

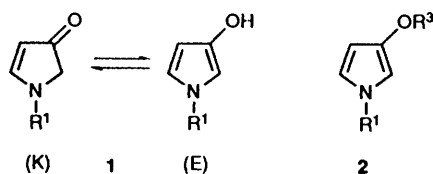
3-Hydroxypyrroles and 1*H*-Pyrrol-3(2*H*)-ones. Part 11.¹ ¹H and ¹³C NMR Spectra of 1-Substituted and 1,2-Disubstituted 3-Hydroxy- and 3-Alkoxy-pyrroles

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The ¹H and ¹³C NMR parameters of a range of 1-substituted and 1,2-disubstituted 3-hydroxy- and 3-alkoxy-pyrroles are reported. Typical values for 1-*tert*-butyl-3-hydroxypyrrole (*J* values in Hz) are: δ_{H} 5.50 (³*J*_{4,5} 2.9, ⁴*J*_{2,4} 2.0, 4-H), 6.26 (⁴*J*_{2,4} 2.0 and ⁴*J*_{2,5} 2.6, 2-H) and 6.49 (³*J*_{4,5} 2.9 and ⁴*J*_{2,5} 2.6, 5-H); δ_{C} 97.60 (¹*J*_{4-H} 167.9, ²*J*_{5-H} and ³*J*_{2-H} 6.8, C-4), 101.16 (¹*J*_{2-H} 182.7, ³*J*_{4-H} and ³*J*_{5-H} 4.3, C-2), 114.18 (¹*J*_{5-H} 182.5, ²*J*_{4-H} and ³*J*_{2-H} 6.9, C-5) and 143.37 (²*J*_{2-H} 4.3, ³*J*_{5-H} 9.0, C-3).

In earlier parts of this series, we have shown that polar, hydrogen-bond acceptor solvents such as dimethyl sulfoxide (DMSO) substantially favour the enol form **1E** of the 1*H*-pyrrol-3(2*H*)-one-3-hydroxypyrrole equilibrium,² and that the

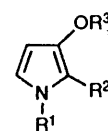


system can be regioselectively *O*-alkylated to give a good synthesis of 3-alkoxypyrroles, **2**.¹ In this paper, we report a detailed study of the ¹H and ¹³C NMR spectra of simple 1-substituted and 1,2-disubstituted 3-hydroxy- and 3-alkoxy-pyrroles, all of which clearly share common structural features. This work complements our earlier report of the NMR spectra of the 1*H*-pyrrol-3(2*H*)-one system, **1K**.³

The 3-hydroxypyrroles **3**, **6**, **10**, **12**, **14** and **16** were prepared as their 1*H*-pyrrol-3(2*H*)-one tautomers by flash vacuum pyrolysis of appropriate aminomethylene Meldrum's acid derivatives,⁴ and the enol forms were generated by solution in [²H₆]DMSO. The corresponding 3-alkoxypyrroles **4**, **5**, **7-9**, **11**, **13**, **15** and **17** were made as described in part 10,¹ and their spectra were normally recorded using [²H]chloroform as the solvent. The range of compounds studied was selected to include 1-alkyl-3-hydroxy- and alkoxy-pyrroles (**3-5**), and 1-aryl derivatives (**6-9**), together with 1,2-dialkyl (**10-11**), 1-alkyl-2-aryl (**12-13**), 1-aryl-2-alkyl (**14-15**), and 1,2-diaryl (**16-17**) compounds.

Results and Discussion

¹H NMR Spectra.—The ¹H NMR parameters of the ring protons of the pyrroles **3-17** are given in Table 1. The assignment of chemical shifts as $\delta_{5\text{-H}} > \delta_{2\text{-H}} > \delta_{4\text{-H}}$ follows intuitively, since the α -protons of pyrroles are usually deshielded relative to the β -protons,⁵ and the conjugative electron-donating effect of the hydroxy- or alkoxy-substituent would be expected to affect only the 2-position. A number of experiments have confirmed these assignments. Thus the spectrum of the [2-¹³C]-labelled 3-hydroxy-2-phenylpyrrole (**6**)⁶ provides unambiguous confirmation of $\delta_{2\text{-H}}$, and a nuclear Overhauser effect (NOE) experiment on the corresponding 3-methoxy compound **7** has established the relationship between 4-H and 5-H, since irradiation at $\delta_{\text{H}} = 6.14$ gives a significant enhancement at $\delta_{\text{H}} = 6.95$. In addition, a spectrum of [2,4-²H₂]-1-*tert*-butyl-3-hydroxypyrrole (**3**)³ showed the remaining



