## A Novel Phosphomolybdate Structure: Crystal Structure of $\left[\mathrm{NH}_{4}\right]_{5}\left[\left(\mathrm{MoO}_{3}\right)_{5}\left(\mathrm{PO}_{4}\right)\left(\mathrm{HPO}_{4}\right)\right], 3 \mathrm{H}_{2} \mathrm{O}$

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The crystal structure of the title compound has been studied by $X$-ray diffraction methods from counter data. Crystals are orthorhombic, space group $P 2_{1} 2_{1} 2_{1}$, with parameters $a=14.699(2), b=9.725(1), c=18.201$ (2) A. The structure was solved by direct methods and refined by full-matrix least squares to $R 0.029$ for 4.808 observed reflections. The anion consists of a ring of five distorted $\mathrm{MoO}_{6}$ octahedra. Of the five links in the ring, four involve shared edges, and the fifth a shared apex of $\mathrm{MoO}_{6}$ octahedra. The crown thus formed is capped on one face by $\mathrm{PO}_{4}{ }^{3-}$ and on the other by $\mathrm{HPO}_{4}{ }^{2-}$. The three phosphate oxygen atoms shared by the $\mathrm{MoO}_{6}$ octahedra are of two types: one type (two on each phosphate) consists of oxygen atoms bridging two molybdenum atoms, and the other, the third phosphate oxygen, is shared by only one molybdenum atom. The phosphomolybdate anions are held together by a network of strong hydrogen bonds.

THE most characteristic tungsten and molybdenum heteropolyanions are species presenting a molybdenum or tungsten : heteroatom ratio of twelve (series twelve); these include $\left[\mathrm{SiW}_{12} \mathrm{O}_{40}\right]^{4-}$ and $\left[\mathrm{PMO}_{12} \mathrm{O}_{40}\right]^{5-}$ whose structure has been determined by Keggin. ${ }^{1}$ When the central atom is phosphorus or arsenic, there are compounds which contain two heteroatoms, such as
$\left[\mathrm{P}_{2} \mathrm{~W}_{18} \mathrm{O}_{62}\right]^{6-}$. These compounds are obtained under conditions different from those in the first group, but they have similar properties. Their structure, derived from Keggin's model, was determined by Dawson: ${ }^{2}$ in these compounds, the phosphate anions are surrounded

[^0]by $\mathrm{WO}_{6}$ octahedra and each phosphate oxygen is bonded to at least one tungsten atom. The $\mathrm{PO}_{4}$ tetrahedra are located at the centre of the cavity formed by the assemblage of $\mathrm{WO}_{6}$ octahedra.

The moderate alkaline hydrolysis of the series twelve compounds yields new compounds presenting molybdenum or tungsten : heteroatom ratios of eleven, e.g. $\left[\mathrm{PW}_{11} \mathrm{O}_{39}\right]^{7-}$; under more stringent conditions, the compounds are completely hydrolysed into tungstate or molybdate, according to reaction (1). In the case

$$
\begin{align*}
{\left[\mathrm{PMO}_{11} \mathrm{O}_{39}\right]^{7-} } & +\underset{\left[\mathrm{HPO}_{4}\right]^{2-}}{ } \mathbf{1 7 \mathrm { OH } ^ { - }} 11\left[\mathrm{MoO}_{4}\right]^{2-}+8 \mathrm{H}_{2} \mathrm{O}
\end{align*}
$$

of the phosphomolybdates, however, an intermediate step exists in which a series of compounds containing molybdenum : heteroatom ratios of $5 / 2$ are formed according to reaction (2). Under moderate conditions,

$$
2\left[\mathrm{PMO}_{11} \mathrm{O}_{39}\right]_{\left[\mathrm{P}_{2} \mathrm{MO}_{5} \mathrm{O}_{23}\right]^{7-}+26 \mathrm{O} \mathrm{H}^{-}}+17\left[\mathrm{MoO}_{4}\right]^{2-}+13 \mathrm{H}_{2} \mathrm{O}
$$

these compounds can be hydrolysed to $\left[\mathrm{HP}_{2} \mathrm{Mo}_{5} \mathrm{O}_{23}\right]^{5-}$ and, eventually, to $\left[\mathrm{HPO}_{4}\right]^{2-}$ and $\left[\mathrm{MoO}_{4}\right]^{2-} .{ }^{-3}$ In this case, it is not likely that the $\mathrm{PO}_{4}$ tetrahedra occupy the


Figure 1 Stereovicw of the anion $\left[\left(\mathrm{MOO}_{3}\right)_{5}\left(\mathrm{PO}_{4}\right)\left(\mathrm{HPO}_{4}\right)\right]^{5-} ; \mathrm{MoO}_{6}$ octahedra are shown by filled bonds, $\mathrm{PO}_{4}$ tetrahedra by open bonds
centre of cavities formed by assemblages of $\mathrm{MoO}_{6}$ octahedra, because of the small number of octahedra available. Since no crystalline structure of a member of this class of compounds was known, we have determined that of the compound $\left[\mathrm{NH}_{4}\right]_{5}\left[\left(\mathrm{MoO}_{3}\right)_{5}\left(\mathrm{PO}_{4}\right)-\right.$ $\left.\left(\mathrm{HPO}_{4}\right)\right], 3 \mathrm{H}_{2} \mathrm{O}$ by $X$-ray diffraction methods.

