperature activation energy in the resistivity increases with  $x$  as might be expected for narrower  $\sigma_{x^2-y^2}^*$  bands.

The  $x = 0.75$  sample, which is beyond the percolation limit  $x = 0.59$  for a square-planar net (31), has a quite different character: it exhibits a simple Curie law with  $\mu_{\text{eff}} = 2.73 \mu_B$  for all temperatures, and the sample is a better semiconductor (see Fig. 9) with the typical green color of a Ni(II) oxide. Thus the existence of a  $T_d$  and of a high-temperature Weiss constant  $\theta$  is clearly associated with Ni— $O_{II}$ —Ni interactions. The fact that the  $Ni^{2+}$  and  $Ti^{4+}$  ions remain disordered in the  $x = 0.5$  sample is itself unusual; it may reflect a stabilization associated with Ni— $O_{II}$ —Ni interactions and/or the disorder of the  $La^{3+}$  and  $Sr^{2+}$  ions.

If  $T_d$  in  $La_2NiO_4$  reflects a cooperative displacement of  $O_{II}$  atoms within a basal plane, then it would appear, from the blurring of  $T_d$ , that the atomic displacements are only short-range cooperative in the mixed systems.

### F. The T' Phase

In the T'-tetragonal phases  $Pr_2CuO_4$  and

$Nd_2CuO_4$ , the significantly larger Cu— $O_{II}$ —Cu distance will narrow the  $\sigma_{x^2-y^2}^*$  band, and the removal of the  $O_I$  atoms to tetrahedral interstices of the  $Ln_2$  bilayer guarantees a  $d_{z^2}^2$  state completely below the Fermi energy  $E_F$  as pictured in Fig. 15a. The observation of an activation energy in the resistivity of 0.069 eV with  $T_{\text{min}} \approx 700$  K, see Fig. 9a, indicates that the  $\sigma_{x^2-y^2}^*$  electrons are probably strongly correlated, but it is nevertheless dangerous to assume that, because the copper makes no apparent contribution to the susceptibility below 300 K, it must be antiferromagnetically coupled (16). It would be useful to have neutron-diffraction data to clarify this point.

### G. Random Comments

In a previous communication, one of us (21) suggested that the resistivity minimum occurring in high-temperature  $La_2NiO_4$  might be due to a suppression of the electron correlations in the  $\sigma_{x^2-y^2}^*$  band as a result of an increase in the  $c/a$  ratio with temperature. However, it is more probably due to an  $E_a \approx \Delta H_m$  becoming  $\Delta H_m < kT$ , as discussed in connection with Eq. (3). In the present study, we have found no correlation between the resistivity minimum and changes in the  $c/a$  ratio. Moreover, the electronic conductivity appears to be better described by a diffusive motion.

The ESR signals observed from the system  $La_{2-x}Pr_xCuO_4$  are not necessarily associated with  $Cu^{2+}$  ions in the host structure. Oxygen vacancies containing a single electron must also be considered. It does not appear relevant to the present study to attempt to sort out the assignments of the various signals observed.

The observation of a magnetic susceptibility that obeys a Curie-Weiss law to lowest temperatures with no apparent magnetic ordering, as we report for  $La_2NiO_4$ , is not completely without precedence in oxides, but it has not previously been noted. It can be seen, for example, in the magnetic-sus-

ceptibility data reported for the bronze  $\text{Na}_{0.33}\text{V}_2\text{O}_5$  (32) and for  $\text{LaSrCoO}_4$  (33), both low-dimensional systems. Such a behavior has also been observed in the valence-fluctuation systems  $\text{LnCu}_2\text{Si}_2$  (34); in this case, a quasi-Boltzmann partition function has been invoked to account for it (35).

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