# Triaquahenicosatungstodiphosphate(6-) Heteropolyanion, $\left[\mathrm{P}_{2} \mathbf{W}_{21} \mathrm{O}_{71}\left(\mathrm{OH}_{2}\right)_{3}\right]^{6-}$ : $X$-Ray Crystallographict and ${ }^{183} \mathbf{W}$ Nuclear Magnetic Resonance Structural Studies 

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The single-crystal $X$-ray structure of $\mathrm{K}_{4} \mathrm{H}_{2}\left[\mathrm{P}_{2} \mathrm{~W}_{21} \mathrm{O}_{71}\left(\mathrm{OH}_{2}\right)_{3}\right] \cdot 28 \mathrm{H}_{2} \mathrm{O}$ [space group $P 6_{3} / m m c, a=$ 16.295(2), $c=19.771$ (5) $\AA$, and $Z=2$; Mo radiation, $R=0.037$ for 1042 unique data] has been determined and the ${ }^{183} \mathrm{~W}$ n.m.r. spectrum of the anion in $\mathrm{H}_{2} \mathrm{O}-\mathrm{D}_{2} \mathrm{O}$ has been recorded. The anion has true point symmetry $C_{2 v}$ but occupies a $D_{3 h}$ site in the crystal with orientational disorder about a crystal three-fold axis. It contains two $\alpha-\mathrm{A}-\mathrm{PW}_{9} \mathrm{O}_{34}{ }^{9}$ units, each with $C_{3 v}$ symmetry, linked through three equatorial $\mathrm{WO}\left(\mathrm{OH}_{2}\right)^{4+}$ units. Two equatorial W atoms are closer to, and the third is further from, the anion (crystal $C_{3}$ ) axis. The $\mathrm{H}_{2} \mathrm{O}$ ligand on the unique $W$ is directed towards the interior of the anion and is hydrogen-bonded to the oxo ligand, also directed internally, on each of the other equatorial $W$.

The partial degradation of the $\left[\mathrm{PW}_{12} \mathrm{O}_{40}\right]^{3-}$ heteropolyanion by aqueous base affords $\left[\mathrm{PW}_{11} \mathrm{O}_{39}\right]^{7-}$, from which $\left[\mathrm{PW}_{12^{-}}\right.$ $\left.\mathrm{O}_{40}\right]^{3-}$ is regenerated on acidification together with a second heteropolyanion of partial empirical formula $\mathrm{P}_{2} \mathrm{~W}_{21} \cdot{ }^{1}$ The latter has received little attention since it was first reported, apart from one study ${ }^{2}$ which confirmed the $P: W$ ratio but gave no structural information. Our interest in this anion was stimulated by the preparation ${ }^{3}$ of what appear to be derivatives in which two W atoms have been replaced by $\mathrm{Co}^{11}$, etc., and by the characterization of an $\mathrm{As}^{\mathrm{II}}{ }_{2} \mathrm{~W}_{21}$ heteropolyanion and its substitution products, ${ }^{4}$ including the $X$-ray structural analysis ${ }^{5}$ of $\mathrm{Rb}_{4} \mathrm{H}_{2}\left[\mathrm{As}_{2} \mathrm{~W}_{21} \mathrm{O}_{69}\left(\mathrm{OH}_{2}\right)\right] \cdot 34 \mathrm{H}_{2} \mathrm{O}$. $X$-Ray diffraction is nowadays a routine method for determining the structures of heteropolyanions, ${ }^{6}$ but the resolution obtainable is frequently limited by orientational disorder. In recent years ${ }^{78183} \mathrm{~W}$ n.m.r. spectroscopy has proved to be a powerful complementary technique. The number and relative intensities of ${ }^{183} \mathrm{~W}$ resonances will often directly distinguish between possible isomeric structures, ${ }^{8}$ and further information is furnished by the analysis of $\mathrm{W}-\mathrm{W}$ coupling, ${ }^{9}$ including two-dimensional spectroscopy. ${ }^{10}$ We have made use of both $X$-ray and n.m.r. methods in the present work.

## Results and Discussion

Chemical analysis confirms that the anion is a 21 -tungstodiphosphate and indicates that the charge is -6 . We formulate the anion as $\left[\mathrm{P}_{2} \mathrm{~W}_{21} \mathrm{O}_{71}\left(\mathrm{OH}_{2}\right)_{3}\right]^{6-}$ for reasons which will be set out below.

Crystallographic Results.-The anion (Figure 1) in $\mathrm{K}_{4} \mathrm{H}_{2}$ $\left[\mathrm{P}_{2} \mathrm{~W}_{21} \mathrm{O}_{71}\left(\mathrm{OH}_{2}\right)_{3}\right] \cdot 28 \mathrm{H}_{2} \mathrm{O}$ lies at a site of crystallographic point symmetry $\overline{6} 2 m\left(D_{3 h}\right)$ in space group $P 6_{3} / \mathrm{mmc}$. Atomic coordinates are given in Table 1. The site symmetries for $\mathrm{P}, \mathrm{W}(1)$, and $\mathrm{W}(3)$ are respectively $3 m, m$, and $m m ; W(2)$ is at a general position. The anion contains two $x-\mathrm{A}-\mathrm{PW}_{9} \mathrm{O}_{34}{ }^{9-}$ moieties (for

[^0]the notation designating isomers, see ref. 11), each of which is derived from the well known Keggin ( $x-\mathrm{PW}_{12} \mathrm{O}_{40}{ }^{3-}$ ) structure ${ }^{12}$ by the removal of three adjacent corner-sharing $\mathrm{WO}_{6}$


Figure 1. The $\left[\mathrm{P}_{2} \mathrm{~W}_{21} \mathrm{O}_{71}\left(\mathrm{OH}_{2}\right)_{3}\right]^{6-}$ anion