## EXPERIMENTAL

Crystals of the title compound were prepared by the method of ref. 4. Preliminary cell data were obtained from precession photographs. Refined unit-cell dimensions and their estimated standard deviations were obtained by the method of Busing and Levy, ${ }^{5}$ from diffractometer data, with $\mathrm{Mo}-K_{\alpha}$ radiation.
${ }^{3}$ P. Souchay and J. Faucherre, Bull. Soc. chim. France, 1951, 18, 355.
${ }^{4}$ P. Souchay, ' Ions Minéraux Condensés,' Masson, 1969, p. 96.
times, and $p$ is an empirical coefficient of the net count $I$. An initial $p$ value of 0.05 was used. A total of 11733 reflections were measured in the range $6.0^{\circ}<20<90^{\circ}$, of which 4808 had $\sigma(I) / I<0.35$ and were considered observed. Absorption corrections were computed by numerical integration using the program DATAP. ${ }^{6}$ Since the absorption factors varied between 1.207 and 1.234 , no absorption corrections were applied.

Structure Solution and Refinement.-The presence of five molybdenum atoms in the asymmetric unit precludes the use of Patterson methods, and the crystal structure was therefore solved by direct methods. Normalized structure factors were computed for all reflections having $\sigma(I) / I$ $<0 \cdot 45$, using the programs SAP1 and SAP2 ${ }^{7}$ (Table 1). The origin- and enantiomorph-fixing reflections were

[^1]determined by the program MULTAN. ${ }^{8}$ The reflections used were:

|  |  |  | $\alpha$ | $E$ |
| :---: | :---: | :---: | :---: | :---: |
| 2 | 9 | 0 | 0 | $3 \cdot 40$ |
| 5 | 6 | 0 | $\pi / 2$ | $3 \cdot 00$ |
| 0 | 2 | 11 | 0 | $2 \cdot 42$ |
|  | 0 | 21 | $\pi / 2$ | $2 \cdot 07$ enantiomorph |

With these reflections and 12 phases determined by the $\Sigma_{1}$ procedure, the values of 93 initial phases were reliably determined by the subroutine FASTAN.

Table 1
Distribution of normalized structure factors computed using reflections with $\sigma(I) / I<0 \cdot 45$

$E$ values, and the initial set of 97 reflections was refined and extended by use of the program DP4. ${ }^{7}$ An $E$ map computed using the phases determined for 487 reflections revealed the positions of the five molybdenum atoms; this model gave $R 0 \cdot 33$. A Fourier map computed with these positions revealed the position of all other non-hydrogen atoms. The positions of the nitrogen atoms were assigned on the basis of the known contact distance of $4 \AA$ between neighbouring $\mathrm{NH}_{4}{ }^{+}$cations; $R$ was then $0 \cdot 18$.

In all structure-factor calculations, the scattering factors used were taken from ref. 9, modified according to ref. 10 , and with corrections for the effects of anomalous dispersion for molybdenum and phosphorus atoms, taken from ref. 11. The initial model was then refined with isotropic temperature factors for all atoms. ${ }^{12}$ The function minimized was: $\quad \Sigma w\left(\left|F_{\mathrm{o}}\right|-\left|F_{\mathrm{c}}\right|\right)^{2}$, where $w=1 / \sigma^{2}\left(F_{\mathrm{o}}\right)$. After three cycles $R$ was 0.06 , and the weighted factor $R^{\prime}$ was $0.07 \quad\left\{R^{\prime}=\left[\Sigma w\left(\left|F_{\mathrm{o}}\right|-\left|F_{\mathrm{c}}\right|\right)^{2} / \Sigma w\left|F_{\mathrm{o}}\right|^{2}\right]^{1 / 2}\right\}$. Anisotropic temperature factors were introduced for all atoms and refinement was continued. At this stage, the $p$ value was changed to 0.03 to satisfy Cruickshank's ${ }^{13}$ weighting

Table 2
Atomic co-ordinates and anisotropic temperature factors * $\left(\times 10^{5}\right)$, with their standard deviations in parentheses


The $\Sigma_{2}$ relationships were computed ${ }^{7}$ by use of the program DP3 with the 500 reflections having the highest
${ }^{8}$ G. Germain, P. Main, and M. H. Woolfson, Acta Cryst., 1970, B26, 274.
${ }_{9}$ F. M. Moore, Acta Cryst., 1963, 16, 1169.
${ }^{10}$ V. Vand, I'. F. Eiland, and R. Pepinsky, Acta Cryst., 1957, 10. 303.
${ }_{11}$ D. T. Cromer, Acta Cryst., 1965, 18, 17.
criterion. After three cycles of refinement, all changes in parameters were $<0 \cdot 1 \sigma$ and refinement was terminated.

[^2]The final value of $R$ was 0.029 and $R^{\prime} 0.030$. The standard deviation of a unit weight observation was $1 \cdot 06$. The final Fourier map revealed no peaks $>0 \cdot 4 e^{\AA} \AA^{-3}$.
All computations were made with a Univac 1108 computer. Other programs used include ORTEP by C. K. Johnson ${ }^{14}$ and local programs (by J. F.) for Fourier and least-squares planes.

