

## Single-crystal Raman and Infrared Study of Aluminium Trichloride Hexahydrate

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Single-crystal Raman spectra obtained at 115 K are reported for  $[\text{Al}(\text{OH}_2)_6]\text{Cl}_3$  and its deuteriate. Single-crystal i.r.-reflectance spectra have been recorded at ambient temperature for both materials. All the Raman bands predicted by factor-group analysis (f.g.a.) are observed, as are most of the i.r. bands. On the basis of the f.g.a. an assignment is made of the 'external' modes (wag, twist, and rock) of co-ordinated water with the order wag > twist > rock, and  $\nu_1$  (of  $\text{AlO}_6$ ) is placed at  $524\text{ cm}^{-1}$ . An alternative assignment places  $\nu_1$  at  $701\text{ cm}^{-1}$  but yields less satisfactory force constants. The chief ambiguity remaining is in the location of  $\nu_3$  (of  $\text{AlO}_6$ ) which is probably at ca.  $670\text{ cm}^{-1}$ .

ALTHOUGH much is known about the vibrational motions of water co-ordinated to metal ions, our understanding of these data is still unsatisfactory in many respects. Two reviews<sup>1,2</sup> give the background and summarise data up to 1968. There is relatively little Raman and far-i.r. work on hydrated metal ions in the solid state, the majority of our knowledge being confined to the  $250\text{--}4000\text{ cm}^{-1}$  i.r. region. The principal experimental evidence produced in support of assignments is based on changes induced by deuteration, but very little has been done to establish the symmetries of the modes thus assigned. Despite the faith placed by many workers in normal-co-ordinate analysis (n.c.a.) calculations such as those reported for the i.r.-active modes of  $[\text{M}(\text{OH}_2)_n]^{2+}$

species ( $n = 4$  or  $6$ ),<sup>3</sup> we find such calculations unconvincing in the absence of prior proof of assignment. A strict examination of the real, substantiated, evidence for assignment of hexahydrated cations, in particular, shows that their spectra are less well understood than the very much more complex spectra of the various phases of ice.

In this paper we report our i.r. and Raman work on  $[\text{Al}(\text{OH}_2)_6]\text{Cl}_3$ , for which no recent vibrational study has been made. Three Raman single-crystal investigations were made in the mercury-arc era, two<sup>4,5</sup> being confined to the internal modes of water. The third of these reports dealt with the region of shifts up to  $1000\text{ cm}^{-1}$ ;<sup>6</sup> our work confirms most of their results for the stronger bands but reveals much more detail. The internal modes of water in  $[\text{Al}(\text{OH}_2)_6]\text{Cl}_3$  have also been studied

<sup>1</sup> D. M. Adams, 'Metal-Ligand and Related Vibrations,' Arnold, London, 1967.

<sup>2</sup> G. Brun, *Rev. Chim. minérale*, 1968, **5**, 889.

<sup>3</sup> I. Nakagawa and T. Shimanouchi, *Spectrochim. Acta*, 1964, **20**, 429.

<sup>4</sup> A. Galy, *Compt. rend.*, 1953, **236**, 284.

<sup>5</sup> A. Weil-Marchand, *Compt. rend.*, 1955, **241**, 1456.

<sup>6</sup> G. Champier and A. Galy, *Compt. rend.*, 1954, **B238**, 1708.

by i.r. spectroscopy.<sup>7</sup> Studies of  $[\text{Ni}(\text{OH}_2)_6][\text{SnCl}_6]$ ,<sup>8,9</sup> and  $[\text{Ni}(\text{OH}_2)_6][\text{SO}_4]$ <sup>10</sup> have been made recently and now provide a good basis for understanding hexa-aqua-species, and there are partial Raman studies of  $[\text{Mg}(\text{OH}_2)_6][\text{SO}_4 \cdot \text{H}_2\text{O}]$ <sup>11</sup> and  $[\text{Mg}(\text{OH}_2)_6][\text{PH}_2\text{O}_2]$ .<sup>12</sup>

When water is co-ordinated to a metal ion the three translational and the three rotational degrees of freedom of water become incorporated into those of the complex in ways that have often been described: see, for example, refs. 2 and 13. For a single co-ordinated water molecule there will be a  $\nu(\text{M}-\text{OH}_2)$  mode, two skeletal modes involving deformations of the M-O bond, and three 'external' modes (rock  $\rho_r$ , twist  $\rho_t$ , and wag  $\rho_w$ ; for details see Figure 1 of ref. 13). The energy order of the three external modes has been the subject of some debate, which has been reviewed,<sup>13</sup> but there is now evidence from monohydrated anions, such as  $[\text{FeCl}_5(\text{OH}_2)]^{2-}$ , that the order  $\rho_w > \rho_r$  is usually obeyed, as is to be expected from the relative values of the moments of inertia associated with the rotational motions of water.<sup>13</sup> This is contrary to the order supported by n.c.a. calculations.<sup>3</sup> Deuteration evidence supports the order  $\rho_w > \rho_r > \nu(\text{M}-\text{OH}_2)$ .<sup>8,9,13</sup> Much less is known about  $\rho_t$  because it is likely to be weak in i.r. spectra. It originates as a rotation,  $R(z)$ , of symmetry  $A_2$  for the  $C_{2v}$  free molecule, and  $A_2$  is not associated with i.r. activity. It may become i.r. active in a complex, but it is the symmetry of the field, subtended by the rest of the complex, that creates the possibility that  $\rho_t$  will be seen. In  $[\text{Ni}(\text{OH}_2)_6][\text{SnCl}_6]$ <sup>8</sup> bands at 290(236)  $\text{cm}^{-1}$  (i.r.) and 357(272) and 365(292)  $\text{cm}^{-1}$  (Raman) have been attributed to  $\rho_t$  in the complex (deuteriate values in parentheses): in all the cases these bands were only seen clearly at  $\leq 15$  K and the assignment cannot be

TABLE I

Selected literature data (wavenumbers/ $\text{cm}^{-1}$ ) for mono- and *trans*-diaqua-complexes (deuteriate data in parentheses)