Table 1. Atomic co-ordinates $\left(\times 10^{4}\right)$ for $\mathrm{K}_{4} \mathrm{H}_{2}\left[\mathrm{P}_{2} \mathrm{~W}_{21} \mathrm{O}_{71},\left(\mathrm{OH}_{2}\right)_{3}\right]$. $28 \mathrm{H}_{2} \mathrm{O}$

| Atom | $x$ | $y$ | $z$ |
| :--- | :--- | :--- | :--- |
| $\mathrm{~W}(1)$ | $4029.3(5)$ | $5970.7(5)$ | $4349.3(6)$ |
| $\mathrm{W}(2)$ | $3267.9(7)$ | $4477.4(6)$ | $5884.5(4)$ |
| $\mathrm{W}(3 \mathrm{e})^{a}$ | $2001.2(23)$ | $7998.8(23)$ | 7500 |
| $\mathrm{~W}(3 i)^{b}$ | $2213.9(21)$ | $7786.1(21)$ | 7500 |
| P | 3333 | 6667 | $5813(7)$ |
| K | $4940(8)$ | $5059(8)$ | 7500 |
| $\mathrm{O}(1)$ | $4439(8)$ | $5561(8)$ | $3698(11)$ |
| $\mathrm{O}(11)$ | $2790(8)$ | $7210(8)$ | $3958(10)$ |
| $\mathrm{O}(22 \mathrm{a})$ | $4499(7)$ | $5501(7)$ | $6101(10)$ |
| $\mathrm{O}(22 \mathrm{~b})$ | $1927(8)$ | $8073(8)$ | $5701(11)$ |
| $\mathrm{O}(2 \mathrm{P})$ | $2821(8)$ | $7179(8)$ | $6068(10)$ |
| $\mathrm{O}(12)$ | $3462(9)$ | $4963(9)$ | $4986(7)$ |
| $\mathrm{O}(2)$ | $3455(12)$ | $3561(12)$ | $5777(7)$ |
| $\mathrm{O}(23)$ | $2977(10)$ | $8651(11)$ | $6824(7)$ |
| $\mathrm{O}(1 \mathrm{P})$ | 3333 | 6667 | $5031(15)$ |
| $\mathrm{O}(3 \mathrm{e})$ | $14448(12)$ | $8552(12)$ | 7500 |
| $\mathrm{O}(31 \mathrm{i})^{a}$ | $3092(104)$ | $7364(102)$ | 7500 |
| $\mathrm{O}(32 \mathrm{i})^{a}$ | $2847(33)$ | $7153(33)$ | 7500 |
| $\mathrm{Aq}(1)^{c}$ | $1679(19)$ | $8321(19)$ | $4114(21)$ |
| $\mathrm{Aq}(2)^{c}$ | $7265(44)$ | $2735(44)$ | 7500 |
| $\mathrm{Aq}(3)^{c}$ | $6882(94)$ | $5979(86)$ | $6899(46)$ |

${ }^{a}$ Site occupancy factor $\frac{1}{3} \cdot{ }^{b}$ Site occupancy factor $\frac{2}{3}$. ${ }^{\text {c }}$ Water molecule.
octahedra and consists of a 'cap' of three edge-sharing octahedra $[W(1)]$ and a 'belt' of six octahedra [W(2)]. The belt octahedra are linked by alternate corner- and edge-sharing, and also share corners with the cap. Each W(3) atom in the equatorial plane of the anion is linked via $O(23)$ atoms with a pair of edge-linked $\mathrm{WO}_{6}$ octahedra in the belt above, and with a pair in the belt below, i.e. is bonded to oxygen atoms at the vertices exposed by the generation of $\mathrm{PW}_{9} \mathrm{O}_{34}{ }^{9-}$ from $\mathrm{PW}_{12} \mathrm{O}_{40}{ }^{3-}$. The anion exhibits three-fold disorder about the principal axis. The $X$-ray analysis shows that each $\mathrm{W}(3)$ is split between adjacent exterior and interior $m m$ sites, W(3e) (more distant from the principal axis) and $\mathrm{W}(3 \mathrm{i})$ (nearer the axis). The refinement of alternative models and of the site-occupancy factors strongly indicates that these equatorial sites are occupied in the ratio $\mathrm{W}(3 \mathrm{e}): \mathrm{W}(3 \mathrm{i})=1: 2$. Thus the true anion symmetry, as confirmed by the ${ }^{183} \mathrm{~W}$ n.m.r. spectrum, is mm $\left(C_{2 v}\right)$. The disorder as revealed by $X$-rays is nevertheless confined to the equatorial plane. There are no indications of alternative sites for $\mathrm{W}(1)$ and $\mathrm{W}(2)$, and the $\mathrm{W}-\mathrm{O}, \mathrm{P}-\mathrm{O}$, and $\mathrm{W} \cdot \mathrm{W}$ W distances in the $\mathrm{PW}_{9} \mathrm{O}_{34}{ }^{9-}$ moieties (Table 2) agree well with the values found ${ }^{13}$ for the similar units in $x$ $\left[\mathrm{P}_{2} \mathrm{~W}_{18} \mathrm{O}_{62}\right]^{6-}$ and $\left[\mathrm{KP}_{2} \mathrm{~W}_{20} \mathrm{O}_{72}\right]^{13-}$.

