

1075. Phosphonitrilic Derivatives. Part IX.¹ The Crystal Structure of Octamethylcyclotetraphosphonitrile.

By MARYON W. DOUGILL.

The X-ray crystal-structure analysis of octamethylcyclotetraphosphonitrile, $[\text{PN}(\text{CH}_3)_2]_4$, shows that four discrete molecules, with $\bar{4}$ symmetry, crystallise in a tetragonal cell, with dimensions $a = b = 15.705$, $c = 6.425$ Å, and space group $I4_1/a$. The crystallographically non-equivalent P-N bond lengths are found, by three-dimensional anisotropic refinement, to be equal (1.591 and 1.601 Å; S.D. 0.003 Å). The average P-C bond length is 1.805 Å (S.D. 0.004 Å) and the ring angles are $119^\circ 48'$ ($\angle \text{NPN}$) and $131^\circ 57'$ ($\angle \text{PNP}$).

THE crystal structures of four phosphonitriles have already been published; three of these are halides² and the fourth is the dimethylamide derivative.³ In each case phosphorus is bonded to an electronegative element and the P-N bond lengths within the ring are short and equal. The actual length depends on the substituent on phosphorus.

The present work was undertaken to provide an accurate structure determination of a simple phosphonitrile containing only light atoms and to observe the structural effect of replacing the strongly electronegative fluorine atom by the isoelectronic methyl group.

There is also interest in the abnormally high melting point of the methyl derivatives;⁴ these are 195° and 163° for the trimer and tetramer respectively, whilst the analogous ethyl tetramer is a liquid at room temperature.⁵

EXPERIMENTAL

Crystals of octamethylcyclotetraphosphonitrile, recrystallised from light petroleum, were kindly prepared by Searle.⁴ Small equant crystals of maximum dimension 0.30 mm. were sealed inside a thin-walled glass capillary tube, to prevent hydration.

The photographs were taken at 140°K , by cooling the crystals in a stream of cold, dry nitrogen, in the apparatus described by Robertson.⁶ The cell dimensions were obtained from oscillation photographs in the Straumanis position. Multiple-film, equi-inclination Weissenberg photographs of the a and c axes were recorded for the layers $0kl$ to $10kl$ and $hk0$ to $hk4$. A total of 817 of the possible 886 reflections gave measurable intensities; these were estimated visually by comparison with a calibration strip. Lorentz polarisation factors were calculated and applied on the Leeds University Pegasus computer by a method devised by Dr. F. M. Lovell. No correction was made for absorption.

The three-dimensional refinement was carried out on the Leeds University Pegasus⁷ computer by the method of least squares, using the SFSL programme. The scattering factor used for phosphorus was that of Tommie and Stam,⁸ and for carbon, nitrogen, and hydrogen those of Berghuis *et al.*⁹ were used; $1/F_0$ was used throughout as the weighting factor.⁷ Calculation of the molecular dimensions and analysis of the thermal motion were carried out on the Pegasus computer.⁷

Crystal Data.— $[\text{PN}(\text{CH}_3)_2]_4$, $M = 300.2$, m. p. 163° , tetragonal prisms, $a = b = 15.705 \pm 0.010$, $c = 6.425 \pm 0.005$ Å, $U = 1584.7$ Å³, $D_m = 1.19$ g./c.c. (measured by flotation in a liquid in which the crystals are slightly soluble), $Z = 4$, $D_c = 1.258$ g./c.c., $F(000) = 640$. Space group $I4_1/a$ (C_{4h}^2 , No. 88), origin at $\bar{1}$, molecular symmetry $\bar{4}$, Cu- K_α radiation, $\mu = 39.4$ cm.⁻¹.

¹ Part VIII, Chapman and Paddock, *J.*, in the press.

² (a) Ketelaar and de Vries, *Rev. Trav. chim.*, 1939, **58**, 1081; (b) Wilson and Carroll, *J.*, 1960, 2548; (c) McGeachin and Tromans, *J.*, 1961, 4777.

³ Bullen, *Proc. Chem. Soc.*, 1960, 425.

⁴ Searle, *Proc. Chem. Soc.*, 1959, 7.