Atomic co-ordinates and individual anisotropic thermal parameters are listed in Table 2. Observed and calculated structure factors are available in Supplementary Publication No. SUP 20941 ( 9 pp.).*


Figure 2 Numbering scheme in the anion


Figure 3 Assemblage of $\mathrm{MoO}_{6}$ octahedra in the $\left(\mathrm{MOO}_{3}\right)_{5}$ crown

## DISCUSSION

Description of the Structure.--The crystal structure of $\left[\mathrm{NH}_{4}\right]_{5}\left[\left(\mathrm{MoO}_{3}\right)_{5}\left(\mathrm{HPO}_{4}\right)\left(\mathrm{PO}_{4}\right)\right], 3 \mathrm{H}_{2} \mathrm{O}$ is ionic; it is composed of an assembiage of complex $\left[\left(\mathrm{MoO}_{3}\right)_{5}\left(\mathrm{HPO}_{4}\right)\right.$ -$\left.\left(\mathrm{PO}_{4}\right)\right]^{5-}$ anions, $\left[\mathrm{NH}_{4}\right]^{+}$cations, and molecules of water of crystallisation. Figure 1 is a stereoview of the anion. Figure 2 shows the numbering scheme adopted.

[^3]The molybdenum atoms are surrounded by six oxygen atoms and the five distorted $\mathrm{MoO}_{6}$ octahedra are associated through the sharing of four edges and one

Table 3
Molecular dimensions in the $\left(\mathrm{MoO}_{3}\right)_{5}$ crown, with standard deviation in parentheses
(a) Distances $(\AA)$

| $\mathrm{Mo}(1) \cdots \mathrm{Mo}(2)$ | $3 \cdot 331(6)$ | $\mathrm{Mo}(3)-\mathrm{O}(12)$ | $1 \cdot 700(4)$ |
| :--- | :--- | :--- | :--- |
| $\mathrm{Mo}(2) \cdots \mathrm{Mo}(3)$ | $3 \cdot 374(5)$ | $\mathrm{Mo}(3)-\mathrm{O}(13)$ | $1 \cdot 714(4)$ |
| $\mathrm{Mo}(3) \cdots \mathrm{Mo}(4)$ | $3 \cdot 375(5)$ | $\mathrm{Mo}(3)-\mathrm{O}(9)$ | $1 \cdot 897(3)$ |
| $\mathrm{Mo}(4) \cdots \mathrm{Mo}(5)$ | $3 \cdot 357(5)$ | $\mathrm{Mo}(3)-\mathrm{O}(15)$ | $1 \cdot 922(3)$ |
| $\mathrm{Mo}(5) \cdots \mathrm{Mo}(1)$ | $3 \cdot 688(6)$ | $\mathrm{Mo}(3)-\mathrm{O}(10)$ | $2 \cdot 345(3)$ |
| $\mathrm{Mo}(1)-\mathrm{O}(7)$ | $1 \cdot 712(4)$ | $\mathrm{Mo}(3)-\mathrm{O}(14)$ | $2 \cdot 367(3)$ |
| $\mathrm{Mo}(1)-\mathrm{O}(1)$ | $1 \cdot 717(4)$ | $\mathrm{Mo}(4)-\mathrm{O}(2)$ | $1 \cdot 712(4)$ |
| $\mathrm{Mo}(1)-\mathrm{O}(3)$ | $1 \cdot 910(4)$ | $\mathrm{Mo}(4)-\mathrm{O}(18)$ | $1 \cdot 714(4)$ |
| $\mathrm{Mo}(1)-\mathrm{O}(5)$ | $1 \cdot 931(3)$ | $\mathrm{Mo}(4)-\mathrm{O}(15)$ | $1 \cdot 925(3)$ |
| $\mathrm{Mo}(1)-\mathrm{O}(4)$ | $2 \cdot 270(3)$ | $\mathrm{Mo}(4)-\mathrm{O}(17)$ | $1 \cdot 928(3)$ |
| $\mathrm{Mo}(1)-\mathrm{O}(6)$ | $2 \cdot 307(3)$ | $\mathrm{Mo}(4)-\mathrm{O}(16)$ | $2 \cdot 205(3)$ |
| $\mathrm{Mo}(2)-\mathrm{O}(8)$ | $1 \cdot 709(4)$ | $\mathrm{Mo}(4)-\mathrm{O}(14)$ | $2 \cdot 338(3)$ |
| $\mathrm{Mo}(2)-\mathrm{O}(11)$ | $1 \cdot 709(4)$ | $\mathrm{Mo}(5)-\mathrm{O}(19)$ | $1 \cdot 690(4)$ |
| $\mathrm{Mo}(2)-\mathrm{O}(9)$ | $1 \cdot 898(3)$ | $\mathrm{Mo}(5)-\mathrm{O}(20)$ | $1 \cdot 703(4)$ |
| $\mathrm{Mo}(2)-\mathrm{O}(3)$ | $1 \cdot 946(3)$ | $\mathrm{Mo}(5)-\mathrm{O}(5)$ | $1 \cdot 928(3)$ |
| $\mathrm{Mo}(2)-\mathrm{O}(4)$ | $2 \cdot 172(3)$ | $\mathrm{Mo}(5)-\mathrm{O}(17)$ | $1 \cdot 962(3)$ |
| $\mathrm{Mo}(2)-\mathrm{O}(10)$ | $2 \cdot 427(3)$ | $\mathrm{Mo}(5)-\mathrm{O}(21)$ | $2 \cdot 269(3)$ |
|  |  | $\mathrm{Mo}(5)-\mathrm{O}(16)$ | $2 \cdot 338(3)$ |