Three oxygen atoms $\mathrm{O}(3 \mathrm{e})$ lie in the equatorial plane, at mm sites exterior to the $\mathrm{W}(3 \mathrm{e})$ and $\mathrm{W}(3 \mathrm{i})$ atoms. A reasonable assumption is that $\mathrm{O}(3 \mathrm{e})$ is actually $\mathrm{H}_{2} \mathrm{O}$ when bonded to $\mathrm{W}(3 \mathrm{i})$ [ $\mathrm{W}-\mathrm{O} 2.16(2) \AA$ ] but is unprotonated when bonded to $\mathrm{W}(3 \mathrm{e})$ $[\mathrm{W}-\mathrm{O}$ 1.56(2) $\AA$ ]. There are also three regions of more diffuse electron density between the three $\mathbf{W}(3)$ atoms and the triad axis. These appear to arise from the presence of additional oxygen atoms; but because of the three-fold disorder, the $X$-ray data do not clearly distinguish between three interior oxygens on or near mm sites, each bonded to one W(3), and two interior oxygens each bonded to W(3i) only. In either case the short interior $\mathrm{O} \cdots \mathrm{O}$ distances (ca. $2.4 \AA$ ) seem consistent only with the presence of hydrogen bonds. The ${ }^{183} \mathrm{~W}$ spectra which will now be discussed are relevant to this problem.
${ }^{183} \mathrm{~W}$ N.M.R. Spectrum.-The ${ }^{183} \mathrm{~W}$ nucleus has spin $\frac{1}{2}$ and is $14.3 \%$ abundant. The spectrum of $\left[\mathrm{P}_{2} \mathrm{~W}_{21} \mathrm{O}_{71}\left(\mathrm{OH}_{2}\right)_{3}\right]^{6-}$ shows seven main lines together with coupling satellites (Figure 2). The lines are labelled $A$ to $G$ in order of decreasing frequency (Table

Table 2. Interatomic distances ( $\overline{\mathrm{A}})$ and interbond angles ()

| $\mathrm{W}(1)-\mathrm{O}(1)$ | 1.73(2) | $\mathrm{W}(3 \mathrm{e})-\mathrm{O}(23)$ | 1.94(1) |
| :---: | :---: | :---: | :---: |
| $\mathrm{W}(1)-\mathrm{O}(12)$ | 1.90 (1) | $\mathrm{W}(3 \mathrm{e})-\mathrm{O}(31 \mathrm{i})$ | 2.39(5) |
| $\mathrm{W}(1)-\mathrm{O}(11)$ | 1.95(1) | $\mathrm{W}(3 \mathrm{i})-\mathrm{O}(32 \mathrm{i})$ | 1.87(15) |
| $\mathrm{W}(1)-\mathrm{O}(1 \mathrm{P})$ | 2.38(2) | $\mathrm{W}(3 \mathrm{i})-\mathrm{O}(23)$ | 1.89(1) |
| $\mathrm{W}(2)-\mathrm{O}(2)$ | 1.68(2) | $\mathrm{W}(3 \mathrm{i})-\mathrm{O}(3 \mathrm{e})$ | 2.16(2) |
| $\mathrm{W}(2)-\mathrm{O}\left(23^{1}\right)$ | 1.90(1) | $\mathrm{P}-\mathrm{O}(1 \mathrm{P})$ | 1.54(3) |
| $\mathrm{W}(2)-\mathrm{O}(12)$ | 1.90(1) | $\mathrm{P}-\mathrm{O}(2 \mathrm{P})$ | 1.53(1) |
| $\mathrm{W}(2)-\mathrm{O}(22 \mathrm{a})$ | 1.91(1) | $\mathrm{K}-\mathrm{O}\left(1^{\text {II }}\right.$ ) | 2.95(2) |
| $\mathrm{W}(2)-\mathrm{O}\left(22 \mathrm{~b}^{1}\right)$ | 1.93(1) | $\mathrm{K}-\mathrm{O}(22)$ | 3.03(2) |
| $\mathrm{W}(2)-\mathrm{O}\left(2 \mathrm{P}^{\mathrm{l}}\right)$ | 2.38 (1) | $\mathrm{K}-\mathrm{O}\left(23^{\prime}\right)$ | 3.10(2) |
| $\mathrm{W}(3 \mathrm{e})-\mathrm{O}(3 \mathrm{e})$ | 1.56(2) |  |  |
| W(1) ... W ( $1^{\text {III }}$ ) | 3.402(1) | W(2) . . W $\mathrm{W}^{\left(3 \mathrm{e}^{\text {III }} \text { ) }\right.}$ | 3.669(2) |
| W(1) . . . W (2) | $3.695(1)$ | W(3i) . . W ${ }^{\text {( }} \mathrm{i}^{\text {[II }}$ ) | 5.472(6) |
| $\mathrm{W}(2) \cdots \mathrm{W}\left(2^{\text {lv }}\right)$ | 3.354(2) | W(3e) . . W W (3i'li) | 6.000(6) |
| W (2) ... W $\left(2^{\text {v }}\right.$ ) | 3.674(2) | W(1) . . P ${ }^{\text {P }}$ | 3.497(11) |
| W(2) $\cdot . . W\left(3 i^{\text {III }}\right.$ ) | 3.608(2) | $W(2) \cdots P$ | 3.518(1) |
| $\mathrm{O}(1 \mathrm{P})-\mathrm{P}-\mathrm{O}(2 \mathrm{P})$ | 109.2(9) | $\mathrm{O}(23)-\mathrm{W}(2)-\mathrm{O}(22 \mathrm{a})$ | 88.8(7) |
| $\mathrm{O}(2 \mathrm{P})-\mathrm{P}-\mathrm{O}(2 \mathrm{P})$ | 109.7(9) | $\mathrm{O}(23)-\mathrm{W}(2)-\mathrm{O}(22 \mathrm{~b})$ | 88.4(8) |
| $\mathrm{O}(1)-\mathrm{W}(1)-\mathrm{O}(11)$ | 96.6(7) | $\mathrm{O}(12)-\mathrm{W}(1)-\mathrm{O}(12)$ | 84.8(8) |
| $\mathrm{O}(1)-\mathrm{W}(1)-\mathrm{O}(12)$ | 105.9(6) | $\mathrm{O}(3 \mathrm{e})-\mathrm{W}(3 \mathrm{e})-\mathrm{O}(23)$ | 103.7(6) |
| $\mathrm{O}(11)-\mathrm{W}(1)-\mathrm{O}(11)$ | 85.9(8) | $\mathrm{O}(23)-\mathrm{W}(3 \mathrm{e})-\mathrm{O}(23)$ | 87.2(8) |
| $\mathrm{O}(11)-\mathrm{W}(1)-\mathrm{O}(12)$ | 90.3(6) | $\mathrm{O}(23)-\mathrm{W}(3 \mathrm{e})-\mathrm{O}(23)$ | 86.4(9) |
| $\mathrm{O}(11)-\mathrm{W}(1)-\mathrm{O}(1 \mathrm{P})$ | 73.6(6) | $\mathrm{O}(23)-\mathrm{W}(3 \mathrm{e})-\mathrm{O}(32 \mathrm{i})$ | 76.3(9) |
| $\mathrm{O}(12)-\mathrm{W}(1)-\mathrm{O}(1 \mathrm{P})$ | 84.0(6) | $\mathrm{O}(3 \mathrm{e})-\mathrm{W}(3 \mathrm{i})-\mathrm{O}(23)$ | 85.7(6) |
| $\mathrm{O}(1)-\mathrm{W}(1)-\mathrm{O}(1 \mathrm{P})$ | 166.4(8) | $\mathrm{O}(23)-\mathrm{W}(3 \mathrm{i})-\mathrm{O}(23)$ | 89.3(9) |
| $\mathrm{O}(2)-\mathrm{W}(2)-\mathrm{O}(22 \mathrm{a})$ | 103.1(7) | $\mathrm{O}(23)-\mathrm{W}(3 \mathrm{i})-\mathrm{O}(23)$ | 90.1(9) |
| $\mathrm{O}(2)-\mathrm{W}(2)-\mathrm{O}(22 \mathrm{~b})$ | 99.8(7) | $\mathrm{O}(23)-\mathrm{W}(3 \mathrm{i})-\mathrm{O}(31 \mathrm{i})$ | 86(3) |
| $\mathrm{O}(2)-\mathrm{W}(2)-\mathrm{O}(12)$ | 100.6(7) | $\mathrm{O}(3 \mathrm{e})-\mathrm{W}(3 \mathrm{i})-\mathrm{O}(31 \mathrm{i})$ | 169(5) |
| $\mathrm{O}(2)-\mathrm{W}(2)-\mathrm{O}(23)$ | 98.8(7) | $\mathrm{W}(1)-\mathrm{O}(11)-\mathrm{W}(1)$ | 121.6(9) |
| $\mathrm{O}(12)-\mathrm{W}(2)-\mathrm{O}(2 \mathrm{P})$ | 82.2(6) | $\mathrm{W}(2)-\mathrm{O}(22 \mathrm{a})-\mathrm{W}(2)$ | 149(1) |
| $\mathrm{O}(12)-\mathrm{W}(2)-\mathrm{O}(22 \mathrm{a})$ | 87.9(7) | $\mathrm{W}(2)-\mathrm{O}(22 \mathrm{~b})-\mathrm{W}(2)$ | 120.9(7) |
| $\mathrm{O}(12)-\mathrm{W}(2)-\mathrm{O}(22 \mathrm{~b})$ | 87.3(7) | $\mathrm{W}(2)-\mathrm{O}(2 \mathrm{P})-\mathrm{P}$ | 127.1(8) |
| $\mathrm{O}(23)-\mathrm{W}(2)-\mathrm{O}(2 \mathrm{P})$ | 78.4(7) | $\mathrm{W}(1)-\mathrm{O}(12)-\mathrm{W}(2)$ | 152.1(8) |