⁵ Bilbo, *Z. Naturforsch.*, 1960, **15b**, 330.

⁶ Robertson, *J. Sci. Instr.*, 1960, **37**, 41.

⁷ Cruickshank, Pilling, Bujosa, Lovell, and Truter, "Symposium on Computer Methods," Pergamon Press Ltd., London, 1961.

⁸ Tommie and Stam, *Acta Cryst.*, 1958, **11**, 126.

⁹ Berghuis, Haanappel, Potters, Loopstra, MacGillavry, and Veenendall, *Acta Cryst.*, 1955, **8**, 478.

TABLE 1. (Continued.)

	$ F_o $	F_c		$ F_o $	F_c		$ F_o $	F_c		$ F_o $	F_c		$ F_o $	F_c		$ F_o $	F_c				
	13,11, <i>l</i>			14,6, <i>l</i>			15,2, <i>l</i>			15,10, <i>l</i>			16,8, <i>l</i>			17,5, <i>l</i>			18,5, <i>l</i>		
2	266	235	0	279	286	1	70	40	1	336	-316	0	295	299	2	255	239	1	44	44	
4	187	200	2	85	75	3	231	-247	3	370	344	2	94	-84	4	44	-53	3	32	-28	
			4	83	-77		5	82	77												
	13,12, <i>l</i>			14,7, <i>l</i>			15,3, <i>l</i>			15,11, <i>l</i>			16,9, <i>l</i>			17,6, <i>l</i>			18,6, <i>l</i>		
1	78	77		209	211		430	-444	2	316	296	1	221	-220	1	72	-70	0	196	-176	
			1	203	-229		198	174		15,12, <i>l</i>			146	-145	3	265	-267	2	164	-172	
	13,13, <i>l</i>																				
2	181	187		14,8, <i>l</i>					1	97	94		16,10, <i>l</i>			17,8, <i>l</i>			18,7, <i>l</i>		
				532	545		346	-358					0	284	-243	1	148	148	1	46	-36
	13,14, <i>l</i>			125	-121		353	327	3	187	-176		2	104	109	3	49	62		18,8, <i>l</i>	
1	313	322	2	222	-206	3	109	139	5										0	42	31
			4																		
	14,1, <i>l</i>			14,9, <i>l</i>			15,5, <i>l</i>			16,2, <i>l</i>			16,11, <i>l</i>			17,9, <i>l</i>					
1	276	272	1	454	-498		330	336	4	54	18	1	190	204	2	32	-28		19,1, <i>l</i>		
3	348	-343	3	202	-194	2	44	40	4	38	-31	2							2	88	-93
5	193	-179	3							4	96	-86				16,12, <i>l</i>			17,10, <i>l</i>		
													0	102	99	1	108	111	1	150	165
	14,2, <i>l</i>			14,10, <i>l</i>			15,6, <i>l</i>			16,3, <i>l</i>						17,1, <i>l</i>			18,1, <i>l</i>		
0	325	291	0	632	-682		227	237	3	242	-251		2	165	-150	1	219	-221		19,3, <i>l</i>	
2	257	-264	2	50	25		102	-90	3	306	-261		4	142	139	3	121	116	2	28	29
4	73	70	4	287	308																
										16,4, <i>l</i>											
	14,3, <i>l</i>			14,11, <i>l</i>			15,7, <i>l</i>		0	508	-516					17,2, <i>l</i>			18,2, <i>l</i>		
1	349	-354	1	178	204		112	112	2	64	64		1	160	180	0	80	73	1	50	-42
3	76	-68	3	176	164		104	-103	4	414	431		3	153	123	2	357	359			
5	291	240																			
				14,12, <i>l</i>						16,5, <i>l</i>						17,3, <i>l</i>			18,3, <i>l</i>		
	14,4, <i>l</i>			134	111		180	198	1	301	335		2	297	-271	1	70	68		19,5, <i>l</i>	
0	384	-398					313	-285	3	255	228		4	171	-171	3	215	-220	2	86	-121
2	115	-116		14,14, <i>l</i>																	
4	250	225	0	320	292					16,6, <i>l</i>						17,4, <i>l</i>			18,4, <i>l</i>		
										0	345	303									
1	213	209	2	99	101	2	403	-385	2	86	-85	1	228	-259	0	196	-162		20,2, <i>l</i>		
3	238	253	4	300	-273	4	57	53	4	271	-222	3	294	279	2	44	-49	0	158	135	

TABLE 2.