	R ¹	R ²	R ³
3	Bu ^t	H	H
4	Bu ^t	H	Me
5	Bu ^t	H	Et
6	Ph	H	H
7	Ph	H	Me
8	Ph	H	Et
9	Ph	H	Pr ⁱ
10	Et	Me	H
11	Et	Me	Me
12	Me	Ph	H
13	Me	Ph	Me
14	Ph	Me	H
15	Ph	Me	Me
16	Ph	Ph	H
17	Ph	Ph	Me

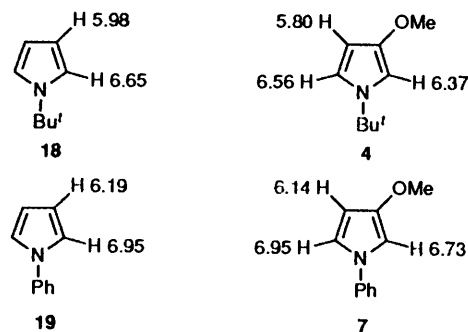


Fig. 1 A comparison of ¹H NMR chemical shifts δ_{H} of the pyrroles **18** and **19**⁷ and the methoxypyrroles **4** and **7**

ring proton signal at $\delta_{\text{H}} = 6.48$, which is fully consistent with the above findings. The relative positions of the 2-, 4- and 5-proton resonances of the 3-hydroxy- and 3-alkoxy-pyrroles are independent of the nature of the 1-, 3- (and, where appropriate 2-) substituent (Table 1), as confirmed by the close similarity in the sizes of the 3- and 4-bond coupling constants (see below) for the various derivatives.

As expected, the incorporation of a 3-methoxy substituent into the pyrrole ring has little effect on $\delta_{4\text{-H}}$ and $\delta_{5\text{-H}}$, but the chemical shift of 2-H is shifted to low frequency (Fig. 1). *N*-Aryl groups have a general deshielding effect on the pyrrole

Table 1 ^1H NMR chemical shifts^a and coupling constants^b of 3-hydroxypyrroles and 3-alkoxypyrroles

Compound	R ¹	R ²	R ³	2-H	4-H	5-H	³ J _{4,5}	⁴ J _{2,4}	⁴ J _{2,5}
3 ^c	Bu'	H	H	6.26	5.50	6.49	2.9	2.0	2.6
4 ^d	Bu'	H	Me	6.37	5.80	6.56	3.0	2.0	2.7
5 ^d	Bu'	H	Et	6.36	5.78	6.54	3.0	2.0	2.6
6 ^c	Ph	H	H	6.74	5.85	7.06	3.1	1.9	2.6
7 ^d	Ph	H	Me	6.73	6.14	6.95	3.1	2.0	2.5
7 ^c	Ph	H	Me	7.19	6.00	7.00	—	—	—
8 ^d	Ph	H	Et	6.68	6.08	6.90	3.1	1.9	2.5
9 ^d	Ph	H	Pr ⁱ	6.67	6.05	6.88	3.1	2.0	2.5
10 ^c	Et	Me	H	—	5.52	6.30	3.0	—	—
11 ^d	Et	Me	Me	—	5.86	6.37	3.2	—	—
12 ^c	Me	Ph	H	—	5.72	6.51	2.8	—	—
13 ^d	Me	Ph	Me	—	6.07	6.55	3.0	—	—
14 ^c	Ph	Me	H	—	5.78	6.56	3.0	—	—
15 ^d	Ph	Me	Me	—	6.18	6.68	3.2	—	—
16 ^c	Ph	Ph	H	—	5.97	6.78	3.1	—	—
17 ^d	Ph	Ph	Me	—	6.19	6.73	3.2	—	—

^a ppm. ^b Hz. ^c [²H₆]DMSO solution. ^d [²H]chloroform solution.