(b) Angles ( ${ }^{\circ}$ )

| $\mathrm{Mo}(1) \cdot \cdots \mathrm{Mo}(2) \cdot$ | 109.91(0.01) |
| :---: | :---: |
| Mo(2) $\cdot$. $\mathrm{Mo}^{(3)}$. . | $108.32(0 \cdot 01)$ |
| Mo(3) $\cdots$ Mo(4) . | $109.52(0.01)$ |
| Mo(4) $\cdots$ Mo(5) $\cdot$. | $104 \cdot 82(0 \cdot 01)$ |
| Mo(5) . - Mo(1) . | 104.70(0.01) |
| $\mathrm{O}(1)-\mathrm{Mo}(1)-\mathrm{O}(3)$ | $99 \cdot 36(0 \cdot 18)$ |
| $\mathrm{O}(3)-\mathrm{Mo}(1)-\mathrm{O}(4)$ | $70 \cdot 87(0 \cdot 14)$ |
| $\mathrm{O}(4)-\mathrm{Mo}(1)-\mathrm{O}(5)$ | $84 \cdot 93(0 \cdot 13)$ |
| $\mathrm{O}(5)-\mathrm{Mo}(1)-\mathrm{O}(1)$ | $100 \cdot 52(0 \cdot 17)$ |
| $\mathrm{O}(6)-\mathrm{Mo}(1)-\mathrm{O}(1)$ | $85 \cdot 66(0 \cdot 16)$ |
| $\mathrm{O}(6)-\mathrm{Mo}(1)-\mathrm{O}(3)$ | $77 \cdot 79(0 \cdot 14)$ |
| $\mathrm{O}(6)-\mathrm{Mo}(1)-\mathrm{O}(4)$ | $84 \cdot 93(0 \cdot 12)$ |
| $\mathrm{O}(6)-\mathrm{Mo}(1)-\mathrm{O}(5)$ | $78 \cdot 12(0 \cdot 13)$ |
| $\mathrm{O}(7)-\mathrm{Mo}(1)-\mathrm{O}(1)$ | $102 \cdot 61(0 \cdot 20)$ |
| $\mathrm{O}(7)-\mathrm{Mo}(1)-\mathrm{O}(3)$ | $101 \cdot 37(0 \cdot 18)$ |
| $\mathrm{O}(7)-\mathrm{Mo}(1)-\mathrm{O}(4)$ | $87.87(0 \cdot 16)$ |
| $\mathrm{O}(7)-\mathrm{Mo}(1)-\mathrm{O}(5)$ | $99 \cdot 30(0 \cdot 17)$ |
| $\mathrm{O}(3)-\mathrm{Mo}(2)-\mathrm{O}(4)$ | $72 \cdot 48(0 \cdot 14)$ |
| $\mathrm{O}(4)-\mathrm{Mo}(2)-\mathrm{O}(9)$ | $83.54(0 \cdot 14)$ |
| $\mathrm{O}(9)-\mathrm{Mo}(2)-\mathrm{O}(8)$ | 101.84(0.18) |
| $\mathrm{O}(8)-\mathrm{Mo}(2)-\mathrm{O}(3)$ | $95 \cdot 06(0 \cdot 18)$ |
| $\mathrm{O}(10)-\mathrm{Mo}(2)-\mathrm{O}(3)$ | $87 \cdot 99(0 \cdot 14)$ |
| $\mathrm{O}(10)-\mathrm{Mo}(2)-\mathrm{O}(4)$ | $71 \cdot 08(0 \cdot 12)$ |
| $\mathrm{O}(10)-\mathrm{Mo}(2)-\mathrm{O}(9)$ | $71 \cdot 19(0 \cdot 14)$ |
| $\mathrm{O}(10)-\mathrm{Mo}(2)-\mathrm{O}(8)$ | $88 \cdot 02(0 \cdot 16)$ |
| $\mathrm{O}(11)-\mathrm{Mo}(2)-\mathrm{O}(3)$ | $98.04(0 \cdot 18)$ |
| $\mathrm{O}(11)-\mathrm{Mo}(2)-\mathrm{O}(4)$ | $97 \cdot 28(0 \cdot 16)$ |
| $\mathrm{O}(11)-\mathrm{Mo}(2)-\mathrm{O}(9)$ | $97 \cdot 34(0 \cdot 18)$ |
| $\mathrm{O}(11)-\mathrm{Mo}(2)-\mathrm{O}(8)$ | $105 \cdot 42(0 \cdot 20)$ |
| $\mathrm{O}(9)-\mathrm{Mo}(3)-\mathrm{O}(10)$ | $73 \cdot 19(0 \cdot 14)$ |
| $\mathrm{O}(10)-\mathrm{Mo}(3)-\mathrm{O}(15)$ | $80 \cdot 55(0 \cdot 13)$ |
| $\mathrm{O}(15)-\mathrm{Mo}(3)-\mathrm{O}(13)$ | 102.01(0.17) |
| $\mathrm{O}(13)-\mathrm{Mo}(3)-\mathrm{O}(9)$ | $99 \cdot 38(0 \cdot 17)$ |
| $\mathrm{O}(12)-\mathrm{Mo}(3)-\mathrm{O}(9)$ | $102.92(0 \cdot 18)$ |
| $\mathrm{O}(12)-\mathrm{Mo}(3)-\mathrm{O}(10)$ | 86.87(0.16) |
| $\mathrm{O}(12)-\mathrm{Mo}(3)-\mathrm{O}(15)$ | $99.99(0 \cdot 17)$ |
| $\mathrm{O}(12)-\mathrm{Mo}(3)-\mathrm{O}(13)$ | $103 \cdot 60(0 \cdot 19)$ |
| $\mathrm{O}(14)-\mathrm{Mo}(3)-\mathrm{O}(9)$ | $79 \cdot 33(0 \cdot 14)$ |
| $\mathrm{O}(14)-\mathrm{Mo}(3)-\mathrm{O}(10)$ | $81 \cdot 6 \mathrm{I}(0 \cdot 12)$ |
| $\mathrm{O}(14)-\mathrm{Mo}(3)-\mathrm{O}(15)$ | 72.48(0.13) |
| $\mathrm{O}(14)-\mathrm{Mo}(3)-\mathrm{O}(13)$ | $88 \cdot 42(0 \cdot 16)$ |
| $\bigcirc(14)-\mathrm{MO}(4)-\mathrm{O}(15)$ | $73 \cdot 11(0 \cdot 13)$ |
| $\mathrm{O}(15)-\mathrm{Mo}(4)-\mathrm{O}(18)$ | $95.59(0 \cdot 17)$ |
| $\mathrm{O}(18)-\mathrm{Mo}(4)-\mathrm{O}(17)$ | $98 \cdot 01(0 \cdot 17)$ |
| $\mathrm{O}(17)-\mathrm{Mo}(4)-\mathrm{O}(14)$ | $88 \cdot 35(0 \cdot 13)$ |
| $\mathrm{O}(16)-\mathrm{Mo}(4)-\mathrm{O}(14)$ | $72 \cdot 96(0 \cdot 12)$ |
| $\bigcirc(16)-\mathrm{Mo}(4)-\mathrm{O}(15)$ | $83 \cdot 10(0 \cdot 14)$ |
| $\mathrm{O}(16)-\mathrm{Mo}(4)-\mathrm{O}(18)$ | $93 \cdot 63(0 \cdot 16)$ |
| $\mathrm{O}(16)-\mathrm{Mo}(4)-\mathrm{O}(17)$ | $74 \cdot 45(0 \cdot 14)$ |
| $\mathrm{O}(2)-\mathrm{Mo}(4)-\mathrm{O}(14)$ | $89 \cdot 91(0 \cdot 17)$ |