Atomic co-ordinates in Å (σ is the standard deviation in Å).

	x	$\sigma(x)$	y	$\sigma(y)$	z	$\sigma(z)$
P	1.7646	0.0006	2.9019	0.0006	1.0113	0.0008
N	0.541	0.002	2.212	0.003	0.264	0.003
C ₁	3.200	0.003	2.528	0.004	-0.011	0.004
C ₂	2.140	0.004	2.122	0.004	2.599	0.004
H ₁	4.07	0.04	2.92	0.04	0.49	0.04
H ₂	3.07	0.04	3.12	0.05	-0.97	0.05
H ₃	3.27	0.04	1.60	0.04	-0.19	0.05
H ₄	3.05	0.05	2.47	0.05	3.00	0.05
H ₅	1.35	0.05	2.23	0.05	3.35	0.06
H ₆	2.32	0.05	1.07	0.05	2.48	0.06

TABLE 3.

Thermal parameters (units in 10^{-4} Å²).

	U_{11}	σ	U_{22}	σ	U_{33}	σ	U_{12}	σ	U_{13}	σ	U_{23}	σ
P	199	3	193	3	294	4	7	4	-23	5	-67	5
N	191	10	285	12	385	14	23	18	-195	21	-27	20
C ₁	234	12	438	18	473	18	6	24	-247	30	-6	26
C ₂	513	20	324	16	407	17	10	28	136	28	-229	28
	U	σ			U	σ			U			
H ₁	157	99	H ₃		170	105	H ₅		375	142		
H ₂	343	135	H ₄		337	144	H ₆		348	142		

TABLE 4.

Magnitude and direction of the principal axes of the ellipsoids of thermal motion with respect to the crystallographic axes. (l , m , and n are direction cosines.)

	Å ²	l	m	n		Å ²	l	m	n
P	0.0188	-0.951	-0.041	-0.306	C ₁	0.0234	-1.000	+0.010	-0.007
	0.0306	-0.301	-0.196	+0.948		0.0580	-0.012	-0.656	+0.755
	0.0192	-0.072	+0.994	+0.088		0.0331	+0.003	+0.755	+0.656
	0.0190	-0.995	+0.101	-0.018		0.0271	+0.270	-0.751	+0.603
N	0.0446	-0.069	-0.521	+0.851	C ₂	0.0593	-0.814	+0.157	+0.559
	0.0226	+0.077	+0.848	+0.525		0.0380	+0.514	+0.642	+0.569

STRUCTURE DETERMINATION

The position of the phosphorus atom was found from the Patterson synthesis projected down $[c]$. Fourier methods were used to locate the positions of the nitrogen and the carbon atoms; these four atoms (and six hydrogen atoms) in the 16-fold general positions are sufficient to define the structure. Two-dimensional refinement, by alternate structure-factor and difference Fourier calculations, was discontinued at $R(hk0) = 0.16$.