Table 2 ^{13}C NMR parameters^a for the ring carbon atoms of 3-hydroxypyrroles^b and 3-alkoxypyrroles^c

Compound	C-2			C-3			C-4			C-5					
	R ¹	R ²	R ³	δ_{C}	¹ J _{2-H}	³ J _{4-H} = ³ J _{5-H}	δ_{C}	² J _{2-H}	³ J _{5-H}	δ_{C}	¹ J _{4-H}	² J _{5-H} = ³ J _{2-H}	δ_{C}	¹ J _{5-H}	² J _{4-H} = ³ J _{2-H}
3	Bu'	H	H	101.16	182.7	4.3	143.37	4.3	9.0	97.60	167.9	6.8	114.18	182.5	6.9
4	Bu'	H	Me	99.76	182.3	4.6	148.36	<i>d</i>	<i>d</i>	95.80	170.9	6.9	115.04	183.3	6.7
5	Bu'	H	Et	100.53	182.8	4.3	147.29	<i>d</i>	<i>d</i>	96.45	170.3	7.0	114.79	183.0	6.8
6	Ph	H	H	101.54	185.8	4.1	146.07	3.8	9.8	102.18	170.9	7.0	115.96	186.5	6.6
7	Ph	H	Me	100.86	185.7	3.9	150.83	<i>d</i>	<i>d</i>	100.32	172.5	7.0	116.99	186.0	6.6
8	Ph	H	Et	101.49	185.8	4.2	149.61	<i>d</i>	<i>d</i>	100.78	172.0	7.0	116.84	186.2	6.4
9	Ph	H	Pr ⁱ	102.98	185.7	4.2	147.79	<i>d</i>	<i>d</i>	101.57	172.5	7.1	116.62	185.7	6.3
10	Et	Me	H	109.94	—	<i>d</i>	139.40	—	9.3 ^e	97.69	168.1	7.5	114.19	182.7	7.7 ^f
11	Et	Me	Me	112.10	—	—	144.05	—	—	95.18	—	—	114.37	—	—
12	Me	Ph	H	116.50	—	<i>d</i>	141.62	—	7.8	98.11	170.0	7.8	120.29	184.3	6.9 ^g
13	Me	Ph	Me	118.44	—	<i>d</i>	145.48	—	<i>d</i>	95.52	170.4	7.9	119.53	186.8	<i>d</i>
14	Ph	Me	H	110.47	—	<i>d</i>	141.40	—	<i>d</i>	100.45	170.8	6.5	116.41	186.2	7.3
15	Ph	Me	Me	112.93	—	<i>d</i>	145.42	—	<i>d</i>	97.21	170.8	7.7	116.75	185.7	6.8
16	Ph	Ph	H	115.04	—	<i>d</i>	143.96	—	9.4	101.08	171.5	7.5	121.46	188.0	7.5
17	Ph	Ph	Me	116.91	—	<i>d</i>	146.93	—	<i>d</i>	97.29	171.9	7.6	120.43	187.4	6.7

^a Coupling constants are quoted in Hz. ^b [²H₆]DMSO solution. ^c [²H]Chloroform solution. ^d Complicated by further coupling. ^e ³J_{2-Me} = 4.0 Hz. ^f ³J_{N-CH₂} = 4.1 Hz. ^g ³J_{N-Me} = 3.5 Hz.

ring proton resonances, due to competitive delocalisation of the nitrogen atom's lone pair (4-H) and/or ring current effects (2- and 5-H) (Table 1 and Fig. 1).

A comparison of the data in Table 1 shows that variation of the alkoxy substituent produces little significant difference in the ^1H NMR parameters of the ring protons (*cf.* 4, 5 and 7–9). The apparent influence of the hydroxy or alkoxy substituent on $\delta_{2\text{-H}}$ and $\delta_{4\text{-H}}$ may be due in part to the change in solvent (*cf.* spectrum of 7 in [²H]chloroform and [²H₆]DMSO, (Table 1)): hydrogen bonding between [²H₆]DMSO and the 3-hydroxy group is known to be important.²

In the *N*-aryl series, a 2-alkyl or 2-aryl substituent causes shielding at the 5-position, but leaves $\delta_{4\text{-H}}$ almost unaffected (Table 1, *cf.* 6, 14, 16 and 7, 15 and 17). The effect is much less regular in the *N*-alkyl series (Table 1), but this may be due to the variation in *N*-alkyl substituent.

