

## Vibrational Spectra of $M_2\text{Cu}(\text{SO}_4)_2 \cdot 6\text{H}_2\text{O}/\text{D}_2\text{O}$ ( $M = \text{NH}_4$ or $\text{K}$ )

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The IR and polarized Raman spectra of  $M_2\text{Cu}(\text{SO}_4)_2 \cdot 6\text{H}_2\text{O}$  ( $M = \text{NH}_4$  or  $\text{K}$ ) and their deuterated analogs have been recorded and analyzed. The site locations for the  $\text{SO}_4^{2-}$  ions in these crystals are found to be identical. These  $\text{SO}_4^{2-}$  tetrahedra are angularly distorted. The vibrational bands of the metal aquo complex for  $(\text{NH}_4)_2\text{Cu}(\text{SO}_4)_2 \cdot 6\text{H}_2\text{O}$  are shifted considerably from those for other Tutton salts. One can infer from the spectral data that the  $\text{NH}_4^+$  ion is not rotating freely in the lattice. Separate bands have been identified for three different types of water molecules in both samples. This interpretation is confirmed by analysis of the spectral changes due to the replacement of hydrogen by deuterium in the  $\text{H}_2\text{O}$  units. © 1989 Academic Press, Inc.

### Introduction

Among the monoclinic double salts of the type  $M^I M^{II}(\text{SO}_4)_2 \cdot 6\text{H}_2\text{O}$  ( $M^I$  and  $M^{II}$  are monovalent and divalent cations, respectively), the copper-containing Tutton salts are not exactly isostructural because the coordination numbers of some of the oxygen atoms bonding to  $\text{NH}_4^+$  and  $\text{K}^+$  ions are different (1). Also, an earlier investigation reported that the arrangement of water molecules about the central copper ion in  $(\text{NH}_4)_2\text{Cu}(\text{SO}_4)_2 \cdot 6\text{H}_2\text{O}$  differs from the general pattern for this series (2). IR and single-crystal Raman studies have been conducted for these compounds in order to understand the difference between the vibrational modes of  $(\text{NH}_4)_2\text{Cu}(\text{SO}_4)_2 \cdot 6\text{H}_2\text{O}$ ,  $\text{K}_2\text{Cu}(\text{SO}_4)_2 \cdot 6\text{H}_2\text{O}$ , and other Tutton salts.

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### Experimental

Single crystals used for the present investigation are grown by slow evaporation of equimolar aqueous solutions of A.R. grade  $\text{CuSO}_4 \cdot 5\text{H}_2\text{O}$  and  $M_2\text{SO}_4$  ( $M = \text{NH}_4$  or  $\text{K}$ ) at room temperature. Partially deuterated samples are obtained by repeated crystallization of solutions of the corresponding samples in pure  $\text{D}_2\text{O}$ . A Spex Ramalog 1401 double monochromator equipped with a Spectra Physics Model 165  $\text{Ar}^+$  laser has been employed to obtain the Raman spectra in the Stokes region of the green line (514.5 nm). The IR spectra have been recorded with a PE 580 spectrophotometer using a Nujol technique.

$(\text{NH}_4)_2\text{Cu}(\text{SO}_4)_2 \cdot 6\text{H}_2\text{O}$  and  $\text{K}_2\text{Cu}(\text{SO}_4)_2 \cdot 6\text{H}_2\text{O}$  belong to the monoclinic system with space group  $P2_1/a$  ( $C_{2h}^2$ ) ( $Z = 2$ ) (2, 3). Group theoretical analysis predicts 234 and