Complex	$\rho_w$	$\rho_r$	$\nu(\text{M}-\text{OH}_2)$		Ref.
			i.r.	Raman	
$\text{K}_2[\text{Fe}^{\text{III}}\text{Cl}_4(\text{OH}_2)_2]$	600	460	390		13
$\text{Cs}_2[\text{Fe}^{\text{III}}\text{Cl}_4(\text{OH}_2)_2]$	540	460	320		13
	(430)	(340)	(310)		
$\text{Rb}_2[\text{Ni}^{\text{II}}\text{Cl}_4(\text{OH}_2)_2]$	621	471	353	342	15
$\text{Cs}_2[\text{Mn}^{\text{II}}\text{Cl}_4(\text{OH}_2)_2]$	570	455	295	290	13
	(430)	(350)	(282)		
$\text{Cs}[\text{Mn}^{\text{III}}\text{F}_4(\text{OH}_2)_2]$	730 <sup>a</sup>	665	370		<i>b</i>
	(525)	(470)	(367)		

<sup>a</sup> The authors preferred not to distinguish between  $\rho_w$  and  $\rho_r$ .

<sup>b</sup> P. Bukovec and V. Kavčič, *J.C.S. Dalton*, 1977, 945.

regarded as well substantiated. Inelastic neutron-scattering<sup>14</sup> studies for several heavily aquated structure types reveals bands attributable to 'external' water

<sup>7</sup> P. J. Lucchesi and W. A. Glasson, *J. Amer. Chem. Soc.*, 1956, **78**, 1347.

<sup>8</sup> J. Jäger and G. Schaack, *Z. Naturforsch.*, 1973, **A28**, 738.

<sup>9</sup> D. M. Adams and W. R. Trumble, *Inorg. Chim. Acta*, 1974, **10**, 235.

<sup>10</sup> Y. S. Jain, H. D. Bist, and A. L. Verma, *J. Raman Spectroscopy*, 1974, **2**, 327.

modes between 300 and 900  $\text{cm}^{-1}$ , a range compatible with results from the many partial (mostly i.r.) studies of aquated complexes. These modes are highly sensitive to metal oxidation state, hydrogen-bonding opportunities, and counter ions, and often show a distinctive thermal dependence. The chief problems in this field are to distinguish the 'external' water modes from  $\nu(\text{M}-\text{OH}_2)$ , and to find for each system the numbers and symmetry species of the modes predicted theoretically. Some helpful background information is collected in Table 1 for mono- and di-hydrated cations. The work on  $\text{Rb}_2[\text{NiCl}_4(\text{OH}_2)_2]$  is of particular value<sup>15</sup> in view of the simplicity of the crystal ( $Z = 1$  in the primitive cell) and the very low temperatures at which the data were collected. The fact that only two bands were found in both i.r. and Raman spectra that could be attributed to 'external' modes is important in indicating that  $\rho_t$  is weak and likely to be absent from spectra. Hexa-aqua-cations will show more bands in each region due to coupling of modes of these types.

## EXPERIMENTAL

Crystals of  $[\text{Al}(\text{OH}_2)_6]\text{Cl}_3$  were grown by slow evaporation of aqueous solutions of  $\text{AlCl}_3$  in  $\text{HCl}-\text{H}_2\text{O}$  (1 : 1 v/v). The

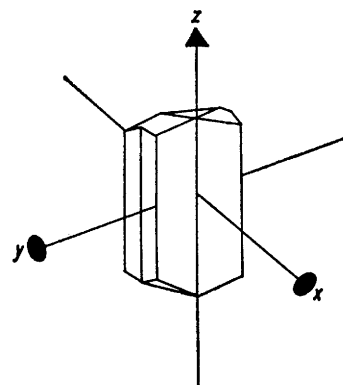


FIGURE 1 Morphology of  $[\text{Al}(\text{OH}_2)_6]\text{Cl}_3$  and the indicatrix axis set used in this work

initially formed precipitate of alumina was filtered off. The composition of the crystals was confirmed by thermogravimetric analysis. The deuteriate was prepared similarly using  $\text{D}_2\text{O}$ , and recrystallised several times from  $\text{D}_2\text{O}$ . The crystals had well developed faces, measured *ca.*  $10 \times 5 \times 2$  mm, and were of excellent optical quality. Extinction directions were located using a polarising microscope and are illustrated in Figure 1. The natural face perpendicular to  $x$  and a face ground and polished normal to  $y$  were used for the Raman study.

Raman spectra were obtained using a Coderg T800 spectrometer, and excited using 514.5-nm radiation from an argon-ion laser. Crystals were mounted on a copper

<sup>11</sup> P. Hillaire, M. Abenoza, and R. Lafont, *Compt. rend.*, 1971, **B273**, 255.

<sup>12</sup> M. Abenoza, P. Hillaire, and R. Lafont, *Comp. rend.*, 1971, **B273**, 297.

<sup>13</sup> D. M. Adams and P. J. Lock, *J. Chem. Soc. (A)*, 1971, 2801.

<sup>14</sup> H. J. Prask and H. Boutin, *J. Chem. Phys.*, 1966, **45**, 3284.

<sup>15</sup> G. E. Shankel and J. B. Bates, *J. Chem. Phys.*, 1976, **64**, 2539.

block with Araldite in a CTI model 20 closed-circuit cryostat and were examined at *ca.* 115 K.

It was impossible to prepare thin enough crystal sections for study by i.r. transmission since the material is deliquescent and mechanically unstable in thin sections. Accordingly these materials were studied in reflectance and the spectra analysed by the Kramers-Krönig procedure to extract the refractive index (*n*), extinction coefficient (*k*), and the real ( $\epsilon'$ ) and imaginary ( $\epsilon''$ ) parts of the complex dielectric constant  $\epsilon^*$ . These quantities are related by  $\epsilon^* = \epsilon' + i\epsilon'' = |n^*|^2$  and  $n^* = n + ik$ . Transverse optical (t.o.) mode frequencies are given by  $\epsilon''$  maxima and by *n/k* crossover points, and longitudinal optical (l.o.) mode frequencies by  $\epsilon'$  nodes and the higher *n/k* crossover points.