Table 3 (Continued)

| $\mathrm{O}(2)-\mathrm{Mo}(4)-\mathrm{O}(15)$ | 100-16(0.18) |
| :---: | :---: |
| $\mathrm{O}(2)-\mathrm{Mo}(4)-\mathrm{O}(18)$ | 104.63(0.20) |
| $\mathrm{O}(2)-\mathrm{Mo}(4)-\mathrm{O}(17)$ | $97 \cdot 30(0 \cdot 18)$ |
| $\mathrm{O}(5)-\mathrm{Mo}(5)-\mathrm{O}(16)$ | 84.73 (0.14) |
| $\mathrm{O}(16)-\mathrm{Mo}(5)-\mathrm{O}(17)$ | $70 \cdot 81(0 \cdot 13)$ |
| $\mathrm{O}(17)-\mathrm{Mo}(5)-\mathrm{O}(19)$ | 99.90 (0.15) |
| $\mathrm{O}(19)-\mathrm{Mo}(5)-\mathrm{O}(5)$ | 101.00(0.17) |
| $\bigcirc(20)-\mathrm{Mo}(5)-\mathrm{O}(5)$ | $99 \cdot 12(0 \cdot 15)$ |
| $\mathrm{O}(20)-\mathrm{Mo}(5)-\mathrm{O}(16)$ | $85 \cdot 17(0 \cdot 13)$ |
| $\mathrm{O}(20)-\mathrm{Mo}(5)-\mathrm{O}(17)$ | $99 \cdot 89(0 \cdot 17)$ |
| $\mathrm{O}(20)-\mathrm{Mo}(5)-\mathrm{O}(19)$ | $103 \cdot 68(0 \cdot 18)$ |
| $\bigcirc(21)-\mathrm{Mo}(5)-\mathrm{O}(5)$ | $80 \cdot 27(0 \cdot 13)$ |
| $\mathrm{O}(21)-\mathrm{Mo}(5)-\mathrm{O}(16)$ | 85-79(0.14) |
| $\mathrm{O}(21)-\mathrm{Mo}(5)-\mathrm{O}(17)$ | $76.84(0 \cdot 14)$ |
| $\bigcirc(21)-\mathrm{Mo}(5)-\mathrm{O}(19)$ | $85 \cdot 26(0 \cdot 13)$ |

