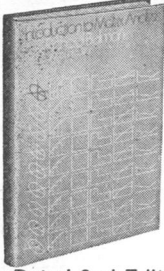


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Mathematics of Computation

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**Department of Anthropology
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Abstract of the paper
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