TABLE I  
VIBRATIONAL SPECTRA DATA (cm<sup>-1</sup>) BAND ASSIGNMENTS

(NH <sub>4</sub> ) <sub>2</sub> Cu(SO <sub>4</sub> ) <sub>2</sub> · 6H <sub>2</sub> O/D <sub>2</sub> O				K <sub>2</sub> Cu(SO <sub>4</sub> ) <sub>2</sub> · 6H <sub>2</sub> O/D <sub>2</sub> O			
Raman		IR		Raman		IR	
H <sub>2</sub> O				H <sub>2</sub> O			
A <sub>g</sub> a(cc)b	B <sub>g</sub> a(cb)c	D <sub>2</sub> O	H <sub>2</sub> O	A <sub>g</sub> a(cc)b	B <sub>g</sub> a(cb)c	D <sub>2</sub> O	H <sub>2</sub> O
57 w				63 w	63 w		
62 m	64 m	64 m		71 m	70 m	70 m	
81 s	81 s	81 s			89 s		
96 m	96 m	96 m		95 m			
106 wbr				104 mbr			
120 s	120 s	120 m		114 w	114 m	114 w	
				118 s	118 s	118 s	
142 m	146 m			142 m	142 m		
176 w	164 wbr			169 w	169 w		
193 m	175 m	175 m	210 s	193 s	192 s	192 s	210 s
223 m	233 w	235 m	230 m	232 m	230 s	232 m	235 m
238 m			245 w	258 s	258 m	258 m	250 w
270 w	264 w			289 m	287 w		
				307 w	307 w	307 w	
342 w	339 w		355 vw	363 w	320 w	320 w	365 vw
373 wbr	370 wbr				369 w		
				384 w	409 w		
403 wbr	393 wbr			406 m	442 s	442 s	440 m
438 w	437 w	438 w	425 wbr	442 m	463 s	463 s	470 w
458 s	458 s	458 s		463 s			
	485 vw	350 wbr	540 wbr	559 mbr	559 mbr	424 mbr	550 wbr
608 w	604 sh	604 w	610 vs	613 s	610 s	610 w	610 w
617 s	618 s	617 s	640 w	622 m	626 m	625 m	615 vs
632 m	633 m			636 s	636 m	636 vw	660 m
	676 wbr		500 vw	691 w	683 vw	500 w	
756 wbr	748 w	548 w	680- 800 br		740 wbr	553 w	775 br

t<sup>s</sup>l<sup>s</sup>p<sup>o</sup>-H...Ol<sup>s</sup>l<sup>n</sup> or p<sup>o</sup>p<sup>o</sup>p<sup>o</sup>p<sup>o</sup>p<sup>o</sup>p<sup>o</sup>...p<sup>o</sup>p<sup>o</sup>p<sup>o</sup>p<sup>o</sup>p<sup>o</sup>p<sup>o</sup>p<sup>o</sup>p<sup>o</sup>p<sup>o</sup>p<sup>o</sup>p<sup>o</sup>p<sup>o</sup>

773 w	784 wbr	575 w	798 wbr	802 w	584 wbr	860 wbr	630 vw
810 wbr	830 vw	860 wbr	848 vw	802 w	584 wbr	860 wbr	
922 w	914 w	914 w	926 w	921 w	921 w	926 w	2 $\nu_2^s$
962 w	964 w	986 vs	970 w	972 w	988 vs	965 s	$\nu_1^s$
986 vs	986 vs		988 vs	988 vs	988 vs	995 w	$\nu_1^s + \nu_1^s$
1052 w	1052 w		1046 w	1046 w			
1079 m	1071 m	1071 s	1081 m	1074 m	1074 s		
1105 m	1106 m	1105 w	1110 m	1110 m	1110 m	1095 vs	$\nu_3^s$
1126 m	1127 s	1127 m	1136 s	1136 s	1136 s	1135 s	
1153 m	1154 m		1161 s	1161 m	1161 m		
1392 w	1408 w	1390 vs					$\nu_4^a$
1441 wbr	1436 mbr	1425 br					
1486 m	1474 mbr						
1626 mbr	1624 mbr	1200 mbr	1638 mbr	1642 w	1200 mbr		W I
1640 mbr	1643 wbr	1218 m	1686 mbr	1706 wbr	1223 m	1530-	$\nu_2$ W II
1685 w	1673 mbr	1254 w	1715 w	1727 wbr	1238 mbr	1670 br	W III
	1691 w						$\nu_2^a$
1713 mbr	1712 wbr						
1752 w	1764 w						$\nu_4^a + \nu_6^a$
	2037 w	2030 w					$\nu_2^a + \nu_6^a$
	2061 w	2200 br					$\nu$ HDO
3025 wbr	3029 w	2640 w			2662 w		$\nu_1^a$
	3096 w	2709 w			2725 w		$\nu_2^a + \nu_4^a$
3125 wbr	3135 wbr	2276 w		2300 w			$\nu_3^a$
3195 wbr	3181 w			3150 wbr			W III
3215 w	3213 w	3140-					$\nu_1$ W II
3257 mbr	3258 w	3200 br					W I
3288 w	3258 w		3250 mbr	3260 mbr	2329 mbr		
3301 w	3301 vw	3300-	3287 mbr	3318 w	2352 mbr	3000-	
		3480 br	3295 wbr	3318 w	2415 mbr	3500 br	
3353 wbr	3356 wbr		3355 w	3357 w	2431 w		W III
3398 wbr	3397 wbr	2550 wbr	3380 w	3382 wbr	2470 m	3400 wbr	$\nu_3$ W II
3432 w	3438 w		3424 wbr		2562 w		W I

Note. Relative intensities: vs, very strong; s, strong; m, medium; w, weak; vw, very weak; sh, shoulder; br, broad.  $\nu_6^a$ , torsional oscillation of  $\text{NH}_4^+$ .