Symmetry code: (I) $x, 1+x-y, z ;$ (II) $y, x, \frac{1}{2}+z ;$ (III) $x, 2 x, z ;$ (IV) $y-x, x, z ;(\mathrm{V}) 1-y, 1-x, z$
3). Their respective intensities are in the ratio $2: 4: 4: 4: 4: 1: 2$. In certain cases (sodium salts with more than $4 \mathrm{Na}^{+}$per anion in $\mathrm{D}_{2} \mathrm{O}$-rich solvent) lines A and B overlap but can sometimes be separated after a lorentzian-gaussian treatment of the freeinduction decay. The anion clearly does not have trigonal ( $\overline{6} 2 m$ ) symmetry, which would require the spectrum to consist of three lines only, with relative intensities $6: 12: 3$. Figure 3 shows how crystallographically indistinguishable atoms form sub-sets for true anion symmetry mm : two $\mathrm{W}(1 \mathrm{a})$ and four each of $\mathrm{W}(1 \mathrm{~b})$, $W(2 a), W(2 b)$, and $W(2 c)$. With the inclusion of two $W(3 i)$ and one $\mathrm{W}(3 \mathrm{e})$, the 2:4:4:4:4:1:2 pattern is explained. The first five main lines, $\mathrm{A}-\mathrm{E}$, are close doublets as the result of coupling through oxygen to ${ }^{31} \mathrm{P}\left(I=\frac{1}{2}\right)$. They must be assigned to W atoms of the $\mathrm{PW}_{9} \mathrm{O}_{34}{ }^{9-}$ moieties, while lines F and G are unsplit and are assigned on the basis of their relative intensities to $\mathrm{W}(3 \mathrm{e})$ and $\mathrm{W}(3 \mathrm{i})$ respectively, which do not share oxygens with $\mathrm{PO}_{4}$ groups. A comparison with the ${ }^{183} \mathrm{~W}$ n.m.r. spectrum of the $\left[\mathrm{As}^{4 \mathrm{III}}{ }_{2} \mathrm{~W}_{21} \mathrm{O}_{69}\left(\mathrm{OH}_{2}\right)\right]^{6-}$ anion ${ }^{5.14,15}$ is instructive. This anion contains two $\mathrm{AsW}_{9} \mathrm{O}_{33}$ moieties linked via one six-co-ordinate and two five-co-ordinate equatorial W atoms. The five-coordinate W gives rise to an n.m.r. line at -43.8 p.p.m., implying weaker shielding compared with all other W nuclei in the anion including the third equatorial $\mathbf{W}(-212$ p.p.m.). In the present spectrum, however, the lines for $\mathrm{W}(3 \mathrm{e})$ and $\mathrm{W}(3 \mathrm{i})$ at -152 and -226 p.p.m. show these atoms to be the most shielded of all and presumably six-co-ordinate, which requires the presence of three interior equatorial oxygens.