For the 2-unsubstituted compounds, 3- and 4-bond coupling constants (³J_{4,5}, ⁴J_{2,4} and ⁴J_{2,5}) were observed in all cases (Table 1) and are expressed in Hz. The relative magnitudes [³J_{4,5} (3.0 ± 0.2) > ⁴J_{2,5} (2.6 ± 0.1) > ⁴J_{2,4} (2.0 ± 0.1)] provided independent confirmation of the consistency of the chemical shift assignments (see above), and are in reasonable agreement with data for other 1,3-disubstituted pyrroles (*e.g.* 1-benzyl-3-nitropyrrole,⁸ ³J_{4,5} 3.2, ⁴J_{2,5} 2.5, ⁴J_{2,4} 1.9). 2-Substituted 3-

alkoxy- and 3-hydroxypyrroles show a value of ³J_{4,5} in line with the above (Table 1).

^{13}C NMR Spectra.—The ^{13}C NMR parameters for the ring carbon atoms of the pyrroles 3–17 are given in Table 2. The assignment of C-2, C-4 and C-5 followed from a proton–carbon correlation experiment on the 1-*tert*-butyl-3-methoxypyrrole (4), which showed that $\delta_{\text{C-5}} > \delta_{\text{C-2}} > \delta_{\text{C-4}}$, *i.e.* the same relative order as in the ^1H NMR spectra. In some cases, the chemical shifts of C-2 and C-4 are very close, but they can be clearly distinguished by their one-bond coupling constants (¹J_{CH}), which are much larger for pyrrole α -carbons than for β -carbon atoms⁹ (see below). This assignment was confirmed for [¹³C-2]-3-hydroxy-1-phenylpyrrole (6)⁶ in which the signal due to the enriched carbon atom was found at δ_{C} 101.45 (*cf.* Table 2).

The effect of the 3-hydroxy or alkoxy substituent on the chemical shift of the pyrrole ring carbon atoms is given in Table 3, where the values are compared with those of the analogous benzene derivatives 20 and 21.¹⁰ In all cases, a large high frequency shift is observed at the *ipso*-position, with the effect greatest in magnitude for the alkoxy compounds. In both pyrrole series, a shielding effect at C-2 and C-4 is observed, with the magnitude greater at C-2 where direct conjugation is

Table 3 Effect of hydroxy and methoxy groups on the ^{13}C NMR chemical shifts of pyrrole and benzene derivatives

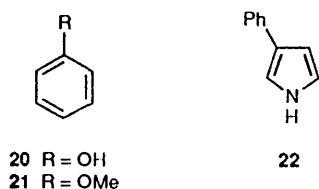
Compound	R ¹	R ³	C-2	C-3	C-4	C-5
3 ^a	Bu'	H	-15.5	+35.5	-9.5	-2.5
4 ^a	Bu'	Me	-16.9	+40.5	-11.3	-1.7
6 ^b	Ph	H	-17.5	+36.0	-7.9	-3.0
7 ^b	Ph	Me	-18.1	+40.7	-9.8	-2.0
		R	<i>ortho</i>	α	<i>meta</i>	
20 ¹⁰		OH	-12.7	+26.9	+1.4	
21 ¹⁰		OMe	-14.4	+31.4	+1.0	

^a *N*-*tert*-butylpyrrole; δ_{C} 116.7 (C-2, C-5), 107.9 (C-3, C-4). ^b *N*-phenylpyrrole; ¹² δ_{C} 119.0 (C-2, C-5) 110.1 (C-3, C-4).

