

27 [9].—SOL WEINTRAUB, *Distribution of Primes between 10^{14} and $10^{14} + 10^8$* , 6 pages of computer output deposited in the UMT file together with a text of 3 pages, 1971

The number of primes between 10^{14} and $10^{14} + 10^8$ is 3102679. (Riemann's formula gives the estimate 3102104.)

For each $k = 2(2)600$, these tables list four quantities:

COUNTS		RATIOS to $k = 2$	
GAPS	PAIRS	ACTUAL	THEORY

GAPS are the number of p_i in this interval such that $p_{i+1} - p_i = k$. PAIRS are the number of p here such that $p + k$ is prime (whether or not it is the next prime). ACTUAL is the ratio

$$\frac{\text{PAIRS}(k)}{\text{PAIRS}(2)}$$

and THEORY is that ratio according to the Hardy-Littlewood Conjecture.

Here are several observations. The most popular gap is for $k = 6$ (237524 specimens). The average gap is, of course, $\ln 10^{14} = 32+$. The number of twins ($k = 2$) is 127084. The first missing gap is $k = 332$. The largest gap is 414 and follows the prime $10^{14} + 13214473$. The most popular pairs are, obviously, for $k = 210$ and 420, namely, 408552 and 406950 specimens, respectively. "Actual" and "Theory" agree closely.

The brief text also mentions triples and quadruples.

See the following references for related tables.

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1. D. H. LEHMER, UMT 3, *MTAC*, v. 13, 1959, pp. 56–57.
2. F. GRUENBERGER & G. ARMERDING, UMT 73, *Math. Comp.*, v. 19, 1965, pp. 503–505.
3. M. F. JONES, M. LAI & W. J. BLUNDON, UMT 20, *Math. Comp.*, v. 21, 1967, p. 262.