588. Molecular Polarisation and Molecular Interaction. Part III. The Use of Dielectric Polarisation Measurements in studying the Extent of Molecular Interaction in Solution. The System Aniline-Dioxan-Benzene.

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#### Abstract

On the assumption that when two molecular species A and B associate in solution to give a complex AB the active masses can be represented by the molar concentrations, an equation has been derived relating the equilibrium constant $(K)$ of the association process and the molecular polarisation ( $P_{\mathrm{AB}}$ ) of the complex with the apparent increase in the molecular polarisation of A at infinite dilution. This relation permits the values of $K$ and of $P_{\mathrm{AB}}$ to be deduced from measurements of the molecular polarisation of $A$ in various mixtures of $B$ with an inert solvent. The method has been applied to data derived from measurements on dilute solutions of aniline in mixtures of dioxan with benzene, and leads to the inference that the dipole moment of the complex formed between aniline and dioxan is about 1.88 D ., whilst at infinite dilution in pure dioxan about $65 \%$ of the aniline is in the form of complex.


Dielectric polarisation measurements have long presented a potential means not only for detecting the formation of intermolecular complexes in the liquid state but also for determining the extent to which such complexes are formed. Earp and Glasstone ( $J ., 1935,1709$ ) considered the case of a mixture of compounds A and B which can yield an additive compound AB in which a definite linkage is formed. They supposed that the extrapolated value of the molecular polarisation of A at infinite dilution in $\mathrm{B}\left(P_{\mathrm{A}_{\infty}}\right)$, calculated on the assumption that the molecular polarisation of $\mathrm{B}\left(P_{\mathrm{B}}\right)$ remains constant, gives the contribution of A and of the new linkage in the compound, and hence that the molecular polarisation of the compound is given by $P_{A_{\infty}}+$ $P_{\mathrm{B}}$. From this value, combined with a knowledge of the value $\left(P_{\mathrm{A}}\right)$ of the molecular polarisation of A in solutions of equal dielectric constant in solvents in which no compound is formed, they interpreted the molecular polarisation of solutions containing finite concentrations of A in B in terms of the relation

$$
\begin{equation*}
P=P_{\mathrm{A}}\left(f_{\mathrm{A}}-x\right) /(1-x)+P_{\mathrm{B}}\left(f_{\mathrm{B}}-x\right) /(1-x)+P_{\mathrm{AB}} x /(1-x) \tag{1}
\end{equation*}
$$

where $f_{\mathrm{A}}$ and $f_{\mathrm{B}}$ are the molar fractions of the initial components A and B , respectively, and $x$ denotes the amounts of these which pass into the form of compound. This equation permits the calculation of $x$, which in turn allows the derivation of a mass-action constant $K=x(1-x) /\left(f_{\mathrm{A}}-x\right)\left(f_{\mathrm{B}}-x\right)$ wherein the activities are expressed by the molar fractions.

This approach was criticised by Hammick, Norris, and Sutton ( $J ., 1939,1755$ ) on the grounds that unless $K$ is infinite, all the $A$ is not in the form of $A B$ at infinite dilution. Further, they pointed out that in the calculation of $P$ the mean molecular weight of the solution was taken by Earp and Glasstone as $M_{\mathrm{A}} f_{\mathrm{A}}+M_{\mathrm{B}} f_{\mathrm{B}}$, whereas its true value is ( $M_{\mathrm{A}} f_{\mathrm{A}}+M_{\mathrm{B}} f_{\mathrm{B}}$ )/(1-x), so that equation (1) should be written

$$
\begin{equation*}
P=P_{\mathbf{A}}\left(f_{\mathrm{A}}-x\right)+P_{\mathrm{B}}\left(f_{\mathrm{B}}-x\right)+P_{\mathrm{AB}} x \tag{2}
\end{equation*}
$$

Finally they also questioned the applicability of the mass-action law over the full composition range of binary mixtures.