<sup>a</sup> Superscripts n, s, c, and w refer to modes of  $\text{NH}_4^+$ ,  $\text{SO}_4^{2-}$ ,  $[\text{Cu}(\text{H}_2\text{O})_6]^{2+}$ , and  $\text{H}_2\text{O}$ , respectively. The l and t represent the librational and translational modes, respectively.

186 normal modes (including three acoustic modes) for  $\text{NH}_4\text{Cu}$  and  $\text{KCu}$ , respectively. They are distributed as

$$\Gamma_{234}^{\text{NH}_4\text{Cu}} = 57A_g(\text{R}) + 57B_g(\text{R}) \\ + 60A_u(\text{IR}) + 60B_u(\text{IR})$$

and

$$\Gamma_{186}^{\text{KCu}} = 45A_g(\text{R}) + 45B_g(\text{R}) \\ + 48A_u(\text{IR}) + 48B_u(\text{IR}).$$

### Internal Modes of $\text{SO}_4^{2-}$

The ion occupies a lower site symmetry  $C_1$  in both  $(\text{NH}_4)_2\text{Cu}(\text{SO}_4)_2 \cdot 6\text{H}_2\text{O}$  and  $\text{K}_2\text{Cu}(\text{SO}_4)_2 \cdot 6\text{H}_2\text{O}$  crystals. As a result, the IR-inactive  $\nu_1$  and  $\nu_2$  modes may become active, and the degeneracies of  $\nu_2$ ,  $\nu_3$ , and  $\nu_4$  modes may be removed. For both crystals,  $\nu_1(A_1)$  modes are found to split into two components in their Raman spectra. However, in the IR spectra, only one band is observed at  $975 \text{ cm}^{-1}$  for  $(\text{NH}_4)_2\text{Cu}(\text{SO}_4)_2 \cdot 6\text{H}_2\text{O}$  whereas  $\text{K}_2\text{Cu}(\text{SO}_4)_2 \cdot 6\text{H}_2\text{O}$  possesses two bands in this region. As the correlation field splitting is usually large for hydrogen bonded systems (4), the observed splittings rule out the possibility of the existence of two types of  $\text{SO}_4^{2-}$  ions in  $\text{K}_2\text{Cu}(\text{SO}_4)_2 \cdot 6\text{H}_2\text{O}$  crystal as suggested earlier by Gupta *et al.* (5). The splittings for both crystals are due to a correlation field effect. The partial or complete lifting of the degeneracy of  $\nu_2(E)$ ,  $\nu_3(F_2)$ , and  $\nu_4(F_2)$  modes in the IR and Raman spectra is due to a crystalline field. The removal of the degeneracy of the bending modes in the Raman spectra suggests that the angular distortion of  $\text{SO}_4^{2-}$  is greater than the linear distortion. From the order of splittings in the IR spectra it is evident that the distortion is greater for the  $\text{K}_2\text{Cu}(\text{SO}_4)_2 \cdot 6\text{H}_2\text{O}$  crystal.

### Internal Modes of $[\text{Cu}(\text{H}_2\text{O})_6]^{2+}$

The vibrational assignments of this complex (see Table I) are based on the earlier

normal coordinate analysis by Brown and Ross (6) and the observation of metal aquo complex bands for other Tutton salts (7, 8). Appearance of multiple bands for  $\nu_4$  (IR, Raman) and  $\nu_5$  (Raman) is due to the reduction of the site symmetry of the complex from  $O_h$  to  $C_i$ . As a consequence of the strain produced by the crystalline field (9),  $\nu_3$  and  $\nu_4$  modes are found to be active in the Raman spectra. Comparing the spectra of  $(\text{NH}_4)_2\text{Cu}(\text{SO}_4)_2 \cdot 6\text{H}_2\text{O}$  and  $\text{K}_2\text{Cu}(\text{SO}_4)_2 \cdot 6\text{H}_2\text{O}$ , one observes that all of the bands of the complex are shifted to low wave numbers for  $(\text{NH}_4)_2\text{Cu}(\text{SO}_4)_2 \cdot 6\text{H}_2\text{O}$ . This shift is due to larger Cu–H<sub>2</sub>O bond lengths (2). Because the bands due to the vibrational modes of the complex are weak and fall in the low wave number region, it is difficult to observe all of the corresponding bands for the deuterated samples.