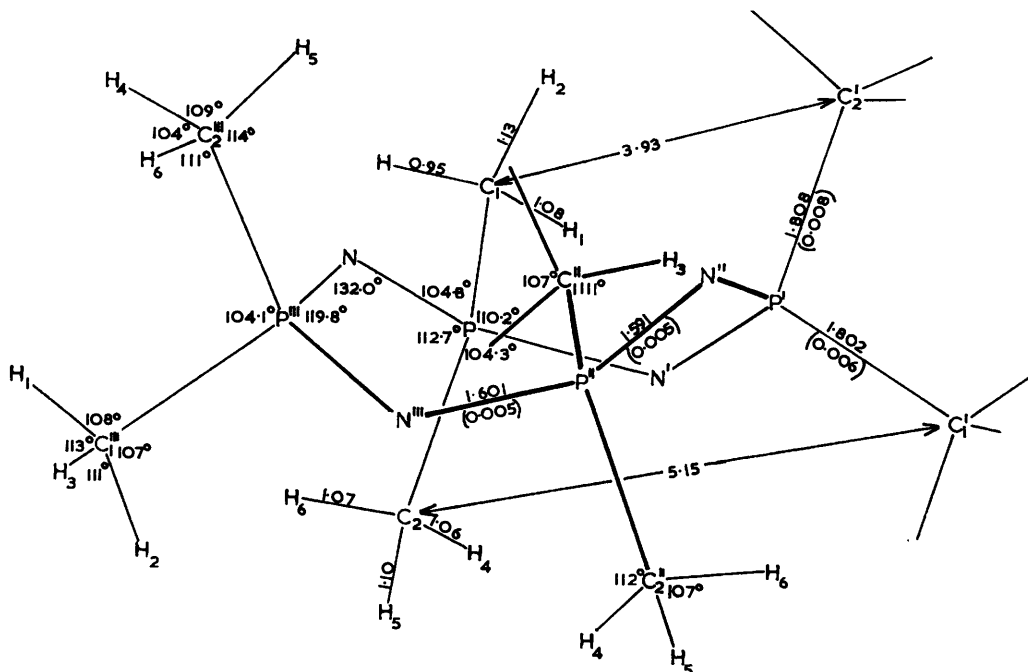


FIG. 1. The bond lengths (Å) and angles in the $[\text{PN}(\text{CH}_3)_2]_4$ molecule. The sum of the standard deviation and thermal motion correction is shown in Å in parentheses; for the angles at the phosphorus atom this value is 0.2° and 0.3° for the angle NPN' .¹⁰

The z -co-ordinate of the phosphorus atom was obtained from the $0kl$ Patterson synthesis. The x , y , and z parameters were refined simultaneously in this projection to $R(0kl) = 0.13$. Individual isotropic temperature factors were applied in the last two calculations.

TABLE 5.

Magnitudes and directions of the principal axes of translational and oscillational ellipsoids.

\AA^2	l	m	n	θ	l	m	n
0.0188	+0.5209	-0.8536	-0.0014	1.50°	+0.0003	+0.0001	+1.0000
0.0197	-0.0014	-0.0006	+1.0000	2.97°	-0.8599	-0.5105	+0.0003
0.0188	+0.8763	+0.4818	+0.0010	2.79°	-0.5105	+0.8599	+0.0000

Corrections to the atomic co-ordinates due to the thermal motion (Å).

	x	y	z		x	y	z
P	+0.0027	-0.0017	+0.0005	C_1	+0.0044	-0.0021	-0.0018
N	+0.0009	-0.0027	-0.0013	C_2	+0.0030	-0.0027	+0.0040

The initial cycle of three-dimensional refinement was computed with isotropic temperature factors, individual anisotropic temperature factors being used thereafter. During five cycles of refinement, R decreased from 0.262 to 0.077. Examination of the low-order reflections revealed that extinction alone could not account for the discrepancy between the observed and

¹⁰ Darlow, *Acta Cryst.*, 1960, **13**, 683.

the calculated structure factors. The contributions of the six hydrogen atoms were consequently included. The hydrogen atoms were placed in the staggered orientation with respect to the other ligands on the phosphorus atom, and the co-ordinates were chosen to make the C-H bond length equal to 1.09 Å. An isotropic temperature factor corresponding to a mean-square amplitude of vibration of 0.06 Å² was used. After three further cycles, in which all the atoms were allowed to move, a final *R* of 0.057 was obtained (observed reflections only). The refinement was judged to be complete when the shifts in the atoms, excluding hydrogen