Hammick, Norris, and Sutton tested various alternative methods for the solution of this problem, but reached the conclusion that the only dielectric-constant method which produced significant results involved measurements on dilute solutions of the two components in a third, unreactive, solvent. If the two reactive components were present in a constant proportion, the values of the molecular polarisation of the solution compared with those expected if no compound were formed (corrected for the variation of the molecular polarisations with the dielectric constant of the medium) were found to increase linearly with increasing concentration. They deduced that, if $R$ is the difference between the observed and the theoretical value of the molecular polarisation of the mixture then

$$
\begin{equation*}
R=\left(P_{\mathrm{AB}}-P_{\mathrm{A}}-P_{\mathrm{B}}\right) x /\left(f_{\mathrm{A}}+f_{\mathrm{B}}\right) . \tag{3}
\end{equation*}
$$

Hence either $P_{\mathrm{AB}}$ or $x$ could be evaluated if the other were known, whereas, if neither was known, the function $\left(P_{\mathrm{AB}}-P_{\mathrm{A}}-P_{\mathrm{B}}\right) x$ could be used to give comparative data.

It was found that this function was large for mixtures of chloroform and triethylamine, noticeable for chloroform and diisopropyl ether, and within experimental error for chloroform and nitromethane. As this was in accord with the known behaviours of tertiary amines, ethers, and nitro-compounds, respectively, as electron-donors in hydrogen-bond formation, it supported this general approach to the problem. The limitations of the method were well appreciated by the authors, but the method depends on the determination of the difference between the molecular-polarisation values for solutions of a mixture of $A$ and $B$ and of $A$ and $B$ separately in an inert solvent at finite concentrations of all three components. As the molecular polarisation of a polar solute decreases with increasing concentration in a manner which so far cannot be calculated on any theoretical basis, the results must be regarded as approximate and only comparative for various systems. Also, whilst the method gives an indication of molecular interaction, the extent to which the latter occurs cannot be deduced by this means.

A more promising approach seems to be the " Method 4 " discussed by Hammick, Norris, and Sutton. This involves the determination of the apparent molecular polarisation at infinite dilution of a compound $A$ in an active solvent $B$, in an inert solvent $S$, and in mixtures of $B$ and $S$ in constant proportion. This method was rejected by them on account of the results obtained with the system diisopropyl ether-chloroform-benzene, which led to different results according to whether the ether or the chloroform was considered as the solvent at low concentration. These grounds seem rather inadequate, as this system covers a wide range of dielectric constants, and examination of their experimental data shows that there was a considerable possible error in the values used for the molecular polarisation.

Such a system may, however, be treated as follows. If the weight fractions of A, B, and S in a solution are $w_{\mathrm{A}}, w_{\mathrm{B}}$, and $w_{\mathrm{S}}$, respectively, and amounts $\Delta w_{\mathrm{A}}$ and $\Delta w_{\mathrm{B}}$ of A and B , respectively, pass into the form of a compound $A B$, then the total specific polarisation of the solution is given by $p=p_{\mathrm{A}}\left(w_{\mathrm{A}}-\Delta w_{\mathrm{A}}\right)+p_{\mathrm{B}}\left(w_{\mathrm{B}}-\Delta w_{\mathrm{B}}\right)+p_{\mathrm{AB}}\left(\Delta w_{\mathrm{A}}+\Delta w_{\mathrm{B}}\right)+p_{\mathrm{S}} w_{\mathrm{S}}$ where $p_{\mathrm{A}}, p_{\mathrm{B}}, p_{\mathrm{AB}}$, and $p_{\mathrm{S}}$ are the specific polarisations of $\mathrm{A}, \mathrm{B}$, the compound, and S , respectively. The apparent specific polarisation of $\mathrm{A}\left(p_{\mathrm{A}}{ }^{*}\right)$, calculated on the assumption of no compound formation, is given by $w_{\mathrm{A}} p_{\mathrm{A}}{ }^{*}=p-w_{\mathrm{B}} p_{\mathrm{B}}-w_{\mathrm{S}} p_{\mathrm{S}}$, and hence $w_{\mathrm{A}}\left(p_{\mathrm{A}}{ }^{*}-p_{\mathrm{A}}\right)=p_{\mathrm{AB}}\left(\Delta w_{\mathrm{A}}+\right.$ $\left.\Delta w_{\mathrm{B}}\right)-\Delta w_{\mathrm{B}} p_{\mathrm{B}}-\Delta w_{\mathrm{A}} p_{\mathrm{A}}$. On introducing the relation $\Delta w_{\mathrm{A}} / \Delta w_{\mathrm{B}}=M_{\mathrm{A}} / M_{\mathrm{B}}$, where $M_{\mathrm{A}}$ and $M_{\mathrm{B}}$ are the molecular weights of A and B , respectively, we obtain the expression