### Internal Modes of Water

The internal modes of water are identified on the basis of H<sub>2</sub>O units involving three different hydrogen bond lengths [2.826 Å ( $w_1$ ), 2.727 Å ( $w_2$ ), and 2.683 Å ( $w_3$ )] in  $(\text{NH}_4)_2\text{Cu}(\text{SO}_4)_2 \cdot 6\text{H}_2\text{O}$  crystal. In  $\text{K}_2\text{Cu}(\text{SO}_4)_2 \cdot 6\text{H}_2\text{O}$ , the bond lengths are close to these values. In the Raman spectra, separate weak broadbands with frequencies shifted from their free state values have been observed for all of the modes for the three different types of water molecules. Due to the lower site symmetries of H<sub>2</sub>O and  $\text{NH}_4^+$  ions in the crystal, vibrational interaction between the groups is possible in the high-frequency (3120–3440  $\text{cm}^{-1}$ ) region. However, assignments of water bands are proposed with help from the spectrum of a deuterated sample (see Table I). The considerable shifting of the bending modes that is observed in both the Raman and IR spectra for  $(\text{NH}_4)_2\text{Cu}(\text{SO}_4)_2 \cdot 6\text{H}_2\text{O}$  indicates strong hydrogen bonding for water, probably stronger than that for ammonium ions, consistent with the crystal data (10).

### Internal Modes of $\text{NH}_4^+$

Internal modes of ammonium group are identified on the basis of their free state values (11), their hydrogen bond strength, and their deuterium substitution. The appearance of  $\nu_2$  around  $1400\text{ cm}^{-1}$  in IR indicates moderate (probably weak) hydrogen bonding for this ion (12). It is the low polarizability and anharmonic force fields of  $\text{NH}_4^+$  that cause the bands to be weaker and broader than the corresponding modes of  $\text{SO}_4^{2-}$  ions even though they occupy similar types of sites ( $C_1$ ) in the crystal. From the presence of combination bands in the region  $1750\text{--}2070\text{ cm}^{-1}$  in the Raman spectra and at  $2030\text{ cm}^{-1}$  in the IR spectra, one can infer that  $\text{NH}_4^+$  is not freely rotating in the lattice (13).

### External Modes

It is difficult to observe the translational modes of the complex as they are strongly mass dependent. Also, the translational modes of  $\text{NH}_4^+$  overlap with the internal modes of the complex in the region  $150\text{--}225\text{ cm}^{-1}$ . Hence only the assignments of external modes of  $\text{SO}_4^{2-}$  ion have been proposed (see Table I), taking into account the fact that the translatory modes are generally weak in the Raman spectra whereas the libratory modes will appear with appreciable intensity.

### Tutton Salts: A Comparison

Comparison of IR and polarized Raman data of  $\text{K}_2\text{Mg}(\text{SO}_4)_2 \cdot 6\text{H}_2\text{O}$  (7),  $(\text{NH}_4)_2\text{M}(\text{SO}_4)_2 \cdot 6\text{H}_2\text{O}$  ( $M = \text{Zn}, \text{Mn}$ ) (14),  $(\text{NH}_4)_2\text{Mg}(\text{SO}_4)_2 \cdot 6\text{H}_2\text{O}$  (8), and  $M_2\text{Cu}(\text{SO}_4)_2 \cdot 6\text{H}_2\text{O}$  ( $M = \text{NH}_4, \text{K}$ ) (see Table 1) shows that the  $\text{SO}_4^{2-}$  tetrahedron is more angularly distorted in all of the compounds except  $(\text{NH}_4)_2\text{Mg}(\text{SO}_4)_2 \cdot 6\text{H}_2\text{O}$ . From the split-

tings of the bending modes, one can infer that this distortion in different compounds is in the order  $\text{K}_2\text{Cu}(\text{SO}_4)_2 \cdot 6\text{H}_2\text{O} > (\text{NH}_4)_2\text{Cu}(\text{SO}_4)_2 \cdot 6\text{H}_2\text{O} > (\text{NH}_4)_2\text{Mn}(\text{SO}_4)_2 \cdot 6\text{H}_2\text{O} > (\text{NH}_4)_2\text{Zn}(\text{SO}_4)_2 \cdot 6\text{H}_2\text{O} > \text{K}_2\text{Mg}(\text{SO}_4)_2 \cdot 6\text{H}_2\text{O}$ . The distortion in  $\text{K}_2\text{Cu}(\text{SO}_4)_2 \cdot 6\text{H}_2\text{O}$  is to such an extent that the degeneracy of the  $\nu_2$  mode is completely removed in the IR spectrum. Combination bands indicate that the  $\text{NH}_4^+$  ions are not rotating freely in the lattice of all four compounds. Bands of the metal aquo complex in  $(\text{NH}_4)_2\text{Cu}(\text{SO}_4)_2 \cdot 6\text{H}_2\text{O}$  considerably shift from those of other compounds, indicating a difference in the nature of the  $\text{Cu-H}_2\text{O}$  bonds.

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