

- 50 [7].—C. MOSIER & D. D. SHILLADY, *A Fast, Accurate Approximation for  $F_0(z)$  Occurring in Gaussian Lobe Basis Electronic Calculations*, Chemistry Department, Virginia Commonwealth University, Richmond, Virginia. Ms. of 3 typewritten pp. and 2 computer sheets deposited in the UMT file.

The mathematical function referred to in the title is defined by the definite integral  $F_0(z) = \int_0^1 \exp(-zu^2) du$ , which is expressible in terms of the error function by the relation  $F_0(z) = \frac{1}{2}(\pi/z)^{1/2} \text{Erf}(z^{1/2})$ , as the authors note.

Specifically, the function  $F_0(z)$  is herein approximated for positive  $z$  not exceeding 22.5 by a quartic polynomial in  $z - s_i$ , where the interval  $i$  and the corresponding shift  $s_i$  are calculated from a given value of  $z$  by simple formulas presented in the explanatory text. An accompanying table consists of 16S decimal values (in floating-point form) of the coefficients of this approximating polynomial for  $i = 1(1)119$ .

The authors claim that the error in their approximation is everywhere less than  $4 \cdot 10^{-12}$ . Moreover, tests performed by the authors on an IBM 360/50 system have revealed their algorithm to be faster than those based on comparable approximations cited in the literature.

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- 51 [7].—ROBERT PIESSENS & MARIA BRANDERS, *Chebyshev Polynomial Expansions of the Riemann Zeta Function*, 3 pages of tables and 2 pages of explanatory text, reproduced on the microfiche card attached to this issue.

Herein are six 23D tables of the coefficients of the respective expansions of  $x\zeta(x+1)$  and  $\zeta(x+k)$  for  $k = 2(1)5, 8$  in terms of the shifted Chebyshev polynomials  $T_n^*(x)$ , for  $0 \leq x \leq 1$ .

These tables were calculated on an IBM 1620 at the Computing Centre of the University of Leuven, and each table was checked by calculating  $\zeta(x)$  therefrom for several values of  $x$  and then comparing the results with corresponding entries in the tables of McLellan [1].

Coefficients of the Chebyshev expansion of  $x(\zeta + 1)$  have been published to 20D by Luke [2]; however, several entries are incorrect beyond 16D, as noted by the present authors. As a further check on Table 1 in the set under review, this reviewer has successfully compared it with a similar, unpublished 40D table of Thacher [3].

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1. ALDEN MCLELLAN IV, *Tables of the Riemann Zeta Function and Related Functions*, Desert Research Institute, University of Nevada, Reno, Nevada, 1968. (See *Math. Comp.*, v. 22, 1968, pp. 687–688, RMT 69.)

2. YUDELL L. LUKE, *The Special Functions and Their Approximations*, v. II, Academic Press, New York and London, 1969.

3. H. C. THACHER, JR., *On Expansions of the Riemann Zeta Function*.

- 52 [7].—GORO SHIMURA, *Introduction to the Arithmetic Theory of Automorphic Functions*, Princeton Univ. Press, Princeton, N.J., 1971, xiv + 267 pp., 24 cm. Price \$10.00.

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