$$
\begin{equation*}
P_{\mathrm{A}}{ }^{*}-P_{\mathrm{A}}=\Delta P\left(\Delta w_{\mathrm{A}} / w_{\mathrm{A}}\right) \tag{4}
\end{equation*}
$$

where $\Delta P=P_{\mathrm{AB}}-P_{\mathrm{A}}-P_{\mathrm{B}}$, i.e., the increase in molecular polarisation attending the formation of 1 g .-mol. of AB .

This expression is similar in form to equation (3) derived by Hammick, Norris, and Sutton, but with the increment in polarisation referred to the apparent increase of $P_{\mathrm{A}}$ instead of to the increase of $P$ above the theoretical value. The equation should hold generally whether any inert third component is present or not, and, since for any particular system $\Delta P$ is constant,
the value of $P_{\mathrm{A}}{ }^{*}-P_{\mathrm{A}}$ will be proportional to the fraction of the B present which passes into the form of compound.

Further, if the active masses of the reactants can be expressed by their concentrations in g.-mol. per c.c., then by the law of mass action it follows that $K=c_{\mathrm{AB}} / c_{\mathrm{A}} c_{\mathrm{B}}=\Delta w_{\mathrm{A}} / c_{\mathrm{B}}\left(w_{\mathrm{A}}-\right.$ $\Delta w_{\mathrm{A}}$ ), or

$$
\begin{equation*}
w_{\mathbf{A}} / \Delta w_{\mathbf{A}}=1+1 / K c_{\mathbf{B}} \tag{5}
\end{equation*}
$$

But, from equation (4), $w_{\mathrm{A}} / \Delta w_{\mathrm{A}}=\Delta P /\left(P_{\mathrm{A}}{ }^{*}-P_{\mathrm{A}}\right)$, and, as $c_{\mathrm{B}}=w_{\mathrm{B}} d / M_{\mathrm{B}}$, where $d$ is the density of the solution, therefore

$$
\begin{equation*}
\Delta P /\left(P_{\mathrm{A}^{*}}-P_{\mathrm{A}}\right)=M_{\mathrm{B}} / K w_{\mathrm{B}} d+1 \tag{6}
\end{equation*}
$$

At infinite dilution of A in B or in mixtures of B and S in constant proportions, $w_{\mathrm{B}}$ is the actual weight fraction of $B$ in the solvent mixture used, and hence the validity of the assumptions made can be tested by studying the apparent molecular polarisation of A in such solutions and deriving the values at infinite dilution in each case. From equation (6) a plot of $1 /\left(P_{\Delta}{ }^{*}-P_{\Delta}\right)$ against $1 / w_{\mathrm{B}} d$ should be linear, with a slope $M_{\mathrm{B}} / K \Delta P$ and an intercept on the $y$ axis equal to $1 / \Delta P$.

Since the molecular polarisation of aniline varies only slightly with the dielectric constant of the medium, it appeared to be a suitable solute to study from this point of view, particularly as it shows abnormally high molecular polarisation, attributable to hydrogen bonding, in dioxan, a solvent the dielectric constant of which differs only a little from that of benzene (Few and Smith, this vol., p. 753) The apparent molecular polarisation of aniline in three constantratio mixtures of benzene and dioxan has therefore been studied, and the values at infinite dilution derived. The results are summarised in Table I, together with the figures for solutions of aniline in benzene and in dioxan recorded previously (loc. cit.). The symbols have the same significance as in the previous communications. As is to be expected the value of $P_{2 \infty}$ increases progressively with increasing concentration of dioxan.