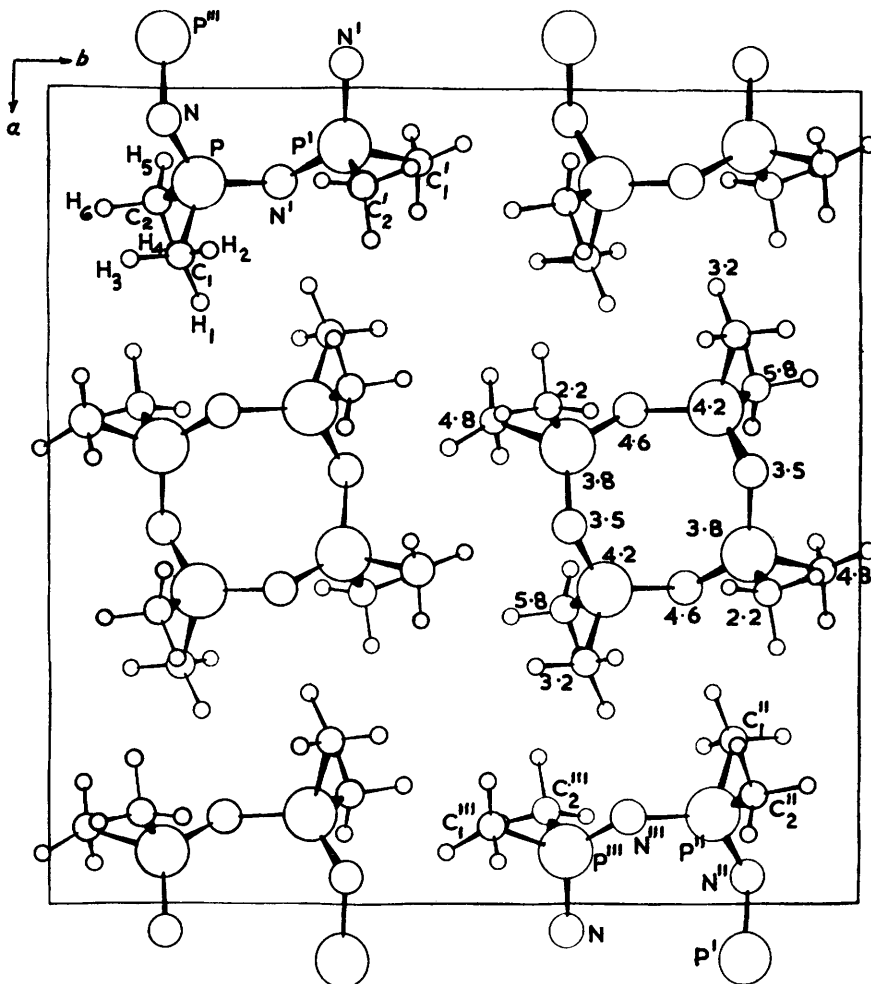
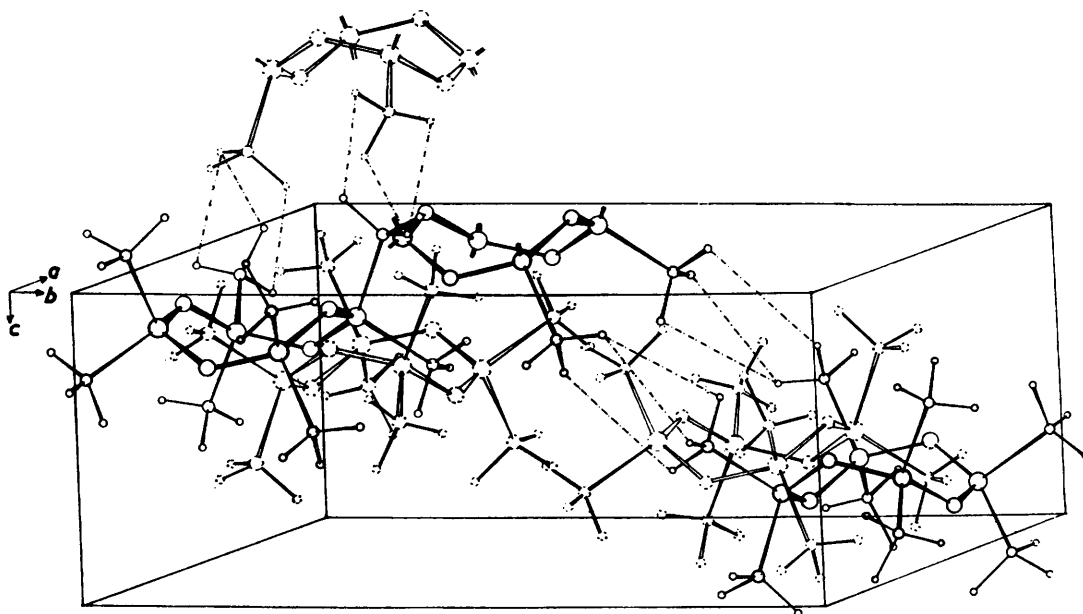