Table 4
Equation of least-squares plane through the molybdenum atoms, and deviations $(\AA)$ of these atoms from the plane

$$
\begin{aligned}
& \text { Plane: } \operatorname{Mo(1)-(5)} \\
& \quad-0.9935 x-0.0787 y-0.0822 z+2 \cdot 1790=0 \\
& \operatorname{Mo(1)} 0.2481, \mathrm{Mo}(2)-0.1539, \mathrm{Mo}(3) 0.0207, \mathrm{Mo}(4) 0.1199, \\
& \mathrm{Mo}(5)-0.1964 ; \sigma \text { all } 4
\end{aligned}
$$

apex to form a crown of composition $\mathrm{Mo}_{5} \mathrm{O}_{21}$; Figure 3 shows this crown and demonstrates the assemblage of the edges of the $\mathrm{Mo}(1)$ and $\mathrm{Mo}(2), \mathrm{Mo}(2)$ and $\mathrm{Mo}(3)$, $\mathrm{Mo}(3)$ and $\mathrm{Mo}(4)$, and $\mathrm{Mo}(4)$ and $\mathrm{Mo}(5)$ octahedra. The ring so formed is closed at $\mathrm{Mo}(1), \mathrm{Mo}(5)$, which share an apex. Bond lengths and angles in the anion are listed in Table 3. The five molybdenum atoms are not coplanar, as shown by their distances from their leastsquares plane (Table 4).

However, the distances $\mathrm{Mo}(\mathrm{l}) \cdots \mathrm{Mo}(5)$ and $\mathrm{Mo}(2) \cdots \mathrm{Mo}(4)$ are related by a pseudo-two-fold axis passing through the middle of $\mathrm{Mo}(\mathrm{I}) \cdots \mathrm{Mo}(5)$ and by Mo(3). The existence of the two-fold axis is confirmed by the symmetry of the $\mathrm{Mo}(1) \cdots \mathrm{Mo}(2) \cdots \mathrm{Mo}(3)$ and $\operatorname{Mo}(3) \cdots \operatorname{Mo}(4) \cdots \operatorname{Mo}(5)$, and $\operatorname{Mo}(4) \cdots \operatorname{Mo}(5) \cdots \operatorname{Mo}(1)$, and $\operatorname{Mo}(5) \cdots \operatorname{Mo}(1) \cdots \operatorname{Mo}(2)$ angles on the one hand and the symmetry of the $\operatorname{Mo}(1) \cdots \operatorname{Mo}(2)$ and $\operatorname{Mo}(4) \cdots \operatorname{Mo}(5)$, and $\operatorname{Mo}(2) \cdots \operatorname{Mo}(3)$ and $\operatorname{Mo}(3) \cdots \operatorname{Mo}(4)$ distances on the other. This pseudo-symmetry is preserved for all the atoms of the complex anion, within a deviation of $c a .0 \cdot 6 \AA$.

The $\mathrm{MoO}_{6}$ octahedra are all deformed, as shown by the Mo-O bond lengths and the $\mathrm{O}^{-}-\mathrm{Mo}-\mathrm{O}$ angles (Table 4). The $\mathrm{Mo}^{-} \mathrm{O}$ bonds form three pairs. One contains the short $\mathrm{Mo}{ }^{-} \mathrm{O}$ bonds of $1.690-1.717 \AA$, belonging to terminal oxygen atoms, and probably double $\mathrm{Mo}=\mathrm{O}$ bonds. A second pair ( 1.897 and $1.962 \AA$ ) consists of the oxygen atoms shared by two molybdenum and the third ( $2 \cdot 172$ and $2.427 \AA$ ) is composed of the oxygen atoms shared by two molybdenum and one phosphorus atoms. The two phosphate anions cap the faces of the crown. Distances and angles in the $\mathrm{PO}_{4}$ tetrahedra are listed in Table 5.

The trend observed for $\mathrm{Mo}-\mathrm{O}$ is parallelled in the $\mathrm{P}-\mathrm{O}$ bond lengths. Thus, for the oxygen atoms shared by the phosphorus and molybdenum atoms, the longest bond lengths $(1.530-1.566 \AA)$ correspond to those oxygen atoms shared by a phosphorus and two molyb-
denum atoms namely $\mathrm{O}(4), \mathrm{O}(\mathbf{1 0}), \mathrm{O}(\mathbf{1 4})$, and $\mathrm{O}(\mathbf{1 6})$. The oxygen atoms $O(6)$ and $O(21)$, shared by one phosphorus and one molybdenum atom, have shorter

## Table 5

Bond lengths $(\AA)$ and angles $\left({ }^{\circ}\right)$ in the phosphate anions, with standard deviation in parentheses
(a) Distances

| $\mathrm{P}(1)-\mathrm{O}(6)$ | $1.511(3)$ | $\mathrm{P}(2)-\mathrm{O}(23)$ | $1.449(3)$ |
| :--- | :--- | :--- | :--- |
| $\mathrm{P}(1)-\mathrm{O}(10)$ | $1.530(3)$ | $\mathrm{P}(2)-\mathrm{O}(21)$ | $1.530(3)$ |
| $\mathrm{P}(1)-\mathrm{O}(16)$ | $1.535(3)$ | $\mathrm{P}(2)-\mathrm{O}(14)$ | $1.547(3)$ |
| $\mathrm{P}(1)-\mathrm{O}(22)$ | $1.569(3)$ | $\mathrm{P}(2)-\mathrm{O}(4)$ | $1.566(3)$ |
| $\mathrm{P}(1)-\mathrm{Mo}(1)$ | $3.330(1)$ | $\mathrm{P}(2)-\mathrm{Mo}(1)$ | $3.573(1)$ |
| $\mathrm{P}(1)-\mathrm{Mo}(2)$ | $3.539(1)$ | $\mathrm{P}(2)-\mathrm{Mo}(2)$ | $3.345(1)$ |
| $\mathrm{P}(1)-\mathrm{Mo}(3)$ | $3.482(1)$ | $\mathrm{P}(2)-\mathrm{Mo}(3)$ | $3.483(1)$ |
| $\mathrm{P}(1)-\mathrm{Mo}(4)$ | $3.408(1)$ | $\mathrm{P}(2)-\mathrm{Mo}(4)$ | $3.518(1)$ |
| $\mathrm{P}(1)-\mathrm{Mo}(5)$ | $3.576(1)$ | $\mathrm{P}(2)-\mathrm{Mo}(5)$ | $3.341(1)$ |