Reflectance spectra were obtained from 40 to 1 000  $\text{cm}^{-1}$  at ambient temperature using a Beckman-RIIC FS-720 Fourier spectrometer equipped with a RS-7F reflectance module and Perkin-Elmer wire-grid polarisers. Crystals were mounted on copper discs using epoxy-resin. Many attempts were made to obtain reflectance spectra at low temperatures but these experiments were frustrated by loss of reflectivity at the sample. Attempts to obtain reflectance spectra at  $>1\,000\text{ cm}^{-1}$  using a dispersive instrument also failed due to partial dehydration of the crystals by the heat of the beam.

### THEORY

The compound  $\text{AlCl}_3 \cdot 6\text{H}_2\text{O}$  crystallises with the symmetry of space group  $R\bar{3}c$  ( $D_{3d}^6$ ) in a bimolecular primitive cell.<sup>16,17</sup> A factor-group analysis (f.g.a.) is given in Table 2(a). The

TABLE 2

Factor-group analysis and correlation for crystalline  $[\text{Al}(\text{OH}_2)_6]\text{Cl}_3$

(a) F.g.a.<sup>a</sup>

$D_{3d}^6$	$N_T$	$T_A$	$T$	$R$	$N_S$	$\rho_\omega$	$\rho_r$	$\rho_t$	$\delta$	$\nu$	Activities
$A_{1g}$	10	1	1	2	1	1	1	1	2		$x^2 + y^2, z^2$
$A_{2g}$	11	2	1	2	1	1	1	1	2		
$E_g$	21	3	2	4	2	2	2	2	4		$(x^2 - y^2, xy), (xz, yz)$
$A_{1u}$	11	2	3	1	1	1	1	1	2		
$A_{2u}$	12	1	2	3	1	1	1	1	2		$z$
$E_u$	23	1	4	6	2	2	2	2	4		$(x, y)$

(b) Correlation for skeletal modes of  $\text{AlO}_6$

$O_h$		Site, $S_6$	Crystal, $D_{3d}^6$
$\nu_1$	$a_{1g}$	$A_g$	$A_{1g} + A_{2g}$
$\nu_2$	$e_g$	$E_g$	$2E_g$
$\nu_5$	$t_{2g}$	$A_g + E_g$	$A_{1g} + A_{2g} + 2E_g$
$\nu_3$	$t_{1u}$	$A_u + E_u$	$A_{1u} + A_{2u} + 2E_u$
$\nu_4$	$t_{1u}$	$A_u + E_u$	$A_{1u} + A_{2u} + 2E_u$
$\nu_6$	$t_{2u}$	$A_u + E_u$	$A_{1u} + A_{2u} + 2E_u$

<sup>a</sup>  $N_T$  = Total number of modes =  $3N$ ,  $T_A$  = number of acoustic modes,  $T$  = number of optic branch translatory modes,  $R$  = number of libratory modes,  $N_S$  = number of internal vibrations of  $\text{AlO}_6$ ,  $\rho_\omega$ ,  $\rho_r$ , and  $\rho_t$  = numbers of wag, twist, and rock modes of co-ordinated water,  $\delta = \nu_2$  bending modes of water, and  $\nu = \nu(\text{O-H})$  modes of water. <sup>b</sup> This column sums to  $N_S$ .

correlation scheme of Table 2(b) is helpful in indicating that for the  $\text{AlO}_6$  skeletal modes *A*- and *E*-symmetry bands should be in close proximity because they would be degenerate if the complex ion were of  $O_h$  symmetry. The

<sup>16</sup> K. R. Andress and C. Carpenter, *Z. Krist.*, 1934, **87**, 446.

<sup>17</sup> D. R. Buchanan and P. M. Harris, *Acta Cryst.*, 1968, **B24**, 953.

overall symmetry of  $[\text{Al}(\text{OH}_2)_6]^{3+}$  is  $S_6$  thereby requiring both components of the  $O_h$ -inactive  $\nu_6$  mode to be i.r. active.

The order of the skeletal modes of a regular octahedral

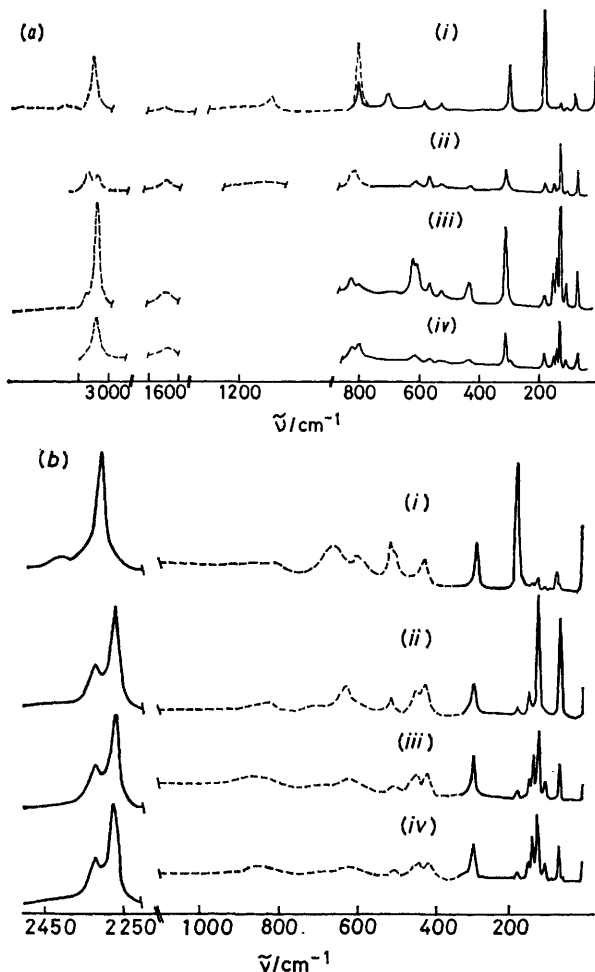


FIGURE 2 Single-crystal Raman spectra for (a)  $[\text{Al}(\text{OH}_2)_6]\text{Cl}_3$  and (b)  $[\text{Al}(\text{OD}_2)_6]\text{Cl}_3$  at 115 K. Spectra were excited with *ca.* 400-mW 514.5-nm radiation at the sample. Spectral slit widths were as indicated in Table 3. (i)  $y(zz)x$ , (ii)  $y(xy)x$ , (iii)  $y(xz)x$ , and (iv)  $y(zy)x$

species follows from the dynamical equations and is  $\nu_1 - (a_{1g}) > \nu_2(e_g) > \nu_5(t_{2g})$ ,  $\nu_3 > \nu_4$  (both  $t_{1u}$ ), and  $\nu_5 \approx 2\nu_6(t_{2u})$ . The position of  $\nu_3$  relative to  $\nu_1$  and  $\nu_2$  (the other two skeletal stretching modes) depends on the magnitude of the *GF* matrix elements<sup>18</sup> and may be greater or less than  $\nu_1$ , but greater than  $\nu_2$ .