FIG. 2. Projection of the structure down the *c* axis. The heights of the atoms are in Å.

atoms, were less than one-third of their estimated standard deviation. The validity of the hydrogen atom co-ordinates is indicated by the decrease of their thermal motion during the refinement (Table 3).

Results.—A list of observed and calculated structure factors for the observed reflections is given in Table 1. The final atomic co-ordinates with their standard deviations are given in Table 2; co-ordinates with four places of decimals were used to calculate the bond lengths and angles given in Fig. 1. The low values found for the standard deviations are partly due to the small thermal motion observed at this temperature.

Table 3 shows the parameters of anisotropic thermal motion for the four heavy atoms, and the isotropic thermal motion for the hydrogen atoms. The U_{ij} values, which give the magnitudes and orientation of the vibration ellipsoids with respect to the crystallographic axes, were used to calculate the principal axes of the vibration ellipsoids for each atom and their direction cosines with respect to the tetragonal axes (Table 4).¹¹ The direction of the maximum amplitude of vibration for the phosphorus atom almost coincides with the normal to the plane containing the phosphorus atom and the two adjacent nitrogen atoms. No simple correlation can be found relating a molecular axis with the ellipsoid of vibration for the nitrogen atom. The assumption was made that the molecule behaves as a rigid body in order that the anisotropic thermal parameters could be analysed into translational and oscillational



○ P ○ N ○ C ○ H

FIG. 3. A clinographic drawing of the structure. Molecules are shown whose centres are at $0, \frac{1}{4}, \frac{3}{8}$; $1, \frac{1}{4}, \frac{1}{8}$; $1, \frac{3}{4}, \frac{7}{8}$ (drawn with solid lines), and $\frac{1}{2}, \frac{1}{4}, \frac{3}{8}$; $\frac{1}{2}, \frac{1}{4}, -\frac{5}{8}$; $\frac{1}{2}, \frac{3}{4}, \frac{5}{8}$ (drawn with open bonds and dotted circles). Chain lines show the short H...H distances between interlocking methyl groups.

motion.¹² The results are given in Table 5, which also includes the corrections to the co-ordinates due to the rotational oscillations. The effects of these corrections¹³ on the bond lengths and angles are very small (0.003 Å and less than 0.1°), because the intensity data were recorded at 140° K; they are not exact since the agreement between the observed and the calculated values of U_{ij} indicate some internal vibrations. Since the corrections increase the uncertainty of the molecular dimensions they have been added to the standard deviations; the sum is shown in Fig. 1.

Description of the Structure.—The structure is composed of discrete molecules of $[\text{PN}(\text{CH}_3)_2]_4$, forming puckered eight-membered rings whose mean planes are parallel to the ab plane and related to each other by glide planes (Figs. 2 and 3). The ring consists of alternate phosphorus and nitrogen atoms related by $\bar{4}$ symmetry. The departure of the ring from planarity may be assessed by the difference in z co-ordinates of adjacent phosphorus (0.42 Å) and nitrogen atoms (1.08 Å).

¹¹ Cruickshank, *Acta Cryst.*, 1956, **9**, 747.

¹² Cruickshank, *Acta Cryst.*, 1956, **9**, 754.

¹³ Cruickshank, *Acta Cryst.*, 1956, **9**, 757.