Table 4 Effect of pyrrole rings on the ^{13}C NMR chemical shift of the *para*-carbon atom of phenylpyrroles

Compound	R ¹	R ²	R ³	(C- <i>para</i>)	$\Delta\delta_{\text{C}}^a$
6	Ph	H	H	124.07	-4.4
7	Ph	H	Me	124.82	-3.7
19	<i>N</i> -phenylpyrrole ¹²			125.3	-3.2
6	Ph (keto form) ³			122.97	-5.5
15	Ph	Me	Me	126.17	-2.3
12	Me	Ph	H	125.08	-3.4
13	Me	Ph	Me	126.02	-2.4
22	3-phenylpyrrole ¹³			124.5	-4.0

^a Assumes δ_{C} (benzene) 128.5.¹⁰



possible. The average of these is similar in size to the *ortho*-effect in the benzene derivatives. Surprisingly, a small shielding effect is found at C-5 of the pyrroles, whereas the shift is in the opposite direction in the benzene series. Very similar results to these have been reported for certain highly substituted alkoxy-pyrroles.¹¹

As expected, *N*-aryl substitution causes deshielding of the pyrrole resonances due to competitive delocalisation of the lone pair of the nitrogen atom: the effect is most pronounced at the 3- and 4-positions (Table 2). 2-Aryl substituents can fully interact with the pyrrole ring only by conjugative electron withdrawal and the net effect is to cause substantial deshielding at C-5 (Table 2). These interactions are also manifest in the chemical shift of the *para*-carbon atom of the aryl ring (Table 4): in all cases, the aryl ring acts as an electron acceptor, with the resonance shifted to low frequency with respect to benzene. In the *N*-aryl series, the alkoxy- and hydroxy-pyrroles are slightly better electron donors than pyrrole itself (Table 4),¹² but the effect is reduced on substitution at the 2-position where the two rings are unable to achieve coplanarity. It is of interest that the 1*H*-pyrrol-3(2*H*)-one system³ (1*K*: R¹ = Ph) is a much better electron donor into an *N*-phenyl substituent than the hydroxy- or alkoxy-pyrroles: the delocalisation of the lone pair through the enaminone system may therefore be less efficient than that required to obtain a 6 π system in the 'aromatic' pyrroles. In the *N*-methyl-2-phenyl series 12 and 13 (where coplanarity may again be a problem), it is clear that the pyrrole ring nevertheless acts as an electron donor, with the effect of similar magnitude

to that of a methyl group.¹⁰ However, a larger shift has been recorded with other *C*-arylpyrroles¹³ (Table 4).

Alkyl substitution at the 2-position causes substantial deshielding at C-2 of the pyrrole ring (*ca.* 10 ppm) and shielding at C-3 (*ca.* 4 ppm) with very much smaller effects at the other positions. Similar effects have been noted in the spectra of other alkoxy-pyrroles.¹¹

One bond carbon-proton couplings for the β (C-4) and α (C-2 and -5) positions of the 3-hydroxy- and 3-alkoxy-pyrroles are fairly constant at 170 ± 2 and 185 ± 3 Hz, respectively. There is even less spread if the *N*-phenyl and *N*-alkyl examples are considered separately (Table 2). These values compare well with the corresponding couplings for pyrrole itself⁹ [$^1J_{\text{CH}(\beta)} = 168.8$; $^1J_{\text{CH}(\alpha)} = 183.3$]. These well defined one bond coupling constants further confirmed the assignment of the resonances corresponding to the C-2 and C-4 atoms of 3-hydroxy-1-phenylpyrrole (6); the coupling constant of the signal at $\delta_{\text{C}} = 101.54$ (185.8 Hz) compared with that of the signal at $\delta_{\text{C}} = 102.18$ (170.9 Hz) indicates that in this example the C-2 atom is the more shielded in contrast to the *N*-alkyl examples. The one bond coupling constants in the phenyl substituted cases are all around 3 Hz larger than those for the other derivatives.

Long-range couplings were assigned by substitution of the 1- and/or 2-positions with phenyl or *tert*-butyl groups which are incapable of exhibiting long-range couplings to the ring resonances, and by deuteration of the 2- and 4-positions.