### RESULTS AND DISCUSSION

Raman and i.r. data are in Tables 3 and 4, and are illustrated by Figures 2–4. The extinctions between the spectra obtained with different polarising directions are good.

*Assignment.*—The  $<350\text{ cm}^{-1}$  region. In this low-frequency region the only 'external' mode of water that might appear is  $\rho_r$ , judging by values quoted for it. All the other bands will be due to internal vibrations of

<sup>18</sup> K. Nakamoto, 'Infrared Spectra of Inorganic and Coordination Compounds,' Wiley, New York, 1963, p. 267.

the  $\text{AlO}_6$  group, or to lattice modes. In fact, none of the bands in this region shows a large deuteration shift; therefore we may confidently attribute them as follows.

The region below  $200\text{ cm}^{-1}$  shows exactly the numbers of lattice modes predicted by f.g.a. for all the species other than  $E_u$ , for which one is missing or is accidentally degenerate. All the i.r.-active lattice modes are translatory in type (Table 2). The two lowest-energy Raman-active lattice modes [ $71\text{ cm}^{-1}$  ( $E_g$ ) and  $78\text{ cm}^{-1}$  ( $A_g$ )] are considered to be the two expected libratory modes, the others being translatory in type. In accord with these assignments, all modes  $<200\text{ cm}^{-1}$  show very little or no sensitivity to deuteration, except for the highest  $A_g$  mode ( $183\text{ cm}^{-1}$ ) which is reduced in energy by the amount calculated for a simple translation of the  $[\text{Al}(\text{OH}_2)_6]^{3+}$  ion.

The remaining bands at  $<350\text{ cm}^{-1}$  are assigned as components of the  $\text{AlO}_6$   $\nu_6$ ,  $\nu_5$ , and  $\nu_4$  modes. Of these only  $\nu_5$  is allowed to have an  $A_g$  component: the only reasonable assignment for it is at  $295\text{ cm}^{-1}$ , and it is accompanied at  $310\text{ cm}^{-1}$  by the required  $E_g$  component. Taking their degeneracy-weighted average,  $\nu_6 = 2^{-1}\nu_5$  is calculated to be at  $216\text{ cm}^{-1}$ , in near coincidence with the average of the i.r. bands at  $229(A_u)$  and  $209$  and  $218\text{ cm}^{-1}$  ( $E_u$ ) which are accordingly ascribed to  $\nu_6$ .  $\nu_4$  is present at  $309\text{ cm}^{-1}$  ( $A_{2u}$ ), but no  $E_u$  component was seen

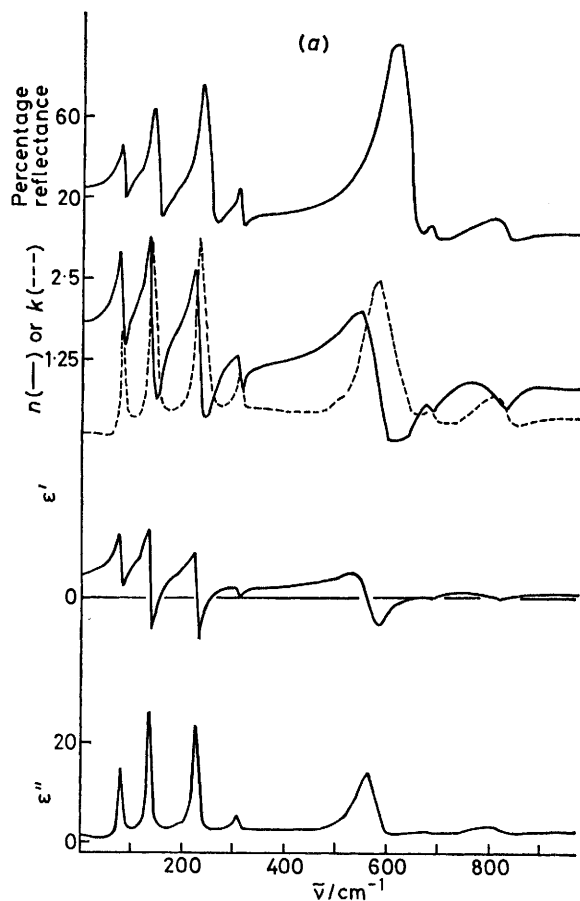


FIGURE 3

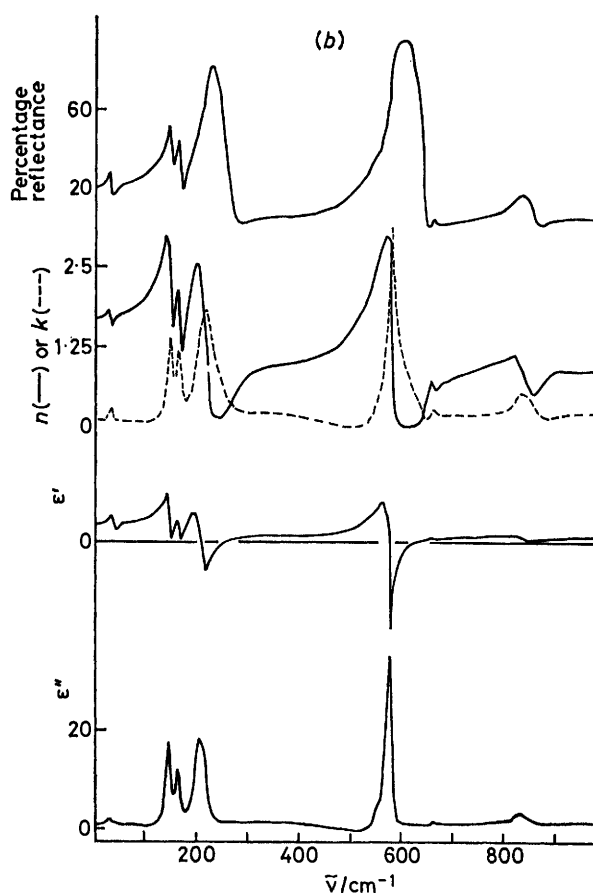


FIGURE 3 Single-crystal i.r. reflectance spectra and derived parameters for  $[\text{Al}(\text{OH}_2)_6]\text{Cl}_3$  at ambient temperature: (a)  $A_{2u}$  modes, (b)  $E_u$  modes

