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Tables of Gaussian Quadrature Rules for the Calculation of Fourier Coefficients, addendum to MOC this issue, p. 245. WALTER GAUTSCHI
Gaussian Quadrature Formulas for the Integration of Oscillating Functions, see review #24, p. 479 ROBERT PIESSENS

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