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## Author's reply<sup>☆</sup>

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In Ref. [1], the author studied the dynamic behaviors of a symmetric gyro with linear-plus-cubic damping mounted on a vibrating base. The system is excited by a harmonic force  $\bar{\ell} \sin \omega t$ . With the definitions

$$x_1 = \theta, \quad x_2 = \dot{\theta}, \quad f = \frac{Mg\bar{\ell}}{I_1}$$

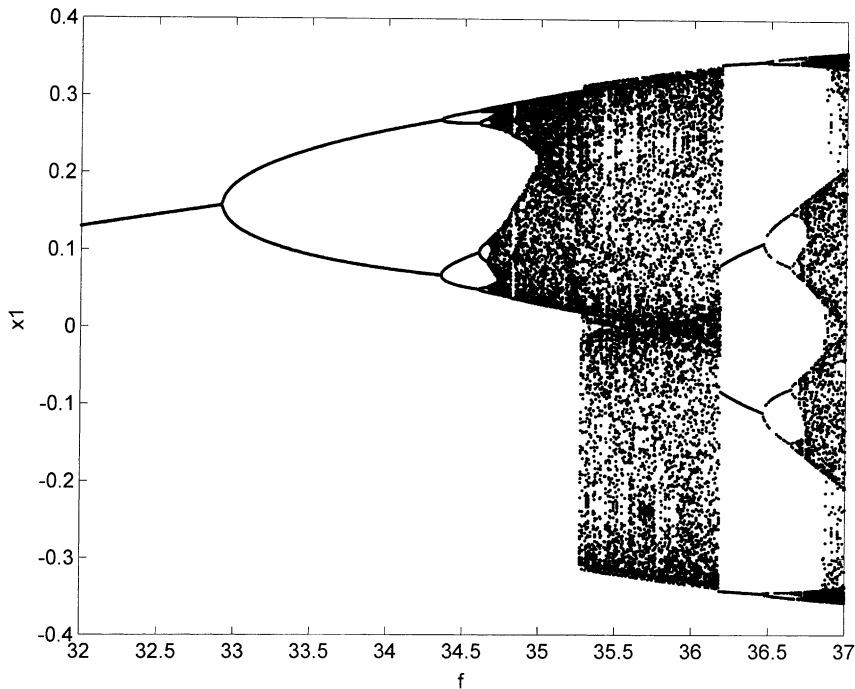


Fig. 1. The bifurcation diagram for  $x_1$  in the range  $32.0 \leq f \leq 37.0$ .

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the equation of motion governing the nutation  $\theta$  of the gyro is given by [1]

$$\begin{cases} \dot{x}_1 = x_2, \\ \dot{x}_2 = -\alpha^2 \frac{(1 - \cos x_1)^2}{\sin^3 x_1} - c_1 x_2 - c_2 x_2^3 + \beta \sin x_1 + f \sin \omega t \sin x_1. \end{cases} \quad (1)$$

The author used  $x_1/4 + x_1^3/12$  to approach  $(1 - \cos x_1)^2/\sin^3 x_1$  in the numerical simulation. Therefore, the critical values of  $f$  at which period doublings occur are different from the results given by Van Dooren [2]. The bifurcation diagram for specific system parameter value set ( $\alpha^2 = 100$ ,  $\beta = 1$ ,  $c_1 = 0.5$ ,  $c_2 = 0.05$ ,  $\omega = 2$ ) as  $f = 32.0-37.0$  is shown in Fig. 1. At the end of the broadest zone of chaotic behavior, a  $4T$ -solution is also obtained. It is evident that the structure of bifurcation diagram is the same as Fig. 1(a) in Ref. [2].

## References

- [1] H.-K. Chen, Chaos and chaos synchronization of a symmetric gyro with linear-plus-cubic damping, *Journal of Sound and Vibration* 255 (2000) 719–740.
- [2] R. Van Dooren, Comments on “Chaos and chaos synchronization of a symmetric gyro with linear-plus-cubic damping”, *Journal of Sound and Vibration* 268 (3) (2003) 632–634, [this issue](#).