at ambient temperature in either the hydrate or the deuterate. However, a weak band was found at  $327\text{ cm}^{-1}$  in a mull of the hydrate at liquid-nitrogen temperature. All these modes show a deuteration shift as is required by forms of their  $G$ -matrix elements, but these shifts are very much smaller than those of the 'external' water modes. Thus  $\nu_5' = \nu_5[m(\text{H}_2\text{O})/m(\text{D}_2\text{O})]^{1/2}$ ; taking masses of 18 and 20 respectively we have the following assignments ( $\text{cm}^{-1}$ ):

$$\nu_5 \begin{cases} 310 \\ 295 \end{cases} \quad \nu_5' \text{ (calc.)} \begin{cases} 294 \\ 278 \end{cases} \quad \nu_5' \text{ (obs.)} \begin{cases} 291 \\ 284 \end{cases}$$

These are in good agreement in view of the crudity of the model.

*The 350—1 000  $\text{cm}^{-1}$  region.* This region contains all the 'external' modes of water (since  $\rho_r$  is shown to be absent at  $<350\text{ cm}^{-1}$ ) together with the  $\text{AlO}_6$  vibrations  $\nu_1$ ,  $\nu_2$ , and  $\nu_3$ . It is here that the real assignment problems arise. The  $A_g$  spectrum should show four bands in this range due to  $\nu_L$ ,  $\rho_\omega$ ,  $\rho_r$ , and  $\rho_r$  (Table 2): four were observed. Similarly, the  $E_g$  spectrum shows exactly the number of bands predicted for the 'external' mode region of co-ordinated water. Of itself this is of significance because these bands must include the elusive  $\rho_r$  and, moreover, place a lower limit at  $524\text{ cm}^{-1}$  on it.

All the four  $A_g$  bands in this region (524, 584, 701, and 800  $\text{cm}^{-1}$ ) are substantially shifted by deuteration, but

Applied to each of the four  $A_g$  modes we have the assignments ( $\text{cm}^{-1}$ ):

TABLE 3

Raman wavenumbers ( $\text{cm}^{-1}$ ) and relative intensities <sup>a</sup> for single-crystal  $[\text{Al}(\text{OH}_2)_6]\text{Cl}_3$  and its deuteriate

$\nu/\text{cm}^{-1}$	$y(\text{zz})x$	$y(xy)x$	$y(xz)x$	$y(\text{zy})x$	Assignment
(a) $[\text{Al}(\text{OH}_2)_6]\text{Cl}_3$					
71	$E_g$		20	40	15 } $\nu_R$
78	$A_{1g}$	15			
110	$E_g$		15	22	10 } $\nu_T$
128	$E_g$		74	100	35 } $\nu_T$
138	$E_g$		37	50	20 } $\nu_T$
150	$E_g$		18	30	14 } $\nu_T$
183	$A_{1g}$	100	8	10	13 } $\nu_s$
295	$A_{1g}$	42			
310	$E_g$		50	80	33 } $\nu_s$
432	$E_g$		5	14	5 } $\nu_2$
524	$A_{1g}$	5			
534	$E_g$		5	8	3 } $\nu_1$
566	$E_g$		10	10	5 } $\nu_1$
584	$A_{1g}$	10			
610	$E_g$		8	30	7 } $\rho\omega, \rho\tau, \rho_r$
622	$E_g$		6	35	8 } ('external' $\text{H}_2\text{O}$ modes)
701	$A_{1g}$	15			
800	$A_{1g}$	30		5	10 } $\nu_1(\text{H}_2\text{O})$
825	$E_g$		15 <sup>b</sup>	12	12 } $\nu_3(\text{H}_2\text{O})$
1 094	$A_{1g}$	15			
1 645	$A_{1g} + E_g$	3	8	10	6 } $\delta(\text{OH}_2)$
3 045	$E_g$		13	80	30 } $\nu_1(\text{H}_2\text{O})$
3 053	$A_{1g}$	45			
3 076	$E_g$		18	11	
3 162	$A_{1g}$	3			
3 289	$A_{1g}$	2			2 $\times \delta(\text{OH}_2)$
(b) $[\text{Al}(\text{OD}_2)_6]\text{Cl}_3$					
71	$E_g$		70	25	25 } $\nu_R$
78	$A_{1g}$	20			
109	$E_g$			12	13 } $\nu_T$
128	$E_g$		80	48	50 } $\nu_T$
139	$E_g$			30	30 } $\nu_T$
149	$E_g$		15	15	14 } $\nu_T$
180	$A_{1g}$	90			
284	$A_{1g}$	30			
291	$E_g$		20	30	25 } $\nu_s$
418	$A_{1g} + E_g$	10	15	10	8 } $\nu_2 + \text{'external'}$
					( $\text{D}_2\text{O}$ )
443	$E_g$		(10)	10	8 } $\nu_1(504 \text{ cm}^{-1})$ and
497	$A_{1g}$	10			
504	$A_{1g} + E_g$	15	7	6	4 } $\rho\omega, \rho\tau, \rho_r$
593	$A_{1g}$	8			
617	$E_g$		15	8	5 } ('external' $\text{D}_2\text{O}$ modes)
650	$A_{1g}$	12			
820	$E_g$		5	6	5 } $\delta(\text{OD}_2)$
(1 208) <sup>b</sup>	$E_g$				
2 272	$E_g$		60	60	60 } $\nu_1(\text{D}_2\text{O})^c$
2 309	$A_{1g}$	85			
2 320	$E_g$		28	25	25 } $\nu_3(\text{D}_2\text{O})^c$
2 416	$A_{1g}$	18			2 $\times \delta(\text{OD}_2)$