The molecular dimensions are shown in Fig. 1. The difference of 0.009_6 \AA between the two P-N bond lengths (1.591_1 and 1.600_7 \AA) is not significant;¹⁴

$$\begin{aligned} \sigma^2(\Delta 1) = & \\ & \sigma^2(\text{P}) + \sigma^2(\text{N}) - \sigma^2(\text{P}) \cos \angle \text{NPN} - \sigma^2(\text{N}) \cos \angle \text{PNP} \text{ in the direction P-N} + \\ & \sigma^2(\text{P}) + \sigma^2(\text{N}) - \sigma^2(\text{P}) \cos \angle \text{NPN} - \sigma^2(\text{N}) \cos \angle \text{PNP} \text{ in the direction P'-N} = \\ & 0.0049 \text{ \AA} \end{aligned}$$

The P-C bond lengths (1.808_2 and 1.801_3 \AA) are not significantly different; $\sigma(\Delta 1) = 0.0055 \text{ \AA}$.

Although the bisectors of the angles NPN' and C_1PC_2 are almost collinear, the dihedral angle between the plane containing NPN' and C_1PC_2 is $94^\circ 46'$.

Intermolecular distances are found to be greater than the sum of the van der Waals radii of the methyl groups (4.0 \AA) with the exception of $\text{C}_1xyz \dots \text{C}_2(\frac{1}{2} + y, \frac{1}{2} - x, -\frac{1}{2} + z)$, which is 3.68 \AA .

DISCUSSION

The molecular geometry is unlikely to be greatly affected by van der Waals forces between molecules. Even within the molecule, distances between carbon atoms belonging to different phosphorus atoms can be varied without change of the ring angles at phosphorus and nitrogen. The distance $\text{C}_1\text{-C}_2'$ (3.93 \AA), although only slightly altered by twisting a model of the molecule, may be increased to a value greater than 4 \AA . This distance would be less than 3.9 \AA if the angle PNP were only 120° ; presumably compensation could be achieved by a more puckered ring and greater $\text{C}_1\text{PN}'$ and C_2PN angles. It is thought, therefore, that in such a flexible molecule the angles in the ring are not controlled by van der Waals forces within the molecule.

The two P-N bond lengths (1.591 and 1.601 \AA) are equal within experimental error, and are appreciably shorter than the sum of the single covalent radii¹⁵ (1.76 \AA), the value found in sodium phosphoramidate¹⁶ (Table 6). The average P-N bond length is close to that in the trimeric phosphonitrilic chloride (Wilson *et al.*²) and to that quoted by Bullen³

TABLE 6.

Bond lengths of P-N and P-C in other structures (Å).							
P-N	σ		Ref.	P-C	σ	Ref.	
1.76	0.02	NaH_3NPO_3	16	1.837	0.007	$[\text{H}_2\text{BP}(\text{CH}_3)_2]_3$	<i>b</i>
1.653	0.005	$(\text{NH}_2)_3\text{PBH}_3$	<i>a</i>	1.82, 1.84	0.015	$[(\text{C}_2\text{H}_5)_2\text{PS}]_2$	<i>c</i>
1.66, 1.69		$(\text{PNCI}_2)_4$	<i>2a</i>	1.82, 1.88		$[\text{C}_2\text{H}_5(\text{CH}_3)\text{PS}]_2$	<i>d</i>
1.57, 1.60, 1.61	0.017	$(\text{PNCI}_2)_3$	<i>2b</i>	1.813		$(\text{CH}_3)_2\text{PO}$	<i>e</i>
1.59 cyclic		$\{\text{PN}[\text{N}(\text{CH}_3)_2]_2\}$	3	1.87	0.02	$\text{P}(\text{CH}_3)_3$	<i>f</i>
1.75, 1.84 exocyclic				1.937	0.017	$\text{P}(\text{CF}_3)_3$	<i>g</i>
1.49, 1.51, 1.52	0.02	$(\text{PNF}_2)_4$	<i>2c</i>	1.906	0.02	$\text{P}(\text{CF}_3)_5$	<i>h</i>

References: (a) Nordman, *Acta Cryst.*, 1960, **13**, 535. (b) Hamilton, *Acta Cryst.*, 1955, **8**, 199. (c) Dutta and Wolfson, *Acta Cryst.*, 1961, **14**, 178. (d) Wheatley, *J.*, 1960, 523. (e) Wang, Forsvaretsforskningsinstitut (Norway) Intern. Rapport IR-K-225 (1960). (f) Springall and Brockway, *J. Amer. Chem. Soc.*, 1938, **60**, 996. (g) Bowen, *Trans. Faraday Soc.*, 1954, **50**, 463. (h) Spencer and Lipscomb, *Acta Cryst.*, 1961, **14**, 250.