The 2-unsubstituted hydroxy and alkoxy compounds give triplets of doublets corresponding to the C-2, C-4 and C-5 atoms. Thus, each of these carbon atoms couples to the hydrogen atoms attached to the other two with approximately the same coupling constant. Both the 2J and 3J couplings to the C-4 and C-5 positions are between 6.5 and 7.0 Hz which are reasonably close to the corresponding 3J couplings in pyrrole itself⁹ ($^3J_{\text{C-4,2-H}} 7.43$, $^3J_{\text{C-5,2-H}} 6.63$) but rather less than the related 2J couplings⁹ ($^2J_{\text{C-5,4-H}} 8.69$, $^2J_{\text{C-4,5-H}} 8.34$). The 3J couplings observed to the 2-position are 4.2 ± 0.4 Hz, which is considerably less than those observed in the parent compound ($^3J_{\text{C-2,4-H}} 7.45$, $^3J_{\text{C-2,5-H}} 6.63$). 2-Substituted 3-hydroxy- and 3-alkoxy-pyrroles give unresolved multiplets for the signals corresponding to the C-2 atom, due to coupling to the substituent, but show well resolved 2J coupling for the C-4 and C-5 atoms (Table 2). The C-5 resonances are sometimes further split by coupling to the *N*-substituent: for example this is found to be 3.5 Hz in 3-hydroxy-1-methyl-2-phenylpyrrole (12).

The long-range couplings to the C-3 atom attached to the oxygen function is more complex and often not resolved, particularly in the case of the alkoxy derivatives. However, these interactions have been analysed for 2-unsubstituted-3-hydroxypyrrroles with the aid of deuterated examples. A doublet of doublets pattern is normally observed for these cases, with couplings of *ca.* 4 and 9 Hz. The [2,4- $^2\text{H}_2$]-1-*tert*-butyl-3-hydroxypyrrrole (3) gives rise to a doublet of 9.6 Hz and the larger value is therefore assigned to the three-bond coupling to 5-H. As the 2-substituted compounds which give well defined C-3 signals (*e.g.* 12 or 16) do not show the smaller (4 Hz) coupling it is clear this must be the two bond coupling to 2-H. The complete long-range coupling pattern of 1-*tert*-butyl-3-hydroxypyrrrole is depicted in Fig. 2.

In one example, 3-hydroxy-1-methyl-2-phenylpyrrole (12), a coupling of less than 2 Hz is also observed which may be a 2J coupling to 4-H which is not resolved in more complex cases ($^2J_{\text{C-3,4-H}}$ in pyrrole itself⁹ is 4.61 Hz). 2-Methyl groups can further split the C-3 signal into quartets with a coupling of around 4 Hz (*e.g.* 10).

Experimental

^1H and ^{13}C NMR spectra were generally recorded at 200 and

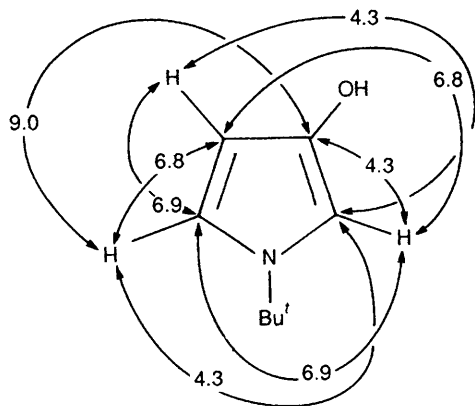


Fig. 2 Long-range couplings ${}^nJ_{\text{CH}}/\text{Hz}$ for the 3-hydroxypyrrole 3

50 MHz respectively using a Bruker WP200SY instrument. The digital resolution in the ${}^1\text{H}$ and ${}^{13}\text{C}$ spectra was 0.27 and 1.4 Hz respectively.

3-Hydroxypyrrole Derivatives 3, 6, 10, 12, 14 and 16.—These compounds were prepared as their 1*H*-pyrrol-3(2*H*)-one tautomers as previously described,⁴ and the hydroxy form was generated in [${}^2\text{H}_6$]DMSO solution.²

3-Alkoxyppyrrrole Derivatives 4, 5, 7–9, 11, 13, 15 and 17.—These derivatives were obtained as reported in part 10 of this series.¹

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