Further assignments may be made from an examination of the ${ }^{183} \mathrm{~W}-\mathrm{O}-{ }^{183} \mathrm{~W}$ couplings. The evidence to date ${ }^{9}$ is that the coupling in polyoxotungstates is distinctly stronger if the $\mathrm{WO}_{6}$


Figure 2. ${ }^{183} \mathrm{~W}$ N.m.r. spectrum of $\left[\mathrm{P}_{2} \mathrm{~W}_{21} \mathrm{O}_{71}\left(\mathrm{OH}_{2}\right)_{3}\right]^{6-}\left(15.005 \mathrm{MHz}, 303 \mathrm{~K}, 13 \mathrm{~g}\right.$ salt in 4 g solvent; 15000 scans; reference $2 \mathrm{~mol}_{\mathrm{dm}}{ }^{-3}$ $\mathrm{Na}_{2} \mathrm{WO}_{4}$ in $\mathrm{D}_{2} \mathrm{O}$ ). Lower: $\mathrm{Na}_{6}$ salt in $\mathrm{D}_{2} \mathrm{O}-\mathrm{H}_{2} \mathrm{O}\left(1.4: 1\right.$ ). Upper (lines A, B, F, G only; external lock): $\mathrm{Na}_{4} \mathrm{H}_{2}$ salt in $\mathrm{D}_{2} \mathrm{O}$

Table 3. ${ }^{183} \mathrm{~W}$ N.m.r. chemical shifts and coupling constants for $\mathrm{Na}_{4} \mathrm{H}_{2}\left[\mathrm{P}_{2} \mathrm{~W}_{21} \mathrm{O}_{71}\left(\mathrm{OH}_{2}\right)_{3}\right]$ in water

| Line | Assignment | Chemical shift,$\delta \pm 0.1 \text { p.p.m. }$ | Coupling constants $\pm 0.3 \mathrm{~Hz}$ |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  |  | ${ }^{2} J[\mathrm{~W}(\mathrm{i})-\mathrm{O}-\mathrm{W}(\mathrm{j})$ ] | ${ }^{2} \int[\mathrm{~W}(\mathrm{i})-\mathrm{O}-\mathrm{P}]$ |
| A | W(1a) | - 108.3 | $\mathrm{W}(1 \mathrm{~b}) 9.6, \mathrm{~W}(2 \mathrm{a}) 21.5$ | 0.7 |
| B | W(1b) | - 108.5 | $\mathrm{W}(1 \mathrm{a}) 9.6 ; \mathrm{W}(2 \mathrm{~b}), \mathrm{W}(2 \mathrm{c})$ 22.0 | 0.9 |
| C | W(2b) | - 124.7 | $\begin{aligned} & \mathrm{W}(2 \mathrm{a}) 8.5, \mathrm{~W}(\mathrm{lb}) 22.0, \\ & \mathrm{~W}(2 \mathrm{c}) 25.2, \mathrm{~W}(3 \mathrm{i}) 19.4 \end{aligned}$ | 1.6 |
| D | W(2c) | -129.7 | $\mathrm{W}(1 \mathrm{~b}) 21.5, \mathrm{~W}(2 \mathrm{~b}) 25.2$, <br> W(3e) 21.9 | 1.4 |
| E | W(2a) | -131.2 | $\begin{aligned} & \mathrm{W}(2 \mathrm{~b}) 8.5, \mathrm{~W}(1 \mathrm{a}) 21.5, \\ & \mathrm{~W}(3 \mathrm{i}) 19.4 \end{aligned}$ | 1.5 |
| F | W(3e) | - 152.3 | $\mathrm{W}(2 \mathrm{c}) 21.9$ | No coupling |
| G | W(3i) | -225.9 | W(2a), W(2b) 19.4 | No coupling |

octahedra in question share corners ( ${ }^{2} J c a .20 \mathrm{~Hz}$ ) than if they share edges ( ${ }^{2} J 8-9 \mathrm{~Hz}$ ). Despite the overlappings of lines the following connectivities can be deduced:

| Atom | Number in anion | Corner-linked to: | Edge-linked to: |
| :---: | :---: | :---: | :---: |
| W(1a) | 2 | Two W(2a) | Two W(1b) |
| W(1b) | 4 | One W(2b), one W(2c) | One W(1a) |
| W(2a) | 4 | One W(1a), one W(2c) | One W(2b) |
| W(2b) | 4 | One W(1b), one $W(2 c)$, one W(3i) | One W(2a) |
| W(2c) | 4 | One W(1b), one $W(2 b)$, one W(3e) | None |
| W(3i) | 2 | Two W(2a), two W(2b) | None |
| W(3e) | 1 | Four W(2c) | None |