(b) Angles

| $\mathrm{O}(6)-\mathrm{P}(1)-\mathrm{O}(10)$ | $111 \cdot 60(0 \cdot 20)$ |
| :--- | :--- |
| $\mathrm{O}(6)-\mathrm{P}(1)-\mathrm{O}(16)$ | $109 \cdot 08(0 \cdot 20)$ |
| $\mathrm{O}(6)-\mathrm{P}(1)-\mathrm{O}(22)$ | $110 \cdot 68(0 \cdot 21)$ |
| $\mathrm{O}(10)-\mathrm{P}(1)-\mathrm{O}(16)$ | $110 \cdot 90(0 \cdot 19)$ |
| $\mathrm{O}(10)-\mathrm{P}(1)-\mathrm{O}(22)$ | $107 \cdot 65(0 \cdot 20)$ |
| $\mathrm{O}(16)-\mathrm{P}(1)-\mathrm{O}(22)$ | $106 \cdot 81(0 \cdot 20)$ |
| $\mathrm{O}(23)-\mathrm{P}(2)-\mathrm{O}(21)$ | $112 \cdot 16(0 \cdot 22)$ |
| $\mathrm{O}(23)-\mathrm{P}(2)-\mathrm{O}(14)$ | $112 \cdot 61(0 \cdot 21)$ |
| $\mathrm{O}(23)-\mathrm{P}(2)-\mathrm{O}(4)$ | $107 \cdot 88(0 \cdot 21)$ |
| $\mathrm{O}(21)-\mathrm{P}(2)-\mathrm{O}(14)$ | $109 \cdot 09(0 \cdot 20)$ |
| $\mathrm{O}(21)-\mathrm{P}(2)-\mathrm{O}(4)$ | $105 \cdot 56(0 \cdot 20)$ |
| $\mathrm{O}(14)-\mathrm{P}(2)-\mathrm{O}(4)$ | $109 \cdot 25(0 \cdot 19)$ |

distances $(1.511$ and $1.530 \AA$ ). The two oxygen atoms bonded only to phosphorus, $[\mathrm{O}(22)$ and $\mathrm{O}(23)]$, have distances of 1.569 and $1.499 \AA$, the latter being the shortest $\mathrm{P}-\mathrm{O}$ bond length in the present structure, and therefore attributed to a double $\mathrm{P}=\mathrm{O}$ bond. The other is the longest, and is ascribed to an OH radical, whence the formulation of the anion as $\left[\left(\mathrm{MoO}_{3}\right)_{5}\left(\mathrm{PO}_{4}\right)\left(\mathrm{HPO}_{4}\right)\right]^{5--}$.