Table I.
Polarisation Data for Aniline in Benzene-Dioxan Mixtures.


Table II shows the values of $1 / w_{\mathrm{B}} d$ and $1 /\left(P_{\mathrm{A}_{\infty}}{ }^{*}-P_{\mathrm{A}_{\infty}}\right)$, where $P_{\mathrm{A}_{\infty}}$ is taken as the $P_{2_{\infty}}$ value for benzene solution, and $P_{\mathrm{A}_{\infty}} *$ as the corresponding value for solutions in the dioxancontaining solvent. The linearity of the plot of $1 / w_{\mathrm{B}} d$ against $1 /\left(P_{\mathrm{A}_{\infty}} *-P_{\mathrm{A}_{\infty}}\right)$ supported the assumptions made in the derivation of equation (6). From the intercept of the best straight line through these points, derived by the method of least squares, the value of $\Delta P$ is 28.6 c.c., and thence from the slope $(0.0301) K$ is 128.

However the apparent molecular polarisation of aniline in dioxan solution decreases fairly rapidly with increasing concentration, i.e., with increasing dielectric constant of the medium (Part I), and in the present work it has been found that the rate of decrease in the mixed solvents, although less than in pure dioxan, is much greater than in benzene itself. That this rate of decrease is much greater than can be accounted for by the decrease in the proportion of aniline which passes into the form of complex, and hence that it is attributable to a large solvent effect, is shown by the following argument. On the assumption that the mass action law holds, $P_{\mathrm{A}}^{*}-P_{\mathrm{A}}$ should be proportional to the fraction of the aniline introduced which passes into the form of complex, i.e., to $\Delta w_{2} / w_{2}$ (equation 4). For infinite dilution in pure dioxan this is $16 \cdot 76 / 28 \cdot 6=0.582$. Now equation (5) can be written $w_{\mathrm{A}} / \Delta w_{\mathrm{A}}=1+M_{\mathrm{B}} / w_{\mathrm{B}} d K$. For a solution of aniline in dioxan in which the weight fraction of aniline is $0.11089, w_{\mathrm{B}}=0.88911$,
$d=1 \cdot 0292$ (Part I, Table II), and hence, on the assumption that $K=128$ and $M_{\mathrm{B}}=88 \cdot 1$, $\Delta w_{\mathrm{A}} / w_{\mathrm{A}}=0.571$. This leads to a theoretical value of 16.44 for $P_{\mathrm{A}}^{*}-P_{\mathrm{A}}$ at this concentration, whereas the observed value was 9.81 as compared with benzene solution at infinite dilution or 11.66 relative to the molecular polarisation of aniline in benzene solution at the same dielectric constant.

As the decrease of molecular polarisation with increasing concentration must be due principally to the solvent effect, and only subsidiarily to the decrease in the degree of association, an approximate correction for the solvent effect has been made by interpolating the values of $P_{\mathrm{A}}{ }^{*}$ in each solvent at a dielectric constant equal to that of benzene. This led to the modified values, $P_{\mathrm{A}_{\infty}}{ }^{*}$ (corr.), shown in the fifth column of Table II. Using these " corrected " values, the plot of $1 / w_{\mathrm{B}} d$ against $1 /\left(P_{\mathrm{A}_{\infty}} *-P_{\Delta_{\infty}}\right)$ leads to $\Delta P=25 \cdot 6$ and $K=116$.

Whilst this treatment can be regarded as only approximate, if $\Delta P=25 \cdot 6$ c.c. the orientation polarisation of the complex is 71.6 c.c. and its dipole moment 1.88 D . This increase as compared with the moment of aniline in benzene seems reasonable if it is due to an increase in the mesomeric moment of aniline caused by the proton displacement towards the dioxan molecule and by a shift of the electrons in the dioxan molecule. This result leads to the inference that at infinite dilution of aniline in pure dioxan about $65 \%$ of the aniline is in the form of the complex.