Clearly, the strong couplings predominate. Coupling constants are listed in Table 3. The line assignments are assisted by a moderately well resolved two-dimensional COSY contour plot (Figure 4). Line G ( -226 p.p.m.) is connected to C ( -125 p.p.m.) and E ( -131 p.p.m.), and line F ( -152 p.p.m.) to $D(-$ 130 p.p.m.). Since $F$ and $G$ correspond to equatorial atoms $\mathrm{W}(3 \mathrm{e})$ and $\mathrm{W}(3 \mathrm{i}), \mathrm{C}, \mathrm{D}$, and E correspond to belt $\mathrm{W}(2)$ atoms. After a suitable line-broadening treatment no weak-coupling lines appear at the foot of line D which therefore corresponds to $\mathrm{W}(2 \mathrm{c})$ whose connections with all other W [except the second $\mathrm{W}(2 \mathrm{c})]$ are via corner sharing. The assignments of line C to $W(2 b)$ and of line $E$ to $W(2 a)$ follow from the relative intensities of the strong-coupling lines, while the main line intensities identify $A$ with $W(1 a)$ and $B$ with $W(1 b)$.

Further information is obtainable from the dependence of the


Figure 3. Tungsten framework labelled for $m m\left(C_{2 v}\right)$ symmetry. Thick lines imply that the $\mathrm{WO}_{6}$ octahedra share edges, and thin lines that they share corners
structure of lines $F$ and $G$, respectively due to $W(3 e)$ and $W(3 i)$, on the solvent $\left(\mathrm{D}_{2} \mathrm{O} / \mathrm{H}_{2} \mathrm{O}\right)$ composition. As shown in Figure 5, in pure water both atoms give rise to a triplet consisting of a main line and two equally spaced satellites whose relative intensities are ca. 0.30:1:0.30 [calculated, 0.333:1:0.333 for coupling to four W , if ${ }^{183} \mathrm{~W} 14.28 \%$ abundant; note that the $\mathrm{W}(3 \mathrm{i})-\mathrm{W}(2 \mathrm{a})$ and $\mathrm{W}(3 \mathrm{i})-\mathrm{W}(2 \mathrm{~b}){ }^{2} J$ coupling constants are identical]. In $\mathrm{D}_{2} \mathrm{O}-\mathrm{H}_{2} \mathrm{O}$, however, both the F and G resonances become a triplet of triplets whose relative intensities depend on the $\mathrm{D}_{2} \mathrm{O} / \mathrm{H}_{2} \mathrm{O}$ ratio (Figure 5). We regard this as due to slow hydrogen-deuterium exchange on protonated ligands of $W(3)$ atoms. This is the $\beta$ effect described elsewhere, for example for some carbohydrates where the ${ }^{13} \mathrm{C}$ resonance for a hydroxylated atom is shifted upfield on deuteriation and appears as a doublet under conditions of slow exchange. ${ }^{16}$ Where the magnetic nucleus is adjacent to a ligand with $n$ exchangeable protons, slow exchange results in a multiplet of $(n+1)$ lines; an example is the 13 -peak ${ }^{59} \mathrm{Co}$ resonance for $\left[\mathrm{Co}(\mathrm{en})_{3}\right]^{3+}$ (en $=$ ethylenediamine) in $\mathrm{H}_{2} \mathrm{O}-\mathrm{D}_{2} \mathrm{O} .{ }^{17}$ In the present case, the evidence indicates that two, and only two, H atoms in the equatorial plane undergo slow exchange. The $\mathbf{H}_{2} \mathrm{O}$ ligand exterior to $\mathrm{W}(3 \mathrm{i})$ is expected to undergo rapid exchange; therefore the two slowly exchanging protons are in the interior of the anion. The most satisfactory picture is one in which $\mathrm{W}(3 \mathrm{e})$ carries one interior $\mathrm{H}_{2} \mathrm{O}$ ligand, hydrogen-bonded to the interior oxo oxygen atom on each W(3i), as shown in Figure 6. The $\left[\mathrm{As}^{111}{ }_{2} \mathrm{~W}_{21} \mathrm{O}_{69}\right]^{6-}$ anion, in contrast, contains just one oxo atom and no $\mathrm{H}_{2} \mathrm{O}$ in interior sites in the equatorial plane, ${ }^{5}$ and no $\beta$ effect can be detected ${ }^{15}$ in its ${ }^{183} \mathrm{~W}$ n.m.r. spectrum. In the present case, the replacement of $\mathrm{H}_{2} \mathrm{O}$ by $\mathrm{D}_{2} \mathrm{O}$ weakens the internal hydrogen bonds but does not affect the ${ }^{2} J$


Figure 4. Two-dimensional COSY ${ }^{183} \mathrm{~W}$ n.m.r. spectrum of $\mathrm{Na}_{4}$ $\mathrm{H}_{2}\left[\mathrm{P}_{2} \mathrm{~W}_{21} \mathrm{O}_{71}\left(\mathrm{OH}_{2}\right)_{3}\right]$ in $\mathrm{D}_{2} \mathrm{O}-\mathrm{H}_{2} \mathrm{O}(c a .4: 1)$ at 303 K . The single and the paired arrows respectively imply couplings involving $\mathrm{W}(3 i)$ and W(3e)
$\mathrm{W}(2)-\mathrm{O}-\mathrm{W}(3)$ couplings; the $\mathrm{W}(3 \mathrm{e})$ resonance moves upfield by 0.587 p.p.m., while the $\mathrm{W}(3 \mathrm{i})$ resonance moves downfield by 0.980 p.p.m. We have not been able to observe the ${ }^{1} \mathrm{H}$ resonance of the slowly exchanging atoms directly. The $\beta$ effect is independent of pH in solutions of $\mathrm{Na}_{x} \mathrm{H}_{6-x}\left[\mathrm{P}_{2} \mathrm{~W}_{21} \mathrm{O}_{71}\left(\mathrm{OH}_{2}\right)_{3}\right]$ ( $x=0-6$ ), and the spectra do not change over a period of months although white deposits slowly form on the walls of the container. Solutions of the acid when treated with more than 6 equivalents of NaOH show complex spectra lacking the characteristic lines A-G and showing that degradation of the anion has occurred.