Table 6
Intramolecular contact distances, with standard deviation in parentheses

| $\mathrm{N}(1) \cdots \mathrm{O}\left(15^{\text {II }}\right)$ | 2.811 (8) | $\mathrm{N}(5) \cdots \mathrm{O}(23)$ | 2.917(7) |
| :---: | :---: | :---: | :---: |
| N(1) . . W ${ }^{\text {(2) }}$ | 2.823(8) | $\mathrm{N}(5) \cdots \mathrm{O}\left(18^{1 \mathrm{I}}\right)$ | $2 \cdot 924$ (8) |
| $\mathrm{N}(1) \cdots \mathrm{O}\left(13^{\mathrm{vI}}\right)$ | 2.888(7) | $\mathrm{N}(5) \cdots \mathrm{O}\left(2^{\mathrm{VI}}\right)$ | 2.964(8) |
|  |  | $\mathrm{N}(5) \cdots \mathrm{O}\left(20^{\text {II }}\right)$ | $2 \cdot 973$ (7) |
| $\mathrm{N}(2) \cdots \mathrm{O}\left(23^{\mathrm{VII}}\right)$ | 2.708(6) | $\mathrm{N}(5) \cdots \mathrm{O}(7)$ | $2 \cdot 990$ (7) |
| $\mathrm{N}(2) \cdots \mathrm{W}\left(3^{\mathrm{VII}}\right)$ | $2 \cdot 790$ (7) |  |  |
| $\mathrm{N}(2) \cdots \mathrm{O}\left(8^{\text {III }}\right)$ | $2 \cdot 828$ (6) | W(1) $\cdot \cdots \mathrm{O}(1)$ | 2-842(6) |
| $\mathrm{N}(2) \cdots \mathrm{O}(5)$ | $2 \cdot 980$ (6) | $\mathrm{W}(\mathrm{l}) \cdots \mathrm{O}\left(13^{\text {IV }}\right)$ | 2.923(7) |
|  |  | W (1) $\cdots$ N( $4^{\text {IV }}$ ) | 2.988(8) |
| $\mathrm{N}(3) \cdots \mathrm{O}(6)$ | $2 \cdot 790$ (6) | $\mathrm{W}(\mathrm{l}) \cdots \mathrm{N}\left(3^{\mathbf{I V}}\right)$ | $2.995(8)$ |
| $\mathrm{N}(3) \cdots \mathrm{W}\left(3^{\mathrm{VII}}\right)$ | 2.914(8) |  |  |
| $\mathrm{N}(3) \cdots \mathrm{O}\left(7^{\mathrm{VII}}\right)$ | $2 \cdot 915(8)$ | W(2) $\cdots$ N(1) | 2.823(7) |
| $N(3) \cdots W\left(l^{v}\right)$ | $2 \cdot 995(7)$ | $\mathrm{W}(2) \cdots \mathrm{O}\left(11^{\mathrm{III}}\right)$ | $2 \cdot 828$ (7) |
|  |  | $\mathrm{W}(2) \cdots \mathrm{O}(5)$ | 2.907(6) |
| $\mathrm{N}(4) \cdots \mathrm{O}\left(19^{\text {VII }}\right)$ | $2 \cdot 801(8)$ |  |  |
| $\mathrm{N}(4) \cdots \mathrm{O}\left(23^{\text {VIII }}\right)$ | $2 \cdot 842$ (8) | $\mathrm{W}(3) \cdots \mathrm{N}\left(2^{\mathrm{II}}\right)$ | $2 \cdot 760(6)$ |
| $\mathrm{N}(4) \cdots \mathrm{O}(8)$ | $2 \cdot 941$ (6) | W(3) $\cdots \mathrm{O}\left(3^{\mathrm{v}}\right)$ | 2.805(7) |
| N(4) $\cdots$ W ${ }^{\text {I }}$ ) | $2 \cdot 988(8)$ | W(3) $\cdot \cdots \mathrm{O}(2)$ | 2.854(7) |
|  |  | $\mathrm{W}(3) \cdots \mathrm{N}\left(3^{\mathrm{II}}\right)$ | 2.914(8) |

Roman numeral superscripts refer to the following transformations of the co-ordinates:

$$
\begin{array}{lr}
\text { I } \bar{x}, \frac{1}{2}+y, \frac{1}{2}-z & \text { V } \frac{1}{2}-x, 1-y, \frac{1}{2}+z \\
\text { II } \frac{1}{2}+x, \frac{1}{2}-y, 1-z & \text { VI } \frac{1}{2}-x, 1-y,-\frac{1}{2}+z \\
\text { III } x,-1+y, z & \text { VII }-\frac{1}{2}-x, \frac{1}{2}-y, 1-z \\
\text { IV } \bar{x},-\frac{1}{2}+y, \frac{1}{2}-z & \text { VIII }-\frac{1}{2}+x, \frac{3}{2}-y, 1-z
\end{array}
$$

The anions are directly held together by only one contact $<2.73 \AA: \quad \mathrm{O}(21) \cdots \mathrm{O}(22) \quad 2.575 \AA$. This contact is attributed to the presence of a strong hydrogen
bond between the hydrogen phosphate and an oxygen atom of the $\left(\mathrm{MoO}_{3}\right)_{5}$ ring. Table 6 lists contacts $<3 \AA$ between ammonium cations and water molecules. The analysis of these contacts shows that the structure is in fact a network of $\left[\left(\mathrm{MoO}_{3}\right)_{5}\left(\mathrm{PO}_{4}\right)\left(\mathrm{HPO}_{4}\right)\right]^{5-}$ anions joined by hydrogen bonds.

The structure of the $\mathrm{Mo}_{5} \mathrm{O}_{21}$ assemblage can be compared to that of the six molybdenum rings found ${ }^{2}$ in $\mathrm{K}_{6}$ $\left[\left(\mathrm{WO}_{3}\right)_{18}\left(\mathrm{PO}_{4}\right)_{2}\right], 14 \mathrm{H}_{2} \mathrm{O}$, in $\left[\mathrm{NH}_{4}\right]_{6}\left[\left(\mathrm{MoO}_{3}\right)_{6} \mathrm{TeO}_{6}\right], 7 \mathrm{H}_{2} \mathrm{O},{ }^{6}$ and in $\mathrm{NH}_{4}\left[\left(\mathrm{WO}_{3}\right)_{6} \mathrm{H}_{6} \mathrm{O}_{6}\right], 16 \mathrm{H}_{2} \mathrm{O} .{ }^{16}$ These structures have confirmed the model first suggested by Anderson ${ }^{17}$ formed by a crown of six $\mathrm{MO}_{6}$ octahedra. The cavity thus formed contains an octahedral deficiency, with three oxygen atoms located on each face of the cycle. It is thus possible to put a heteroatom within the cavity. In the present case, however, the volume of
the cavity is no longer sufficient to contain a heteroatom. Because of the decrease of the diameter of the ring relative to that with six octahedra, the three oxygen atoms can no longer be bonded to an atom located within the cavity. Thus the two phosphate anions cap the two faces of the $\left(\mathrm{MoO}_{3}\right)_{5}$ ring, and the novel structure therefore results.

We thank Professor P. Souchay and co-workers for the gift of crystals, and the National Research Council of Canada for a post-doctoral fellowship (to L. R.).
[3/602 Received, 22nd March, 1973]

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