## Experimental.

The materials were purified by the methods described in Part I, and the same procedures were used for the determination of the dielectric constants, specific volumes, and refractive indices, and for the derivation of the values of $P_{2 \infty}$ and $\mu$. The benzene-dioxan mixtures were made up in batches by weight. and each group of aniline solutions was prepared from the same batch of solvent mixture.

The results are recorded in Table III, where the symbols have the same significance as previously.
Table III.
Polarisation Data for Solutions of Aniline in Benzene-Dioxan Mixtures.

| $100 \%_{2}$. | $\varepsilon_{12}$. | $v_{12}$. | $p_{12}$. | $P_{2}$ 74 wt. | $\begin{gathered} n_{\mathrm{D}} \\ \text { dioxan. } \end{gathered}$ | $r_{12}$. | $\left[R_{\mathrm{D}}\right]$. | $\Delta \varepsilon / w^{\prime}{ }_{2}$. | $\Delta v / w_{2}$. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $0 \cdot 0000$ | $2 \cdot 2689$ | $1 \cdot 12831$ | 0.33538 |  | 1.4920 | $0 \cdot 32733$ |  |  |  |
| $1 \cdot 0641$ | $2 \cdot 3024$ | $1 \cdot 12661$ | $0 \cdot 34104$ | $80 \cdot 77$ | $1 \cdot 4929$ | $0 \cdot 32738$ | $30 \cdot 94$ | $3 \cdot 15$ | -0.160 |
| $1 \cdot 5949$ | $2 \cdot 3190$ | $1 \cdot 12577$ | $0 \cdot 34380$ | $80 \cdot 40$ | $1 \cdot 4935$ | $0 \cdot 32745$ | $31 \cdot 18$ | $3 \cdot 14$ | -0.159 |
| $2 \cdot 3401$ | $2 \cdot 3427$ | 1-12456 | $0 \cdot 34769$ | $80 \cdot 22$ | $1 \cdot 4941$ | 0.32746 | 30.99 | $3 \cdot 154$ | -0.160 |
| 3.7367 | $2 \cdot 3875$ | 1-12233 | $0 \cdot 35492$ | 79.93 | $1 \cdot 4953$ | $0 \cdot 32749$ | $30 \cdot 88$ | 3•174 | -0.160 |
| $5 \cdot 4726$ | $2 \cdot 4436$ | 1-11957 | $0 \cdot 36372$ | $79 \cdot 46$ | $1 \cdot 4969$ | $0 \cdot 32753$ | $30 \cdot 82$ | 3•192 | -0.1597 |
| $6 \cdot 3068$ | $2 \cdot 4713$ | 1-11826 | $0 \cdot 36797$ | $79 \cdot 35$ | $1 \cdot 4977$ | $0 \cdot 32763$ | 30.93 | $3 \cdot 209$ | -0.1594 |
| $7 \cdot 5222$ | $2 \cdot 5114$ | 1-11620 | $0 \cdot 37395$ | 78.98 | $1 \cdot 4987$ | $0 \cdot 32756$ | $30 \cdot 79$ | $3 \cdot 237$ | $-0 \cdot 1610$ |
| 10•1202 | $2 \cdot 5988$ | 1-11221 | $0 \cdot 38667$ | 78.43 | 1-5013 | $0 \cdot 32783$ | $30 \cdot 94$ | $3 \cdot 260$ | $-0.1591$ |
| $15.524 \mathrm{wt} .-\%$ dioxan. |  |  |  |  |  |  |  |  |  |
| $0 \cdot 0000$ | $2 \cdot 2658$ | $1 \cdot 11717$ | 0.33150 | - | $1 \cdot 4877$ | 0.32170 |  |  | - |