<sup>a</sup> In part (a) spectral slit widths for  $y(\text{zz})x$  experiments were 1.5  $\text{cm}^{-1}$  for bands at  $<800 \text{ cm}^{-1}$ , 3.3  $\text{cm}^{-1}$  for bands at  $>800 \text{ cm}^{-1}$ . Equivalent settings for all the other orientations were 2.4 and 4.7  $\text{cm}^{-1}$  respectively. In part (b), for all the crystal orientations, modes in the 0–300 and 1 000–3 100  $\text{cm}^{-1}$  intervals were recorded at a spectral slit width of 1  $\text{cm}^{-1}$ , those from 300 to 1 000  $\text{cm}^{-1}$  at 2.9  $\text{cm}^{-1}$ . <sup>b</sup> Calculated from predicted isotope shift: <sup>23</sup>  $\delta(\text{D}_2\text{O}) = \delta(\text{H}_2\text{O}) \times 0.732$ . <sup>c</sup> Assignment based on deuteration shift relations: <sup>23</sup>  $\nu_1'(\text{D}_2\text{O}) = \nu_1(\text{H}_2\text{O}) \times 0.723$ ; and  $\nu_3'(\text{D}_2\text{O}) = \nu_3(\text{H}_2\text{O}) \times 0.732$ .

it is not immediately obvious which band shifts to where when relating the two spectra. The shift in  $\nu_1$  on deuteration is given by  $\nu_1' = \nu_1[m(\text{H}_2\text{O})/m(\text{D}_2\text{O})]^{\frac{1}{2}}$ .

$A_g$ mode ( $\text{H}_2\text{O}$ )	$\nu_1'$ (calc.)	$A_g$ mode ( $\text{D}_2\text{O}$ ) obs.
524	497	418
584	554	504
701	665	593
800	759	650

Since the highest  $A_g$  mode in the deuteriate is at 650  $\text{cm}^{-1}$  it is plain that  $\nu_1$  cannot be at 800  $\text{cm}^{-1}$ , and the

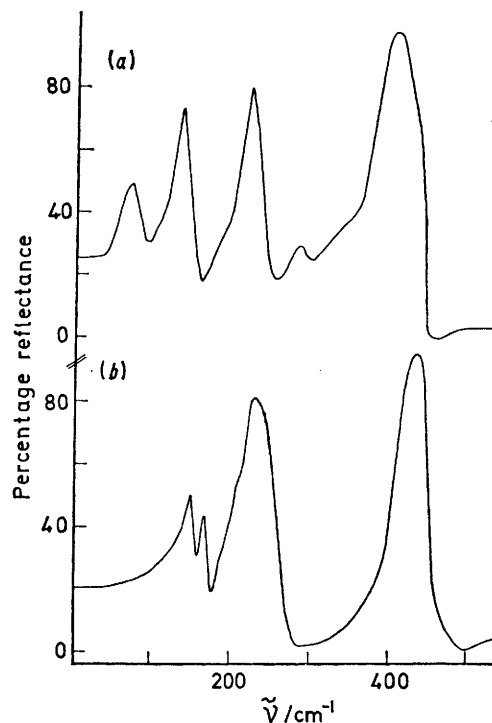


FIGURE 4 Single-crystal i.r. reflectance spectra for  $[\text{Al}(\text{OD}_2)_6]\text{Cl}_3$  at ambient temperature: (a)  $A_{2u}$  modes, (b)  $E_u$  modes

TABLE 4

Infrared wavenumbers ( $\text{cm}^{-1}$ ) for (a) single-crystal  $[\text{Al}(\text{OH}_2)_6]\text{Cl}_3$  and its deuteriate (in parentheses) at ambient temperature, and (b) a mull of the hydrate at liquid-nitrogen temperature

(a)	$A_{2u}$	$E_u$	Assignment
		55	
	82 (80)	151 (151)	$\nu_T$
	138 (138)	167 (167)	
	229 (215)	209 <sup>a</sup> (208)	$\nu_6$
		218	
	309 (282)		$\nu_4$
	560 (400)	580 (420)	$\rho_r$
	678	664	$\nu_3$
	790 [588] <sup>b</sup>	836 [623]	$\rho\omega$
(b)	57m $E_u$	205s $E_u$	$\nu_6$
	92m $A_{2u}$	224s $E_u$	
	145(sh) $A_{2u}$	250s $A_{2u}$	$\nu_4$
	154s $E_u$	316m $A_{2u}$	
	174s $E_u$	327w $E_u$	

<sup>a</sup> The shape of the reflectance band and Kramers–Krönig analysis both indicate the presence of two bands, and mull spectra at low temperature show an additional peak in this region. <sup>b</sup> Calculated position for deuteriate taking  $\rho = 0.745$  [i.e.  $(I_s/I_a)^{\frac{1}{2}}$ ].

shift required for the band at 584 cm<sup>-1</sup> also eliminates it as a possible  $\nu_1$ . However, the bands could be paired either as 800(593), 701(650), 584(504), and 524(418) cm<sup>-1</sup> for  $\nu_1$  at 701, or as 800(650), 701(593), 584(418), and 524(504) cm<sup>-1</sup> for  $\nu_1$  at 524 cm<sup>-1</sup>.

We now consider three lines of argument aimed at resolving this problem. First, we note that there have been several Raman studies<sup>19-21</sup> of aqueous solutions of AlCl<sub>3</sub> which agree in showing bands at <sup>20</sup>525 (polarised) ( $\nu_1$ ), 447 (depolarised) ( $\nu_2$ ), and 340 cm<sup>-1</sup> ( $\nu_5$ ), with deuteriate values of 503, 433, and 313 cm<sup>-1</sup> respectively. These are very close to bands observed in solid [Al(OH<sub>2</sub>)<sub>6</sub>]Cl<sub>3</sub> and its deuteriate and support the lower value for  $\nu_1$ . We assign  $\nu_2$  to the  $E_g$  band at 432 cm<sup>-1</sup> which is in a reasonable position relative to  $\nu_5$ .

