

- 35 [7].—HENRY E. FETTIS & JAMES C. CASLIN, *Tables of Toroidal Harmonics, III: Functions of the First Kind—Orders 0—10*, Report ARL 70-0127, Aerospace Research Laboratories, Air Force Systems Command, United States Air Force, Wright-Patterson Air Force Base, Ohio, July 1970, iv + 391 pp., 28 cm. [Copies obtainable from National Technical Information Service, Springfield, Virginia 22151. Price \$3.00.]

The first table in this report consists of 11S values (in floating-point form) of the Legendre function of the first kind, $P_{n-1/2}^m(s)$, for $m = 0(1)10$, $s = 1.1(0.1)10$, and degree n ranging from 35 to 160, as in two earlier companion reports [1], [2], which were devoted to the tabulation of the Legendre function of second kind, $Q_{n-1/2}^m(s)$.

This table is followed by a tabulation, also to 11S, of the same function for similar orders m and for arguments $s = \cosh \eta$, where $\eta = 0.1(0.1)3$. The upper limit for the degree, n , here varies from 34 to 450.

A concluding table gives values of the cross product $P_{n+1/2}^m(s)Q_{n-1/2}^m(s) - Q_{n+1/2}^m(s)P_{n-1/2}^m(s)$ to 16S for $m = 0(1)10$, $n = 0(1)450$. This table evolved from spot-checking the other tables by means of identities that were derived from the known Wronskian relation and that are presented in the introductory section describing the method [3] of calculation by means of IBM 1620 and IBM 7094 systems.

Also included is a discussion of the application of toroidal functions to the determination of the potential field induced by a charged circular torus.

J. W. W.

1. HENRY E. FETTIS & JAMES C. CASLIN, *Tables of Toroidal Harmonics, I: Orders 0—5, All Significant Degrees*, Report ARL 69-0025, Aerospace Research Laboratories, Office of Aerospace Research, United States Air Force, Wright-Patterson Air Force Base, Ohio, February 1969. (See *Math. Comp.*, v. 24, 1970, pp. 489–490, RMT 36.)

2. HENRY E. FETTIS & JAMES C. CASLIN, *Tables of Toroidal Harmonics, II: Orders 5—10, All Significant Degrees*, Report ARL 69-0209, Aerospace Research Laboratories, Office of Aerospace Research, United States Air Force, Wright-Patterson Air Force Base, Ohio, December 1969. (See *Math. Comp.*, v. 24, 1970, pp. 989–990, RMT 70.)

3. HENRY E. FETTIS, "A new method of computing toroidal harmonics," *Math. Comp.*, v. 24, 1970, pp. 667–670.

- 36 [8].—LUDO K. FREVEL, *Evaluation of the Generalized Binomial Density Function*, Department of Chemistry, The Johns Hopkins University, Baltimore, Maryland, 1972. Ms. of 13 pp. deposited in the UMT file.

The author defines herein a generalized binomial density function by the relation

$$\beta(x; n, \alpha) = \frac{\Gamma(1 + 2n)(\sin \alpha)^{2(n+x)}(\cos \alpha)^{2(n-x)}}{\Gamma(1 + n + x)\Gamma(1 + n - x)}$$

which reduces to the standard binomial function $b(k; m, p)$ when $x = m/2 - k$, $n = m/2$, and $\alpha = \arcsin p^{1/2}$.

A table of this function is included for $\alpha = \pi/4$, $x = 0(0.05)3$, and $n = -0.1, 0, 0.1, 1, 2$; it was computed to 10D on a Wang 360 calculator before truncation of the final tabular entries to 8D.

In addition, a probability density function $\phi_n(x)$ is defined in terms of $\beta(x; n, \alpha)$ by the relation