in his preliminary report on the structure of octakisdimethylamidotetraphosphonitrile. The length indicates partial double-bond character, as expected theoretically,¹⁷ though the amount is presumably less than in the tetrameric fluoride (McGeachin *et al.*²), which has a shorter P-N bond. The P-C bond is a little shorter than the sum of the covalent radii¹⁵ and is close to those reported for other organic compounds of quinquivalent phosphorus (Table 7).

The angle at the nitrogen atom in the present structure (132°) is greater than the 120° expected on the simplest basis, though the difference is less than for the fluoride. Such

¹⁴ Cruickshank and Robertson, *Acta Cryst.*, 1953, **6**, 698.

¹⁵ Pauling, "Nature of the Chemical Bond," Cornell University Press, 3rd edn., pp. 224, 229.

¹⁶ Hobbs, Corbridge, and Raistrick, *Acta Cryst.*, 1953, **6**, 621; Cruickshank, unpublished work.

¹⁷ Craig and Paddock, *Nature*, 1958, **181**, 1052; Craig, *J.*, 1959, 997; Dewar, Lucken, and Whitehead, *J.*, 1960, 2423.

an effect is common where chains and rings are formed from alternate first- and second-row elements, notably in octamethylcyclotetrasiloxane¹⁸ (Si-O-Si = 143°), in octamethylcyclotetrasilazane¹⁹ (Si-N-Si = 123°), and in ammonium²⁰ and sodium tetrametaphosphate²¹ (P-O-P = 131° and 133°). The ring angle at phosphorus is almost the same in the octamethylcyclotetraphosphonitrile as in other tetrameric phosphonitriles. The exocyclic C-P-C angle is 104°; it is greater than the F-P-F angle in the fluoride (100°) because of the lower electronegativity of the methyl group.²²

There is no indication of hydrogen bonding in the structure; all intermolecular C-N distances are greater than 3.59 Å, the sum of the van der Waals radii for the methyl group and nitrogen atom being 3.50 Å. However, a P-C bond of one molecule is directed towards a carbon atom on another to give the distance 3.68 Å; as a result two hydrogen atoms of $C_2(\frac{1}{4} + y, \frac{1}{4} - x, -\frac{3}{4} + z)$ fall in the spaces between the three hydrogen atoms on $C_1(x, y, z)$. Such interlocking of methyl groups has also been observed for sodium hydrogen diacetate,²³ and, aided by the high molecular symmetry, may account in part for the high melting point of the phosphonitrile.

It is a pleasure to thank Dr. M. R. Truter for her valuable advice and Dr. D. W. J. Cruickshank and Mr. N. L. Paddock for helpful discussion. I am grateful to the Directors and staff of the Computing Laboratory for carrying out the computations, to Albright and Wilson (Mfg.) Ltd. for financial support and to the Imperial Chemical Industries Limited for the loan of some of the equipment.

DEPARTMENT OF INORGANIC & STRUCTURAL CHEMISTRY,
THE UNIVERSITY, LEEDS, 2.

[Seconded from ALBRIGHT & WILSON (MFG.) LTD.]

[Received, July 11th, 1961.]

¹⁸ Steinfink, Post, and Fankuchen, *Acta Cryst.*, 1955, **8**, 420.

¹⁹ Yokoi and Yamasaki, *J. Amer. Chem. Soc.*, 1953, **75**, 4139.

²⁰ Romers, Ketelaar, and MacGillavry, *Acta Cryst.*, 1951, **4**, 114; Cruickshank, unpublished work.

²¹ Ondik, Block, and MacGillavry, *Acta Cryst.*, 1961, **14**, 555.

²² Linnett and Mellish, *Trans. Faraday Soc.*, 1954, **50**, 657.

²³ Speakman and Mills, *J.*, 1961, 1164.