Comparison with 21-Tungstodiarsenate(iII).-The salts $\mathrm{K}_{4} \mathrm{H}_{2}$ $\left[\mathrm{P}^{\mathrm{V}}{ }_{2} \mathrm{~W}_{21} \mathrm{O}_{71}\left(\mathrm{OH}_{2}\right)_{3}\right] \cdot 28 \mathrm{H}_{2} \mathrm{O}$ and $\mathrm{Rb}_{4} \mathrm{H}_{2}\left[\mathrm{As}^{\mathrm{III}}{ }_{2} \mathrm{~W}_{21} \mathrm{O}_{69^{-}}\right.$ $\left.\left(\mathrm{OH}_{2}\right)\right] \cdot 34 \mathrm{H}_{2} \mathrm{O}^{5}$ crystallize in the same space group with similar cell dimensions and anion packing. In each case, the unique locatable cation (three per anion) lies in the equatorial plane $60^{\circ}$ from the exterior $\mathrm{W}(3)-\mathrm{O}$ bonds and serves to link the anions. The anions show three-fold disorder in both salts, but whereas the $\mathrm{P}_{2} \mathrm{~W}_{21}$ anion contains $\mathrm{PO}_{4}$ tetrahedra oriented apex outwards along the anion axis, the $\mathrm{As}_{2} \mathrm{~W}_{21}$ anion contains trigonal-pyramidal $\mathrm{AsO}_{3}$ groups with a lone pair on each As directed towards the equatorial region. Thus the $\mathrm{As}_{2} \mathrm{~W}_{21}$ anion may be regarded as derived from two $x-\mathrm{B}$ (not $x-\mathrm{A}$ ) $\mathrm{As}^{\text {III }} \mathrm{W}_{9} \mathrm{O}_{33}{ }^{9-}$ units, each formed from $\alpha-\left[\mathrm{As}^{v} \mathrm{~W}_{12} \mathrm{O}_{40}\right]^{3-}$ by the removal of three edge-linked $\mathrm{WO}_{6}$ octahedra including one oxygen of the central $\mathrm{AsO}_{4}$ group. These units are linked via three equatorial W atoms. A result of this is that the $\mathrm{O}(23)$ atoms bonded to the equatorial $\mathrm{W}(3)$ in $\mathrm{As}_{2} \mathrm{~W}_{21}$ are only $2.89 \AA$ from the anion axis, and the midpoint between a pair bonded to the same $W(3)$ is only $2.58 \AA$ from the axis, whereas the corresponding distances in $\mathrm{P}_{2} \mathrm{~W}_{21}$ are 3.56 and $3.30(2) \AA$. In turn, the $\mathrm{W}(3)$ atoms in $\mathrm{As}_{2} \mathrm{~W}_{21}$ lie at only 3.028 and 2.474(5) $\AA$ from the axis, compared with 3.760 and $3.159(4) \AA$ in $\mathrm{P}_{2} \mathrm{~W}_{21}$.

(i)

Figure 5. The ${ }^{183} \mathrm{~W}$ n.m.r. signals due to $\mathrm{W}(3 \mathrm{e})$ (line F ) and $\mathrm{W}(3 \mathrm{i})$ (line $G$ ) for $\mathrm{Na}_{x} \mathrm{H}_{6-x}\left[\mathrm{P}_{2} \mathrm{~W}_{21} \mathrm{O}_{71}\left(\mathrm{OH}_{2}\right)_{3}\right]$ in $\mathrm{D}_{2} \mathrm{O}-\mathrm{H}_{2} \mathrm{O}$, showing the $\beta$ effect. Values of $x$ and the $\mathrm{D}_{2} \mathrm{O}-\mathrm{H}_{2} \mathrm{O}$ ratio for (i) to (vi) are: $0,0.4 ; 0,4.0 ; 4,0$ (natural water); 4, 0.4; $6,1.4$, and $4,4.5$

Consequently $\mathrm{As}_{2} \mathbf{W}_{21}$ cannot accommodate more than one interior equatorial oxygen atom, and two $\mathbf{W}(3)$ are in exterior sites with square-pyramidal co-ordination, while just one is in an interior site with an interior oxo atom and an exterior $\mathrm{H}_{2} \mathrm{O}$ as unshared ligands. This contrasts with the situation inferred for $\left[\mathrm{P}_{2} \mathrm{~W}_{21} \mathrm{O}_{71}\left(\mathrm{OH}_{2}\right)_{3}\right]^{6-}$.

## Experimental

21-Tungstodiphosphate Anion.-The sparingly soluble potassium salt was obtained from $\mathrm{K}_{3}\left[\mathrm{PW}_{12} \mathrm{O}_{40}\right]$ via $\mathrm{K}_{7-}$ [ $\mathrm{PW}_{11} \mathrm{O}_{39}$ ] by published methods, ${ }^{1,18}$ and was recrystallized from $1 \mathrm{~mol} \mathrm{dm}^{-3} \mathrm{HCl}$. The number of $\mathrm{K}^{+}$per anion $(4-6)$ was sensitive to the acidity of the solutions; the most satisfactory single crystals contained $4-4.5 \mathrm{~K}^{+}$per anion. The crystalline free acid was obtained by passage of a saturated solution of the salt through a sulphonic-acid type cation exchanger and evaporation of the effluent. Solutions of the sodium salt were obtained by the addition of known amounts of $\mathrm{NaHCO}_{3}$ to the aqueous acid.
${ }^{183}$ W N.M.R. Spectroscopy.-Spectra were recorded by use of a Bruker WP- 360 spectrometer equipped with a wide-bore probe head. Normally, sample tubes of 15 mm outside diameter were used, with $\mathrm{D}_{2} \mathrm{O}$ as internal lock. Coaxial tubes ( 15 and 5 mm ) were used in experiments with an external lock.