| 1•1133 | $2 \cdot 3020$ | 1-11549 | $0 \cdot 33760$ | 81.90 | $1 \cdot 4889$ | $0 \cdot 32191$ | 31.71 | $3 \cdot 25$ | -0.151 |
| 1-6537 | $2 \cdot 3198$ | 1-11467 | 0.34056 | 81.89 | $1 \cdot 4895$ | $0 \cdot 32199$ | 31.59 | 3-26 | -0.151 |
| $2 \cdot 4258$ | $2 \cdot 3453$ | 1-11349 | $0 \cdot 34470$ | 81.54 | $1 \cdot 4902$ | $0 \cdot 32204$ | $31 \cdot 26$ | $3 \cdot 28$ | -0.152 |
| $3 \cdot 3157$ | $2 \cdot 3746$ | 1-11217 | $0 \cdot 34947$ | $81 \cdot 34$ | $1 \cdot 4909$ | $0 \cdot 32205$ | $30 \cdot 95$ | 3.281 | -0.151 |
| $5 \cdot 2919$ | $2 \cdot 4405$ | 1-10918 | $0 \cdot 35982$ | $80 \cdot 71$ | $1 \cdot 4928$ | $0 \cdot 32223$ | $30 \cdot 89$ | 3-301 | -0.1510 |
| $5 \cdot 9930$ | $2 \cdot 4642$ | $1 \cdot 10817$ | $0 \cdot 36347$ | 80.55 | 1.4936 | $0 \cdot 32239$ | 31.03 | 3.311 | $-0.1502$ |
| $7 \cdot 3878$ | $2 \cdot 5116$ | 1-10606 | $0 \cdot 37058$ | $80 \cdot 13$ | $1 \cdot 4948$ | $0 \cdot 32244$ | $30 \cdot 89$ | 3-327 | -0.1504 |
| $8 \cdot 2259$ | $2 \cdot 5403$ | $1 \cdot 10485$ | $0 \cdot 37485$ | 79.95 | $1 \cdot 4955$ | $0 \cdot 32248$ | $30 \cdot 83$ | $3 \cdot 339$ | -0.1498 |
| 49.211 wt .- \% dioxan. |  |  |  |  |  |  |  |  |  |
| $0 \cdot 0000$ | $2 \cdot 2474$ | 1.05909 | 0.31104 | - | $1 \cdot 4629$ | 0.29167 |  |  |  |
| 1-6643 | $2 \cdot 3105$ | 1.05745 | $0 \cdot 32149$ | $87 \cdot 44$ | $1 \cdot 4652$ | $0 \cdot 29246$ | 31.58 | $3 \cdot 79$ | -0.098 |
| $2 \cdot 4221$ | $2 \cdot 3396$ | 1.05669 | $0 \cdot 32619$ | 87.21 | $1 \cdot 4661$ | $0 \cdot 29271$ | $31 \cdot 16$ | $3 \cdot 81$ | -0.099 |
| $3 \cdot 3692$ | 2.3757 | 1.05580 | $0 \cdot 33194$ | 86.73 | $1 \cdot 4672$ | $0 \cdot 29305$ | 30.98 | $3 \cdot 81$ | -0.0976 |
| $4 \cdot 5705$ | $2 \cdot 4219$ | $1 \cdot 05460$ | $0 \cdot 33912$ | $86 \cdot 18$ | $1 \cdot 4686$ | 0.29351 | 30.90 | 3.818 | -0.0982 |
| $5 \cdot 8568$ | $2 \cdot 4716$ | 1.05334 | $0 \cdot 34665$ | 85.59 | $1 \cdot 4703$ | $0 \cdot 29403$ | 30.92 | $3 \cdot 828$ | -0.0982 |
| $7 \cdot 4558$ | $2 \cdot 5343$ | 1.05179 | $0 \cdot 35590$ | 85.00 | 1.4722 | $0 \cdot 29463$ | $30 \cdot 86$ | $3 \cdot 848$ | -0.0979 |
| $8 \cdot 2950$ | $2 \cdot 5667$ | $1 \cdot 05094$ | $0 \cdot 36055$ | 84.55 | 1.4734 | $0 \cdot 29506$ | 30.98 | $3 \cdot 849$ | -0.0982 |
| 9•7794 | $2 \cdot 6241$ | $1 \cdot 04949$ | $0 \cdot 36861$ | 83.79 | $1 \cdot 4754$ | $0 \cdot 29570$ | 31.00 | 3.852 | -0.0982 |

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