Secondly, having now assigned  $\nu_1$  (two possibilities),  $\nu_2$ , and  $\nu_5$  we may use them to determine the three force constants necessary to describe an octahedral complex on the basis of the Urey-Bradley force field, and hence to calculate the positions of  $\nu_3$  and  $\nu_4$ . The results were:

	$\nu_3$ (calc.)	$\nu_4$ (calc.)	$\nu_4$ (obs.)	$K$	$F$	$H$
$\nu_1 = 701$	591	209	309	1.22	0.92	-0.28
$\nu_1 = 524$	653	319	321	1.79	0.26	0.09

Here  $K$  is the Al-O bond-stretching force constant,  $F$  is the stretch-stretch interaction, and  $H$  the angle-bending force constant (in 10<sup>-5</sup> m dyn Å<sup>-1</sup>).\* The Al-O distance was taken as 1.88 Å.<sup>17,22</sup>

These results strongly support the lower choice for  $\nu_1$ . The calculated value of  $\nu_4$  is very close to that observed, and  $K$  and  $F$  have reasonable magnitudes. In contrast  $F$  is too big relative to  $K$  for  $\nu_1$  at 701 cm<sup>-1</sup>. A similar calculation for the deuteriate, with  $\nu_1$  at 504 cm<sup>-1</sup>, gave  $\nu_3$  at 644 and  $\nu_4$  at 302 cm<sup>-1</sup> [cf.  $\nu_4$  (obs.) at 282 cm<sup>-1</sup>]. We defer further consideration of  $\nu_3$ .

The third line of reasoning by which the  $\nu_1$  assignment may be illuminated begins by noting that for each  $\rho_r$ ,  $\rho_\omega$ , and  $\rho_r$  mode there should be a group of three bands bearing the symmetry labels  $A_g$ ,  $E_g$ , and  $E_g$  (Table 2). How much splitting there might be between the members of a group may be guessed at from the behaviour of  $\nu$ (OH) and  $\delta$ (HOH). The latter shows no detectable splitting between the  $A_g$  and  $E_g$  components. The  $\nu$ (OH) bands are all low compared with situations in which little or no hydrogen bonding is possible {e.g. 3 300 and 3 400 cm<sup>-1</sup> in the Raman spectrum<sup>15</sup> of *trans*-[NiCl<sub>4</sub>(OH<sub>2</sub>)<sub>2</sub>]<sup>2-</sup>}. The two predicted  $A_g$  components are due to  $\nu_1$  and  $\nu_3$  of H<sub>2</sub>O respectively, but two of the  $E_g$  modes are missing. The most probable assignment is to regard the two observed  $E_g$  bands as components, of  $\nu_1$ , which then shows a total Davydov splitting of 31 cm<sup>-1</sup>. It is evident that the water molecules vibrating around Al<sup>3+</sup> are coupled but not very strongly. From this we deduce that there should be equally modest splittings between the components of  $\rho_\omega$ ,  $\rho_r$ , and  $\rho_r$ .

\* Throughout this paper: 1 dyn = 10<sup>-5</sup> N.

<sup>19</sup> J. P. Mathieu, *Compt. rend.*, 1950, **231**, 896.

<sup>20</sup> A. da Silveira, M. A. Marques, and N. M. Marques, *Compt. rend.*, 1961, **252**, 3983.

Armed with this insight we consider two alternative groupings, depending on the choice of  $\nu_1$ . Thus:

$\nu_1 = 524$	$\rho_r$	$\rho_\omega$	$\rho_r$	} Raman
	825 $E_g$	701 $A_{1g}$	584 $A_{1g}$	
	800 $A_{1g} + E_g$	622 $E_g$	566 $E_g$	
		610 $E_g$	534 $E_g$	
$\Delta\nu/\text{cm}^{-1}$		836wm $E_u$	(678w $A_{2u}$ )	580vs $A_{2u}$
		790wm $A_{2u}$	(664w $E_u$ )	560vs $E_u$
	46	91	50	} i.r.
or				
$\nu_1 = 701$	$\rho_r$	$\rho_\omega$	$\rho_r$	} Raman
	825 $E_g$	622 $E_g$	566 $E_g$	
	800 $A_{1g} + E_g$	610 $E_g$	534 $E_g$	
		584 $A_{1g}$	524 $A_{1g}$	
$\Delta\nu/\text{cm}^{-1}$	46	94	56	

Here the i.r. assignment is the same in each case and the values in parentheses will be commented on later. The total Davydov splitting,  $\Delta\nu$ , is relatively large for the middle group of bands whichever choice of  $\nu_1$  is made.

In this region both  $A_{2u}$  and  $E_u$  i.r. spectra show reflectance bands at similar positions (Figure 3) and of comparable intensities. The  $A_{2u}$  spectrum has three of the four bands predicted but the  $E_u$  spectrum shows only three of the theoretical eight. The reason for this deficiency is simply that the coupling between the two complex ions in the primitive unit cell is weak. This is no surprise in that, physically, coupling must be *via* the weakly hydrogen-bonded chlorides which separate the complex ions. In this situation the appropriate selection rules are those of the site group ( $S_6$ ) which describes the symmetry of the field acting on one complex ion [Table 2(b)]. This correctly accounts for the observation that  $\nu_2$  and  $\nu_5$  show only one  $E_g$  component each. Since the  $A_{2g}$  modes are inactive no further test of the strength of the correlation field can be made for these modes. The exception to this behaviour is  $\nu_6$  for which both  $E_u$  components were seen in mull spectra at low temperature, and for which the shape of the  $\epsilon''$  function, calculated from room-temperature data, indicates that two components are present *ca.* 210 cm<sup>-1</sup>.

The appellations  $\rho_\omega$ ,  $\rho_r$ , and  $\rho_r$  applied to the bands grouped above are supported by the following considerations, neglecting for the moment the fact that we have yet to locate  $\nu_3$  in our spectra. For a free water molecule the rotational motions that in a co-ordination complex become  $\rho_\omega$ ,  $\rho_r$ , and  $\rho_r$  have moments of inertia in the ratios 1:1.9:2.9. When water is co-ordinated to a metal ion these moments of inertia are altered since the Al-O axis probably lies at *ca.* 110° to the HOH plane and the mass of the rest of the complex must be considered. Nevertheless, the largest displacements will still be associated with the hydrogen atoms. Therefore we take, as a working hypothesis, the order  $\rho_\omega > \rho_r > \rho_r$  for the 'external' modes of co-ordinated water. There is good evidence that, at least in mono- and di-aquated complexes,  $\rho_\omega > \rho_r$  but the place of  $\rho_r$  is unsettled. We propose that it lies between the other two, at least in hexa-aqua-complexes. Secondly, the feebleness of the i.r.

