

and where,

$$\bar{x} = \sum_{i=1}^n x_i/n,$$

$$s^2 = \sum_{i=1}^n (x_i - \bar{x})^2/(n - 1),$$

and

$$\sqrt{nk} = t(n - 1, u_\alpha \sqrt{n}, 1 - P).$$

Here $t(f, \delta, \epsilon)$ [1] is the 100ϵ percentage point of the non-central t distribution with f degrees of freedom, δ is the measure of non-centrality in the definition of t , and u_α is the $100(1 - \alpha)$ percentage point of the unit normal distribution with zero mean.

By use of the tables (especially Table IV) and iteration of the approximations given by Johnson and Welch in [1] the authors obtain values of the coefficient \sqrt{nk} to 4S, for $n = 5(1)20(5)50(10) 100(100) 300$, for P and $\alpha = .90, .95, .99$. A method for determination of these coefficients is given in [1], but the calculations are, of course, quite tedious, so that the present tables render a valuable service for practical applications to one-sided tolerance limits.

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Let $q = w/s$, where w is a sample range based on n values, and s is an independent estimate of standard deviation based on m values. Then tables of q' have been prepared for $Pr(q \geq q') = \alpha$, where $\alpha = .01, .05, .10$, $n = 2 (1) 20$, and $m = 1 (1) 20, 24, 30, 40, 60, 120, \infty$. Three significant figures are given throughout. The work of Harter [1] has been used in improving the accuracy throughout, particularly for $\alpha = .01$. For $\alpha = .01$ and $.05$, these tables correct errors in [2].

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2. J. M. MAY, "Extended and corrected tables of the upper percentage points of the 'Studentized' range," *Biometrika*, v. 39, 1952, p. 192-193. [RMT 1080, *MTAC*, v. 7, 1953, p. 94]

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Let $S_1/n_1, S_2/n_2$ denote independent covariance matrices arising from samples of sizes n_1 and n_2 from two p -variate normal populations, and $U^{(s)} = \text{trace } S_2^{-1} S_1$, where s is the number of non-zero roots. Two approximations are compared with the