

76[K].—R. DOORNBOS & H. J. PRINS, "On slippage tests. I," *Indagationes Mathematicae*, v. 20, 1958, p. 38–46 (*Proc. Kon. Ned. Ak. van Wetensch.*, v. 61, Sec. A, 1958, p. 38–46); "On slippage tests. II," *Ibid.*, p. 47–55; "On slippage tests. III," *Ibid.*, p. 438–447.

The tables, which appear in part III, are related to two of the special cases included in this series of papers. In the first, from each of  $k$  Poisson distributions, with means  $\mu_i$ , a random drawing  $Z_i$  is taken ( $i = 1, 2, \dots, k$ ). To test the null hypothesis that  $u_i = u$ ,  $i = 1, \dots, k$ , for which the table is prepared, against the alternate that one of the  $u_i$ 's is greater than the others which have equal values, the authors propose the statistic,  $\max Z_i$ . For  $k = 2(1)10$  and the sum of the  $k$  observations,  $n = 2(1)25$ , values of  $\max Z_i$  are given for which the significance levels are near 5% and 1%. In each case the actual significance levels are given to 3D.

In the second case, each of  $k$  objects is ranked by each of  $m$  observers. The null hypothesis under test is that each of the  $m$  rankings is independently and randomly chosen from the set of permutations of the integers  $1, 2, \dots, k$ . As a test against the alternate that one of the objects has a higher probability of being ranked low while the others are ranked in random order, the proposed statistic is  $\min S_i$  where  $S_i$  is the sum of ranks assigned the  $i$ -th object ( $i = 1, 2, \dots, k$ ). Critical values  $S_\alpha$  of  $\min S_i$  for significance levels near  $\alpha = .05, .025, .01$  are tabled for  $m = 3(1)9$  and  $k = 2(1)10$ . Again in each case true significance levels are shown to 3D.

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77[K].—F. G. FOSTER, "Upper percentage points of the generalized beta distribution. III," *Biometrika*, v. 45, 1958, p. 492–503.

Let  $\theta_{\max}$  denote the greatest root of  $|v_2B - (v_1A + v_2B)| = 0$  where  $A$  and  $B$  are independent estimates, based on  $v_1$  and  $v_2$  degrees of freedom, of a parent dispersion matrix of a four-dimensional multinormal distribution. Define

$$I_x(4; p, q) = \Pr(\theta_{\max} \leq k)$$

with  $p = \frac{1}{2}(v_2 - 3)$ ,  $q = \frac{1}{2}(v_1 - 3)$ . Employing methods similar to those used in two preceding papers [1], [2] for the two and three-dimensional cases, the author tabulates 80%, 85%, 90%, 95%, and 99% points of  $I_x(4; p, q)$  to 4D for  $v_1 = 5(2)195$  and  $v_2 = 4(1)11$ .

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1. F. G. FOSTER & D. H. REES, "Upper percentage points of the generalized beta distribution. I," *Biometrika*, v. 44, 1957, p. 237–247. [*MTAC*, Rev. 165, v. 12, 1958, p. 302]

2. F. G. FOSTER, "Upper percentage points of the generalized beta distribution. II," *Biometrika*, v. 44, 1957, p. 441–453. [*MTAC*, Rev. 167, v. 12, 1958, p. 302.]

78[K].—W. HETZ & H. KLINGER, "Untersuchungen zur Frage der Verteilung von Objekten auf Plätze," *Metrika*, v. 1, 1958, p. 3–20.

For the classical distribution problem in which  $k$  indistinguishable objects are randomly distributed into  $n$  distinguishable cells (as in Maxwell-Boltzmann

statistics) the authors take the number,  $s$ , of occupied cells as a statistic to test the hypothesis of uniform probability over the cells. Let  $P(s | n, k)$  be the probability density for  $s$ . The correspondence is noted between this distribution and the results of a series of  $n$  drawings from a discrete distribution in which the random variable assumes only the values  $0, 1, 2, \dots$ , and in which the sample sum is  $k$  and the number of non-zero values is  $s$ . In developing a recursion formula for  $P(s | n, k)$  it is shown that the uniform distribution over cells arises from the Poisson distribution, and the binomial and negative binomial distribution give particular non-uniformities. The function tabulated is  $Z_{k;\alpha}$ , which is defined under the hypothesis of uniformity by  $\sum_{s=1}^{Z_{k;\alpha}} P(s | n, k) \leq \alpha$  and  $\sum_{s=1}^{Z_{k;\alpha}+1} P(s | n, k) > \alpha$ , for  $\alpha = .05, .01, .001; n = 3(1)20$ , and ranges of  $k$  varying from  $(3, 15)$  for  $n = 3$  to  $(2, 100)$  for  $n = 20$ .

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**79[K].**—A. HUITSON, "Further critical values for the sum of two variances," *Biometrika*, v. 45, 1958, p. 279–282.

Let  $s_i^2, i = 1, 2$ , be an estimate of the variance  $\sigma_i^2$  with  $f_i$  degrees of freedom so that  $f_i s_i^2 / \sigma_i^2$  is distributed as  $\chi^2$  with  $f_i$  dif. To assign confidence limits to the form  $\lambda_1 \sigma_1^2 + \lambda_2 \sigma_2^2$ , where  $\lambda_1$  and  $\lambda_2$  are arbitrary positive constants, the author has previously [1] tabulated upper and lower 5% and 1% critical values of

$$(\lambda_1 s_1^2 + \lambda_2 s_2^2) / (\lambda_1 \sigma_1^2 + \lambda_2 \sigma_2^2).$$

The present tables are an extension, giving upper and lower  $2\frac{1}{2}\%$  and  $\frac{1}{2}\%$  critical values for the same function to 2D for  $\lambda_1 s_1^2 / (\lambda_1 s_1^2 + \lambda_2 s_2^2) = 0(.1)1$  and  $f_1, f_2 = 16, 36, 144, \infty$ .

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1. A. HUITSON, "A method of assigning confidence limits to linear combinations of variances," *Biometrika*, v. 42, 1955, p. 471–479. [*MTAC*, Rev. 19, v. 12, 1958, p. 71.]

**80[K].**—SOLOMON KULLBACK, *Information Theory and Statistics*, John Wiley & Sons, New York, 1959, xvii + 395 p., 24 cm. Price \$12.50.

This interesting book, which discusses logarithmic measures of information and their applications to the testing of statistical hypotheses, contains three extended tables in addition to a number of shorter or more specialized ones. Table I gives  $\log_e n$  and  $n \log_e n$  to 10D for  $n = 1(1)1000$ . Table II lists values of

$$p_1 \log_e \frac{p_1}{p_2} + (1 - p_1) \log_e \frac{1 - p_1}{1 - p_2} \text{ to 7D for } p_1, p_2 = .01(.01).05(.05).95$$

$(.01).99$ . Table III gives 5% points for noncentral  $\chi^2$  to 4D with  $2n$  degrees of freedom for  $n = 1(1)7$  and noncentrality parameter  $\beta^2$  for  $\beta = 0(.2)5$ . As it is stated, this is taken directly from an equivalent table of R. A. Fisher [1].

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