<sup>21</sup> A. da Silveira, M. A. Marques, and N. M. Marques, *Mol. Phys.*, 1965, **9**, 271.

<sup>22</sup> T. E. Hopkins, A. Zalkin, and D. H. Templeton, *Inorg. Chem.*, 1969, **8**, 2421.

bands tentatively attributed to  $\rho_r$  is consistent with this assignment because  $\rho_r$  arises from a motion inactive in  $C_{2v}$ , made active only by the field subtended by the surroundings.

We return to the problem of the location of  $\nu_3$ . Since the evidence now strongly favours  $\nu_1$  at  $524\text{ cm}^{-1}$  we must look for  $\nu_3$  near the calculated position of  $653\text{ cm}^{-1}$ , shifting to  $644\text{ cm}^{-1}$  in the deuteriate. These values do not exactly coincide with any observed i.r. bands. Two possible assignments may be advanced. First,  $\nu_3$  is roughly coincident with the intense bands at  $560\text{ cm}^{-1}$  ( $A_{2u}$ ) and  $580\text{ cm}^{-1}$  ( $E_u$ ) or, more probably, near their high-frequency edges. However, the assignment of these intense bands to  $\rho_r$  modes cannot be disturbed since they both suffer very large deuteration shifts to  $400\text{ cm}^{-1}$  ( $\rho\ 0.71$ ) and  $420\text{ cm}^{-1}$  ( $\rho\ 0.72$ ) respectively, which are very close to the expected  $\rho = 0.72$  for rocking modes as calculated either by taking  $(I_c/I_c')^{\frac{1}{2}}$  (where  $I_c$  is the moment of inertia of water about the  $c$  axis) or by Krimm's method.<sup>23</sup> Unfortunately the i.r.-reflectance spectra for the deuteriate in the  $>500\text{ cm}^{-1}$  region were of much lower quality than those of the hydrate. It was not possible to be certain whether or not there were weak bands at *ca.*  $644\text{ cm}^{-1}$  that might be attributed to  $\nu_4$ . Alternatively, we might assign  $\nu_3$  to the weak bands at  $664$  and  $678\text{ cm}^{-1}$  which were considered above as candidates for  $\rho_r$ . Suppressing our natural feeling that  $\nu_3$  should be intense, this second alternative makes sense because the missing  $A_{2u}$  band is now  $\rho_r$  and not  $\nu_3$ , which is more probable than the reverse. Removal of these two bands from the groupings above does not reduce the Davydov splitting attributed to  $\rho_r$  for  $\nu_1$  at  $524\text{ cm}^{-1}$ , although it would for  $\nu_1$  at  $701\text{ cm}^{-1}$ , at the expense of much greater ambiguities.

In the  $E_g$  spectrum of the deuteriate it appears that some of the observed bands must be ascribed to more than one mode since fewer bands were found than in the hydrate and the span of the spectrum will be reduced by the shifts. We note that all these  $E_g$  bands are due to 'external' modes of co-ordinated water since we have

<sup>23</sup> S. Krimm, *J. Chem. Phys.*, 1960, **32**, 1780; values for water calculated by R. W. Berg (personal communication).

previously located  $\nu_2$  at  $432\text{ (418)}\text{ cm}^{-1}$ . On the basis of relative intensities, equivalents are proposed as follows [ $\rho = \nu(\text{D})/\nu(\text{H})$ ]:

Protiate	Deuteriate	$\rho$
534	418	0.78
566	443	0.78
610	504	0.83
825	617	0.75

The deuteriate assignments are not entirely satisfactory. For their definitive and final assignment much more detailed experimental evidence must be obtained over a range of temperature for both i.r. and Raman spectra in the  $350\text{--}1\ 000\text{ cm}^{-1}$  region.

Comparison of our assignment with those for  $\text{MO}_6$  skeletal modes of  $[\text{M}(\text{OH}_2)_6]^{2+}$  ions ( $\text{M} = \text{Mg}$  or  $\text{Ni}$ ) (Table 5) shows that all the frequencies are considerably

TABLE 5

Comparison of skeletal modes (wavenumbers/ $\text{cm}^{-1}$ ) for  $[\text{Mg}(\text{OH}_2)_6][\text{H}_2\text{PO}_2]^{12}$ ,  $[\text{Ni}(\text{OH}_2)_6][\text{SnCl}_6]^{18}$  and  $[\text{Al}(\text{OH}_2)_6]\text{Cl}_3$

$[\text{Mg}(\text{OH}_2)_6]^{2+}$	$[\text{Ni}(\text{OH}_2)_6]^{2+}$	$[\text{Al}(\text{OH}_2)_6]^{3+}$	Assignment
	142, 146	209, 208, 229	$\nu_6$
268—285 <sup>a</sup>	209, 191	295, 310	$\nu_5$
200—215 <sup>b</sup>	209, 207	309, 327	$\nu_4$
421	333, 381	664, 678	$\nu_3$
310	301	432	$\nu_2$
363	382	524	$\nu_1$

<sup>a</sup> Five bands. <sup>b</sup> Four bands.

raised by the greater charge on aluminium. Since the masses of Al and Mg are similar, the differences between their hexa-aqua-complex vibrational frequencies are almost entirely due to this charge difference. For  $\text{M} = \text{Ni}$  there is a further reduction in  $\nu_2$ ,  $\nu_3$ , and  $\nu_5$  due to the increased mass of the metal. Equivalent reductions are seen for the 'external' water modes for which the highest values are  $660$  (Raman) and  $662$  (i.r.) for  $\text{M} = \text{Ni}$ , and  $825$  (Raman) and  $836\text{ cm}^{-1}$  (i.r.) for  $\text{M} = \text{Al}$ .

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