Figure 6. Atomic arrangement in the vicinity of the equatorial plane of $\left[\mathrm{P}_{2} \mathrm{~W}_{21} \mathrm{O}_{71}\left(\mathrm{OH}_{2}\right)_{3}\right]^{6-}$

Solutions were equilibrated for $5-12 \mathrm{~h}$ and were passed through membrane filters before the spectra were recorded. The two-dimensional COSY ${ }^{183} \mathrm{~W}$ measurements were made by use of a Bruker WP-400 instrument as described previously ${ }^{10}$ (sodium salt in $\mathrm{D}_{2} \mathrm{O}, 10-\mathrm{mm}$ sample tubes).

X-Ray Structure Determination.-Crystals of the potassium salt are well formed, usually bi-capped, hexagonal prisms. The crystals selected for data collection were cleaved on the basal plane to give roughly equidimensional fragments, ca. 0.1 mm on edge, and were protected after mounting with a film of paraffin oil.

Crystal data. $\mathrm{K}_{4} \mathrm{H}_{2}\left[\mathrm{P}_{2} \mathrm{~W}_{21} \mathrm{O}_{71}\left(\mathrm{OH}_{2}\right)_{3}\right] \cdot 28 \mathrm{H}_{2} \mathrm{O}, \quad M=$ 5775.1 , hexagonal, space group $P 6_{3} / m m c, a=16.295(2), c=$ 19.771(5) $\AA, U=4546.4 \AA^{3}, Z=2, D_{\mathrm{c}}=4.219 \mathrm{~g} \mathrm{~cm}^{-3}$, Mo radiation $(\lambda=0.71069 \AA), \mu=274 \mathrm{~cm}^{-1}, F(000)=5080$.

Data collection and reduction. Two data sets were collected on Enraf-Nonius CAD-4F diffractometers, in both cases by the $\omega$ $2 \theta$ scan method, $2 \theta_{\text {max. }} 50^{\circ}$, and with Lorentz polarization corrections applied. Data set 1 (C.M.T. and G.F.T.): 1540 unique data, absorption corrections by use of $\psi$ scans ( 20 planes) in conjunction with the programs FACIES ${ }^{19}$ (refinement of cell dimensions) and ABSORB. ${ }^{20}$ Data set 2 (T. J. R. W.): 1535 unique data, absorption correction by DIFABS ${ }^{21}$ following isotropic refinement.

Structure solution and refinement. The structural analysis was carried out on both data sets at our respective laboratories, with very similar results. The $W$ atoms were located by direct methods (MULTAN, ${ }^{22}$ SHELX $76^{23}$ ) and the structure was expanded by alternating difference syntheses and cycles of full-matrix least-squares refinement. ${ }^{23.24}$ It quickly became apparent that the anion attained effective three-fold symmetry as the result of disorder, from the anomalously large $U_{\text {iso }}$ of $\mathrm{W}(3)$ and from the presence of residual peaks close to and on either side of $\mathrm{W}(3)$ at mm sites in the equatorial plane which could not be explained by thermal motion. Anisotropic refinement of two plausible models, with $\mathrm{W}(3 \mathrm{e})$ and $\mathrm{W}(3 \mathrm{i})$ present in $2: 1$ or alternatively in $1: 2$ ratio, converged at similar $R$ values but the first model led to a negative $U_{33}$ coefficient for $\mathrm{W}(3 \mathrm{i})$. The site-occupancy factors were also refined (data set 2 ), giving $0.96(9)$ for $W(3 e)$ and $2.04(18)$ for $W(3 i)$. The second model was therefore adopted. Only one unique $\mathrm{K}^{+}$could be located; its thermal motion was large and considerably anisotropic, but attempts to model this by fractional occupancy of several adjacent sites were unsuccessful. Likewise, only three independent lattice $\mathrm{H}_{2} \mathrm{O}$ molecules could be located ( 21 per anion). In the final stages the choice of three interior equatorial oxygens $\mathrm{O}(3 \mathrm{i})$, rather than two $\mathrm{O}(3 \mathrm{i})$ distributed over three equivalent sites, had to be made on the basis of the n.m.r. results as the same $R$ was attained in either case with virtually identical parameters other than $U[O(3 i)]$. For data set 2, refinement (on $F$ ) with three $\mathrm{O}(3 \mathrm{i})$ converged at $R 0.043$ [unit weights, $1172|F| \geqslant 3 \sigma(F), 66$ parameters]. With both data sets, difference syntheses indicated that $\mathrm{O}(3 \mathrm{i})$ had considerable density on either side of the vertical mirror plane through it and in the last cycles with data set $1, \mathrm{O}(3 \mathrm{i})$ was treated as two independent atoms, $\mathrm{O}(31 \mathrm{i})\left[\mathrm{H}_{2} \mathrm{O}\right.$ bonded to $\left.\mathrm{W}(3 \mathrm{e})\right]$ and $\mathrm{O}(32 \mathrm{i})$ [unprotonated O bonded to $\mathrm{W}(3 \mathrm{i})$ ], on one-third-occupied mm and $m$ sites respectively (Figure 6). The co-ordinates and derived dimensions listed in Tables 1 and 2 are those obtained
with data set 1 , with which convergence was reached at $R 0.037$, $R^{\prime} 0.047$ ( 1042 data, 76 parameters); the results obtained with data set 2 are not significantly different.

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